$success: 1 \rightarrow p$   $failure: 0 \rightarrow q$  p+q=1

$$\mu_1 = 1 \cdot p = p$$

$$\sigma_1^2 = (1 - \mu_1)^2 p + (0 - \mu_1)^2 q = (1 - p)^2 p + (0 - p)^2 (1 - p)$$

$$= (1 - p)(p - p^2 + p^2) = p(1 - p) = pq$$

$$\therefore \mu = np$$

$$\therefore \sigma^2 = npq$$

(2) 
$$f(x) = \binom{n}{x} p^x q^{n-x} \qquad @ x = m : f(x) \to maxima$$
 
$$@ x = m : \ln f(x) \to maxima$$

$$f = f(x)$$
  $f' = f'(x)$   $f'(m) = [f'(x)]_{x=m}$   
 $f'(m) = 0$   $(\ln f)'(m) = 0$ 

$$\ln f = \ln f(m) + (\ln f)'(m) (x - m) + \frac{1}{2} (\ln f)''(m) (x - m)^2 + \frac{1}{6} (\ln f)'''(m) (x - m)^3 + \cdots$$

$$\approx \ln f(m) + \frac{1}{2} (\ln f)''(m) (x - m)^2$$

$$f \approx f(m) e^{\frac{1}{2} (\ln f)''(m) (x - m)^2}$$

$$\ln f = \ln \left( \frac{n!}{(n-x)!x!} p^x q^{n-x} \right) = \ln n! - \ln(n-x)! - \ln x! + \ln p^x + \ln q^{n-x}$$

$$\approx n \ln n - n - (n-x) \ln(n-x) + (n-x) - x \ln x + x + x \ln p + (n-x) \ln q$$

$$= n \ln n - n - n \ln(n-x) + x \ln(n-x) + n - x - x \ln x + x + x \ln p + n \ln q - x \ln q$$

$$(\ln f)' = -n \frac{-1}{n-x} + \ln(n-x) + x \frac{-1}{n-x} - 1 - (\ln x + 1) + 1 + \ln p - \ln q$$

$$= \frac{n}{n-x} + \ln(n-x) - \frac{x}{n-x} - 1 - \ln x - 1 + 1 + \ln p - \ln q$$

$$= 1 + \ln(n-x) - 1 - \ln x - 1 + 1 + \ln p - \ln q = \ln(n-x) - \ln x + \ln p - \ln q = \ln \left( \frac{(n-x)p}{xq} \right)$$

$$(\ln f)'(m) = 0$$
 
$$\ln \left(\frac{(n-m)p}{mq}\right) = 0 \qquad \frac{(n-m)p}{mq} = 1$$

$$(n-m)p = mq$$
  $np - mp = mq$   $np = m(p+q)$   $\therefore m = np = \mu$ 

$$(\ln f)'' = (\ln(n-x) - \ln x + \ln p - \ln q)' = -\frac{1}{n-x} - \frac{1}{x}$$

$$(\ln f)''(m) = -\frac{1}{n-m} - \frac{1}{m} = -\frac{1}{n-np} - \frac{1}{np} = -\frac{1}{nq} - \frac{1}{np} = \frac{-p-q}{npq} = -\frac{1}{npq} = -\frac{1}{\sigma^2}$$

$$C = f(\mu)$$

$$\therefore f \approx Ce^{-\frac{1}{2\sigma^2}(x-\mu)^2} = Ce^{-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2}$$