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## conjugacy class

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Entry type Definition
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Synonym conjugate
Synonym conjugate set

Synonym conjugate subgroup Related topic ConjugacyClassFormula Two elements g and g' of a group G are said to be *conjugate* if there exists  $h \in G$  such that  $g' = hgh^{-1}$ . Conjugacy of elements is an equivalence relation, and the equivalence classes of G are called *conjugacy classes*.

Two subsets S and T of G are said to be conjugate if there exists  $g \in G$  such that

$$T = \{gsg^{-1} \mid s \in S\} \subset G.$$

In this situation, it is common to write  $gSg^{-1}$  for T to denote the fact that everything in T has the form  $gsg^{-1}$  for some  $s \in S$ . We say that two subgroups of G are conjugate if they are conjugate as subsets.