Lecture 1: Basic R

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Basic

- help system: ?, '??'. eg. ?seq, ??sequence
- c()
- arithmetic
- logical vector & | !=, any, all
- factor
- character
- missing values NA, NaN
- index vector for selection a[]. Either positive integer or logical vector.

example

```
# logical vectors
logi_1 = c(T,T,F)
logi_2 = c(F,T,T)

logi_12 = logi_1 & logi_2
print(logi_12)
```

[1] FALSE TRUE FALSE

Arrays

An array is a table of numbers. A matrix is a 2-dimensional array.

- array arithmetic: element-by-element.
- %*%, solve, eigen

example: simple regression—OLS estimation with one x regressor and a constant.

- literally translate $\hat{\beta} = (X'X)^{-1}X'y$ into code.
- t-statistic: $\left(\hat{\beta}_2 \beta_{02}\right)/\hat{\sigma}_{\hat{\beta}_2}$.

```
# check the OLS fitting
rm(list = ls())
set.seed(111) # can be removed to allow the result to change

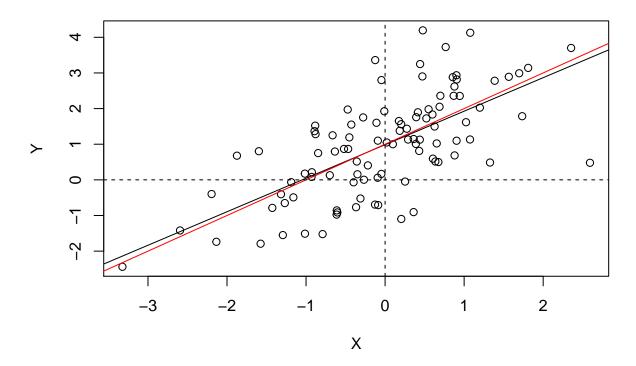
# set the parameters
n = 100
b0 = matrix(1, nrow = 2)

# generate the data
e = rnorm(n)
X = cbind(1, rnorm(n))
Y = X %*% b0 + e

# OLS estimation
bhat = solve(t(X) %*% X, t(X)%*% Y)
```

```
# plot
plot( y = Y, x = X[,2], xlab = "X", ylab = "Y", main = "regression")
abline( a= bhat[1], b = bhat[2])
abline( a = b0[1], b = b0[2], col = "red")
abline( h = 0, lty = 2)
abline( v = 0, lty = 2)
```

regression



```
# calculate the t-value
bhat2 = bhat[2] # parameter we want to test
e_hat = Y - X %*% bhat
sigma_hat_square = sum(e_hat^2)/ (n-2)
sig_B = solve( t(X) %*% X ) * sigma_hat_square
t_value_2 = ( bhat2 - b0[2]) / sqrt( sig_B[2,2] )
print(t_value_2)
```

[1] -0.5615293

Packages

An initial installation of R is small, but R has an extensive system of add-on packages. A package can be installed and invoked by

```
install.packages("package_name")
library(package_name)
```

eg: The following packages are useful for parallel computing.

```
library(AER)
## Loading required package: car
## Loading required package: lmtest
## Loading required package: zoo
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
##
       as.Date, as.Date.numeric
## Loading required package: sandwich
## Loading required package: survival
Mixed data types
  • list
  • data.frame
data("CreditCard")
head(CreditCard)
     card reports
                       age income
                                         share expenditure owner selfemp
                0 37.66667 4.5200 0.033269910 124.983300
## 1 yes
                                                             yes
                                                                      no
                0 33.25000 2.4200 0.005216942
## 2
      yes
                                                  9.854167
                                                              no
                                                                      no
## 3
               0 33.66667 4.5000 0.004155556
                                                 15.000000
      yes
                                                             yes
                                                                      no
                0 30.50000 2.5400 0.065213780 137.869200
## 4
      yes
                                                             no
                                                                      no
## 5
      yes
                0 32.16667 9.7867 0.067050590 546.503300
                                                             yes
                                                                      no
## 6 yes
                0 23.25000 2.5000 0.044438400
                                               91.996670
                                                              no
                                                                      no
     dependents months majorcards active
## 1
              3
                    54
                                1
                                       12
## 2
              3
                                1
                                       13
                    34
## 3
              4
                    58
                                1
                                        5
## 4
              0
                                        7
                    25
                                1
## 5
              2
                                        5
                    64
                                1
## 6
                    54
                                        1
help(CreditCard)
## starting httpd help server ...
## done
Input and output
  • read.table()
  • write.table()
example
HEX = read.csv("http://ichart.finance.yahoo.com/table.csv?s=0388.HK")
print(head(HEX))
```

write.csv(HEX, file = "HEX.csv")

Statitics

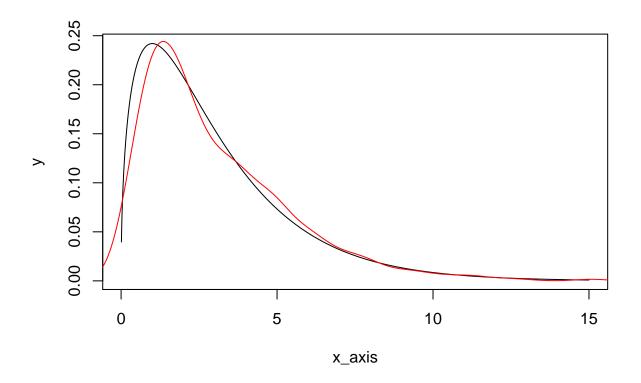
• p, d, q, r

example:

- 1. plot the density of $\chi^2(3)$ over x_axis = seq(0.01, 15, by = 0.01)
- 2. generate 1000 observations for the above distribution. plot the kernel density.
- 3. calculate the 95-th quantile and the empirical probability of observing a value greater than the 95-th quantile.

```
set.seed(888)
x_axis = seq(0.01, 15, by = 0.01)

y = dchisq(x_axis, df = 3)
plot(y = y, x=x_axis, type = "l")
z = rchisq(1000, df = 3)
lines( density(z), col = "red")
```



```
crit = qchisq(.95, df = 3)
mean( z > crit )
## [1] 0.047
```

User-defined function

• fun_name = function(args) {expressions}

• variables defined in a functions are local.

example: given a sample, calculate the 95% two-sided asymptotic confidence interval according to a central limit theorem.

```
# construct confidence interval

CI = function(x){
    # x is a vector of random variables

n = length(x)
    mu = mean(x)
    sig = sd(x)
    upper = mu + 1.96/sqrt(n) * sig
    lower = mu - 1.96/sqrt(n) * sig
    return( list( lower = lower, upper = upper) )
}
```

Flow control

- if
- for, while

example: calculate the empirical coverage probability of a poisson distribution of degree of freedom 2.

```
Rep = 1000
sample_size = 100
capture = rep(0, Rep)

pts0 = Sys.time() # check time
for (i in 1:Rep){
   mu = 2
   x = rpois(sample_size, mu)
   bounds = CI(x)
   capture[i] = ( ( bounds$lower <= mu  ) & (mu <= bounds$upper) )
}
mean(capture) # empirical size</pre>
```

```
## [1] 0.938
pts1 = Sys.time() - pts0 # check time elapse
print(pts1)
```

Time difference of 0.06104398 secs

Statistical models

• lm(y~x, data =)