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proof of class equation theorem

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$X$  is a finite disjoint union of finite orbits:  $X = \cup_i Gx_i$ . We can separate this union by considering first only the orbits of 1 element and then the rest:  $X = \cup_{j=1}^l \{x_{i_j}\} \cup \cup_{k=1}^s Gx_{i_k} = Gx \cup_{k=1}^s Gx_{i_k}$ . Then using the orbit-stabilizer theorem, we have  $\#X = \#Gx + \sum_{k=1}^s [G : G_{x_{i_k}}]$  where for every  $k$ ,  $[G : G_{x_{i_k}}] \geq 2$ , because if one of them were 1, then it would be associated to an orbit of 1 element, but we counted those orbits first. Then this stabilizers are not  $G$ . This finishes the proof.