

9. 技術A:  $q = \min\{L/2, K/4\}$  技術B:  $q = \min\{L/4, K/2\}$   $w=1$   $r=2$

(A)  $TC = \text{生產成本} + \text{權利金成本}$

$$\text{生產成本A: } q = \frac{L}{2} \quad L = 2q \quad q = \frac{K}{4} \quad K = 4q \quad C = 1 \times 2q + 2 \times 4q = 10q$$

$$\text{生產成本B: } q = \frac{L}{4} \quad L = 4q \quad q = \frac{K}{2} \quad K = 2q \quad C = 1 \times 4q + 2 \times 2q = 8q$$

$$TC_A = 10q + 40 \quad TC_B = 8q + 100$$

(B)  $q=20$   $TC_A = 240$   $TC_B = 260$ , 買A

(C)  $q=40$   $TC_A = 440$   $TC_B = 420$ , 買B

(D) 若  $TC_A$  要小於  $TC_B$ ,  $q$  應低於 30

11.  $q = 10L^{0.5}K^{0.5}$ ,  $w=r=10$ , 設  $K$  固定為  $K_0$

(A)  $q = 10L^{0.5}K^{0.5} \rightarrow L^* = \frac{q^2}{100K}$

$$STC = \left(\frac{q^2}{10K}\right) + 10K \quad AC = \frac{q}{10K} + \frac{10K}{q}, \quad MC = \frac{q}{5K}$$

(B)  $\frac{\partial STC}{\partial K} = \frac{-q^2}{10K^2} + 10 = 0 \Rightarrow K^* = \frac{q}{10}$ , 代入  $STC$  函數,

$$TC = STC(K=K^*) = \frac{q^2}{10 \times (q/10)} + 10 \frac{q}{10} = q + q = 2q$$

12.  $q=20 \rightarrow AC, AVC$  差 10 元,  $q=40 \rightarrow AC, AVC$  差?

$$q=20, AC - AVC = AFC = 10 \rightarrow AFC \times q = 10 \times 20 = 200$$

$$q=40, AC - AVC = AFC = \frac{FC}{q} = 200 \div 40 = 5$$

13.  $MC = 10q$ ,  $C = 100$  元, 產量 10 單位  $AT$  之  $TC$ ?

$$VC(10) = \int_0^{10} 10q dq = 5q^2 \Big|_0^{10} = 500, \quad TC = VC + FC = 500 + 100 = 600$$