

```
def luhn_sum(n):  
    if n < 10:  
        return n  
    else:  
        all_but_last, last = split(n)  
        return luhn_sum_double(all_but_last) + last
```

```
def luhn_sum_double(n):  
    all_but_last, last = split(n)  
    luhn_digit = sum_digits(2 * last)  
    if n < 10:  
        return luhn_digit  
    else:  
        return luhn_sum(all_but_last) + luhn_digit
```