

$$\begin{aligned}
& \mathfrak{Z} \\
& \mathcal{G} = \\
& (V, E) \\
& V = \\
& \{1, \dots, m\} \\
& E \subseteq \\
& V \times \\
& V \\
& (s, t) \in \\
& E \\
& \text{undi-} \\
& \text{rected} \\
& (s, t) \\
& (t, s) \\
& \text{di-} \\
& \text{rected} \\
& (s \rightarrow \\
& t) := \\
& (s, t) \\
& \text{Remark:} \\
& (s, s) \notin \\
& E, \forall s \in \\
& V \\
& \mathcal{G}' = \\
& (V', E') \\
& \mathcal{G} = \\
& (V, E) \\
& V' \subseteq \\
& V \\
& E' \subseteq \\
& E \\
& V' \subseteq \\
& V \\
& \mathcal{G} = \\
& (V, E) \\
& \text{vertex-} \\
& \text{induced} \\
& \text{sub-} \\
& \text{graph} \\
& \mathcal{G}'(V') = \\
& (V', E(V')) \\
& E(V') = \\
& \{(s, t) \in \\
& E \mid s, t \in \\
& V'\} \\
& E' \subseteq \\
& E \\
& \mathcal{G} = \\
& (V, E) \\
& \text{edge-} \\
& \text{induced} \\
& \text{sub-} \\
& \text{graph} \\
& \mathcal{G}'(E') = \\
& (V(E'), E') \\
& V(E') = \\
& \{s \in \\
& V \mid (s, t) \in \\
& E'\} \\
& P = \\
& (V(P), E(P)) \\
& V(P) = \\
& \{v_0, \dots v_k\} \\
& V(P) = \\
& \{(v_0, v_1), (v_1, v_2) \dots (v_{k-1}, v_k)\} \\
& v_0 \\
& v_k \\
& \mathcal{G} = \\
& (V, E) : V(P) \subseteq \\
& V, E(P) \subseteq \\
& E \\
& \mathcal{C} = \\
& (V(C), E(C)) \\
& V(C) = \\
& \{v_0, \dots v_k\} \\
& E(C) = \\
& \{(v_0, v_1), (v_1, v_2) \dots (v_{k-1}, v_k), \dots (v_k, v_0)\} \\
& \mathcal{G} = \\
& (V, E) \\
& V = \\
& V_a \dot{\cup} V_b \\
& (s, t) \in \\
& E \Rightarrow \\
& s \in \\
& V_a, t \in \\
& V_b \\
& \mathcal{G} = \\
& (V, E) \\
& V' \subseteq
\end{aligned}$$