$3.3.24,\ 3.4.\big\{4,\ 7,\ 12,\ 13,\ 16,\ 23\big\}$ 

**Colley 3.3.24** Consider the vector field  $\mathbf{F} = 2x\mathbf{i} + 2y\mathbf{j} - 3\mathbf{k}$ .

- (a) Show that  $\mathbf{F}$  is a gradient field.
- (b) Describe the equipotential surfaces of **F** in words and with sketches.

1

**Colley 3.4.4** Calculate the divergence of the vector fields given in Exercises 1-6.

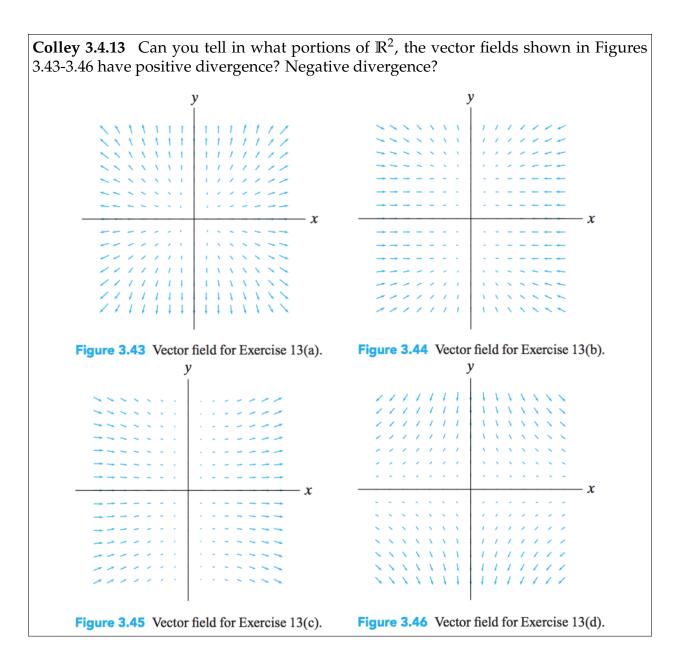
$$\mathbf{F} = z\cos(e^{y^2})\,\mathbf{i} + x\sqrt{z^2 + 1}\,\mathbf{j} + e^{2y}\sin 3x\,\mathbf{k}$$

**Colley 3.4.7** Find the curl of the vector fields given in Exercises 7-11.

$$\mathbf{F} = x^2 \,\mathbf{i} - xe^y \,\mathbf{j} + 2xyz \,\mathbf{k}$$

## **Colley 3.4.12**

- (a) Consider again the vector field in Exercise 8 and its curl. Sketch the vector field and use your picture to explain geometrically why the curl is as you calculated.
- (b) Use geometry to determine  $\nabla \times \mathbf{F}$ , where  $\mathbf{F} = \frac{(x\mathbf{i} + y\mathbf{j} + z\mathbf{k})}{\sqrt{x^2 + y^2 + z^2}}$ .
- (c) For **F** as in part (b), verify your intuition by explicitly computing  $\nabla \times \mathbf{F}$ .



Colley 3.4.16 Prove Theorem 4.4.

**Colley 3.4.23** In Exercises 21-25, establish the given identities. (You may assume that any functions and vector fields are appropriately differentiable.)

$$\nabla \cdot (f\mathbf{F}) = f\nabla \cdot \mathbf{F} + \mathbf{F} \cdot \nabla f$$