

## 9 09-23-2025

### 9.1 Section 4.1, Checkpoint 4.4

Find the domain and range of the function  $f(x, y) = \sqrt{36 - 9x^2 - 9y^2}$

### 9.2 Section 4.1, Checkpoint 4.5

Find the equation of the level surface of the function

$$g(x, y, z) = x^2 + y^2 + z^2 - 2x + 4y - 6z$$

corresponding to  $c = 2$ , and describe the surface, if possible.

### 9.3 Section 4.2, Exercise 60

Evaluate  $\lim_{(x,y) \rightarrow (1,2)} x$  or explain why the limit does not exist.

### 9.4 Section 4.2, Exercise 77

Evaluate  $\lim_{(x,y) \rightarrow (0,0)} \ln(x^2 + y^2)$  or explain why the limit does not exist.

*Does the limit exist on **any** path?*

### 9.5 Section 4.2, Exercise 81

Evaluate  $\lim_{(x,y) \rightarrow (0,0)} \frac{x^4 - 4y^4}{x + 2y^2}$  or explain why the limit does not exist.

*Do you see any algebraic manipulations?*

### 9.6 Section 4.2, Exercise 86

Evaluate  $\lim_{(x,y) \rightarrow (0,0)} \frac{xy + y^3}{x^2 + y^2}$  or explain why the limit does not exist.

(a) Along the  $x$ -axis ( $y = 0$ )

(b) Along the  $y$ -axis  $x = 0$

(c) Along the path  $y = 2x$

### 9.7 Section 4.2, Exercise 88

Evaluate  $\lim_{(x,y) \rightarrow (0,0)} \frac{x^2y}{x^4 + y^2}$  or explain why the limit does not exist.

(a) Along the  $x$ -axis ( $y = 0$ )

(b) Along the  $y$ -axis  $x = 0$

(c) Along the path  $y = x^2$

## 9.8 Section 4.2, Exercise 95

Determine the region in which the function is continuous. Explain your answer

$$f(x, y) = \begin{cases} \frac{x^2 y}{x^2 + y^2} & \text{if } (x, y) \neq (0, 0) \\ 0 & \text{if } (x, y) = (0, 0) \end{cases}$$

*Hint: maybe this coordinate system isn't helpful. Also remember the Squeeze Theorem?*

*We do NOT expect you to use Squeeze Theorem with completely general functions*