

Date: _____

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Resolution of FOL

1. It is crime for an American to sell weapons to hostile nations.

$$\text{American}(x) \wedge \text{Weapon}(y) \wedge \text{Sells}(x, y, z) \wedge \text{Hostile}(z) \rightarrow \text{Criminal}(x)$$

$$\neg [\text{American}(x) \wedge \text{Weapon}(y) \wedge \text{Sells}(x, y, z) \wedge \text{Hostile}(z)] \vee \text{Criminal}(x)$$

$$\neg \text{American}(x) \vee \neg \text{Weapon}(y) \vee \neg \text{Sells}(x, y, z) \vee \neg \text{Hostile}(z) \vee \text{Criminal}(x)$$

Nono has some missile

$$\exists x : \text{Owns}(\text{Nono}, x) \wedge \text{Missile}(x)$$

$$\text{Owns}(\text{Nono}, m_i) \wedge \text{Missile}(m_i)$$

All of its missiles were sold to it by Colonel West.

$$\forall x \text{ Missile}(x) \wedge \text{Owns}(\text{Nono}, x) \rightarrow \text{Sells}(\text{West}, x, \text{Nono})$$

$$\neg \forall x (\text{Missile}(x) \wedge \text{Owns}(\text{Nono}, x)) \vee \text{Sells}(\text{West}, x, \text{Nono})$$

$$\neg \neg \text{Missile}(x) \vee \neg \text{Owns}(\text{Nono}, x) \vee \text{Sells}(\text{West}, x, \text{Nono})$$

Missiles are weapons:

$\text{Missile}(x) \rightarrow \text{Weapon}(x)$

$\neg \text{Missile}(x) \vee \text{Weapon}(x)$

An enemy of America counts as 'hostile':

$\text{Enemy}(x, \text{America}) \rightarrow \text{Hostile}$

$\neg \text{Enemy}(x, \text{America}) \vee \text{Hostile}$

West, who is American...

$\text{American}(\text{West})$

The Country Nono, an enemy of America.

$\text{Enemy}(\text{Nono}, \text{America})$

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Prove: Criminal (west)

\neg Criminal (west)

\neg American (x) \vee \neg Weapon (y) \vee \neg Sells (x, y, z)
 \vee \neg Hostile (z) \vee Criminal (x)

\neg Criminal (west)

\neg American (west) \vee \neg Weapon (y) \vee \neg Sells (x, y, z)
 \vee \neg Hostile (z)

American (west)

\neg Weapon (y) \vee \neg Sells (west, y, z)
 \vee \neg Hostile (z)

\neg Missile (x) \vee Weapon

\neg Missile (y) \vee \neg Sells (west, y, z)
 \vee \neg Hostile (z)

Missile (M₁)

\neg Sells (west, y, z) \vee \neg Hostile (z)

\neg Missile (x) \vee \neg Owns (Nono, x) \vee Sells (west, x, Nono)

\neg Missile (M₁) \vee \neg Owns (Nono, M₁) \vee \neg Hostile (Nono)

Missile (M₁)

\neg Owns (Nono, M₁) \vee \neg Hostile (Nono)

\neg Hostile (Nono)

Owns (Nono, M₁)

\neg Enemy (x, America) \vee Hostile (x)

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