Release:

Thursday, 23 October 2025

Discussion: Wednesday, 29 October 2025

You do not have to hand in your solutions to the exercises and they will **not** be graded. However, there will be four short tests during the semester. You need to reach $\geq 40\%$ of the total points in order to be admitted to the final exam (Klausur). The tests are held at the start of a lecture (room 25.22.U1.74) at the following dates:

Exercise set #2

Test 1: Thursday, 6 November 2025, 10:30-10:45

Test 2: Thursday, 27 November 2025, 10:30-10:45

Test 3: Thursday, 11 December 2025, 10:30-10:45

Test 4: Thursday, 15 January 2026, 10:30-10:45

Please ask questions in the RocketChat

The exercises are discussed every Wednesday, 14:30-16:00 in room 25.12.02.33.

1. Discounted returns

(a) Assume you observe a sequence of five rewards

$$R_1 = -1, R_2 = 2, R_3 = 6, R_4 = 3, R_5 = 2$$

until you reach a terminal state, i.e. a state that always transitions back to itself with a reward of 0. Calculate the returns G_0, \ldots, G_5 for a discount factor of $\gamma = 0.5$.

(b) Assume an MDP produces an infinite sequence of rewards of 5, i.e.

$$R_1 = 5, R_2 = 5, R_3 = 5, \dots$$

Calculate the return G_0 for the discount factors $\gamma \in \{0, 0.2, 0.5, 0.9, 0.95, 0.99, 0.999\}$. What would happen if the discount factor was $\gamma = 1$?

Hint: You can use the closed form of a special case of the power series.

(c) Assume you observe a sequence of T > 1 rewards

$$R_1 = 0, R_2 = 0, \ldots, R_{T-1} = 0, R_T$$

until you reach a terminal state. Note that all rewards except R_T are zero. How can you choose γ such that the initial return G_0 is equal to $\epsilon > 0$? Calculate these γ for the following situations:

i.
$$\epsilon = 0.1, R_T = 1, T = 10$$

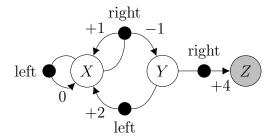
ii.
$$\epsilon = 0.1, R_T = 1, T = 50$$

iii.
$$\epsilon = 0.01, R_T = 1, T = 50$$

2. Value functions

(a) For any given MDP, policy π and terminal state E, what is $v_{\pi}(E)$? All transitions from a terminal state are back to itself with a reward of 0.

(b) Consider the MDP and policy π_1 from the previous exercise set. Note that if action right is taken in state X, then the transitions to X and Y occur with probabilities 0.75 and 0.25, respectively. The deterministic policy π_1 is defined as $\pi_1(X) = \text{right}$, $\pi_1(Y) = \text{right}$.



Calculate the values of states X and Y under policy π_1 , i.e. $v_{\pi_1}(X)$ and $v_{\pi_1}(Y)$, using a discount factor of $\gamma = 0.9$.

Hint: Start with the value of Y.

3. Policy iteration

Implement policy iteration and apply it to the Maze environment from the lecture. Follow the instructions in the Jupyter notebook policy-iteration.ipynb.