



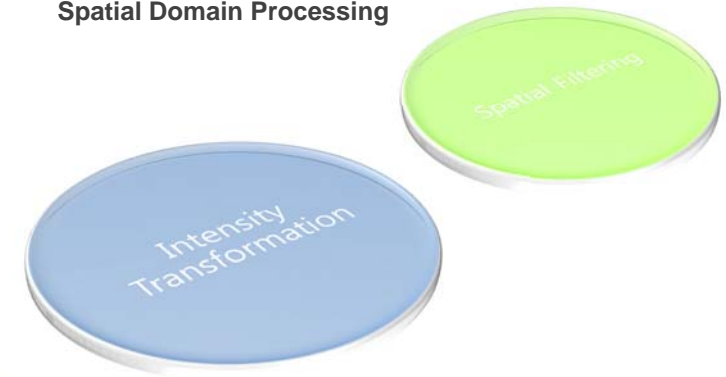
# Image Processing

## Intensity Transformation and Spatial Filtering (Part II)

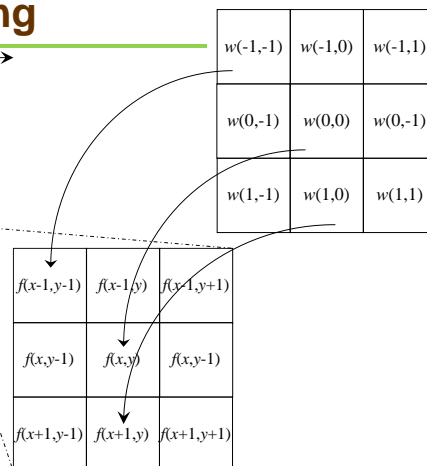
Pattern Recognition and Image Processing Laboratory (Since 2012)

## Introduction

### Spatial Domain Processing



## Spatial Filtering



## Spatial Filtering



## Spatial Filtering

### Linear Spatial Filtering



$y$

-1	-1	-1
-1	8	-1
-1	-1	-1

$f(x-1, y-1)$	$f(x-1, y)$	$f(x-1, y+1)$
$f(x, y-1)$	$f(x, y)$	$f(x, y+1)$
$f(x+1, y-1)$	$f(x+1, y)$	$f(x+1, y+1)$

Coefficient mask

## Spatial Filtering

### Linear Spatial Filtering

A 2-D linear spatial filter usually has the following properties:

- The **mask size** is symmetric, such as 3x3, 5x5, 7x7, ...
- The **operation** of a filter is based on convolution and correlation.

## Spatial Filtering

### Linear Spatial Filtering: Correlation

1 2 3  
4 5 6  
7 8 9

$w(x, y)$

0 0 0 0 0  
0 0 0 0 0  
0 0 1 0 0  
0 0 0 0 0  
0 0 0 0 0

$f(x, y)$

0 0 0 0 0 0 0 0 0  
0 0 0 0 0 0 0 0 0  
0 0 0 0 0 0 0 0 0  
0 0 0 0 0 0 0 0 0  
0 0 0 0 1 0 0 0 0  
0 0 0 0 0 0 0 0 0  
0 0 0 0 0 0 0 0 0  
0 0 0 0 0 0 0 0 0  
0 0 0 0 0 0 0 0 0

Padded  $f(x, y)$

## Spatial Filtering

### Linear Spatial Filtering: Correlation

1 2 3 0 0 0 0 0 0  
4 5 6 0 0 0 0 0 0  
7 8 9 0 0 0 0 0 0  
0 0 0 0 0 0 0 0 0  
0 0 0 0 1 0 0 0 0  
0 0 0 0 0 0 0 0 0  
0 0 0 0 0 0 0 0 0  
0 0 0 0 0 0 0 0 0  
0 0 0 0 0 0 0 0 0  
0 0 0 0 0 0 0 0 0

Initial operation

0 0 0 0 0 0 0 0 0  
0 0 0 0 0 0 0 0 0  
0 0 0 0 0 0 0 0 0  
0 0 0 9 8 7 0 0 0  
0 0 0 6 5 4 0 0 0  
0 0 0 3 2 1 0 0 0  
0 0 0 0 0 0 0 0 0  
0 0 0 0 0 0 0 0 0  
0 0 0 0 0 0 0 0 0  
0 0 0 0 0 0 0 0 0

Correlation result

## Spatial Filtering

Linear Spatial Filtering: **Convolution**

9	8	7	0	0	0	0	0	0	0
6	5	4	0	0	0	0	0	0	0
3	2	1	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	1	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

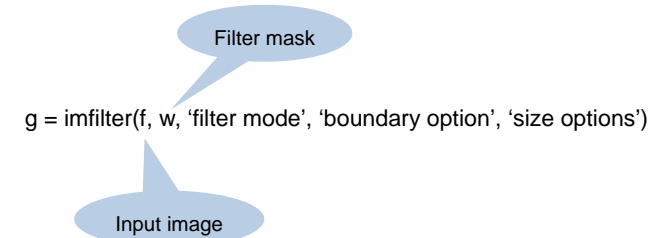
Initial operation

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	1	2	3	0	0	0	0
0	0	0	4	5	6	0	0	0	0
0	0	0	7	8	9	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

Convolution result

## Spatial Filtering

The following syntax is used when implementing IPT standard linear spatial filters.



## Spatial Filtering

**>> ex3\_04 % See demonstration**

## Spatial Filtering

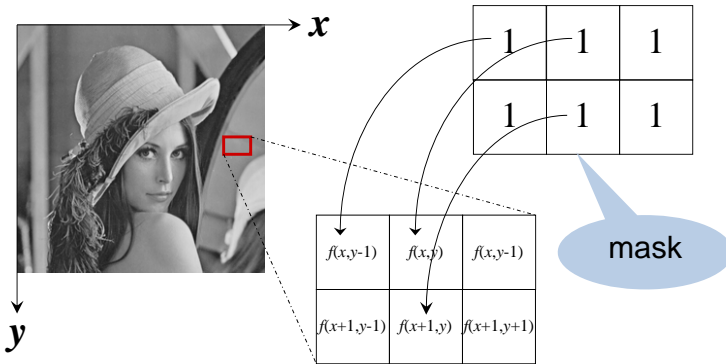
### Non-linear Spatial Filtering

A 2-D non-linear spatial filter usually has the following properties:

- The **mask size** can be both symmetric and asymmetric forms, such as 2x2, 2x3, 3x3, 3x4, 5x7, ...
- The **operation** is directly performed on image pixels.

## Spatial Filtering

### Non-linear Spatial Filtering



## Spatial Filtering

The following syntax is used for implementing generalized non-linear spatial filters.

$g = \text{colfilt}(f, [m \ n], \text{'sliding'}, @\text{function}, \text{parameter})$

mask

Input image

### Applications of Non-linear Spatial Filtering: Image Enhancement

**>> ex3\_04 % See demonstration**

### Applications of Non-linear Spatial Filtering: Noise Filtering

**>> ex3\_04 % See demonstration**

