Chombo/Proto Poisson example

Abstract

Given a charge distribution ρ , and a field ϕ the spatial Helmoltz equation is given by

$$(\alpha I + \beta \nabla)\phi = \rho. \tag{1}$$

where α and β are constants. The Chombo Proto example solves the spatial Helmholtz equation in two or three dimensions using geometric multigrid with standard V-cycles.

We present the performance for a single level calculation on a single node of a Cori Haswell node. The boundary conditions are periodic and the charge distribution has compact support of r = 0.2. Further parameters are as follows.

- Identity coefficient, $\alpha = 1$.
- Laplacian coefficient, $\beta = -0.1$.
- Number of smoothings per relaxation, $n_s = 4$.
- Grid dimensions = 512^3 .
- Domain size $L_x = L_y = L_z = 1$.

All calculations are done with a varying number of threads, keeping the number of computational units constant. If N_t is the number of OpenMP threads and N_m is the number of MPI processes, for all calculations, $N_t N_m = 32$. Floating point rates are calculated as a post-processing step.

| N_t | N_m | T_{vcycle} | F_{resid} |
|-------|-------|--------------|-------------|
| 1 | 32 | 1.223 | 78.1 GFlop |
| 2 | 16 | 2.450 | 39.0 GFlop |
| 4 | 8 | 2.480 | 30.6 GFlop |
| 8 | 4 | 2.334 | 18.4 GFlop |
| 16 | 2 | 2.695 | 10.5 GFlop |
| 32 | 1 | 2.361 | 6.5 MFlop |

 ${\bf Table\ 1:\ AMRPoisson\ performance.}$

| N_t | N_m | T_{vcycle} | F_{resid} |
|-------|-------|--------------|-------------|
| 1 | 32 | 3.89 | 20.1 GFlop |
| 2 | 16 | 6.53 | 12.7 GFlop |
| 4 | 8 | 6.47 | 12.6 GFlop |
| 8 | 4 | 6.27 | 12.6 GFlop |
| 16 | 2 | 6.00 | 12.6 GFlop |
| 32 | 1 | 5.85 | 12.7 GFlop |

Table 2: 7 point stencil proto performance. Same stencil as AMRPoisson

| N_t | N_m | T_{vcycle} | |
|-------|-------|--------------|------------|
| 1 | 32 | 12.4 | 22.9 GFlop |
| 2 | 16 | 20.7 | 14.7 GFlop |
| 4 | 8 | 20.7 | 14.4 GFlop |
| 8 | 4 | 19.7 | 14.7 GFlop |
| 16 | 2 | 18.8 | 14.9 GFlop |
| 32 | 1 | 18.6 | 14.9 GFlop |

Table 3: 27 point stencil proto performance.