Building a Greedy Heuristic and a GRASP Metaheuristic for the Knapsack 0-1 Problem

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Abstract—**Studies have shown that computer theory techniques has been bringing significant improvements. In this paper, a proposal was presented for knapsack 0-1 using a greedy randomized adaptive search procedure (GRASP) metaheuristic. To evaluate the proposed method, different algorithms were compared for evaluated the method proposal. The result showed then grasp algorithm algorithm was equal to the optimal algorithm using dynamic programming.**

Index Terms—**GRASP, Dynamic Programming, Greedy**

I. INTRODUCTION

Along the time, many scientists have contributed a lot of heurists for solving problems that are in class NP-complete. As is the case with *Resende* researcher that created a denominated GRASP algorithm [1].

According *Festa and Resende*, GRASP is a mult-start or iterative process, in which each GRASP iteration consists of two phases, a **construction phase**, in which a feasible solution is produced, and a **local search** phase, in which a local optimum in the neighborhood of the constructed solution is sought. The best overall solution is kept as the result.

The unidimensional knapsack 0-1 [2] is defined by:

$$P = \sum_{i=1}^{n} p_i x_i$$

subject to:

$$\sum_{i=1}^{n} w_i x_i \leq W$$

$$x_i = 0, 1 (i = 1, ..., n)$$

And the weight of the items cannot pass the capacity of the knapsack:

$$\sum_{i=1}^{n} w_i > W$$

$$w_i \leq W (i = 1, ..., n)$$

In this paper, we will be utilizing two algorithms to compare the grasp metaheurisc. The paper is divided into five sections, the first section is the introduction, the following section is the method which will talk the three algorithms utilized for this application, the third section is the experiment and results in this phase will go shown some metrics to evaluate the method proposed, the fourth section is the conclusion where will be determined which technique was the best or got the better result for the respective metrics proposed.

II. METHODS

A. GREEDY ALGORITHM

The greedy algorithm technique was proposed by the following scientists [3]–[5]. It has also been adapted to build several practical programs for *knapsack 0-1* problem [6], [7]. The main contribution of this paper is to use the greedy heuristic method to compare the method grasp and evaluated different instances for the knapsack 0-1 problem.

Basically, the greedy algorithm work of the following form *Algorithm* 1:

B. DYNAMIC PROGRAMMING ALGORITHM

A lot of researchers already implemented several efficient algorithms for the knapsack 0-1 problem, and many of these algorithms using dynamic programming [2], [8]. In this paper was implemented the dynamic programming approach top-down.

The dynamic algorithm is shown in the following procedure *Algorithm* 2:

C. GRASP ALGORITHM

A GRASP is a metaheuristic for combination optimization. Can be implemented using multi-start or iterative process, in which each GRASP iteration consists of two phases, in which a feasible solution is produced, and a local search phase, in which a local optimum in the neighborhood of the constructed solution is sought [1].

For this paper, was use the iterative phase which can be shown following form 3:

III. EXPERIMENTS AND RESULTS

Considering the analysis of the experiment it was set two different plot for some methods in different metrics, the first metric is defined as coefficient determinist determination, in which is used find correlation in dynamic programming and greedy heuristic, and also grasp method metaheuristic [9]. The second plot is one analysis of behavior between the *Dynamic Programming*, *Greedy*, and *GRASP* method.

Algorithm 1 Knapsack Problems 0-1 Using Greedy Method

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procedure KNAPSACK($Value$, $Weight$, $Capacity$, $item$)
// create the array ration which is sorted by value over weight
max_value = 0

    while *element of the ratio array is not visited* **do**
      if $ratio[i] <= capacity$ **then**
        capacity -= weigth[i]
        max_valeu += value[i]
  return max_value

Algorithm 2 Knapsack Problems 0-1 Using Dynamic Programming Method

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procedure KNAPSACK(w, n, $cache$, $wVector$, $valVector$)
  if $n == 0$ or $w == 0$ **then**
    return 0
  if $cache[n-1][w]$!= -1 **then**
    return $cache[n-1][w]$
  if $wVector[n-1] > w$ **then**
    return $knapSack(w, n-1, cache, wVector, valVector)$
  $a = valVector[n-1] + knapSack(w - wVector[n-1], n-1, cache, wVector, valVector)$
  $b = knapSack(w, n-1, cache, wVector, valVector)$
  return $\max(a, b)$

Algorithm 3 Knapsack Problems 0-1 Using GRASP Method

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procedure KNAPSACK($Value$, $Weight$, $Capacity$, $item$, $max_iteration$)
  best = 0
  for $i = 1$; $i < max_iteration$; $i{+}{+}$ **do**
    $solution = Greedy_Randomized_Construction(Value, Weight, Capacity, item)$
    $solution = local_search(Value, Weight, Capacity, item)$
    $best = max(best, cost(solution, Value, Weight, Capacity))$
  return $best$

According to Figure 1, we can do observe the behavior of the instance GRASP (axis X) in relation instance Dynamic Programming (axis Y). Can determine that as correlation and instance Grasp and instance optimal output value. Can go to more deep, can do to determine that are correct maximize value, for instance, greater than 140,000 value according to the optimal algorithm.

The behavior of the *Dynamic Programming*, *Greedy*, and *GRASP* method is shown in the Figure 2. According the figure, one observed that GRASP algorithm is equal to the optimal algorithm (*Dynamic Programming*.

Another analysis is shown in Figure 3 where one can to view which instance that delayed and it can be noted that had the highly execution time was the Dynamic Programming Method that came about 6 min according the graphic, this analysis proves that the grasp method was superior to Dynamic Programming in all of the instances.

IV. CONCLUSION

Finally, one can conclused that metaheuristic *GRASP* was better that methods *Greedy* and *Dynamic Programming*, princepily the measured execution time according the Table I.
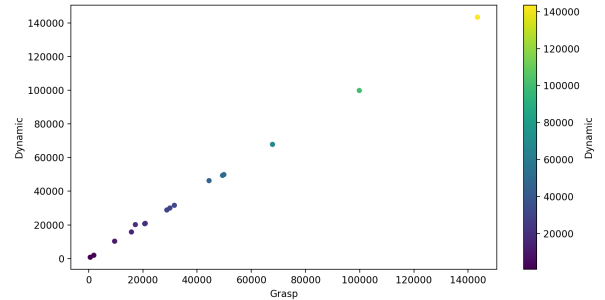

Fig. 1. Coefficient determinist (or score R^2) applied to output instance between the *Dynamic Programming* (axis Y) and *GRASP* method (axis X).

|	MEASURED EXECUTION TIME IN m/s		
Instance	**Dynamic Programming**	**Greedy Heuristic**	**GRASP Metaheuristic**
1	0.299604	0.000049	0.012054
2	0.831294	0.000045	0.035831
3	2.007281	0.000059	0.304420
4	2.014614	0.000049	0.082717
5	1.989233	0.000087	1.203739
6	26.858557	0.000148	5.439759
7	0.598913	0.000224	1.355621
8	0.785180	0.000289	3.156068
9	10.908195	0.000795	7.355839
10	4.878645	0.000086	0.129530
11	7.812857	0.000082	0.260361
12	2203.987961	0.009826	4115.226108
13	1043.048750	0.011252	789.132951
14	431.436847	0.004796	3905.787402
15	3.979783	0.000859	30.129698
16	4.037800	0.000832	22.595806
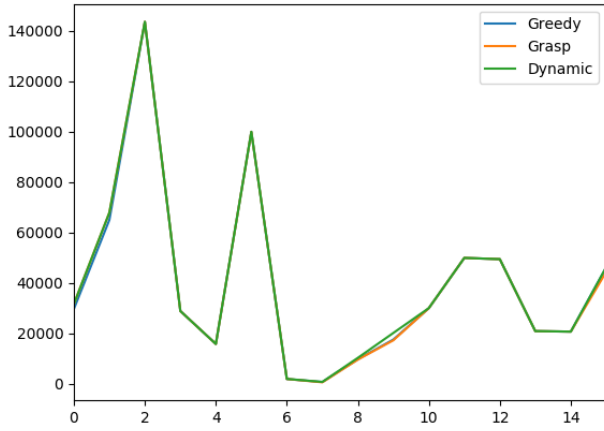
Fig. 2. Behavior of the three methods (*Dynamic Programming*, *Greedy*, and *GRASP*) for the Knapsack 0-1 problem
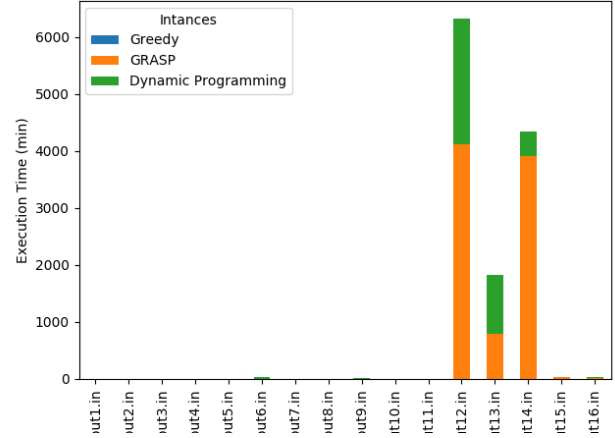

Fig. 3. Execution time analysis for respectively method: the *Dynamic Programming*, *Greedy*, and *GRASP*.

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