

## CSCE 4650/5650 ASSIGNMENT #3 SOLUTION

Consider the following BNF grammar G:

expression ::= identifier | ( expression ) | apply identifier to expression

1. Construct the set of LR(1) items for G (the original grammar given above).

We first rewrite the grammar as follows:

$E \rightarrow E$

$E \rightarrow \text{id} \mid (E) \mid \text{apply id to } E$

The item sets are as follows:

I0	: $E \rightarrow \bullet E, \$$ $E \rightarrow \bullet \text{id}, \$$ $E \rightarrow \bullet (E), \$$ $E \rightarrow \bullet \text{apply id to } E, \$$	
I1	: $E \rightarrow E \bullet, \$$	GOTO (I0, E)
I2	: $E \rightarrow \text{id} \bullet, \$$	GOTO (I0, id)
I3	: $E \rightarrow ( \bullet E), \$$ $E \rightarrow \bullet \text{id}, )$ $E \rightarrow \bullet (E), )$ $E \rightarrow \bullet \text{apply id to } E, )$	GOTO (I0, ( )
I4	: $E \rightarrow \text{apply} \bullet \text{id to } E, \$$	GOTO (I0, apply)
I5	: $E \rightarrow (E \bullet), \$$	GOTO (I3, E)
I6	: $E \rightarrow \text{id} \bullet, )$	GOTO (I3, id), GOTO (I7, id)
I7	: $E \rightarrow ( \bullet E), )$ $E \rightarrow \bullet \text{id}, )$ $E \rightarrow \bullet (E), )$ $E \rightarrow \bullet \text{apply id to } E, )$	GOTO (I3, ( ), GOTO (I7, ( )
I8	: $E \rightarrow \text{apply} \bullet \text{id to } E, )$	GOTO (I3, apply), GOTO (I7, apply)
I9	: $E \rightarrow \text{apply id} \bullet \text{to } E, \$$	GOTO (I4, id)
I10	: $E \rightarrow (E) \bullet, \$$	GOTO (I5, ))
I11	: $E \rightarrow (E \bullet), )$	GOTO (I7, E)
I12	: $E \rightarrow \text{apply id} \bullet \text{to } E, )$	GOTO (I8, id)
I13	: $E \rightarrow \text{apply id to} \bullet E, \$$ $E \rightarrow \bullet \text{id}, \$$ $E \rightarrow \bullet (E), \$$ $E \rightarrow \bullet \text{apply id to } E, \$$	GOTO (I9, to)
I14	: $E \rightarrow (E) \bullet, )$	GOTO (I11, ))
I15	: $E \rightarrow \text{apply id to} \bullet E, )$ $E \rightarrow \bullet \text{id}, )$ $E \rightarrow \bullet (E), )$ $E \rightarrow \bullet \text{apply id to } E, )$	GOTO (I12, to)
I16	: $E \rightarrow \text{apply id to } E \bullet, \$$	GOTO (I13, E)
I17	: $E \rightarrow \text{apply id to } E \bullet, )$	GOTO (I15, E)

2. Merge the sets of items having common cores to give the set of LALR(1) items.

The LALR(1) item sets and their associated states are: I0 (0), I1 (1), {I2, I6} (2), {I3, I7} (3), {I4, I8} (4), {I5, I11} (5), {I9, I12} (6), {I10, I14} (7), {I13, I15} (8), {I16, I17} (9).

3. Construct the LALR(1) parsing table from the set of LALR(1) items.

	id	(	)	apply	to	\$	E
0	s2	s3		s4			1
1						acc	
2			r1			r1	
3	s2	s3		s4			5
4	s6						
5			s7				
6					s8		
7			r2			r2	
8	s2	s3		s4			9
9			r3			r3	

4. Simplify the LALR parsing table using the compaction techniques discussed at the end of Section 4.7.

State	Input	Action	Symbol	State	Goto
0,3,8	id	s2	E	0	1
	(	s3		3	5
	apply	s4		8	9
	any	error			
1	\$	accept			
	any	error			
2	any	r1			
4	id	s6			
	any	error			
5	)	s7			
	any	error			
6	to	s8			
	any	error			
7	any	r2			
9	any	r3			

5. Augment the compacted LALR table with appropriate error recovery calls and routines. Give a general explanation of how your error recovery routines work.

We number errors by the states in which they occur.

0,3,8 - print ("id expected"); s2

1 - print ("unexpected symbol" + input); delete symbol and retry

4 - print ("id expected"); s6

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5 - if input = $ print ("missing "); s7
    else print ("unexpected symbol" + input); delete symbol and retry
6 - print ("to expected"); s8
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