



$$\begin{cases} T(x+dx)\cos(\theta+d\theta) - T(x)\cos\theta = 0 \\ T(x+dx)\sin(\theta+d\theta) - T(x)\sin\theta - g\lambda dL = 0 \end{cases}$$

$$T(x)\cos\theta = T(x+dx)\cos(\theta+d\theta) = T_x$$

$$T(x) = \frac{T_x}{\cos\theta} \quad T(x+dx) = \frac{T_x}{\cos(\theta+d\theta)}$$

$$\frac{T_x}{\cos(\theta+d\theta)}\sin(\theta+d\theta) - \frac{T_x}{\cos\theta}\sin\theta - g\lambda dL = 0$$

$$T_x(\tan(\theta+d\theta) - \tan\theta) - g\lambda dL = 0$$

$$T_x d\tan\theta = g\lambda dL \quad T_x dy' = g\lambda\sqrt{1+(y')^2} dx$$

$$\frac{1}{\sqrt{1+(y')^2}} \frac{dy'}{dx} = \frac{g\lambda}{T_x} \quad \therefore \frac{y''}{\sqrt{1+(y')^2}} = \frac{g\lambda}{T_x}$$

$$\frac{y''}{\sqrt{1+(y')^2}} = (\sinh^{-1} y')' = \frac{g\lambda}{T_x}$$

$$\sinh^{-1} y' = \frac{g\lambda}{T_x} x + c_1$$

$$y' = \sinh\left(\frac{g\lambda}{T_x} x + c_1\right)$$

$$\therefore y = \frac{T_x}{g\lambda} \cosh\left(\frac{g\lambda}{T_x} x + c_1\right) + c_2$$



resources.zip

Resources -