

# homework 1, CS 421

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Apply  $\rho_i$  to denote the environment at the  $i$ th point.

- 1)  $\rho_1 = \emptyset$
- 2)  $\rho_2 = \{a \rightarrow 10, x \rightarrow 21\}$
- 3)  $\rho_3 = \{\{f \rightarrow \langle x \rightarrow y \rightarrow x - y + a, \rho_2 \rangle\} + \rho_2\}$
- 4)  $\rho_4 = \{\{b \rightarrow 21, a \rightarrow 5, x \rightarrow 21\} + \{f \rightarrow \langle x \rightarrow y \rightarrow x - y + a, \rho_2 \rangle\}\}$ ,  $\rho_3$  is put into the stack.
- 5)  $\rho_3$  is retrieved from the stack,  $\rho_5 = \rho_3$
- 6)  $\rho_6 = \{\{f \rightarrow \langle x \rightarrow y \rightarrow x - y + a, \rho_2 \rangle\} + \{a \rightarrow 10, x \rightarrow 1\}\}$
- 7)  $\rho_7 = \{\{h \rightarrow \langle y \rightarrow f \ 2 \ 20, \rho_6 \rangle\} + \rho_6\}$
- 8)  $\rho_7$  is put into the stack,

$$\rho_8 = \{\{h \rightarrow \langle y \rightarrow f \ (y + 4), \rho_7 \rangle\} + \{f \rightarrow \langle x \rightarrow y \rightarrow x * y, \rho' \rangle\} + \rho''\}$$

where  $\rho' = \{\{h \rightarrow \langle y \rightarrow f \ (y + 4), \rho_7 \rangle\} + \rho_6\}$ ,  $\rho'' = \{a \rightarrow 10, x \rightarrow 1\}$

- 9)  $\rho_7$  is retrieved from the stack, and  $\rho_9 = \rho_7$