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semigroup

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Entry type	Definition
Classification	msc 20M99
Synonym	homomorphism
Related topic	groupoid
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Related topic	SubmonoidSubsemigroup
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Defines	semigroup homomorphism

A *semigroup*  $G$  is a set together with a binary operation  $\cdot : G \times G \longrightarrow G$  which satisfies the associative property:  $(a \cdot b) \cdot c = a \cdot (b \cdot c)$  for all  $a, b, c \in G$ .

The set  $G$  is not required to be nonempty.

Let  $G, H$  be two semigroups. A *semigroup homomorphism* from  $G$  to  $H$  is a function  $f : G \rightarrow H$  such that  $f(ab) = f(a)f(b)$ .