# Study guide: Scientific software engineering with a simple ODE model as example

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Mar 21, 2015

# From flat program to module with functions

$$u'(t) = -au(t), \quad t \in (0, T]$$
$$u(0) = I$$

Solution by  $\theta$ -scheme:

$$u^{n+1} = \frac{1 - (1 - \theta)a\Delta t}{1 + \theta a\Delta t}u^n$$

 $\theta=0$ : Forward Euler,  $\theta=1$ : Backward Euler,  $\theta=1/2$ : Crank-Nicolson (midpoint method)

#### Many will make a rough, flat program first

```
from numpy import *
from matplotlib.pyplot import *

A = 1
a = 2
T = 4
dt = 0.2
N = int(round(T/dt))
y = zeros(N+1)
t = linspace(0, T, N+1)
theta = 1
```

```
y[0] = A
for n in range(0, N):
    y[n+1] = (1 - (1-theta)*a*dt)/(1 + theta*dt*a)*y[n]

y_e = A*exp(-a*t) - y
error = y_e - y
E = sqrt(dt*sum(error**2))
print 'Norm of the error: %.3E' % E
plot(t, y, 'r--o')
t_e = linspace(0, T, 1001)
y_e = A*exp(-a*t_e)
plot(t_e, y_e, 'b-')
legend(['numerical, theta=%g' % theta, 'exact'])
xlabel('t')
ylabel('y')
show()
```

#### There are major issues with this solution

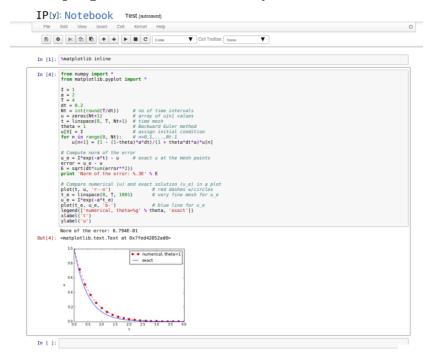
- 1. The notation in the program does not correspond exactly to the notation in the mathematical problem: the solution is called y and corresponds to u in the mathematical description, the variable A corresponds to the mathematical parameter I, N in the program is called  $N_t$  in the mathematics.
- 2. There are no comments in the program.

#### New flat program

```
from numpy import *
from matplotlib.pyplot import *
I = 1
a = 2
T = 4
dt = 0.2
Nt = int(round(T/dt)) # no of time intervals
                           # array of u[n] values
u = zeros(Nt+1)
t = linspace(0, T, Nt+1) # time mesh
theta = 1
                           # Backward Euler method
u[0] = I
                           # assign initial condition
for n in range(0, Nt):
                        # n = 0, 1, ..., Nt - 1
    u[n+1] = (1 - (1-theta)*a*dt)/(1 + theta*dt*a)*u[n]
# Compute norm of the error
u_e = I*exp(-a*t) - u
                           # exact u at the mesh points
error = u_e - u
E = sqrt(dt*sum(error**2))
print 'Norm of the error: %.3E' % E
# Compare numerical (u) and exact solution (u_e) in a plot
plot(t, u, 'r--o') # red dashes w/circles
t_e = linspace(0, T, 1001) # very fine mesh for u_e
```

```
u_e = I*exp(-a*t_e)
plot(t_e, u_e, 'b-')  # blue line for u_e
legend(['numerical, theta=%g' % theta, 'exact'])
xlabel('t')
ylabel('u')
show()
```

# Such flat programs are ideal for IPython notebooks!



# But: Further development of such flat programs require many scattered edits - easy to make mistakes!

The solution formula for  $u^{n+1}$  is completely general and should be available as a Python function with all input data as function arguments and all output data returned to the calling code

```
u[n+1] = (1 - (1-theta)*a*dt)/(1 + theta*dt*a)*u[n]
return u, t
```

Call:

```
u, t = solver(I=1, a=2, T=4, dt=0.2, theta=0.5)
```

# The DRY principle: Don't repeat yourself!

**DRY:** When implementing a particular functionality in a computer program, make sure this functionality and its variations are implemented in just one piece of code. That is, if you need to revise the implementation, there should be *one and only one* place to edit. It follows that you should never duplicate code (don't repeat yourself!), and code snippets that are similar should be factored into one piece (function) and parameterized (by function arguments).

# Make sure any program file is a valid Python module

- Module requires code to be divided into functions :-)
- Why module? Other programs can import the functions

```
from decay import solver
# Solve a decay problem
u, t = solver(I=1, a=2, T=4, dt=0.2, theta=0.5)
```

or prefix function names by the module name:

```
import decay
# Solve a decay problem
u, t = decay.solver(I=1, a=2, T=4, dt=0.2, theta=0.5)
```

#### The requirements of a module are so simple

- 1. The filename without .py must be a valid Python variable name.
- 2. The main program must be executed (through statements or a function call) in the *test block*.

The test block is normally placed at the end of a module file:

```
if __name__ == '__main__':
    # Statements
```

If the file is imported, the if test fails and no main program is run, otherwise, the file works as a program

# The module file decay.py for our example

```
from numpy import *
from matplotlib.pyplot import *
def solver(I, a, T, dt, theta):
def exact_solution(t, I, a):
   return I*exp(-a*t)
def experiment_compare_numerical_and_exact():
   I = 1; a = 2; T = 4; dt = 0.4; theta = 1
   u, t = solver(I, a, T, dt, theta)
    t_e = linspace(0, T, 1001)
                                    # very fine mesh for u e
    u_e = exact_solution(t_e, I, a)
    plot(t, u, 'r--o')
                                    # dashed red line with
       circles
    plot(t_e, u_e, 'b-')
                                    # blue line for u e
    legend(['numerical, theta=%g' % theta, 'exact'])
   xlabel('t')
   ylabel('u')
   plotfile = 'tmp'
    savefig(plotfile + '.png'); savefig(plotfile + '.pdf')
   error = exact_solution(t, I, a) - u
   E = sqrt(dt*sum(error**2))
   print 'Error norm:', E
if __name__ == '__main__':
    experiment_compare_numerical_and_exact()
```

Complete file: decay.py

#### The module file decay.py for our example w/prefix

```
import numpy as np
import matplotlib.pyplot as plt

def solver(I, a, T, dt, theta):
    ...

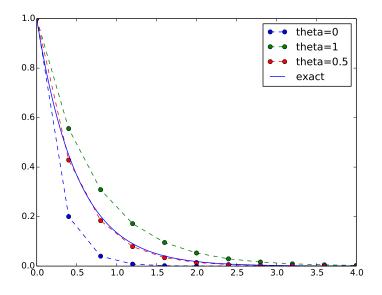
def exact_solution(t, I, a):
    return I*np.exp(-a*t)

def experiment_compare_numerical_and_exact():
    I = 1; a = 2; T = 4; dt = 0.4; theta = 1
    u, t = solver(I, a, T, dt, theta)

    t_e = np.linspace(0, T, 1001)  # very fine mesh for u_e
    u_e = exact_solution(t_e, I, a)

plt.plot(t, u, 'r--o')  # dashed red line with
    circles
```

#### How do we add code for comparing schemes visually?



Think of edits in the flat program that are required to produce this plot (!)

# We just add a new function with the tailored plotting

```
t_e = np.linspace(0, T, 1001)  # very fine mesh for u_e
u_e = exact_solution(t_e, I, a)
plt.plot(t_e, u_e, 'b-')  # blue line for u_e
legends.append('exact')
plt.legend(legends, loc='upper right')
plotfile = 'tmp'
plt.savefig(plotfile + '.png'); plt.savefig(plotfile +
    '.pdf')
```

# The comparison

#### Prefixing imported functions by the module name

MATLAB-style names (linspace, plot):

```
from numpy import *
from matplotlib.pyplot import *
```

Python community convention is to prefix with module name (np.linspace, plt.plot):

```
import numpy as np
import matplotlib.pyplot as plt
```

# Creating user interfaces

- Never edit the program to change input!
- Set input data on the command line or in a graphical user interface
- How is explained next

#### Accessing command-line arguments

- All command-line arguments are available in sys.argv
- sys.argv[0] is the program
- sys.argv[1:] holds the command-line arguments
- $\bullet$  Method 1: fixed sequence of parameters on the command line
- Method 2: --option value pairs on the command line (with default values)

```
Terminal> python myprog.py 1.5 2 0.5 0.8 0.4 Terminal> python myprog.py --I 1.5 --a 2 --dt 0.8 0.4
```

# Reading a sequence of command-line arguments

Required input:

- I
- a
- T
- name of scheme (FE, BE, CN)
- a list of  $\Delta t$  values

Give these on the command line in correct sequence

Terminal> python decay\_cml.py 1.5 0.5 4 CN 0.1 0.2 0.05

#### **Implementation**

```
def define_command_line_options():
    import argparse
    parser = argparse.ArgumentParser()
    parser.add_argument(
        '--I', '--initial_condition', type=float,
        default=1.0, help='initial condition, u(0)',
        metavar='I')
    parser.add_argument(
        '--a', type=float, default=1.0,
        help='coefficient in ODE', metavar='a')
    parser.add_argument(
        '--T', '--stop_time', type=float,
        default=1.0, help='end time of simulation',
        metavar='T')
    parser.add_argument(
        '--scheme', type=str, default='CN',
        help='FE, BE, or CN')
    parser.add_argument(
        '--dt', '--time_step_values', type=float,
        default=[1.0], help='time step values',
        metavar='dt', nargs='+', dest='dt_values')
    return parser
```

Note:

- sys.argv[i] is always a string
- Must explicitly convert to (e.g.) float for computations
- List comprehensions make lists: [expression for e in somelist]

# Working with an argument parser

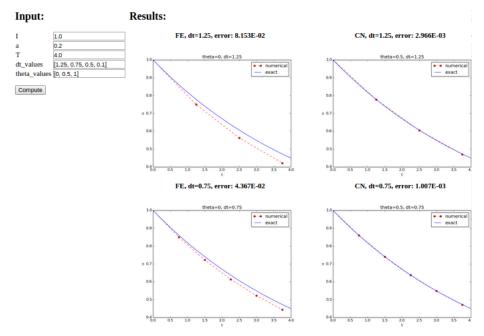
Set option-value pairs on the command line if the default value is not suitable:

Terminal> python decay\_argparse.py --I 1.5 --a 2 --dt 0.8 0.4

#### Code:

(metavar is the symbol used in help output)

# A graphical user interface



Normally very much programming required - and much competence on graphical user interfaces.

Here: use a tool to automatically create it in a few minutes (!)

# The Parampool package

• Parampool is a package for handling a large pool of input parameters in simulation programs

 Parampool can automatically create a sophisticated web-based graphical user interface (GUI) to set parameters and view solutions

**Remark.** The forthcoming material aims at those with particular interest in equipping their programs with a GUI - others can safely skip it.

# Making a compute function

- Key concept: a *compute function* that takes all input data as arguments and returning HTML code for viewing the results (e.g., plots and numbers)
- What we have: decay\_plot.py
- main function carries out simulations and plotting for a series of  $\Delta t$  values
- Goal: steer and view these experiments from a web GUI
- What to do:
  - create a compute function
  - call parampool functionality

# The compute function must return HTML code

```
def main_GUI(I=1.0, a=.2, T=4.0,
            dt_values=[1.25, 0.75, 0.5, 0.1],
            theta_values=[0, 0.5, 1]):
   # Build HTML code for web page. Arrange plots in columns
   # corresponding to the theta values, with dt down the rows
   theta2name = {0: 'FE', 1: 'BE', 0.5: 'CN'}
   html_text = '\n'
   for dt in dt_values:
       html_text += '\n'
       for theta in theta_values:
           E, html = compute4web(I, a, T, dt, theta)
           html_text += """
<center><b>%s, dt=%g, error: %.3E</b></center><br>
""" % (theta2name[theta], dt, E, html)
       html_text += '
   html_text += '\n'
   return html_text
```

# Generating the user interface

Make a file decay\_GUI\_generate.py:

Running decay\_GUI\_generate.py results in

- 1. decay\_GUI\_model.py defines HTML widgets to be used to set input data in the web interface,
- 2. templates/decay\_GUI\_views.py defines the layout of the web page,
- 3. decay\_GUI\_controller.py runs the web application.

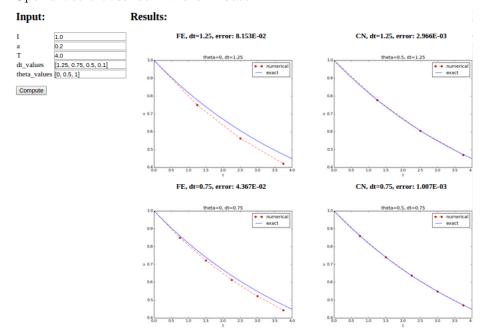
Good news: we only need to run decay\_GUI\_controller.py and there is no need to look into any of these files!

# Running the web application

Start the GUI

Terminal> python decay\_GUI\_controller.py

Open a web browser at 127.0.0.1:5000



#### More advanced use

- The compute function can have arguments of type float, int, string, list, dict, numpy array, filename (file upload)
- Alternative: specify a hierarchy of input parameters with name, default value, data type, widget type, unit (m, kg, s), validity check
- The generated web GUI can have user accounts with login and storage of results in a database

#### **Doctests**

Doc strings can be equipped with interactive Python sessions for demonstrating usage and *automatic testing* of functions.

```
def solver(I, a, T, dt, theta):
    """
    Solve u'=-a*u, u(0)=I, for t in (0,T] with steps of dt.

>>> u, t = solver(I=0.8, a=1.2, T=2, dt=0.5, theta=0.5)
>>> for t_n, u_n in zip(t, u):
    ...    print 't=%.1f, u=%.14f' % (t_n, u_n)
    t=0.0, u=0.8000000000000
t=0.5, u=0.43076923076923
t=1.0, u=0.23195266272189
t=1.5, u=0.12489758761948
t=2.0, u=0.06725254717972
"""
...
```

#### Running doctests

Automatic check that the code reproduces the doctest output:

```
Terminal> python -m doctest decay.py
```

Floats are difficult to compare. Limit the number of digits in the output in doctests! Otherwise, round-off errors on a different machine may ruin the test.

#### Unit testing with nose

- Nose and pytest are a very user-friendly testing frameworks
- Based on unit testing
- Identify (small) units of code and test each unit
- Nose automates running all tests

- Good habit: run all tests after (small) edits of a code
- Even better habit: write tests before the code (!)
- Remark: unit testing in scientific computing is not yet well established

# Basic use of nose and pytest

- 1. Implement tests in test functions with names starting with test\_.
- 2. Test functions cannot have arguments.
- 3. Test functions perform assertions on computed results using assert functions from the nose.tools module.
- 4. Test functions can be in the source code files or be collected in separate files test\*.py.

# Example on a test function in the source code

Very simple module mymod (in file mymod.py):

```
def double(n):
    return 2*n
```

Write test function in mymod.py:

```
def double(n):
    return 2*n

def test_double():
    n = 4
    expected = 2*4
    computed = double(n)
    assert expected == computed
```

Running one of

```
Terminal> nosetests -s -v mymod
Terminal> py.test -s -v mymod
```

makes the framework run all test\_\*() functions in mymod.py.

# Example on test functions in a separate file

Write the test in a separate file, say test\_mymod.py:

```
import mymod

def test_double():
    n = 4
    expected = 2*4
    computed = double(n)
    assert expected == computed
```

Running one of

```
Terminal> nosetests -s -v
Terminal> py.test -s -v
```

makes the frameworks run all test\_\*() functions in all files test\*.py in the current directory and in all subdirectories (pytest) or just those with names tests or \* tests (nose)

**Tip.** Start with test functions in the source code file. When the file contains many tests, or when you have many source code files, move tests to separate files.

#### Test function for solver

return I\*A\*\*n

Use exact discrete solution of the  $\theta$  scheme as test:

```
u^n = I \left( \frac{1 - (1 - \theta) a \Delta t}{1 + \theta a \Delta t} \right)^n def exact_discrete_solution(n, I, a, theta, dt):
    """Return exact discrete solution of the numerical schemes."""
    dt = float(dt) # avoid integer division
    A = (1 - (1-theta)*a*dt)/(1 + theta*dt*a)
```

#### Can test that potential integer division is avoided too

**Warning.** If a,  $\Delta t$ , and  $\theta$  are integers, the formula for  $u^{n+1}$  in the solver function may lead to 0 because of unintended integer division.