

Lecture 1: Basic R

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Basic

- help system: `?`, `'??'` eg. `?seq`, `??sequence`
- `c()`
- arithmetic
- logical vector `!=`, `&` vs `&&`, `any`, `all`
- factor
- character
- missing values `NA`, `NaN`
- index vector for selection `a[]`. Either positive integer or logical vector.

example

```
# logical vectors
logi_1 = c(T,T,F)
logi_2 = c(F,T,T)

logi_12 = logi_1 & logi_2
print(logi_12)
```

```
## [1] FALSE TRUE FALSE
```

Arrays

- array arithmetic. elementwise.
- `%*%`, solve, eigen
- matrix

example: OLS estimator with one x regressor and a constant

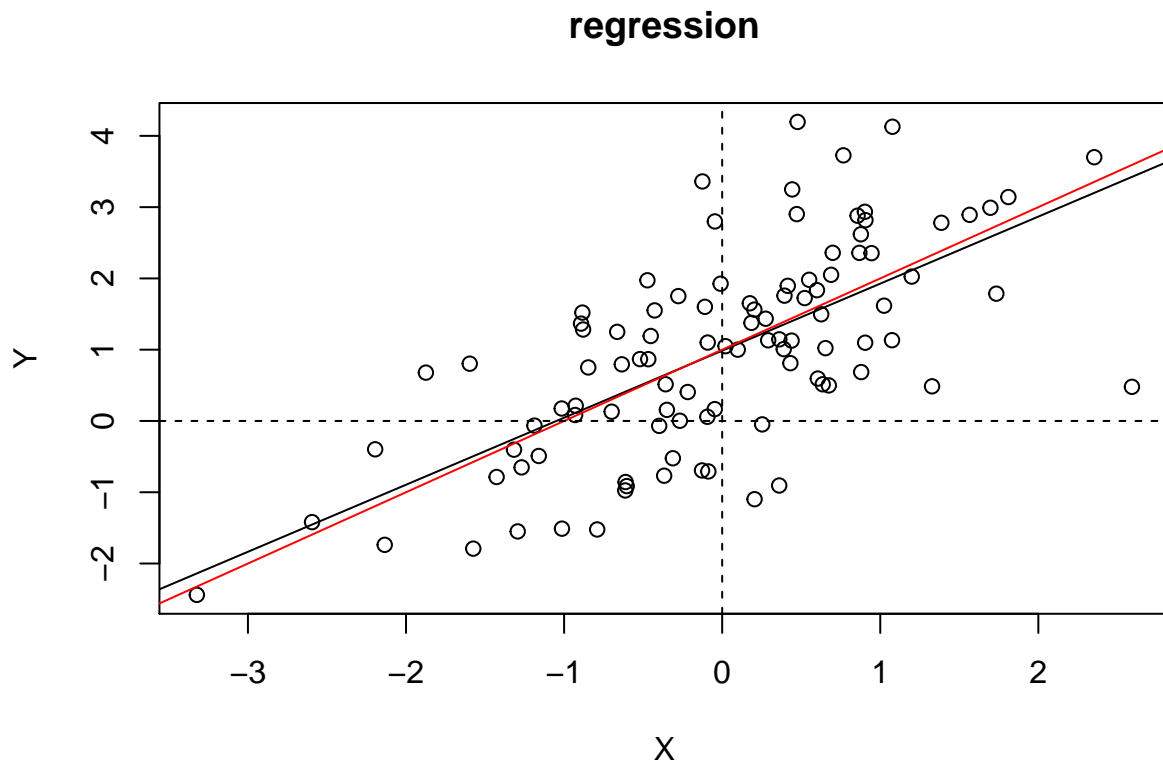
```
# check the OLS fitting
rm(list = ls( ))
set.seed(111)

# set the parameters
n = 100
b0 = matrix(1, nrow = 2 )

# generate the data
e = rnorm(n)
X = cbind( 1, rnorm(n) ) # you can try this line. See what is the difference.
Y = X %*% b0 + e

# OLS estimation
bhat = solve( t(X) %*% X, t(X)%*% Y )
```

```
# plot
plot( y = Y, x = X[,2], xlab = "X", ylab = "Y", main = "regression")
abline( a= bhat[1], b = bhat[2])
abline( a = b0[1], b = b0[2], col = "red")
abline( h = 0, lty = 2)
abline( v = 0, lty = 2)
```



```
# calculate the t-value
bhat2 = bhat[2] # parameter we want to test
e_hat = Y - X %*% bhat
sigma_hat_square = sum(e_hat^2)/ (n-2)
sig_B = solve( t(X) %*% X ) * sigma_hat_square
t_value_2 = ( bhat2 - b0[2]) / sqrt( sig_B[2,2] )
print(t_value_2)
```

```
## [1] -0.5615293
```

Mixed data types

- list
- data.frame

Input and output

- `read.table()`
- `write.table()`

example

```
HEX = read.csv("http://ichart.finance.yahoo.com/table.csv?s=0388.HK")
print(head(HEX))
write.csv(HEX, file = "HEX.csv")
```

Statistics

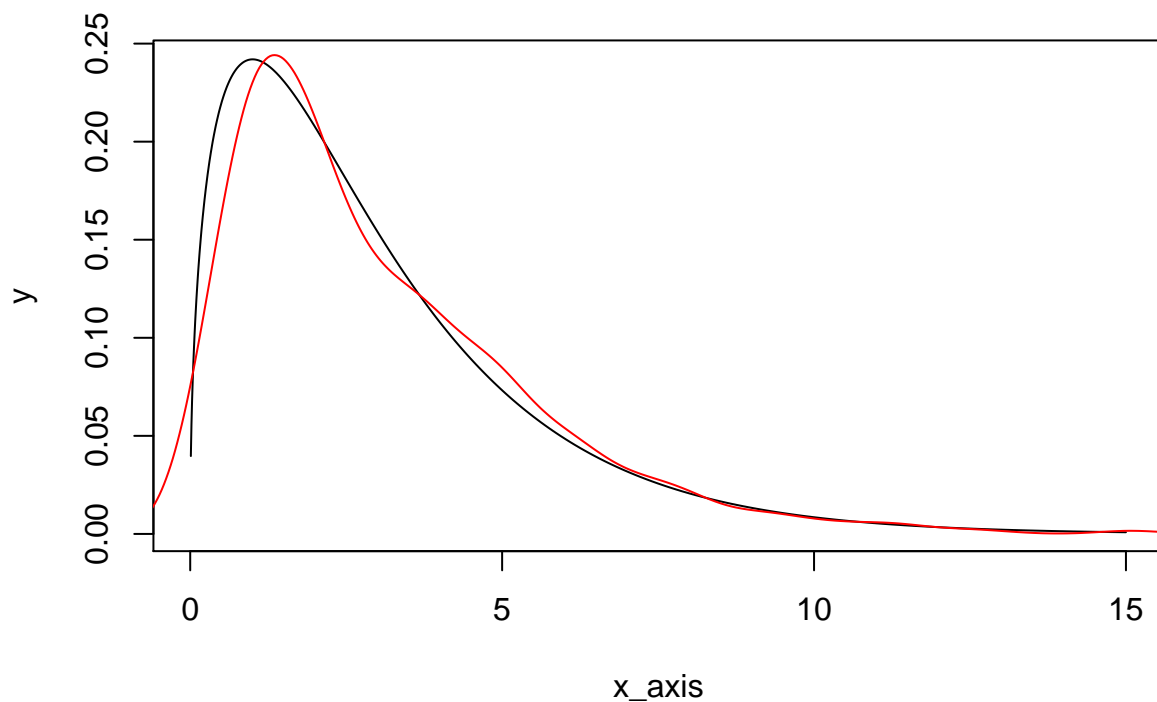
- `p`, `d`, `q`, `r`

example:

1. plot the density of $\chi^2(3)$ over `x_axis = seq(0.01, 15, by = 0.01)`
2. generate 1000 observations for the above distribution. plot the kernel density.
3. calculate the 95-th quantile and the empirical probability of observing a value greater than the 95-th quantile.

```
set.seed(888)
x_axis = seq(0.01, 15, by = 0.01)

y = dchisq(x_axis, df = 3)
plot(y = y, x=x_axis, type = "l")
z = rchisq(1000, df = 3)
lines( density(z), col = "red")
```



```
crit = qchisq(.95, df = 3)
mean( z > crit )
```

```
## [1] 0.047
```

User-defined function

- `fun_name = function(args) {expressions}`
- variables defined in a functions are local.

example: given a sample, calculate the 95% two-sided asymptotic confidence interval according to a central limit theorem.

```
# construct confidence interval

CI = function(x){
  # x is a vector of random variables

  n = length(x)
  mu = mean(x)
  sig = sd(x)
  upper = mu + 1.96/sqrt(n) * sig
  lower = mu - 1.96/sqrt(n) * sig
```

```

    return( list( lower = lower, upper = upper) )
}

```

Flow control

- if
- for, while

example: calculate the empirical coverage probability of a poisson distribution of degree of freedom 2.

```

Rep = 1000
sample_size = 100
capture = rep(0, Rep)

pts0 = Sys.time() # check time
for (i in 1:Rep){
  mu = 2
  x = rpois(sample_size, mu)
  bounds = CI(x)
  capture[i] = ( ( bounds$lower <= mu ) & (mu <= bounds$upper) )
}
mean(capture) # empirical size

```

```
## [1] 0.938
```

```

pts1 = Sys.time() - pts0 # check time elapse
print(pts1)

```

```
## Time difference of 0.06004214 secs
```

Statistical models

- `lm(y~x, data =)`