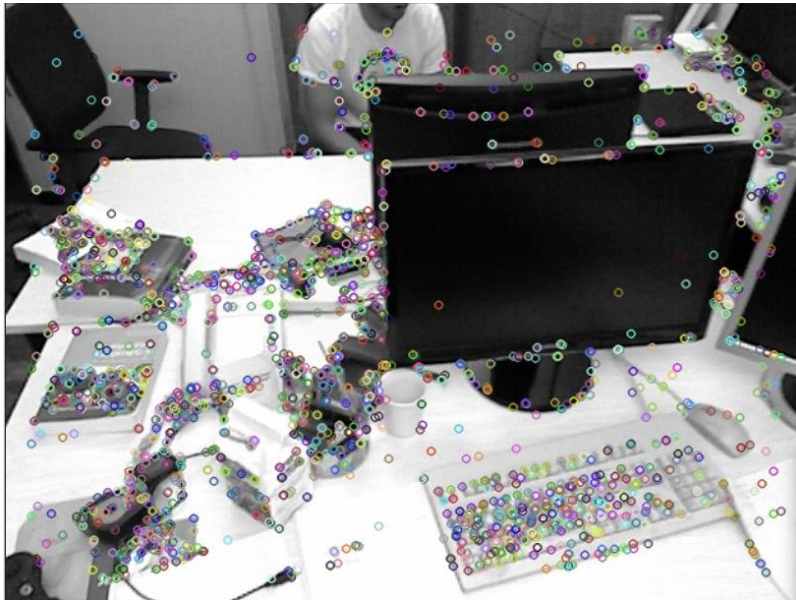


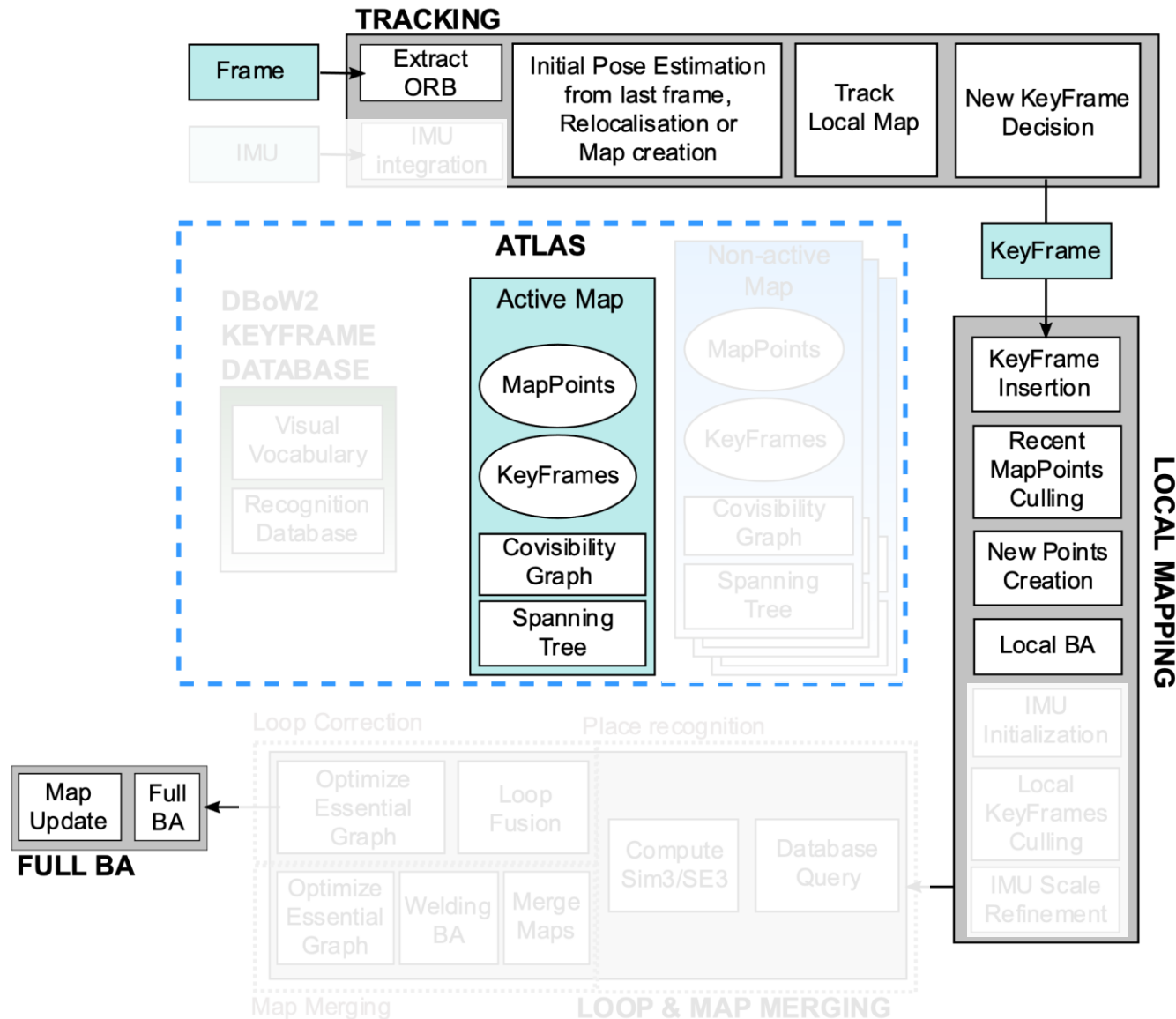
Lab #3. Visual SLAM: Camera Tracking

Juan J. Gómez, Víctor M. Batlle, Juan D. Tardós
Universidad de Zaragoza, Spain

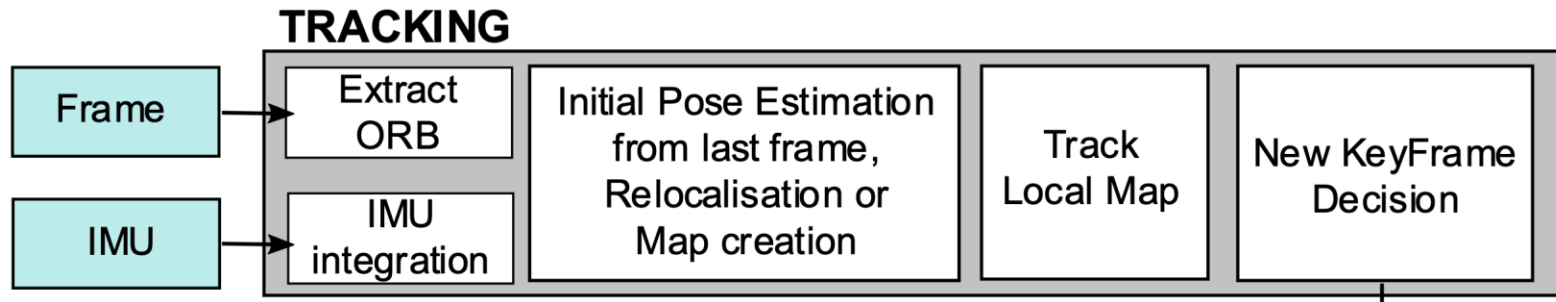
robots.unizar.es/SLAMLAB



Mini-SLAM vs ORB-SLAM3

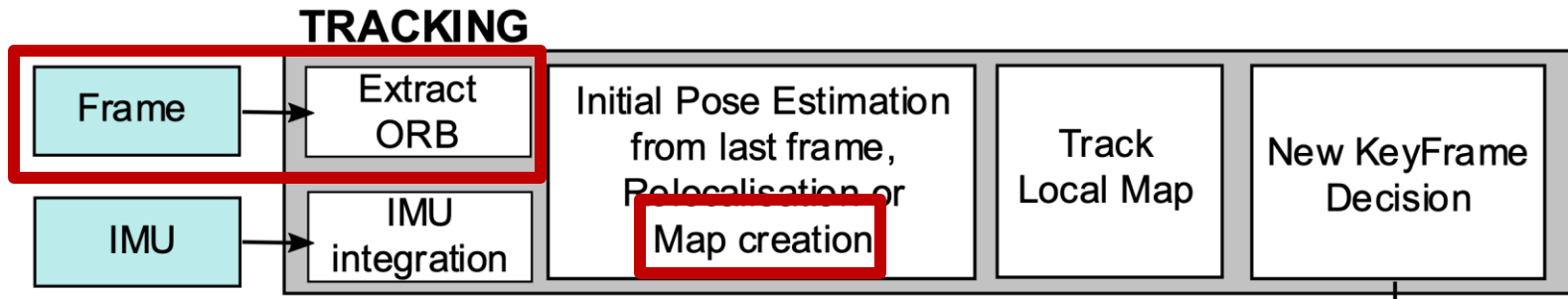


Camera Tracking



- Task 0 — Download the dataset
- Task 1 — Monocular Map Initialization
- Task 2 — Pinhole camera model
- Task 3 — Reprojection error
- Task 4 — Tracking the local map
- Task 5 — Fish-eye camera model

Task 1 — Monocular Map Initialization



2D Feature Matching → 3D Points and Motion

- Compare descriptors to get putative matchings
 - ORB: Hamming distance
 - Improves using ratio to second neighbor (NNR)
- Brute force or guided matching
- Draw the matches to check they are correct

Task 2 — Pinhole camera model

- Projection of point j on camera i

$$\mathbf{X}_c = \mathbf{x}_{ij} = \mathbf{R}_{iw}\mathbf{x}_{wj} + \mathbf{t}_{iw} \quad \mathbf{T}_{iw} \begin{cases} \mathbf{R}_{iw} \in \text{SO}(3) \\ \mathbf{t}_{iw} \in \mathbb{R}^3 \end{cases}$$

- Monocular pin-hole camera model

– Projection

$$\mathbf{x} = \pi_m(\mathbf{X}_c) = \begin{bmatrix} f_x \frac{X}{Z} + c_x \\ f_y \frac{Y}{Z} + c_y \end{bmatrix}, \quad \mathbf{X}_c = [X, Y, Z]^T, \quad \mathbf{x} = [u, v]^T$$

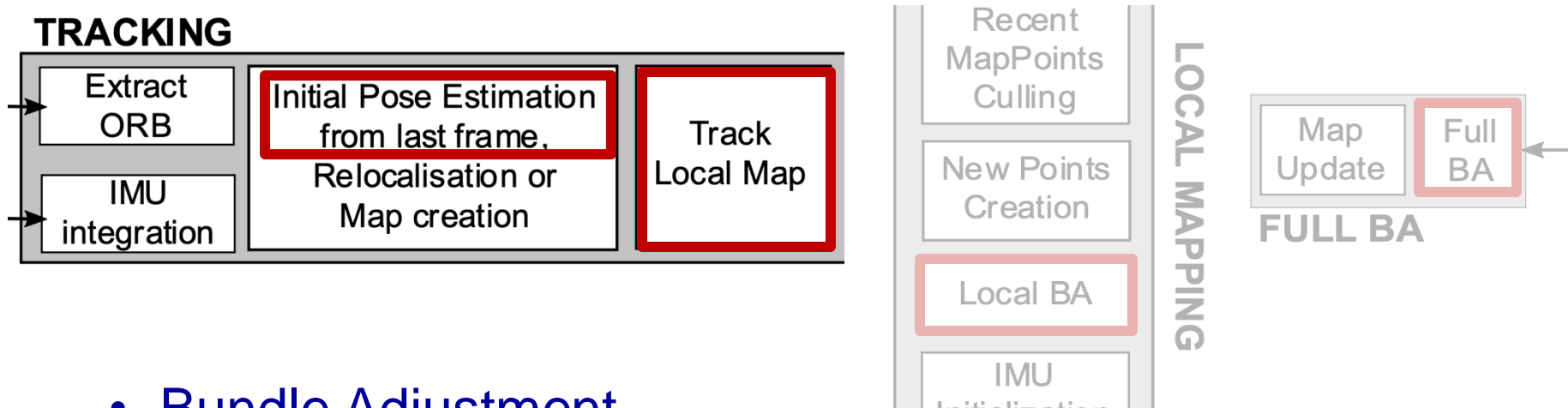
– Unprojection

$$\mathbf{X}_c = \pi_m^{-1}(\mathbf{x}) = ?$$

– Jacobian

$$J_\pi = \begin{pmatrix} \frac{\partial u}{\partial x} & \frac{\partial u}{\partial y} & \frac{\partial u}{\partial z} \\ \frac{\partial v}{\partial x} & \frac{\partial v}{\partial y} & \frac{\partial v}{\partial z} \end{pmatrix} = ?$$

Task 3 — Reprojection error



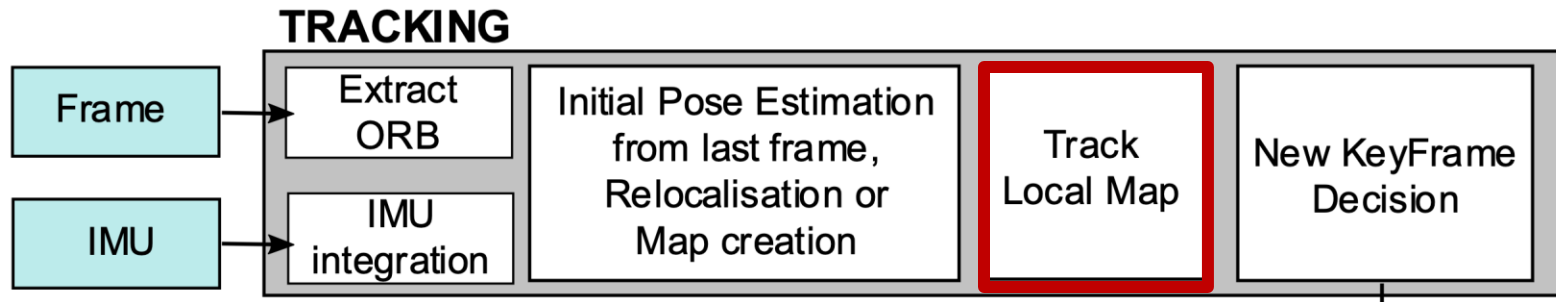
- Bundle Adjustment

$$\{\mathbf{R}_{iw}, \mathbf{t}_{iw}, \mathbf{x}_{wj} \mid i \in \mathcal{C}, j \in \mathcal{P}\}^* = \operatorname{argmin}_{\mathbf{R}_{iw}, \mathbf{t}_{iw}, \mathbf{x}_{wj}} \sum_{i,j} \rho \left(\left\| \mathbf{u}_{ij} - \pi_i (\mathbf{R}_{iw} \mathbf{x}_{wj} + \mathbf{t}_{iw}) \right\|_{\Sigma_{ij}}^2 \right)$$

- Pose-only optimization

$$\{\mathbf{R}_{iw}, \mathbf{t}_{iw}\}^* = \operatorname{argmin}_{\mathbf{R}_{iw}, \mathbf{t}_{iw}} \sum_j \rho \left(\left\| \mathbf{u}_{ij} - \pi_i (\mathbf{R}_{iw} \mathbf{x}_{wj} + \mathbf{t}_{iw}) \right\|_{\Sigma_{ij}}^2 \right)$$

Task 4 — Tracking the local map



- Project MapPoints and match them to features
 - MapPoints that should be visible in the current frame.
 - Features not already matched with a MapPoint.
- Hamming distance, guided matching...
- Check ATE before and after this task

Task 5 — Fish-eye camera model

- Kannala-Brandt projection:

$$r = \sqrt{x^2 + y^2}, \quad \theta = \arctan\left(\frac{r}{z}\right)$$

$$d(\theta) = \theta + k_1\theta^3 + k_2\theta^5 + k_3\theta^7 + k_4\theta^9$$

$$u = f_x d(\theta) \frac{x}{r} + c_x, \quad v = f_y d(\theta) \frac{y}{r} + c_y$$

$$J_\pi = \begin{pmatrix} \frac{\partial u}{\partial x} & \frac{\partial u}{\partial y} & \frac{\partial u}{\partial z} \\ \frac{\partial v}{\partial x} & \frac{\partial v}{\partial y} & \frac{\partial v}{\partial z} \end{pmatrix} = \boxed{?}$$

- Kannala-Brandt backprojection:

$$m_x = \frac{u - c_x}{f_x}, \quad m_y = \frac{v - c_y}{f_y}, \quad r' = \sqrt{m_x^2 + m_y^2}$$

$$\theta = d^{-1}(r')$$

$$\mathbf{d} = \left(\sin \theta \frac{m_x}{r'}, \sin \theta \frac{m_y}{r'}, \cos \theta \right)$$

- Lookup table
- Inverse polynomial
- Newton's method

Results

- What?
 - Short report (discussion, figures...)
Answer the questions for each task
 - Code (clean and with some comments)
Include only *Modules* and *Apps* folders
- When?
 - Submission @ 23:59 on Monday after Lab 3.2 session