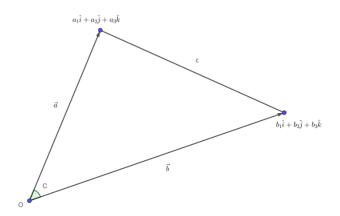


$$a = b \cos C + c \cos B$$
 $a^2 = ab \cos C + ac \cos B$
 $b = a \cos C + c \cos A$ $b^2 = ab \cos C + bc \cos A$
 $c = a \cos B + b \cos A$ $c^2 = ac \cos B + bc \cos A$

$$a^2 + b^2 - c^2 = 2ab\cos C$$

$$\therefore \cos C = \frac{a^2 + b^2 - c^2}{2ab}$$



$$a = |\vec{a}|$$
 $b = |\vec{b}|$ $c = |\vec{a} - \vec{b}|$

$$\vec{a} \cdot \vec{b} = |\vec{a}| |\vec{b}| \cos C = ab \cos C = ab \frac{a^2 + b^2 - c^2}{2ab} = \frac{1}{2} (a^2 + b^2 - c^2)$$

$$= \frac{1}{2} \left(a_1^2 + a_2^2 + a_3^2 + b_1^2 + b_2^2 + b_3^2 - ((a_1 - b_1)^2 + (a_2 - b_2)^2 + (a_3 - b_3)^2) \right)$$

$$= \frac{1}{2} \left(a_1^2 + a_2^2 + a_3^2 + b_1^2 + b_2^2 + b_3^2 - (a_1^2 - 2a_1b_1 + b_1^2 + a_2^2 - 2a_2b_2 + b_2^2 + a_3^2 - 2a_3b_3 + b_3^2) \right)$$

$$= \frac{1}{2} (2a_1b_1 + 2a_2b_2 + 2a_3b_3) = a_1b_1 + a_2b_2 + a_3b_3$$

$$\vec{a} \cdot \vec{b} = a_1 b_1 + a_2 b_2 + a_3 b_3$$

