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//Name: 7. Graph: Minimum Spanning Tree
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```
#include <iostream>
```

```
#include <algorithm>
```

```
#include <climits>
```

```
using namespace std;
```

```
const int MAX_VERTICES = 10;
```

```
struct Edge {
```

```
    int src, dest, weight;
```

```
};
```

```
class DisjointSet {
```

```
public:
```

```
    int parent[MAX_VERTICES];
```

```
    int rank[MAX_VERTICES];
```

```
    DisjointSet(int n) {
```

```
        for (int i = 0; i < n; i++) {
```

```
            parent[i] = i;
```

```
            rank[i] = 0;
```

```
        }
```

```
    }
```

```
    int find(int u) {
```

```
        if (u != parent[u])
```

```
            parent[u] = find(parent[u]);
```

```
        return parent[u];
```

```
    }
```

```

void unionSets(int u, int v) {
    int rootU = find(u);
    int rootV = find(v);
    if (rootU != rootV) {
        if (rank[rootU] > rank[rootV])
            parent[rootV] = rootU;
        else if (rank[rootU] < rank[rootV])
            parent[rootU] = rootV;
        else {
            parent[rootV] = rootU;
            rank[rootU]++;
        }
    }
}

};

void kruskal(Edge edges[], int E, int V) {
    DisjointSet ds(V);
    Edge mst[MAX_VERTICES];
    int mstIndex = 0;
    sort(edges, edges + E, [](Edge a, Edge b) {
        return a.weight < b.weight;
    });
    for (int i = 0; i < E; i++) {
        Edge edge = edges[i];

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    int u = edge.src;
    int v = edge.dest;
    if (ds.find(u) != ds.find(v)) {
        ds.unionSets(u, v);
        mst[mstIndex++] = edge;
    }
}

cout << "Kruskal's MST:\n";
for (int i = 0; i < mstIndex; i++) {
    cout << char(mst[i].src + 'A') << " -- " << char(mst[i].dest + 'A') << " ==
" << mst[i].weight << endl;
}
}

void prim(int graph[MAX_VERTICES][MAX_VERTICES], int V) {
    int parent[MAX_VERTICES];
    int key[MAX_VERTICES];
    bool inMST[MAX_VERTICES];
    for (int i = 0; i < V; i++) {
        key[i] = INT_MAX;
        inMST[i] = false;
        parent[i] = -1;
    }
    key[0] = 0; // Starting from the first vertex
    for (int count = 0; count < V - 1; count++) {

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int minKey = INT_MAX, minIndex;
for (int v = 0; v < V; v++) {
    if (!inMST[v] && key[v] < minKey) {
        minKey = key[v];
        minIndex = v;
    }
}
inMST[minIndex] = true;
for (int v = 0; v < V; v++) {
    if (graph[minIndex][v] && !inMST[v] && graph[minIndex][v] < key[v]) {
        parent[v] = minIndex;
        key[v] = graph[minIndex][v];
    }
}
}

cout << "Prim's MST:\n";
for (int i = 1; i < V; i++) {
    cout << char(parent[i] + 'A') << " -- " << char(i + 'A') << " == " <<
graph[i][parent[i]] << endl;
}
}

int main() {
    const int V = 4;
    const int E = 5;

```

```
Edge edges[E] = {
    {0, 1, 10},
    {0, 2, 6},
    {0, 3, 5},
    {1, 3, 15},
    {2, 3, 4}
};
int graph[MAX_VERTICES][MAX_VERTICES] = {0};
for (int i = 0; i < E; i++) {
    graph[edges[i].src][edges[i].dest] = edges[i].weight;
    graph[edges[i].dest][edges[i].src] = edges[i].weight;
}
kruskal(edges, E, V);
prim(graph, V);
return 0;
}
```