# Study guide: Scientific software engineering with a simple ODE model as example

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### Mathematical model problem

$$u'(t) = -au(t), \quad t \in (0, T]$$
  
$$u(0) = I$$

Solution by  $\theta$ -scheme:

$$u^{n+1} = \frac{1 - (1 - \theta)a\Delta t}{1 + \theta a\Delta t}u^n$$

 $\theta=0$ : Forward Euler,  $\theta=1$ : Backward Euler,  $\theta=1/2$ : Crank-Nicolson (midpoint method)

```
Many will make a rough, flat program first

from numpy import *
from matplotlib.pyplot import *

A = 1
a = 2
T = 4
dt = 0.2
N = int(round(T/dt))
y = zeros(N+1)
t = linspace(0, T, N+1)
theta = 1
y[0] = A
for n in range(0, N):
    y[n+i] = (1 - (i-theta)*a*dt)/(1 + theta*dt*a)*y[n]

y_e = A*exp(-a*t) - y
error = y_e - y
E = sqrt(dt*sum(error**2))
print 'Norm of the error: %.3E' % E
plot(t, y, 'r--o')
t_e = linspace(0, T, 1001)
y_e A*exp(-a*t_e)
plot(t_e, y_e, 'b-')
legend(['numerical, theta*'g' % theta, 'exact'])
zlabel('t')
ylabel('t')
ylabel('t')
show()
```

# There are major issues with this solution

- The notation in the program does not correspond exactly to the notation in the mathematical problem: the solution is called y and corresponds to u in the mathematical description, the variable A corresponds to the mathematical parameter I, N in the program is called N<sub>t</sub> in the mathematics.
- $\ensuremath{ \bullet}$  There are no comments in the program.

```
from numpy import *
from matplotlib.pyplot import *

I = 1
a = 2
T = 4
dt = 0.2
Nt = int(round(T/dt))  # no of time intervals
u = zeros(Nt+1)  # array of u(n) values
t = linspace(0, T, Nt+1)  # time mesh
theta = 1  # Backward Euler method

u[O] = I  # sasign initial condition
for n in range(0, Nt):  # n-0,1,..., Nt-1
u[n+1] = (i - (1-theta)*a*dt)/(1 + theta*dt*a)*u[n]

# Compute norm of the error
u_e = I*exp(-a*t) - u  # esact u at the mesh points
error = u_e - u
E = sqrt(dt*sum(error**2))
print 'Norm of the error: %.3E' % E

# Compare numerical (u) and esact solution (u_e) in a plot
plot(t, u, 'r-o')  # red dashes w/circles
t_e = linspace(0, T, 1001)  # very fine mesh for u_e
u_e = I*exp(-a*t-e)
plot(t, u, 'r-o')  # blue line for u_e
lezand([2]umerical theta=%" % theta, 'exact'])
```

```
Such flat programs are ideal for IPython notebooks!

IP(y): Notebook Tree passes

| Delication |
```

# But: Further development of such flat programs require many scattered edits - easy to make mistakes!

The solution formula for  $u^{n+1}$  is completely general and should be available as a Python function with all input data as function arguments and all output data returned to the calling code

### The DRY principle: Don't repeat yourself!

### DRY:

When implementing a particular functionality in a computer program, make sure this functionality and its variations are implemented in just one piece of code. That is, if you need to revise the implementation, there should be one and only one place to edit. It follows that you should never duplicate code (don't repeat yourself!), and code snippets that are similar should be factored into one piece (function) and parameterized (by function arguments).

## Make sure any program file is a valid Python module

- Module requires code to be divided into functions :-)
- Why module? Other programs can import the functions

```
from decay import solver # Solve a decay problem u, t = solver(I=1, a=2, T=4, dt=0.2, theta=0.5)
```

or prefix function names by the module name:

```
import decay
# Solve a decay problem
u, t = decay solver(I=1, a=2, T=4, dt=0.2, theta=0.5)
```

### The requirements of a module are so simple

- The filename without .py must be a valid Python variable
- The main program must be executed (through statements or a function call) in the test block.

The test block is normally placed at the end of a module file:

```
if __name__ == '__main__':
    # Statements
```

If the file is imported, the if test fails and no main program is run, otherwise, the file works as a program

```
The module file decay, py for our example
    from numpy import *
from matplotlib.pyplot import *
    def solver(I, a, T, dt, theta):
    def exact_solution(t, I, a):
         return T*exp(-a*t)
    def experiment_compare_numerical_and_exact():
    I = 1;    a = 2;    T = 4;    dt = 0.4;    theta = 1
    u, t = solver(I, a, T, dt, theta)
         t_e = linspace(0, T, 1001)
                                               # very fine mesh for u_e
         u_e = exact_solution(t_e, I, a)
          plot(t, u, 'r--o')
                                                # dashed red line with circles
          plot(t_e, u_e, 'b-')
                                                 # blue line for u_e
          legend(['numerical, theta=%g' % theta, 'exact'])
         xlabel('t')
         plotfile = 'tmp'
savefig(plotfile + '.png'); savefig(plotfile + '.pdf')
          error = exact_solution(t, I, a) - u
         E = sqrt(dt*sum(error**2))
print 'Error norm:', E
```

```
The module file decay.py for our example w/prefix
     import numpy as np
import matplotlib.pyplot as plt
     def solver(I, a, T, dt, theta):
     def exact_solution(t, I, a):
          return I*np.exp(-a*t)
     def experiment_compare_numerical_and_exact():
    I = 1;    a = 2;    T = 4;    dt = 0.4;    theta = 1
    u, t = solver(I, a, T, dt, theta)
          t_e = np.linspace(0, T, 1001)
                                                           # very fine mesh for u_e
          u_e = exact_solution(t_e, I, a)
           plt.plot(t, u, 'r--o')
                                                        # dashed red line with circles
          plt.plot(t_e, u_e, 'b-') # dashed red line we plt.plot(t_e, u_e, 'b-') # blue line for u_e plt.legend(['numerical, theta=%g' % theta, 'exact']) plt.xlabel('t')
           plt.ylabel('u')
           plt.savefig(plotfile + '.png'); plt.savefig(plotfile + '.pdf')
           error = exact_solution(t, I, a) - u
          E = np.sqrt(dt*np.sum(error**2))
print 'Error norm:', E
```

# How do we add code for comparing schemes visually? Output O

# def experiment\_compare\_schemes(): """Compare theta=0,1,0.5 in the same plot.""" I = 1; a = 2; T = 4; dt = 0.4 legends = [] for theta in [0, 1, 0.5]: u, t = solver(I, a, T, dt, theta) plt.plot(t, u, '--o') legends append('theta=%g' % theta) t.e = np.linspace(0, T, 1001) # very fine mesh for u.e u.e = exact\_solution(t.e, I, a) plt.plot(t.e, u.e, 'b-') # blue line for u.e legends.append('exact') plt.legend(legends, loc='upper right') pltofile = 'temp' plt.savefig(plotfile + '.png'); plt.savefig(plotfile + '.pdf')

```
Prefixing imported functions by the module name

MATLAB-style names (linspace, plot):

from numpy import *
from matplotlib.pyplot import *

Python community convention is to prefix with module name (np.linspace, plt.plot):

import numpy as np import matplotlib.pyplot as plt
```

```
One of the program to change input!

Set input data on the command line or in a graphical user interface

How is explained next
```

```
Accessing command-line arguments

All command-line arguments are available in sys.argv

sys.argv [0] is the program

sys.argv [1:] holds the command-line arguments

Method 1: fixed sequence of parameters on the command line

Method 2: --option value pairs on the command line (with default values)

Terminal > python myprog.py 1.5 2 0.5 0.8 0.4

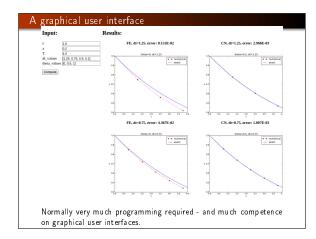
Terminal > python myprog.py --I 1.5 --a 2 --dt 0.8 0.4
```

```
Required input:

• I
• a
• T
• name of scheme (FE, BE, CN)
• a list of \Delta t values

Give these on the command line in correct sequence

Terminal> python decay_cml.py 1.5 0.5 4 CN 0.1 0.2 0.05
```



# Making a compute function Key concept: a compute function that takes all input data as arguments and returning HTML code for viewing the results (e.g., plots and numbers) What we have: decay\_plot.py main function carries out simulations and plotting for a series of Δt values Goal: steer and view these experiments from a web GUI What to do: create a compute function call parampool functionality

# 

# The Parampool package

- Parampool is a package for handling a large pool of input parameters in simulation programs
- Parampool can automatically create a sophisticated web-based graphical user interface (GUI) to set parameters and view solutions

### Remark

The forthcoming material aims at those with particular interest in equipping their programs with a GUI - others can safely skip it.

### Generating the user interface

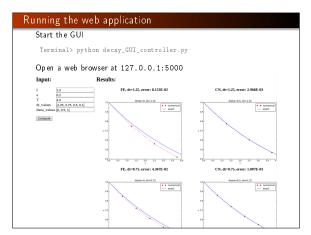
```
Make a file decay_GUI_generate.py:
```

```
from parampool.generator.flask import generate
from decay import main_GUI
generate(main_GUI,
    filename_controller='decay_GUI_controller.py',
    filename_template='decay_GUI_view.py',
    filename_model='decay_GUI_model.py')
```

Running decay\_GUI\_generate.py results in

- decay\_GUI\_model.py defines HTML widgets to be used to set input data in the web interface,
- templates/decay\_GUI\_views.py defines the layout of the web page,
- decay\_GUI\_controller.py runs the web application.

Good news: we only need to run decay\_GUI\_controller.py and there is no need to look into any of these files!



### More advanced use

- The compute function can have arguments of type float, int, string, list, dict, numpy array, filename (file upload)
- Alternative: specify a hierarchy of input parameters with name, default value, data type, widget type, unit (m, kg, s), validity check
- The generated web GUI can have user accounts with login and storage of results in a database

### Doctests

Doc strings can be equipped with interactive Python sessions for demonstrating usage and *automatic testing* of functions.

## Running doctests

Automatic check that the code reproduces the doctest output:

Terminal > python -m doctest decay.py

### Floats are difficult to compare

Limit the number of digits in the output in doctests! Otherwise, round-off errors on a different machine may ruin the test.

## Unit testing with nose

- Nose and pytest are a very user-friendly testing frameworks
- Based on unit testing
- Identify (small) units of code and test each unit
- Nose automates running all tests
- Good habit: run all tests after (small) edits of a code
- Even better habit: write tests before the code (!)
- Remark: unit testing in scientific computing is not yet well established

### Basic use of nose and pytest

- Implement tests in test functions with names starting with test.
- Test functions cannot have arguments.
- Test functions perform assertions on computed results using assert functions from the nose.tools module.
- Test functions can be in the source code files or be collected in separate files test\*.py.

### Example on test functions in a separate file

Write the test in a separate file, say test\_mymod.py:

```
def test_double():
    n = 4
    expected = 2*4
    computed = double(n)
    assert expected == computed
```

### Running one of

import mymod

```
Terminal> nosetests -s -v
Terminal> py.test -s -v
```

makes the frameworks run all test\_\*() functions in all files test\*.py in the current directory and in all subdirectories (pytest) or just those with names tests or \*\_tests (nose)

### Tip

Start with test functions in the source code file. When the file contains many tests, or when you have many source code files, move tests to separate files.

# Can test that potential integer division is avoided too

### Warning

If  $a,\ \Delta t,$  and  $\theta$  are integers, the formula for  $u^{n+1}$  in the solver function may lead to 0 because of unintended integer division.

### Example on a test function in the source code

```
Very simple module mymod (in file mymod.py):
```

```
def double(n):
```

Write test function in mymod.py:

```
def double(n):
    return 2*n

def test_double():
    n = 4
    expected = 2*4
    computed = double(n)
    assert expected == computed
```

### Running one of

```
Terminal> nosetests -s -v mymod
Terminal> py.test -s -v mymod
```

makes the framework run all test\_\*() functions in mymod.py.

### Test function for solver

assert success

Use exact discrete solution of the  $\theta$  scheme as test:

$$u^n = I \left( \frac{1 - (1 - \theta) a \Delta t}{1 + \theta a \Delta t} \right)'$$