



# Image Processing

## Intensity Transformation and Spatial Filtering (Part II)

Pattern Recognition and Image Processing Laboratory (Since 2012)

# Introduction

---

## Spatial Domain Processing

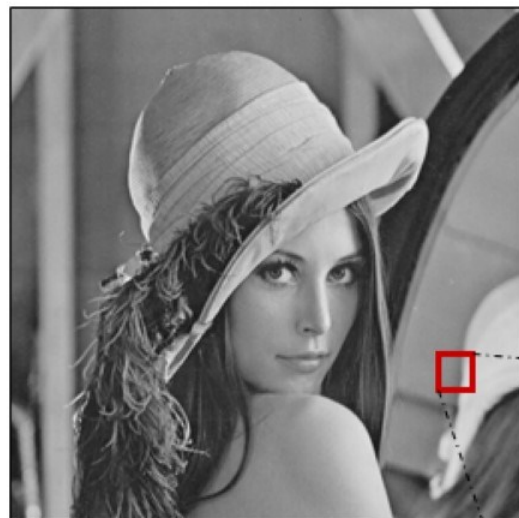


Intensity  
Transformation



Spatial Filtering

# Spatial Filtering



$w(-1,-1)$	$w(-1,0)$	$w(-1,1)$
$w(0,-1)$	$w(0,0)$	$w(0,1)$
$w(1,-1)$	$w(1,0)$	$w(1,1)$

$f(x-1,y-1)$	$f(x-1,y)$	$f(x-1,y+1)$
$f(x,y-1)$	$f(x,y)$	$f(x,y+1)$
$f(x+1,y-1)$	$f(x+1,y)$	$f(x+1,y+1)$

# Spatial Filtering

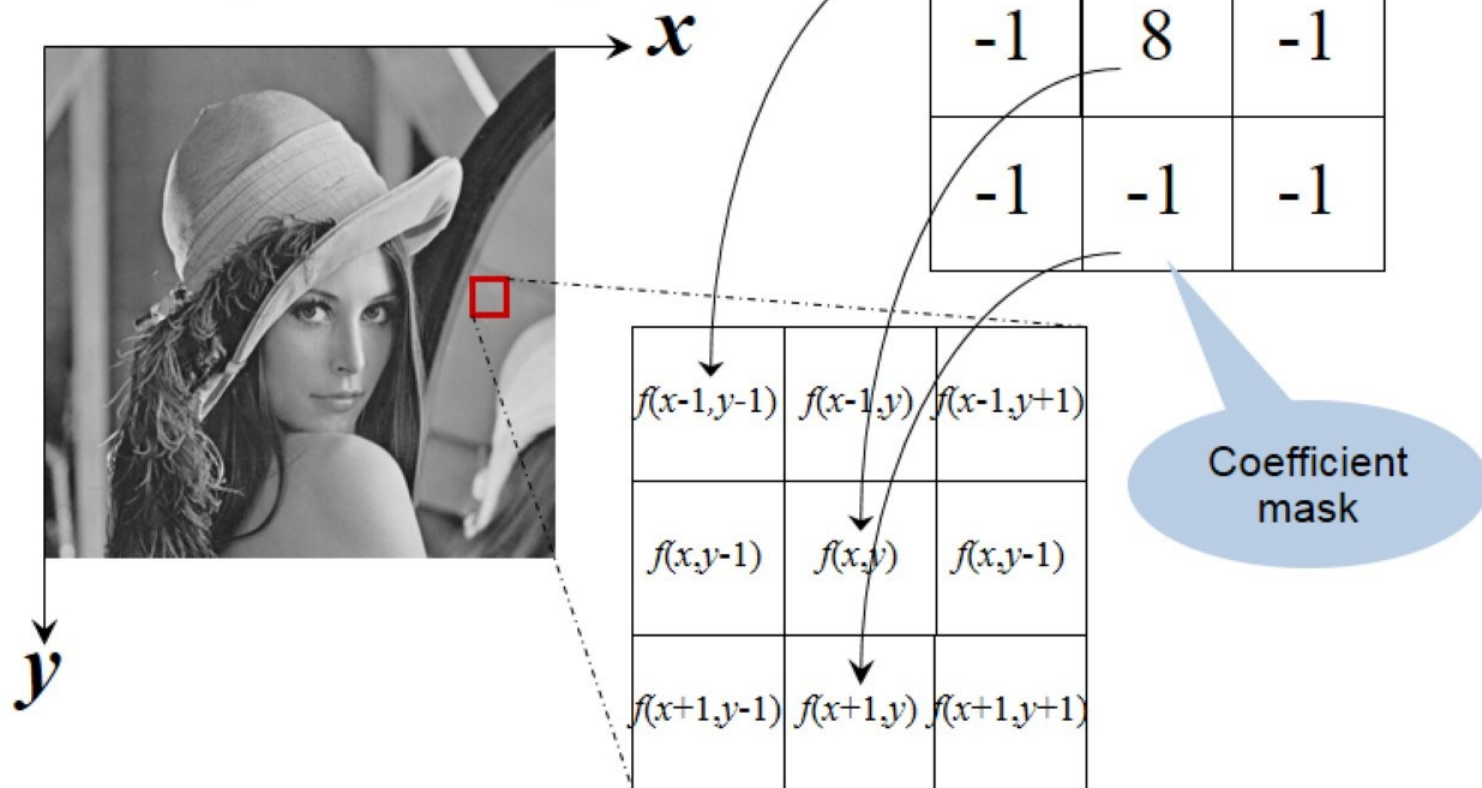
---

Linear Spatial  
Filtering

Non-linear  
Spatial Filtering

# Spatial Filtering

## Linear Spatial Filtering





# Spatial Filtering

---

## Linear Spatial Filtering

A 2-D linear spatial filter usually has the following properties:

- The **mask size** is symmetric, such as 3x3, 5x5, 7x7, ...
- The **operation** of a filter is based on convolution and correlation.



# Spatial Filtering

## Linear Spatial Filtering: Correlation

1 2 3

4 5 6

7 8 9

$w(x,y)$

0 0 0 0 0

0 0 0 0 0

0 0 1 0 0

0 0 0 0 0

0 0 0 0 0

$f(x,y)$

0 0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0 0

0 0 0 0 1 0 0 0 0

0 0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0 0

Padded  $f(x,y)$

# Spatial Filtering

## Linear Spatial Filtering: Correlation

1	2	3	0	0	0	0	0	0
4	5	6	0	0	0	0	0	0
7	8	9	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	1	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0

Initial operation

0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	9	8	7	0	0	0
0	0	0	6	5	4	0	0	0
0	0	0	3	2	1	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0

Correlation result



# Spatial Filtering

## Linear Spatial Filtering: Convolution

9	8	7	0	0	0	0	0	0
6	5	4	0	0	0	0	0	0
3	2	1	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	1	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0

Initial operation

0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	1	2	3	0	0	0
0	0	0	4	5	6	0	0	0
0	0	0	7	8	9	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0

Convolution result

# Spatial Filtering

The following syntax is used when implementing IPT standard linear spatial filters.

`g = imfilter(f, w, 'filter mode', 'boundary option', 'size options')`

Filter mask

Input image



## Spatial Filtering

---

**>> ex3\_04 % See demonstration**



# Spatial Filtering

---

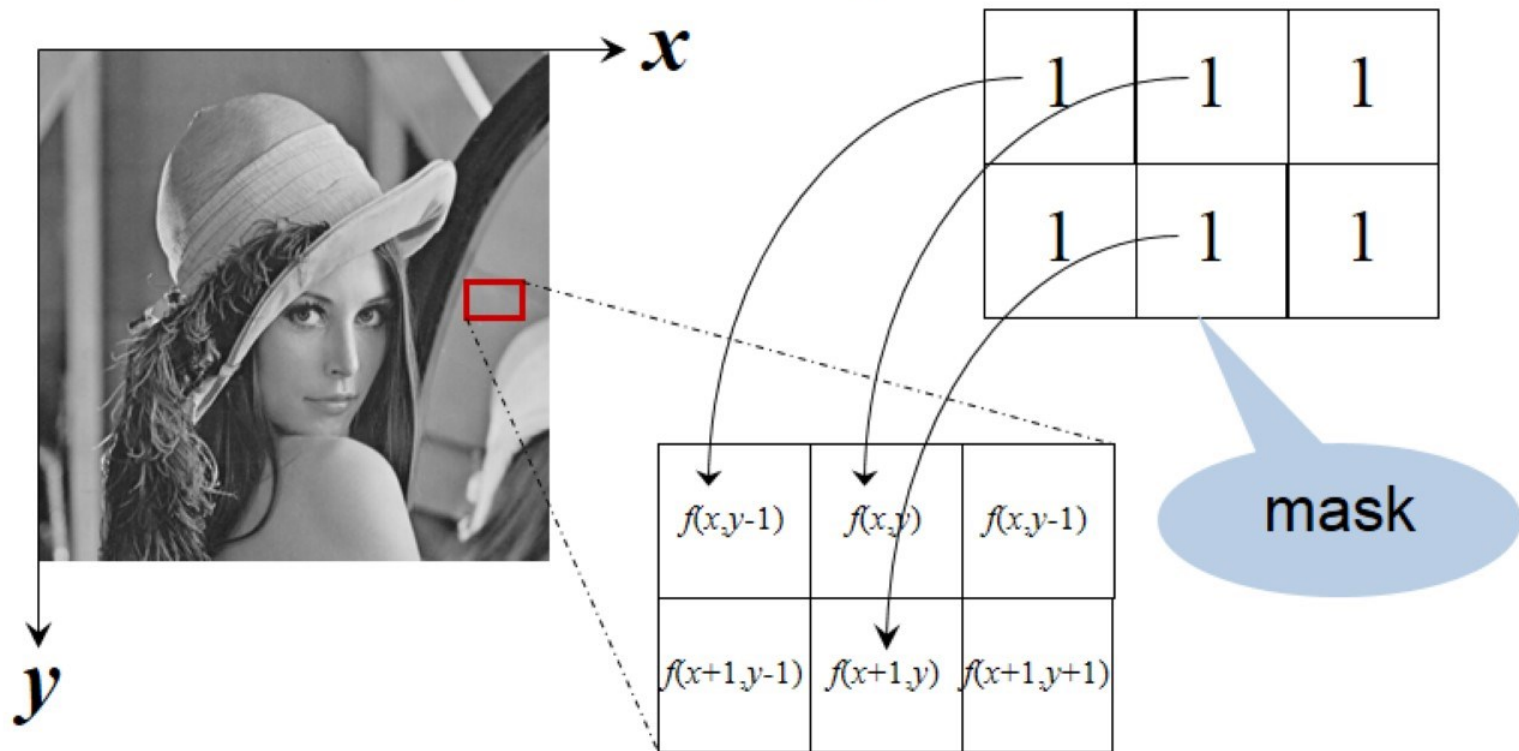
## Non-linear Spatial Filtering

A 2-D non-linear spatial filter usually has the following properties:

- The **mask size** can be both symmetric and asymmetric forms, such as  $2 \times 2$ ,  $2 \times 3$ ,  $3 \times 3$ ,  $3 \times 4$ ,  $5 \times 7$ , ...
- The **operation** is directly performed on image pixels.

# Spatial Filtering

## Non-linear Spatial Filtering





# Spatial Filtering

The following syntax is used for implementing generalized non-linear spatial filters.

mask

`g = colfilt(f, [ m n ], 'sliding', @function, parameter)`

Input image



## Applications of Non-linear Spatial Filtering: Image Enhancement

---

**>> ex3\_04 % See demonstration**



## Applications of Non-linear Spatial Filtering: Noise Filtering

---

**>> ex3\_04 % See demonstration**



---

The end of  
part II

File\_name: Ex3\_04.m

```
clear all;
close all;
%% ----- Linear Filtering -----
f = imread('cirdbw.tif');
w = [0.1 0.1 0.1;
     0.1 0.2 0.1;
     0.1 0.1 0.1];

afterfilter = conv2(double(f), w);
figure(1);
subplot(1,2,1); imshow(f);
subplot(1,2,2); imshow(uint8(afterfilter));

%% --- MATLAB toolbox implementing linear spatial filtering ---
%%
%% its syntax is g = imfilter(f, w, filtering_mode,
%% boundary_options, size_options), where f is the input
%% image, w is the filter mask, g is the filtered result.

% w = [0.1 0.1 0.1;
%      0.1 0.2 0.1;
%      0.1 0.1 0.1];

lowresult1 = imfilter(double(f), w, 'conv', 'replicate');
lowresult2 = imfilter(double(f), w, 'corr', 'replicate');

figure(2);
subplot(2,2,1); imshow(f);
subplot(2,2,2); imshow(lowresult1);
subplot(2,2,3); imshow(lowresult2);
```



```

hw = [1  1  1;
      1 -8  1;
      1  1  1];

hiresult = imfilter(double(f), hw, 'conv', 'replicate');

figure;
subplot(2,2,1); imshow(f);
subplot(2,2,2); imshow(uint8(lowresult1));
subplot(2,2,3); imshow(uint8(hiresult));

% ----- generating a black-white image -----
white(1:50,1:50) = 1;
black(1:50,1:50) = 0;
blkwht = [black white; white black];

w5 = ones(5);
result1 = imfilter(double(blkwht), w5, 'conv');
result2 = imfilter(double(blkwht), w5, 'conv',
'replicate');
result3 = imfilter(double(blkwht), w5, 'conv',
'symmetric');
result4 = imfilter(double(blkwht), w5, 'conv',
'circular');

figure(3);
subplot(2,3,1); imshow(blkwht);
subplot(2,3,2); imshow(im2uint8(mat2gray(result1)));
subplot(2,3,3); imshow(im2uint8(mat2gray(result2)));
subplot(2,3,4); imshow(im2uint8(mat2gray(result3)));
subplot(2,3,5); imshow(im2uint8(mat2gray(result4)));

```

```

%% -- MATLAB toolbox implementing non-linear spatial
filtering ---
%%
%% its syntax is g = ordfilt2(f, order, domain), where
%% f is the input image, w is the filter mask, g is
%% the filtered result.

f = imread('circuit.tif');
nonsf1 = ordfilt2(f, 1, ones(3));
nonsf2 = ordfilt2(f, 5, ones(3));
nonsf3 = ordfilt2(f, 9, ones(3));

figure(4);
subplot(2,2,1); imshow(f);
subplot(2,2,2); imshow(nonsf1);
subplot(2,2,3); imshow(nonsf2);
subplot(2,2,4); imshow(nonsf3);

% ---- Add noise -----
fn = imnoise(f, 'salt & pepper', 0.2);
mf3 = ordfilt2(fn, 5, ones(3));
mf5 = ordfilt2(fn, 13, ones(5));

mf6 = medfilt2(fn, [5 5], 'symmetric');

figure(5);
subplot(2,2,1); imshow(f);
subplot(2,2,2); imshow(fn);
subplot(2,2,3); imshow(mf3);
subplot(2,2,4); imshow(mf5);

figure(6); imshow(mf6);

```

```
%% the toolbox supports a number of predefined 2-D  
linear spatial filters
```

```
f = imread('lena.bmp');
```

```
w1 = fspecial('laplacian', 0);
```

```
w2 = fspecial('sobel');
```

```
w3 = fspecial('prewitt');
```

```
sf1 = imfilter(f, w1, 'conv');
```

```
sf2 = imfilter(f, w2, 'conv');
```

```
sf3 = imfilter(f, w3, 'conv');
```

```
figure(7);
```

```
subplot(2,2,1); imshow(f);
```

```
subplot(2,2,2); imshow(sf1);
```

```
subplot(2,2,3); imshow(sf2);
```

```
subplot(2,2,4); imshow(sf3);
```



# Image Processing

Workshop on Intensity Transformation and  
Spatial Filtering (Part II)

Pattern Recognition and Image Processing Laboratory (Since 2012)

## Workshop on Intensity Transformation (Part II)

1. จงคำนวณหาผลลัพธ์ของการ convolution "ด้วยมือ" เมื่อกำหนดให้ mask คือ  $w(x,y)$  และรูปภาพ คือ  $f(x,y)$

-1	-1	-1
-1	8	-1
-1	-1	-1

$w(x,y)$

1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1
1	1	1	1	1	1	0	0
1	1	1	1	1	0	0	0
1	1	1	1	0	0	0	0
1	1	1	0	0	0	0	0
1	1	0	0	0	0	0	0
1	0	0	0	0	0	0	0

$f(x,y)$



## Workshop on Intensity Transformation (Part II)

2. จงเขียน MATLAB Script เพื่อคำนวณหาผลลัพธ์ของการ convolution ระหว่าง  $w(x,y)$  และ  $f(x,y)$

-1	-1	-1
-1	8	-1
-1	-1	-1

$w(x,y)$

1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1
1	1	1	1	1	1	0	0
1	1	1	1	1	0	0	0
1	1	1	1	0	0	0	0
1	1	1	0	0	0	0	0
1	1	0	0	0	0	0	0
1	0	0	0	0	0	0	0

$f(x,y)$

## Workshop on Intensity Transformation (Part II)

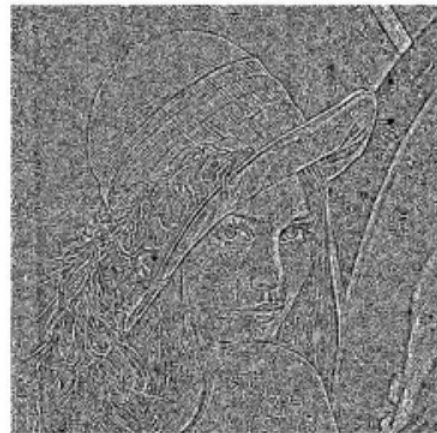
3. จงเขียนฟังก์ชัน myFilter เพื่อทำการกรอง (filtering) รูปภาพ โดยมี mask และ รูปภาพ  $f$  เป็นข้อมูลนำเข้า

-1	-1	-1
-1	8	-1
-1	-1	-1

Filter mask



Original image (f)



Filtered image