

# Wind Farm

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## Abstract

*This will be the abstract of our paper. We will show how cool our research is and how important we are.  
Blabla Lorem ipsum.*

## I. INTRODUCTION

**T**O efficiently use wind resource rich locations and thus minimize the cost of wind energy, wind turbines are constructed in close proximity of each other, resulting in a wind farm. A side effect of wind turbine operation is a wake. When wind turbines are placed in close proximity of each other in a wind farm, wakes can have negative effects on downwind turbines. A wake is developed behind a wind turbine and can have severe effects on the power production and loads of the downwind turbine. A wake can be described by several characteristics (Gebraad Boersma Tutorial), such as a wind velocity deficit and an increased turbulent wind flow caused by the turbine's extraction of energy and the rotation of the turbine blade's, respectively. In addition, wake deflection can occur which can lead to suboptimal power and load conditions (ben wilson, mike van dijk, fleming, bastankah, zalkind).

With an increasing role of wind energy (quantify this) in Europe's energy production new challenges arise [1]. While the electrical power system becomes more dependent on wind energy, it is important for wind farms to be able to meet the demands of the power system by regulating its power output [2]. Traditionally, the need for power regulation of a wind farm was not necessary, because the wind

farms energy production was only a small part of the total energy production. As a result, the wind farms could always perform at maximum capacity, without the risk of overloading the power system. However, because wind energy production has increased in the recent years, and will continue to increase, regulating rather than maximizing power output becomes more important.

Regulating the power output of a wind farm is essential because an under- or overload of energy can decrease the stability of the power system [2]. Instability can lead to suboptimal operation of the power system, such as an energy overload [2] (en ook Hansen). Currently, most wind farms operate based on 'greedy control', meaning that the individual turbines always try to deliver maximum power for the turbine and not taking additional loads into account introduced by power maximization. This causes a problem when, for example, the power demand is low, and the energy dependency of the power system on wind energy is high. This could then result in an overload of the power system. Power regulation of a wind farm can solve this problem.

There are several methods for power regulation of a wind farm, two of which will be discussed in this paper, yaw control and axial induction control. Yaw control can be used as

a method to reduce the power output of a single wind turbine and as a method to increase power output and reduce loads of a wind farm (van dijk, wilson, fleming). A disadvantage of yawing is an increase of load on the yawed turbine, and thus reducing its lifespan [3, 4]. In addition, yawing a turbine can deflect a wake. This can be used as a method to redirect a wake from a downwind turbine. This reduces the loads and increases the power output of the downwind turbine (van dijk, wilson, fleming). However, under unfavorable conditions it can result in an asymmetrical overlap of the wake on the downwind turbine. This can significantly increase the loads of the downwind turbine [5, 6] (nog meer verwijzingen). Therefore, it is necessary to understand the effects of yawing a turbine and what this does with its wake and how this effects the downwind turbines.

Axial induction control influences the power output of a turbine by means of the blade pitch angle, and generator torque. The axial induction factor is denoted by  $a$ , and reflects the relation between the decrease in wind velocity of the free stream wind and the wind velocity leaving the rotor. By varying the axial induction factor of a wind turbine, the power output can be controlled. Loads that are introduced by varying a turbine's axial induction factor will not be discussed in this paper. As yawing of the turbine and the deflection of a wake can cause additional loads on the turbines of a wind farm, a trade-off must be made between power regulation and loads minimization.

Previous studies have mainly focused on maximizing the power output rather than regulating the power output, while also taking the loads into account, so that an optimum is found between the two (Mike van Dijk, Ben Wilson verwijzing naar wie dit heeft gedaan). However, increased loading effects on a turbine due to yaw misalignment were not considered. Furthermore, the objective of these studies is

power maximization rather than power regulation. The use of axial induction factors for regulating power output of a wind farm has been marginally studied. Power regulation through a combination of yaw control and axial induction control while minimizing loads is still novel. This paper will focus on the optimization of power regulation, by means of yaw control and axial induction control, while minimizing the loads. In addition, the loading effects on a turbine caused by yaw misalignment is studied.

Misschien nog een stukje over optimalisatie? Nog een stukje over on site of online gebruik van de optimalisatie. Misschien hier nog iets over DELs. Hier nog een overzicht van wat er in paper te vinden is. Moet later geschreven worden als de rest af is. The methods used are described in the following section.

[Intro staan veel goede dingen maar moet wat strakker.](#)

[Probeer de volgende structuur aan te houden:](#)

[Overview and motivation](#)

[Main challenge \(problem statement\)](#)

[Literature review and what is missing](#)

[General picture](#)

[Contribution of this paper](#)

[Structure of the paper](#)

## II. METHOD

To realize power regulation and minimizing loads by yaw control and axial induction control, it is necessary to know the effect of different flow conditions on the total power of the wind farm and the effect of different flow conditions on the loads for each of the turbine. Moreover there need to be an optimizer which executes the optimization to obtain a set value for the power and to minimize the loads. The total power of the wind farm is calculated in the FLORIS-model. Furthermore, FLORIS is able to adjust the turbine configurations, the

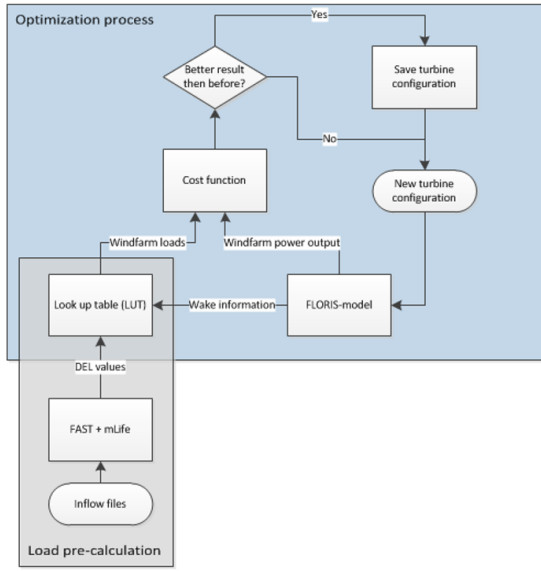


Figure 1: Overview of the optimization procedure.

axial induction and yaw position. The effect of loads on a turbine are given by the programs FAST and MLife. The output of these programs are Damage Equivalent Load values (DELs), which is a measure of equivalent load damage to the turbine concerning the material properties.[11] These DELs are calculated for a different set of wind and turbine conditions and are stored in a look-up table (LUT).

The optimizer takes the desired power production of the wind farm as an input. It then uses the configurations of the turbines from FLORIS to find the corresponding DEL values in the look-up table. If the configurations of the turbines are an improvement compared to the previous one, i.e. a improved power control or a reduce in the loads, FLORIS will save this turbine configurations. An overview of the optimization procedure is shown in Figure 1.

In the following sections, different models and model steps, used to perform the optimization, are explained:

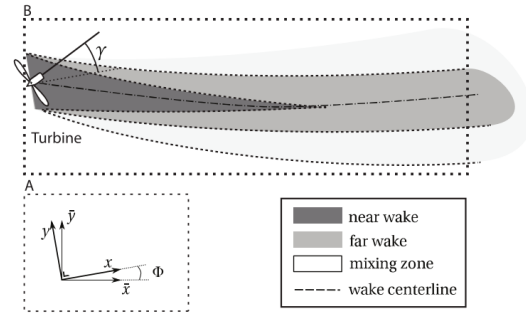


Figure 2: Simplified top view representation of a wake of a turbine by FLORIS.[8]

## i. FLORIS

The FLOW Redirection and Induction in Steady state (FLORIS) model calculates the power of the wind farm as a function of the yaw misalignment and the axial induction. [8] The advantage of FLORIS is that it is a relative accurate[6] and a low computation model, due to the fact that it uses high-fidelity data from a computational fluid dynamics simulation.

### i.1 Wake modelling

As can be seen in Figure 2, FLORIS contains a wake model which divides the wake in different zones: the near wake, the far wake, and the mixing zone,  $q = 1$ ,  $q = 2$ , and  $q = 3$  respectively. Also wake properties as location of the centerline, the diameter of the wake zones and the wind speed in each zone are calculated by FLORIS. (1 to 2).

Let  $D_i$  denote the rotor diameter of the  $i^{\text{th}}$  turbine,  $k_e$  a coefficient that describes expansion of the zones, and  $m_{e,q}$  the expansion factor which are calculated by Gebraad.[8]. The size of the wake diameter  $D_{w,q,i}$  increases proportionally to the downwind distance ( $x$ ). The diameter of the wake diameter is computed by,

$$D_{w,i,q}(x) = \max(D_i + 2k_e m_{e,q}([x - X_i], 0), 0) \quad (1)$$

Also the velocity depends on the downwind distance ( $x$ ), which is an argument of the wake

decay coefficient  $c(x, y)$ . This wake decay coefficient is multiplied by the axial induction factor and subtracted from the free stream velocity  $U_i$ . The axial induction factor is a value for the decrease in wind velocity behind a turbine relative to its own rotor speed. The wake decay coefficient describes the decay of velocity for each wake zone and is defined in 3. The model parameter  $M_{U,q}$ , which depends on the wake zone and the yaw angle, is calculated by Gebraad.[8]

$$U_{w,i}(x, y) = U_i (1 - 2a_i c_i(x, y)) \quad (2)$$

$$c_{i,q}(x) = \left[ \frac{D_i}{D_i + 2k_e m_{U,q}(\gamma_i)[x - X_i]} \right]^2 \quad (3)$$

## ii. FAST & MLife

FAST is a programming tool for the simulation of dynamic (load) responses of wind turbines (by NREL) [9]. It uses wind turbine specifications as well as wind flow situations. By evaluating a flow field, FAST computes the bending moment of a blade. Since the bending moment of a blade does not give direct information about the effect on the life-cycle time of a turbine, the program MLife is used to convert the bending moment to damage equivalent loads (DELs).

## iii. Inflow files, Flow field

FLORIS describes a discrete flow field of a wake, with three zones. The flow field of the wake in FLORIS is calculated with equations ((1 to 2)). The wake is divided into three zones as described in paragraph i.1. A real wake will not have discrete zones, but a more fluent transition between the wake zones. To create a more fluent transition between the different wake-zones a Gaussian distribution of the flow field is preferred [7]. The difference of wake shape between a Gaussian and discrete shape

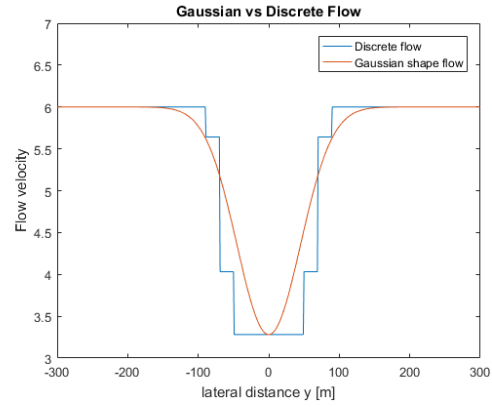


Figure 3: Discrete wake versus Gaussian wake

can be seen in Figure 3. The Gaussian distribution is calculated as followed,

$$G(y, z) = A[e^{-(\frac{y^2}{2\sigma_y} + \frac{z^2}{2\sigma_z})}] \quad (4)$$

where the amplitude of the Gaussian,  $A$ , is equal to the velocity loss of the inner wake zone,  $U_{w,1}$ , which is calculated with equation 2.  $\sigma_y$  and  $\sigma_z$  reflect the Gaussian standard deviation in horizontal and vertical direction, respectively. The standard deviations are related to the outer wake zone  $D_{w,i,q=3}$  which is given in 5,

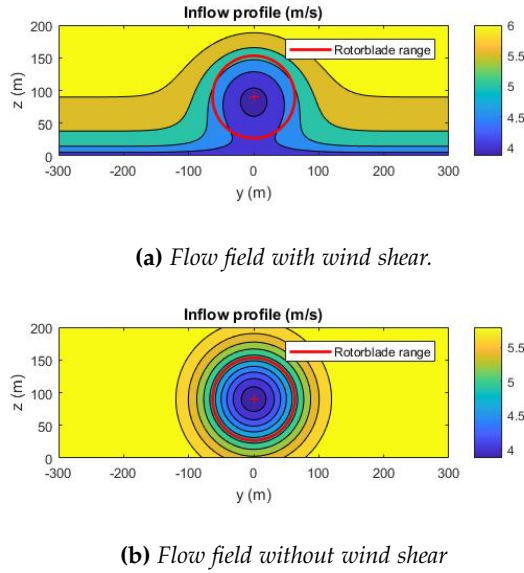
$$\sigma_y, \sigma_z = D_{w,i,q=3}/n \quad (5)$$

Where  $n$  can be modified to change the width of the Gaussian. Consequently, it is possible to fit the Gaussian to the wake zones of Gebraad. (Figure 3)

## iv. Wind shear

Wind shear can cause an important difference in velocity speeds between the rotor hub height, the end of the rotor blades at their highest points and the end of the rotor blades at their lowest point [10]. The velocity distribution is calculated with,

$$v = v_{ref} \left[ \frac{h}{h_{ref}} \right]^\alpha \quad (6)$$



**Figure 4:** Gaussian wind fields with a free stream velocity of 6 m/s at a height of 90 m. The outer diameter of the wake is 220 m and the diameter of the rotor blades is 126.4 m.

where  $v$  and  $v_{ref}$  are the velocity at heights  $h$ , and  $h_{ref}$  respectively. Value  $\alpha$  is the wind shear coefficient which depends on different factors. Coefficient  $\alpha$  is fixed at value 0.1, reflecting a terrain type close to ocean and smooth ground [10]. The wind shear is implemented in the flow field. The difference between a flow field with and without wind shear can be seen in Figure 4

## v. LUT

To reduce computational time during optimization a look-up table (LUT) is created. The LUT is created using FAST and MLife, and it contains a large number of DEL values for a wide variety of wind field conditions on a wind turbine. These different conditions are described by the ranges of the parameters (see Table 1). The parameters are wake characteristics and can be extracted from FLORIS. The parameters chosen for the LUT are:

**Table 1:** Overview of the minimum value, maximum value, and step size of the parameters, diameter of outer wake zone ( $D_{wake}$ ), free stream wind speed ( $U$ ), yaw of the turbine ( $yaw$ ), and the center to center distance between the center of the turbine and the center of the wake ( $y_{wake}$ ).

	Minimum	Maximum	Step-size
$D_{wake}$	180	330	25
$U$	6	8	2
$yaw$	-30	30	*
$y_{wake}$	-250	250	10

\*Input values for yaw are [-30, -10, -5, 0, 5, 10, 30].

- the free stream wind speed,  $U$
- the outer diameter of the wake,  $D_{wake}$
- the yaw of the turbine,  $yaw$
- the center to center distance between the turbine and the wake,  $y_{wake}$

The LUT generation is time consuming, as such, it cannot account for all integer values of the parameters. The step-size of these parameters is chosen such that interpolation will give a representative result. For each parameters step-sizes are selected, as shown in Table (see Table 1). With the use of the pre-calculated LUT, online optimization can be realized.

Linear interpolation is used to estimate the DEL values between the data points of the LUT. It is assumed that the DELs as a result of the windspeed( $U$ ) could be estimated accurately enough using only the 2 outer bounds. These bound were enough for the goal of this paper, though larger windfarms and different inflow wind velocities would require broadening these ranges.

The DEL effect of the  $D_{wake}$  was also found to be accurate enough using fairly large step-sizes. the range of this parameter was chosen so all downwind turbines within .. and .. meters could be accurately fitted.

The  $y_{wake}$  parameter however fluctuates over its range, and could not be accurately

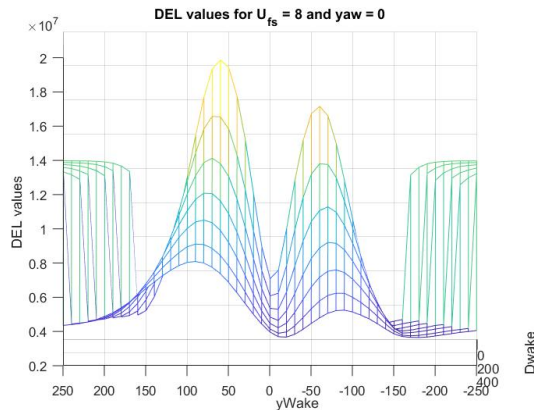


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estimated using linear interpolation over large stepsizes. as mentioned in... A stepsize of 10 meters, totaling a total of 51 steps, was found to be sufficiently accurate.

The yaw parameter is chosen at a stepsize of 10 degree, however extra data points were added at  $\pm 5$  degree to improve the accuracy in the lower yaw regions. This effect is shown in figure 5

## vi. Optimization

### Game Theory

## III. RESULTS

This chapter shall describe, compare and evaluate the results of 3 optimisation cases.

- Maximum power production
- Power production at 80 %
- Power production at 60 %

For all these cases was a 9 turbine windfarm used as shown in fig... And were simulated under constant 8 m/s wind conditions.

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*Case 1: maximum power production:* This, first, case is used to determine the maximum power output that the 9 turbine farm can extract from

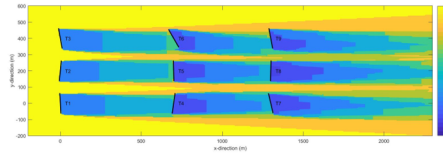


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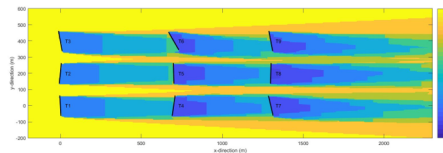


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the previously described wind conditions, this case neglects the loads.

*Case 2 and 3: Power production at 80 and 60%:* These cases are run at 80 and 60 percent of the maximum power output determined in the first case. The goal of these cases is to find the optimal running procedure given a required constant power output. The required power output chosen for this paper is linked to the maximum possible, since ...why?

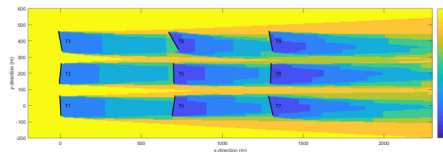


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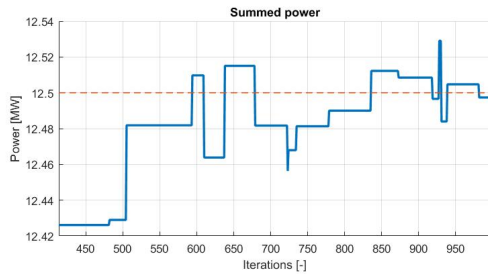


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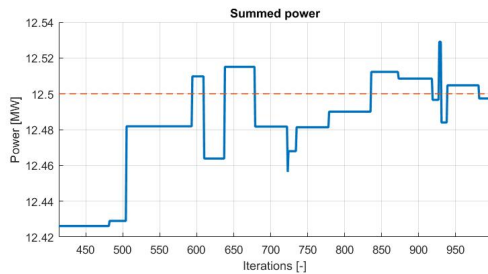


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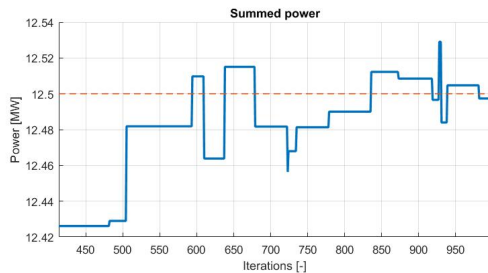


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## i. Comparing

*Power converges* reading out the maximum power, stating that power production does indeed approach the ref power

*DELs decrease* comparing loads, also among eachoter, wat is the effect of lower ref power on the loads/

*More? ....*

## IV. DISCUSSION

What have we done and how to interpret the results

Recommendations for further studies

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