

1.

- a) $\{1, -1\}$
- b) $\{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11\}$
- c) $\{1, 4, 9, 16, 25, 36, 49, 64, 81\}$
- d) $\{\emptyset\}$

2.

- a) $\{x \mid x \text{ is a integer such that } x = 3 \cdot n \text{ where } 0 \leq n \leq 4\}$
- b) $\{x \mid -3 \leq x \leq 3\}$
- c) $\{x \in \mathbb{Z} \mid x \text{ is the alphabet letters where } m \leq x \leq p\}$

3.

- a) equal
- b) not equal
- c) not equal

4. $B \subset A, C \subset D, C \subset A$

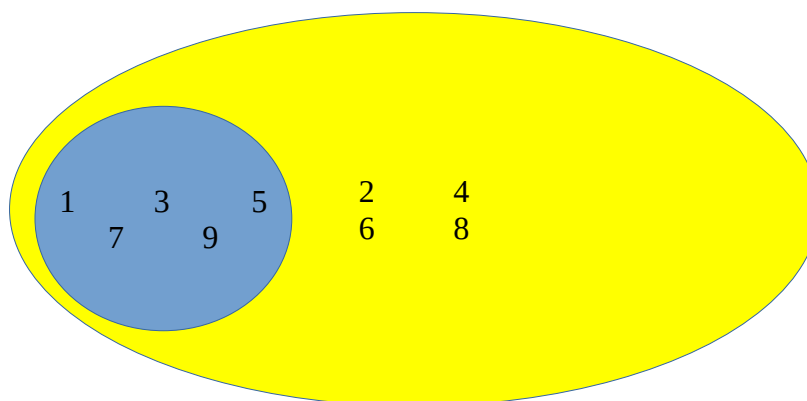
5.

- a) yes
- b) no
- c) yes
- d) no
- e) no
- f) no

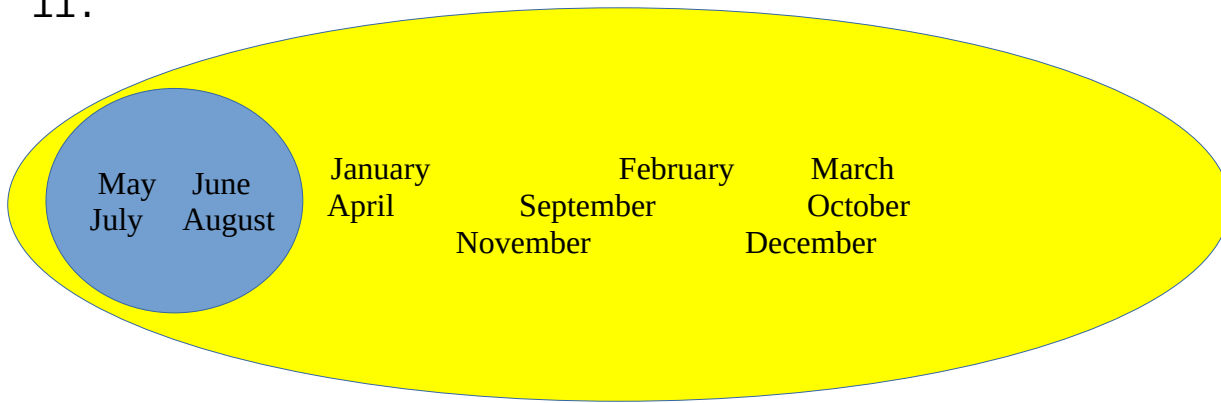
6.

- a) no
- b) no
- c) yes
- d) yes
- e) yes
- f) no

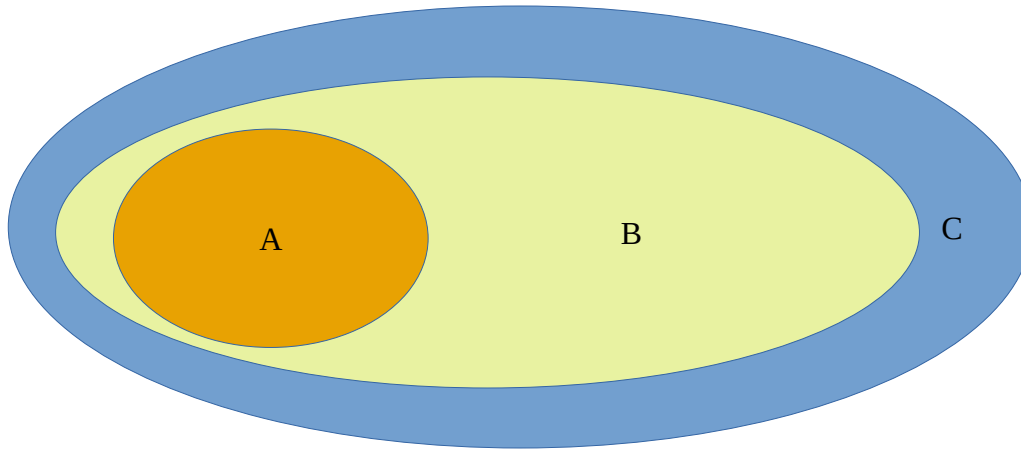
10.



11.



15.



suppose we have element a $a \in A$ if $a \in A$, then $a \in B$ which implies a is in c

16.

$A = \{1, 2\}$, $B = \{1, 2, \{1, 2\}\}$

17.

- a) 1
- b) 1
- c) 2
- d) 3

18.

- a) 0
- b) 1
- c) 2
- d) 3

20. yes

if $P(a) = P(b)$, then $a \subset b \wedge b \subset a$ leading to $a = b$

21.

- a) 8
- b) 16
- c) 2

23.

a)

- $(a, y), (a, z)$
- $(b, y), (b, z)$
- $(c, y), (c, z)$
- $(d, y), (d, z)$

b)

- $(y, a), (y, b), (y, c), (y, d)$
- $(z, a), (z, b), (z, c), (z, d)$

26. a and b are empty sets

27. from the definition of cartesian products

$A \times B = \{(a, b) \mid a \in A \wedge b \in B\}$, and since b is \emptyset then
 $A \times \emptyset$ is \emptyset .

30.

suppose that A is the set $\{a_1, a_2, \dots, a_n\}$ and B is $\{b_1, b_2, \dots, b_n\}$ then

$A \times B$ is $\{(a_1, b_1), (a_2, b_2), \dots (a_n, b_n)\}$

and

$B \times A$ is $\{(b_1, a_1), (b_2, a_2), \dots (b_n, a_n)\}$

which is not equal!

31.

let A be the set $\{a_1, a_2, \dots, a_n\}$

and B $\{b_1, b_2, \dots, b_n\}$

and C $\{c_1, c_2, \dots, c_n\}$

$A \times B \times C = \{(a_1, b_1, c_1), (a_1, b_1, c_2), \dots (a_n, b_n, c_n)\}$

and

$(A \times B) \times C = \{((a_1, b_1), c_1), ((a_2, b_2), c_2), \dots ((a_n, b_n), c_n)\}$

33.

- a) for every real number x , there is no x such that $x^2 = -1$
- b) there exists an integer x , such that $x^2 = 2$
- c) for every integer x , $x^2 > 0$
- d) there exists integer x , such that $x^2 = x$

34.

- a) there exist a real number x , such that $x^3 = -1$
- b) there exists integer x , such that $x + 1 > x$
- c) for every integer x , $x - 1$ is also an integer
- d) for every integer x , x^2 is also an integer

39. we start by choosing by computing every possible combination of the current number of members to choose from to n (number of the elements on the set)