



Math for the people, by the people.

## Frobenius group

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Defines	Frobenius complement

A permutation group  $G$  on a set  $X$  is *Frobenius* if no non-trivial element of  $G$  fixes more than one element of  $X$ . Generally, one also makes the restriction that at least one non-trivial element fix a point. In this case the Frobenius group is called *non-regular*.

The stabilizer of any point in  $X$  is called a *Frobenius complement*, and has the remarkable property that it is distinct from any conjugate by an element not in the subgroup. Conversely, if any finite group  $G$  has such a subgroup, then the action on cosets of that subgroup makes  $G$  into a Frobenius group.