

1, 2, 3, 4, 5

**1** A graph is *outerplanar* if it has an embedding in the plane in which all of its vertices appear on the infinite external face. Show that in an outerplanar graph with  $n \geq 3$  vertices and  $m$  edges,  $m \leq 2n - 3$ .

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2 Show that  $K_4$  is not outerplanar.

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**3** Show that  $K_{2,3}$  is not outerplanar.

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4 Show that a planar graph has a vertex with degree at most 5.

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5 A *maximal planar* graph is a planar graph to which no edge may be added without making it non-planar. Show that a maximal planar graph has at least 4 vertices with degree at most 5.

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