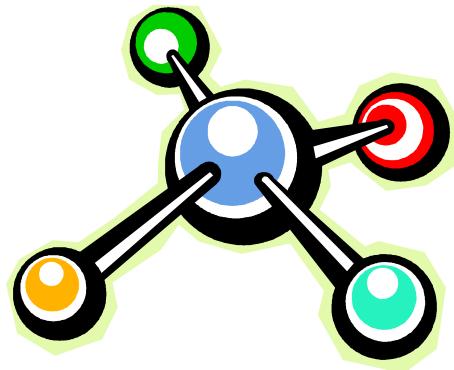


# Model-Based Testing



Harry Robinson  
*Google*  
[harryr@google.com](mailto:harryr@google.com)

# Goals for Today

- Convey techniques for
  - How to model systems
  - How to generate tests
  - How to verify results
- Communicate a mindset
- Provide inspiration
- Foster discontent

# Non-Goals for Today

- Specific tools
- Interfacing with an application

# What are the Problems of Software Testing?



- Time is limited

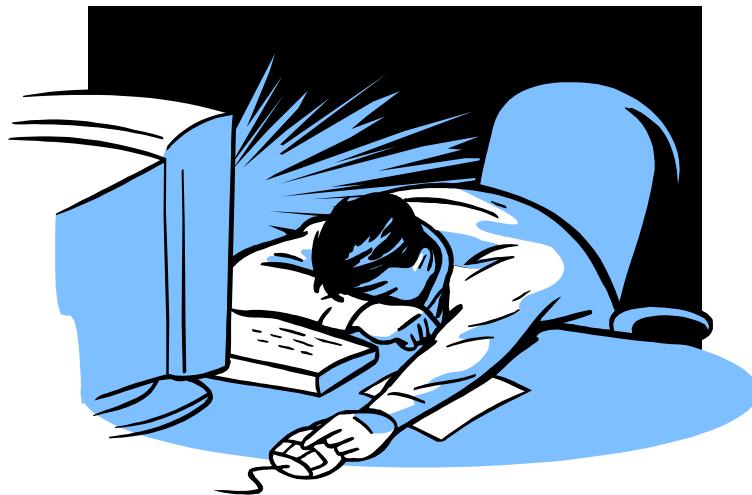


- Applications are complex

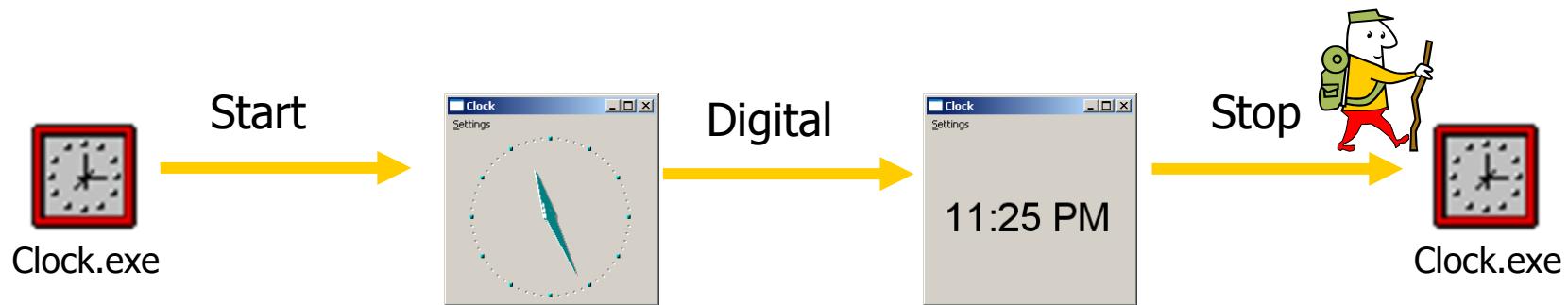


- Requirements are fluid

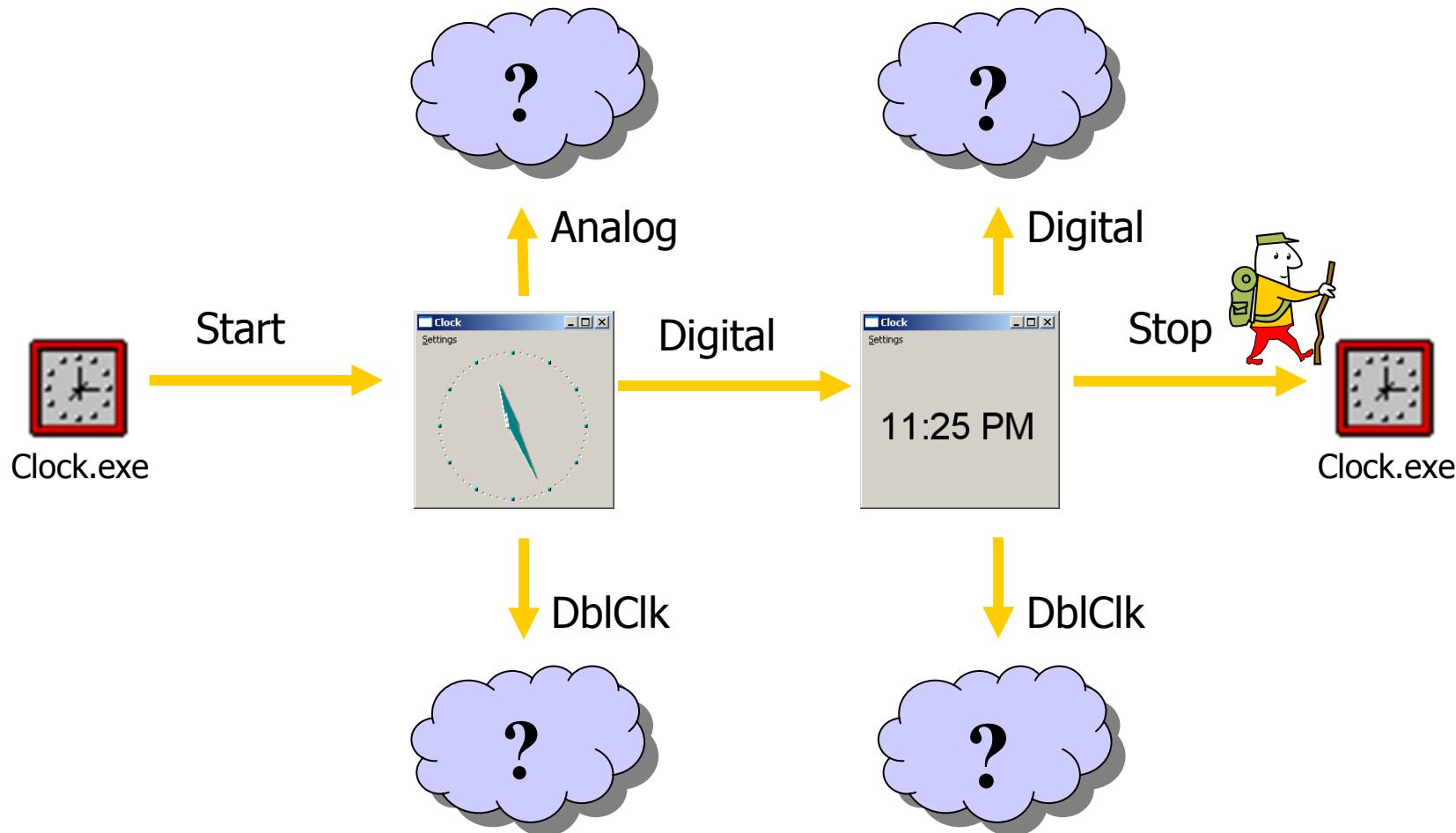
# What's wrong with manual testing?



# Manual testing is ok sometimes ...



# ... but it can rarely go deep enough



# What's wrong with scripting?



# The Villain of this Piece



- Awe-inspiring
- Unchanging
- Indecipherable

```
Currentwindow = WFndWndC("calculator", "scicalc")
WSetWndPosSiz(Currentwindow, 88, 116, 260, 260)
WMenuSelect("@2\@2")
Currentwindow = WFndWndC("calculator", "scicalc")
WSetWndPosSiz(Currentwindow, 88, 116, 480, 317)
WButtonClick("@32")
WButtonClick("@27")
WButtonClick("@38")
WButtonClick("@58")
WMenuSelect("@2\@1")
Currentwindow = WFndWndC("calculator", "scicalc")
WSetWndPosSiz(Currentwindow, 88, 116, 260, 260)
WMenuSelect("@2\@1")
Play "{click 330, 131, Left}"
WToolBarButtonClk("@2", "@6")
WToolBarButtonClk("@2", "@7")
WToolBarButtonClk("@1", "@1")
```

# Scripts are ok for some uses ...

Test case 1: Start Digital Stop Start Analog Stop

Test case 2: Start DblClk Stop Start DblClk Stop

# ... but they pile up quickly ...

Test case 1: Start Digital Stop Start Analog Stop

Test case 2: Start DblClk Stop Start DblClk Stop

Test case 3: Start Digital DblClk Stop Start DblClk Analog Stop

Test case 4: Start DblClk DblClk Digital DblClk DblClk Stop Start Analog Stop

Test case 5: ...

# ... and what are you left with?

Test case 1: Start Digital Stop Start Analog Stop

Test case 2: Start DblClk Stop Start DblClk Stop

Test case 3: Start Digital DblClk Stop Start DblClk Analog Stop

Test case 4: Start DblClk DblClk Digital DblClk DblClk Stop Start Analog Stop

Test case 5: Start Digital Digital Stop Start Analog Stop

Test case 6: Start DblClk Stop Start Analog DblClk Stop

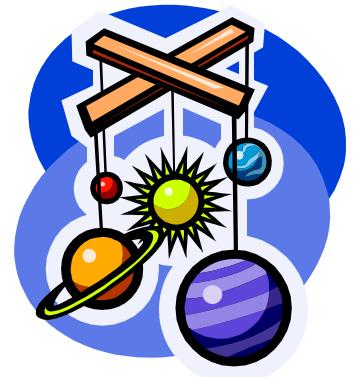
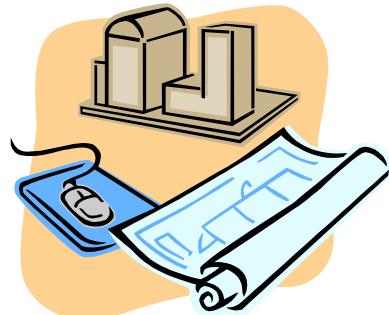
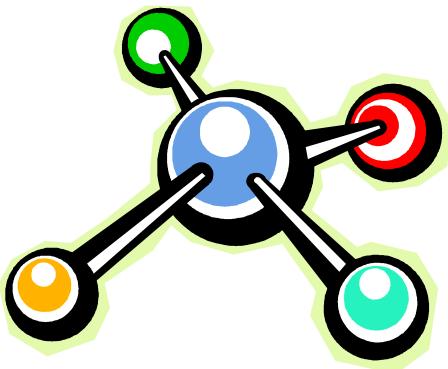
Test case 7: Start Digital DblClk Stop Start Digital DblClk Analog Stop

Test case 8: Start DblClk DblClk Digital Analog DblClk DblClk Stop

Test case 9: ...



# What is a model?



- A model is a description of a system.
- Models are simpler than the systems they describe.
- Models help us understand and predict the system's behavior.

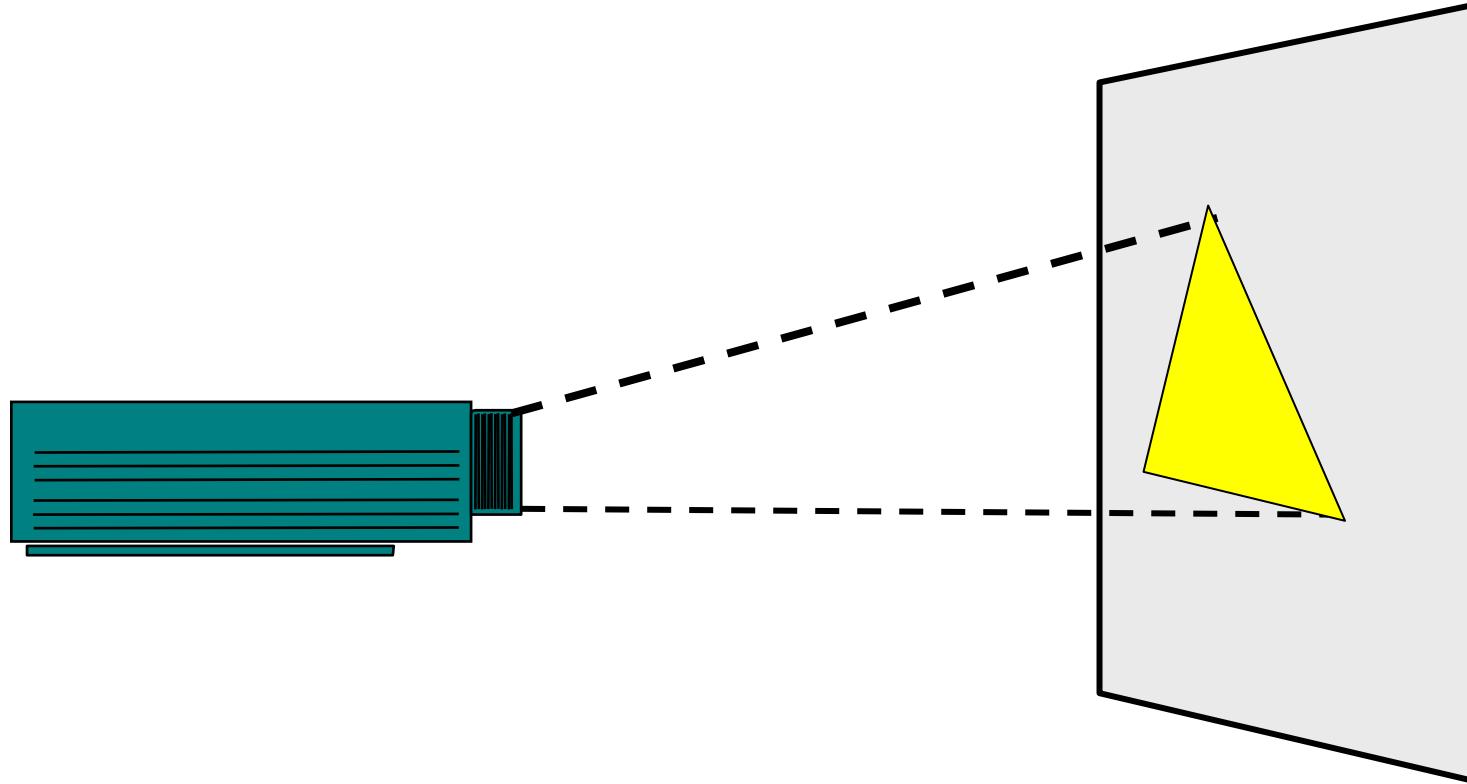
# What is model-based testing?

“Model-based testing is a testing technique where the runtime behavior of an implementation under test is checked against predictions made by a formal specification, or *model*.“ - Colin Campbell, MSR

*In other words*

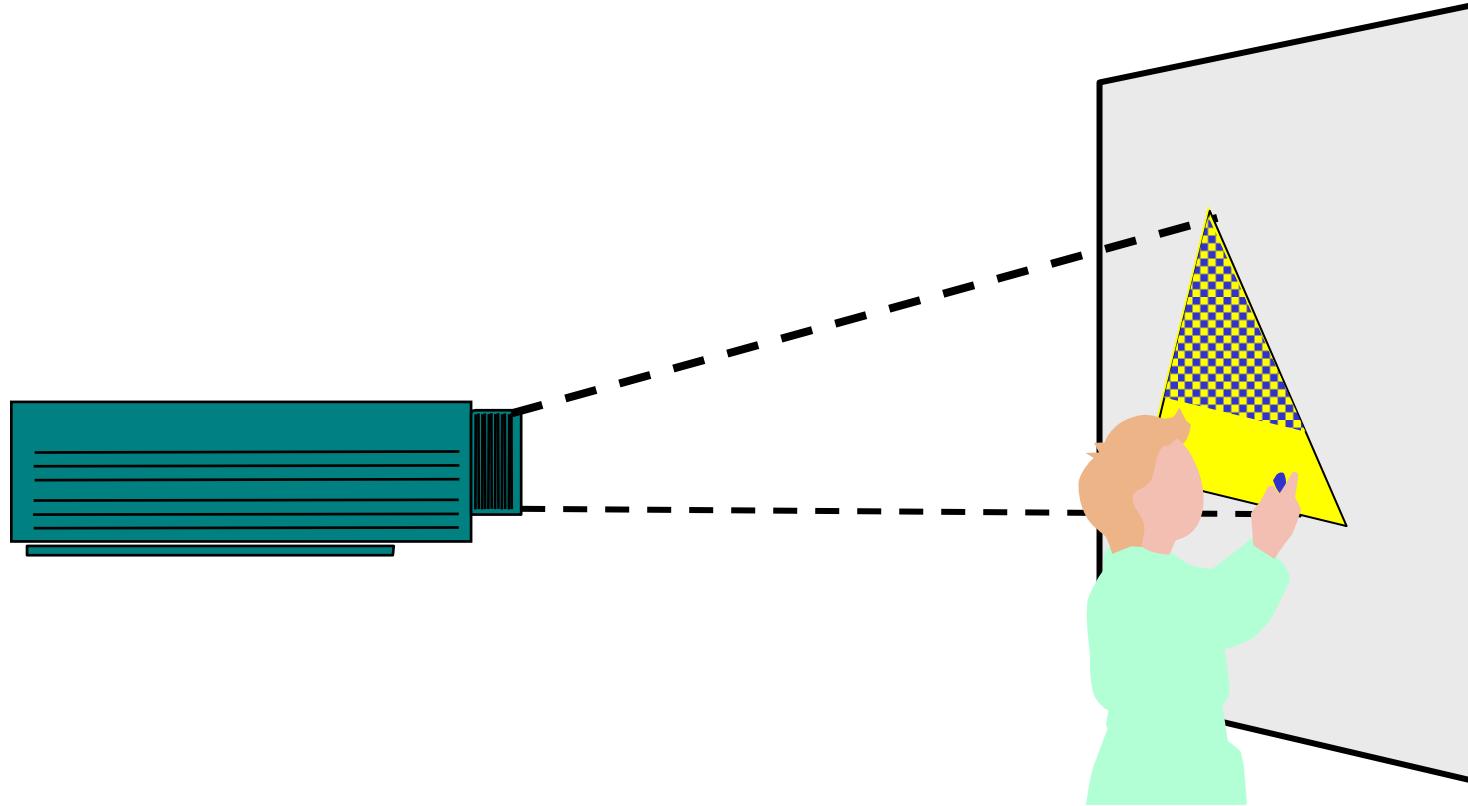
- A model describes how a system should behave in response to an action.
- Supply the action and see if the system responds as you expect.

# Traditional Automated Testing



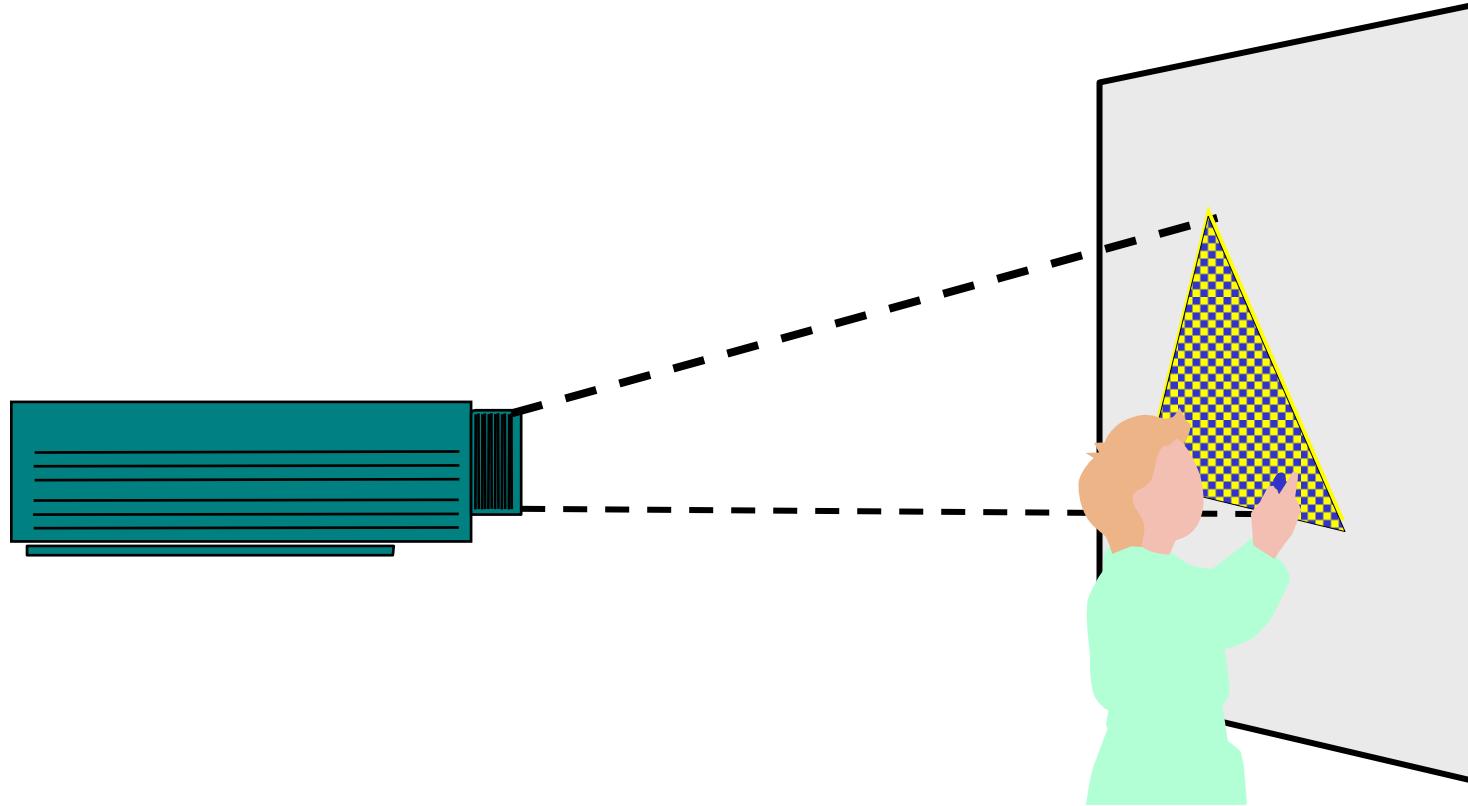
Imagine that this projector is the software you are testing.

# Traditional Automated Testing



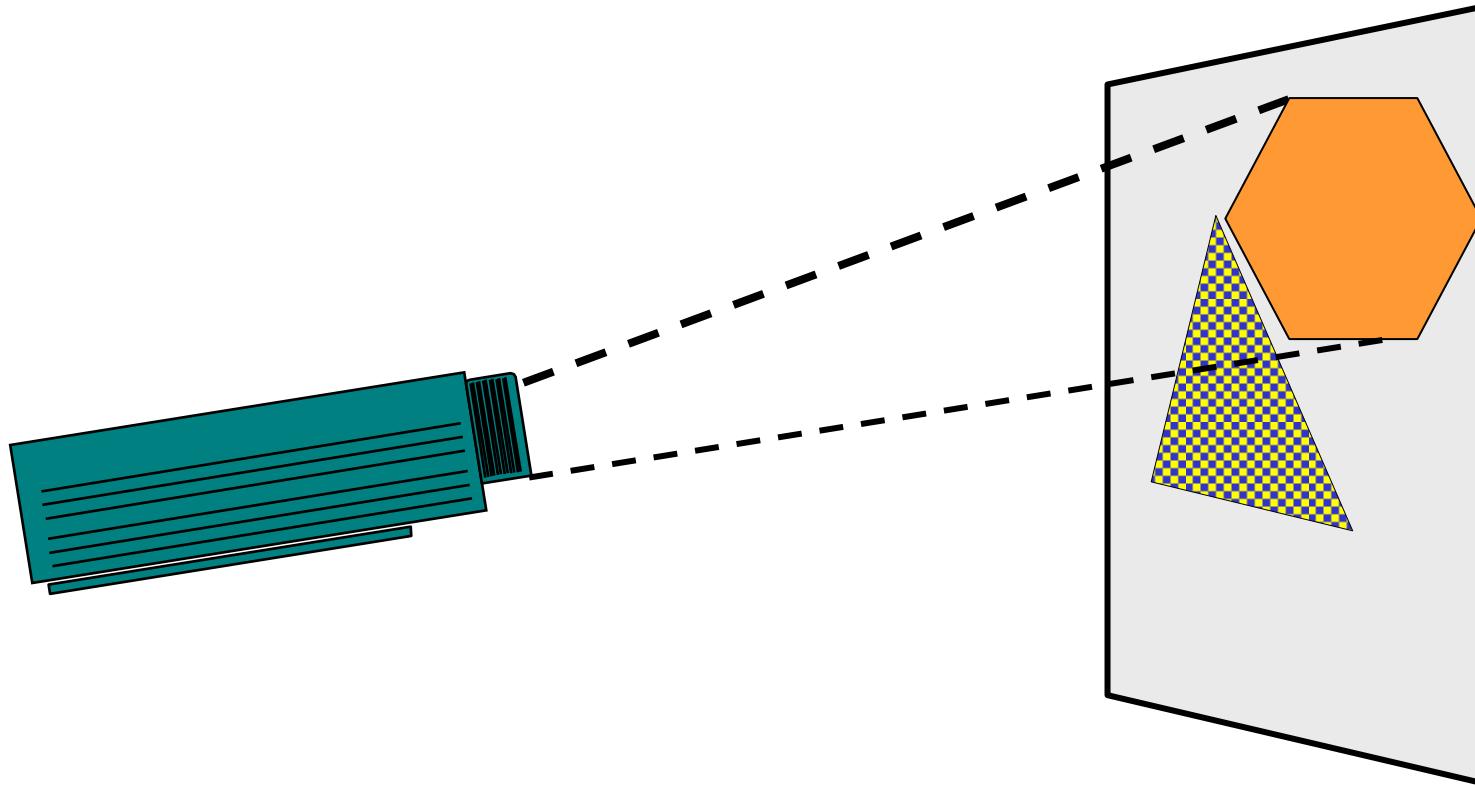
Typically, testers automate by creating static scripts.

# Traditional Automated Testing



Given enough time, these scripts will cover the behavior.

# Traditional Automated Testing



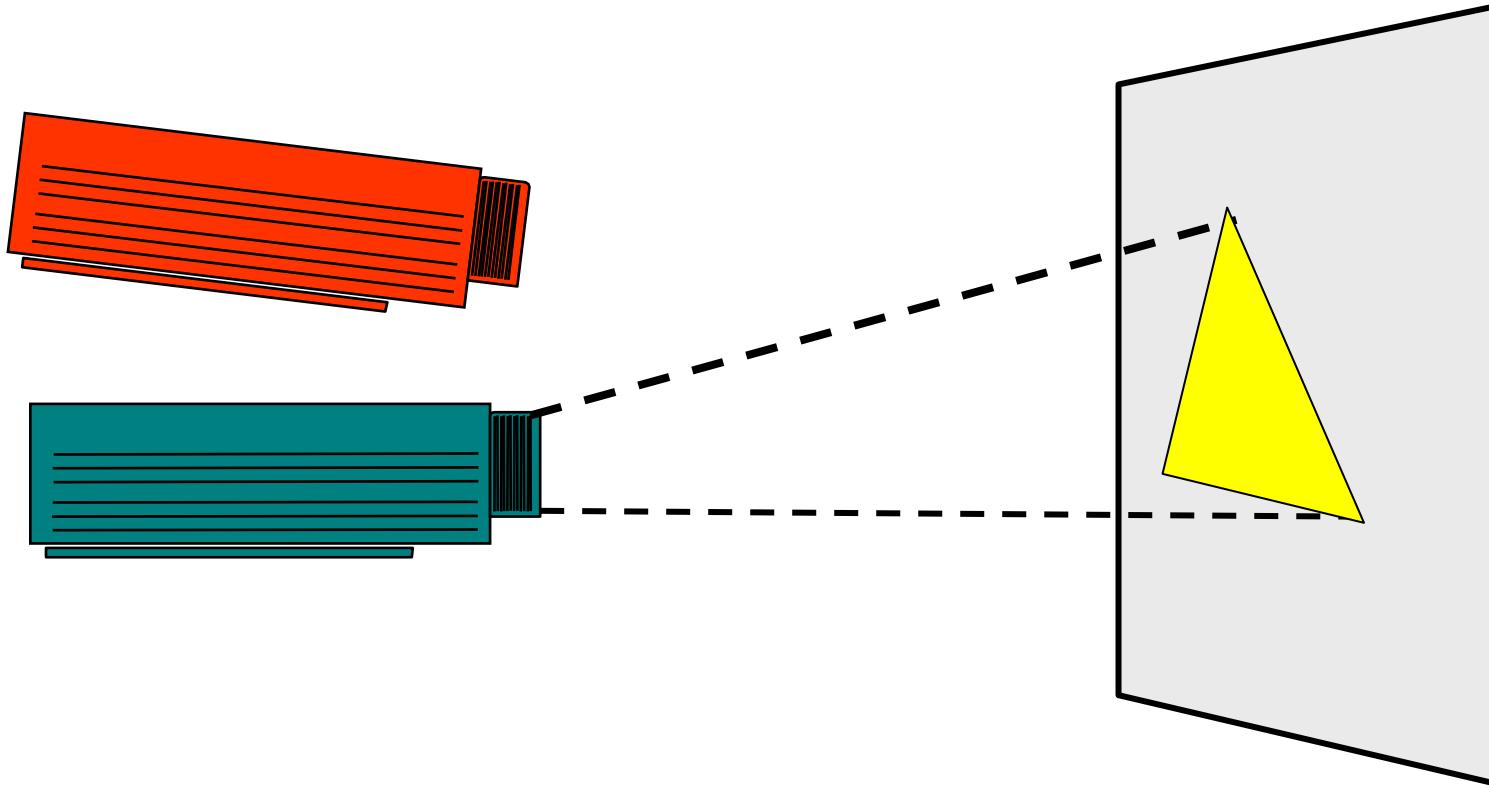
But what happens when the software's behavior changes?

# So What's a Model?



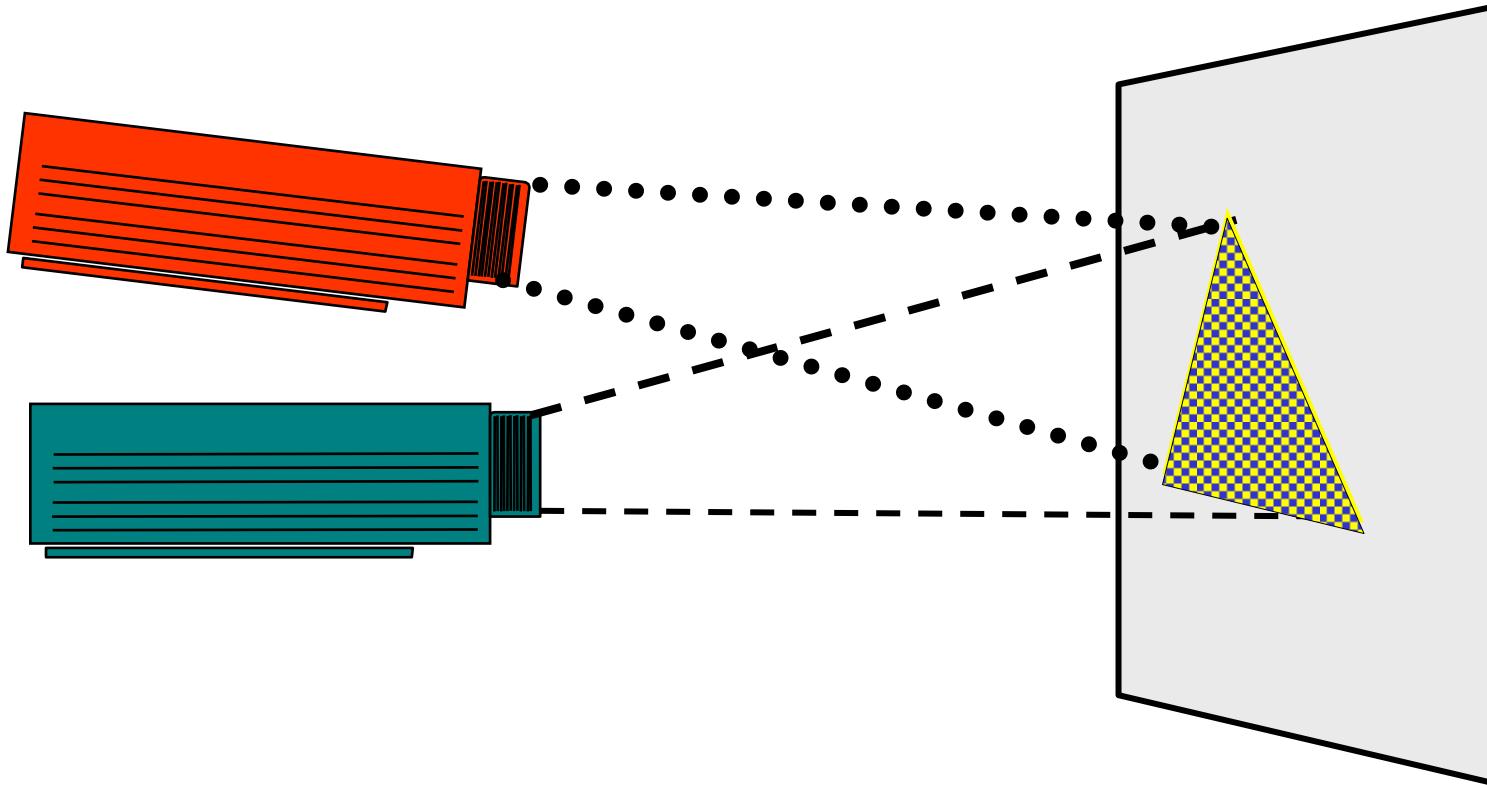
- A model is a description of a system's behavior.
- Models are simpler than the systems they describe.
- Models help us understand and predict the system's behavior.

# Model-Based Testing



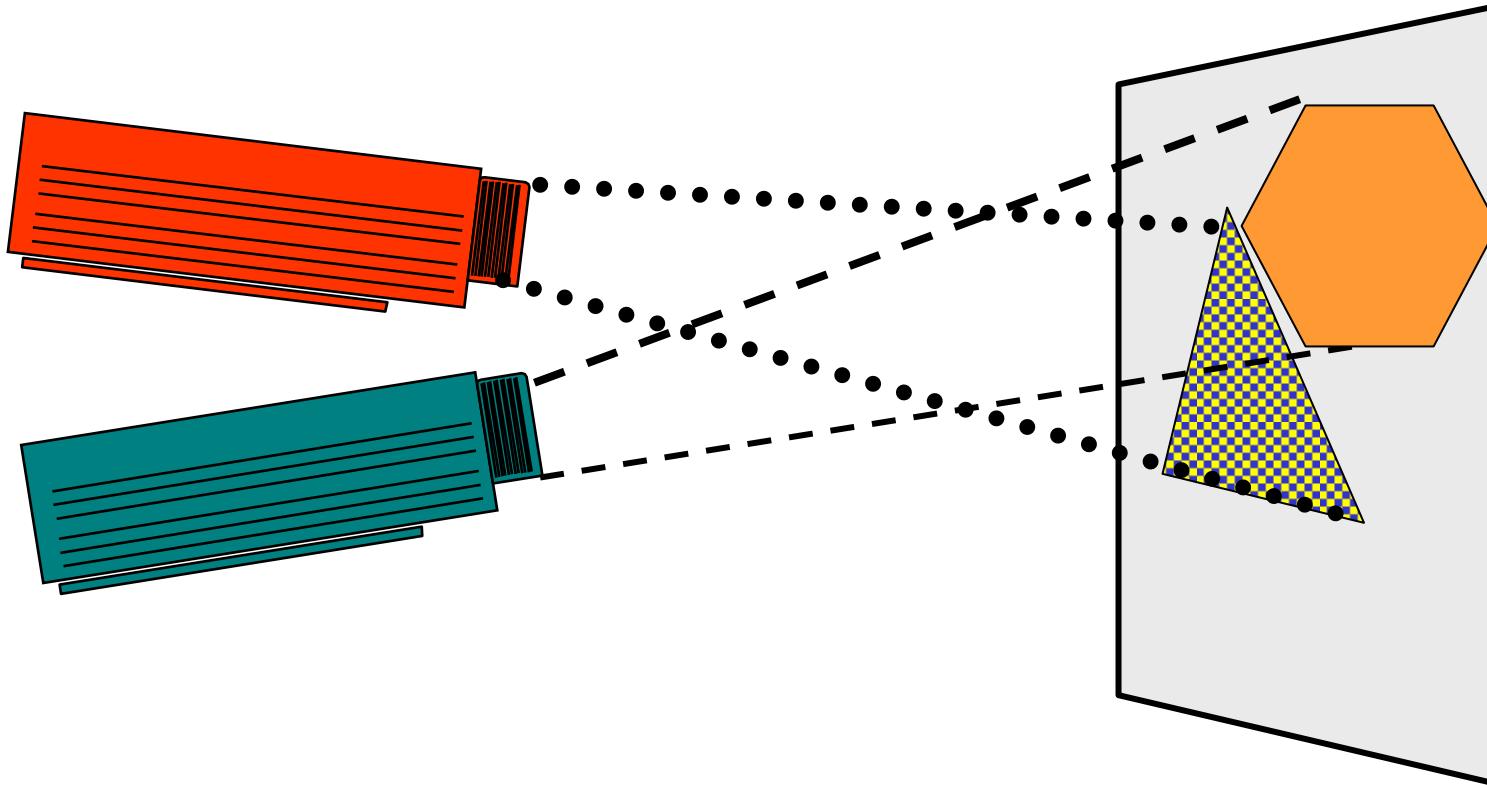
Now, imagine that the top projector is your model.

# Model-Based Testing



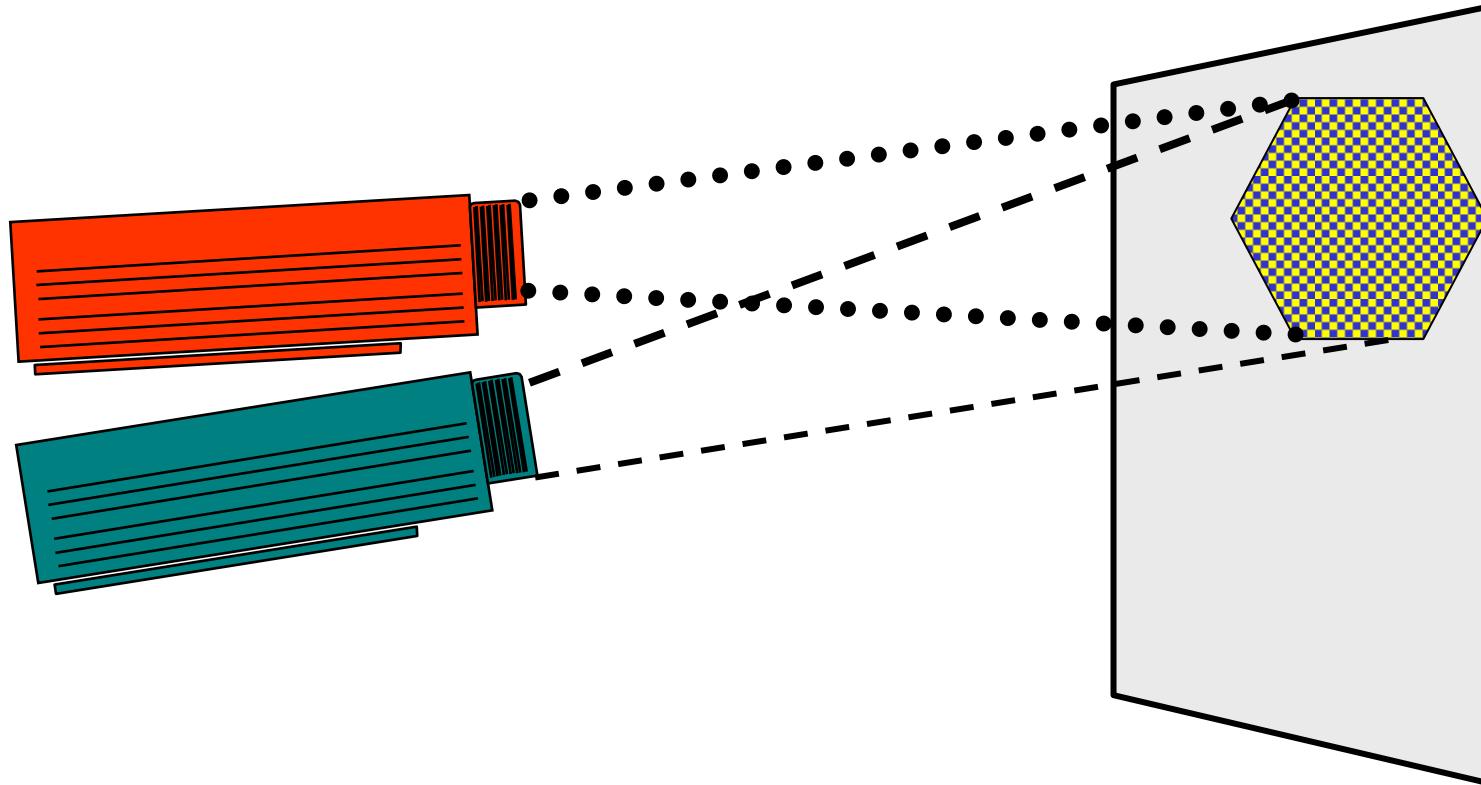
The model generates tests to cover the behavior.

# Model-Based Testing



... and when the behavior changes...

# Model-Based Testing



... so do the tests.

# Using Models to Test

- What type of model do I use?
- How do I create the model?
- How do I choose tests?
- How do I verify results?

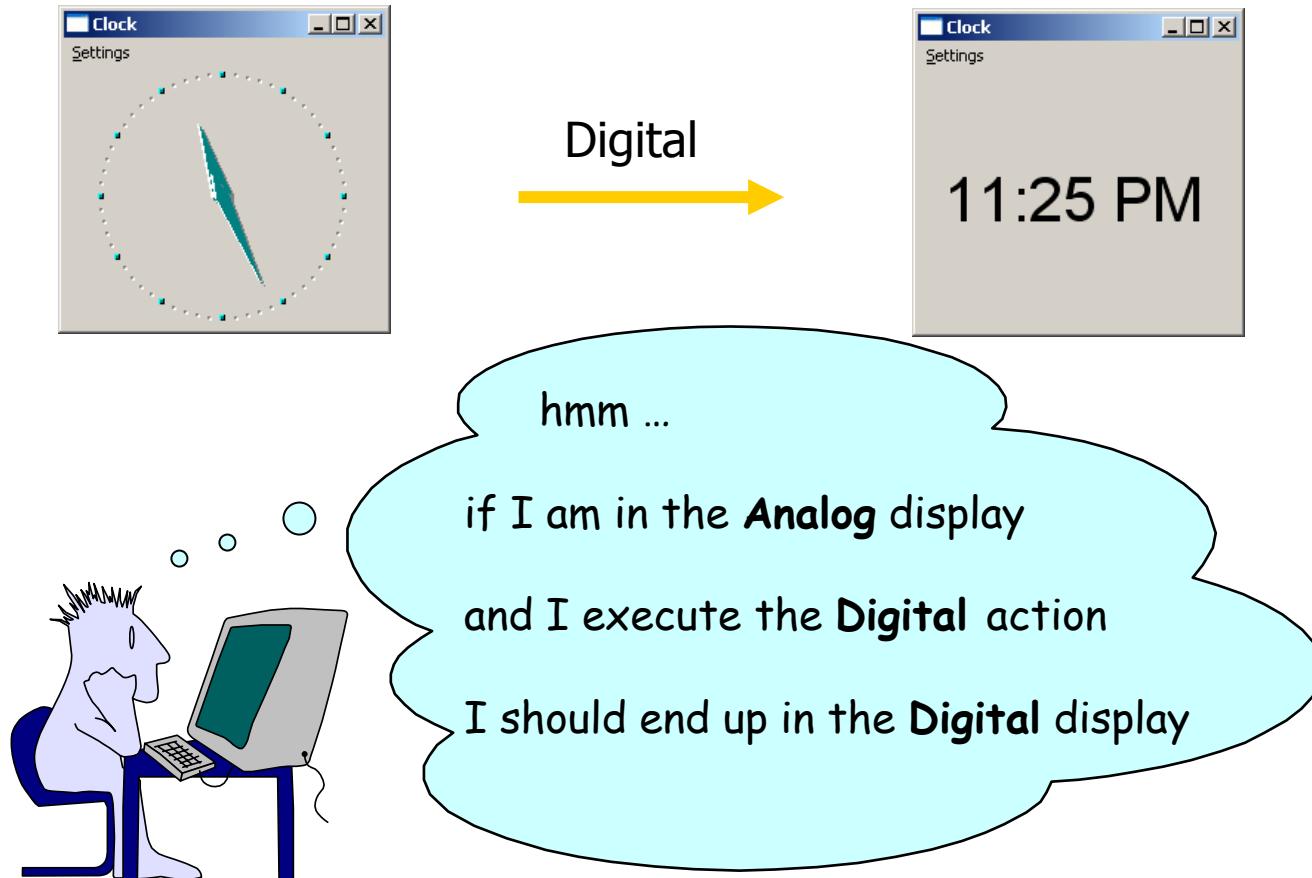
# Many Types of Models

- States
- Monkeys
- Sets
- Grammars
- Combinations
- Other

# Creating a Model



# We All Use Mental Models Already



# State Table Representation

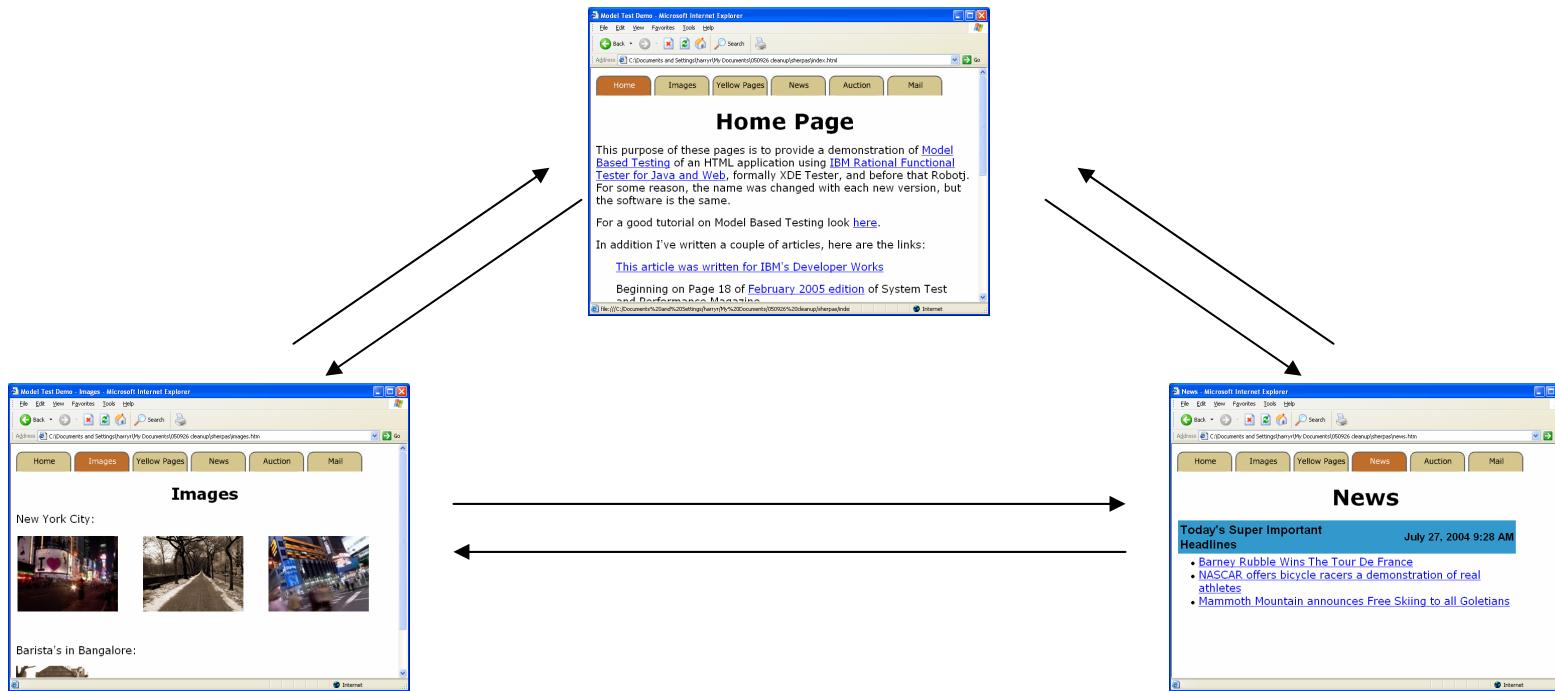


StartState	Action	EndState
Analog	Digital	Digital



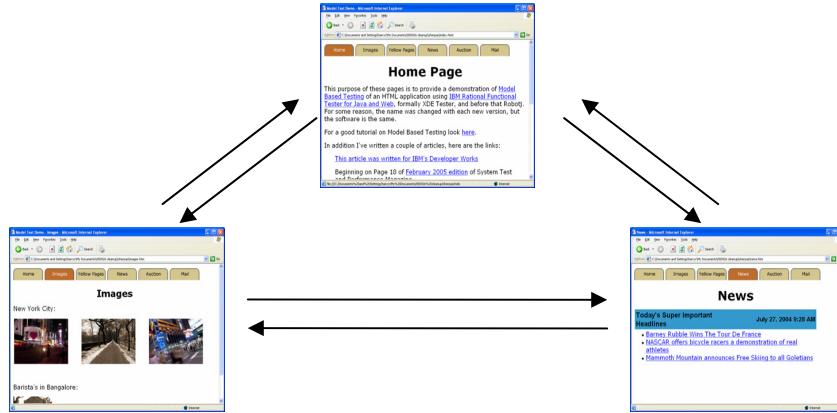
# Exercise 1

# Modeling a Website



Based on “Model-Based Testing: Not for Dummies” by Jeff Feldstein

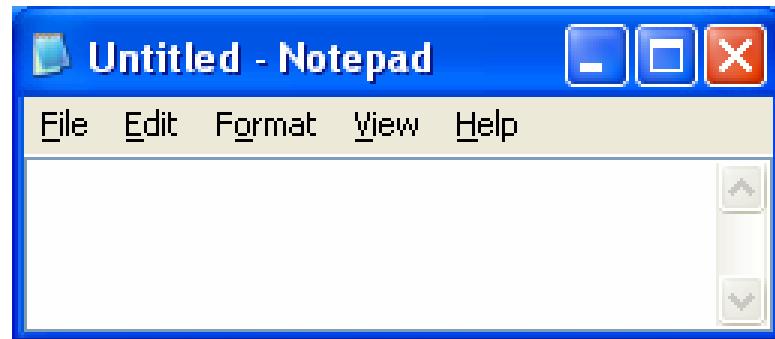
# State Table Representation



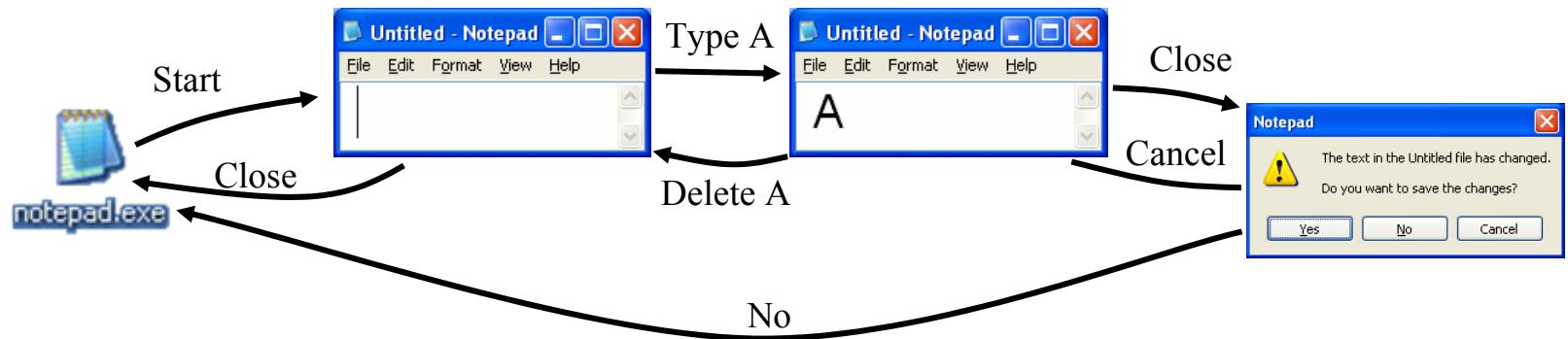
StartState	Action	EndState
HomePage	ImageTab	ImagePage
HomePage	NewsTab	NewsPage
ImagePage	HomeTab	HomePage
ImagePage	NewsTab	NewsPage
NewsPage	HomeTab	HomePage
NewsPage	ImageTab	ImagePage

## Exercise 2

# Modeling Notepad



# Notepad Model

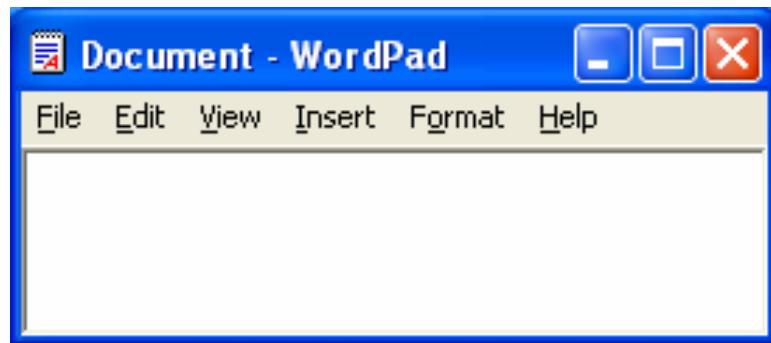


# Notepad State Table

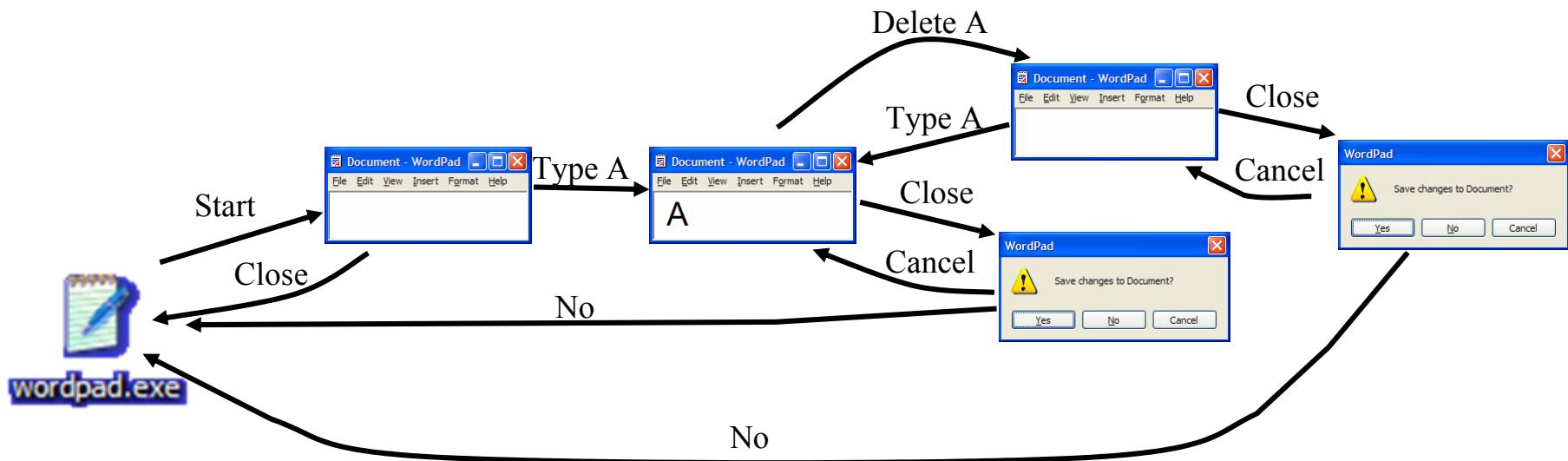
StartState	Action	EndState
NotRunning	Start	Mainwindow
windowEmpty	TypeA	windowDirty
windowEmpty	close	NotRunning
windowDirty	Delete	windowEmpty
windowDirty	close	SaveDialog
SaveDialog	Cancel	windowDirty
SaveDialog	No	NotRunning

## Exercise 3

# Modeling Wordpad



# Wordpad Model

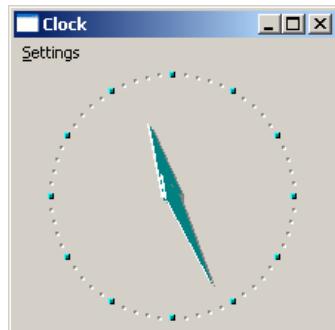


# Wordpad State Table

StartState	Action	EndState
NotRunning	Start	MainWindow
WindowEmpty1	TypeA	WindowDirty
WindowEmpty1	Close	NotRunning
WindowDirty	Delete	WindowEmpty2
WindowDirty	Close	SaveDialog1
WindowEmpty2	TypeA	WindowDirty
WindowEmpty2	Cancel	SaveDialog2
SaveDialog1	Cancel	WindowDirty
SaveDialog1	No	NotRunning
SaveDialog2	Cancel	WindowEmpty2
SaveDialog2	No	NotRunning

## Exercise 4

# Modeling Clock using Rules

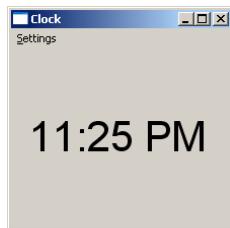


Digital  
→



# Modeling Clock States

In our discussion of the Clock behavior, we only tracked a few data values in the application:



was described as

Running  
Digital  
Framed

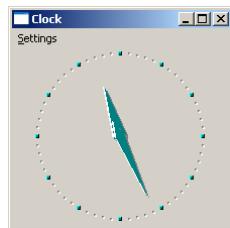


was described as

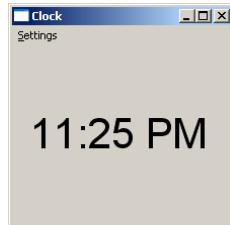
Running  
Analog  
Unframed

# Modeling Clock Actions

We also tracked how our actions change those values:



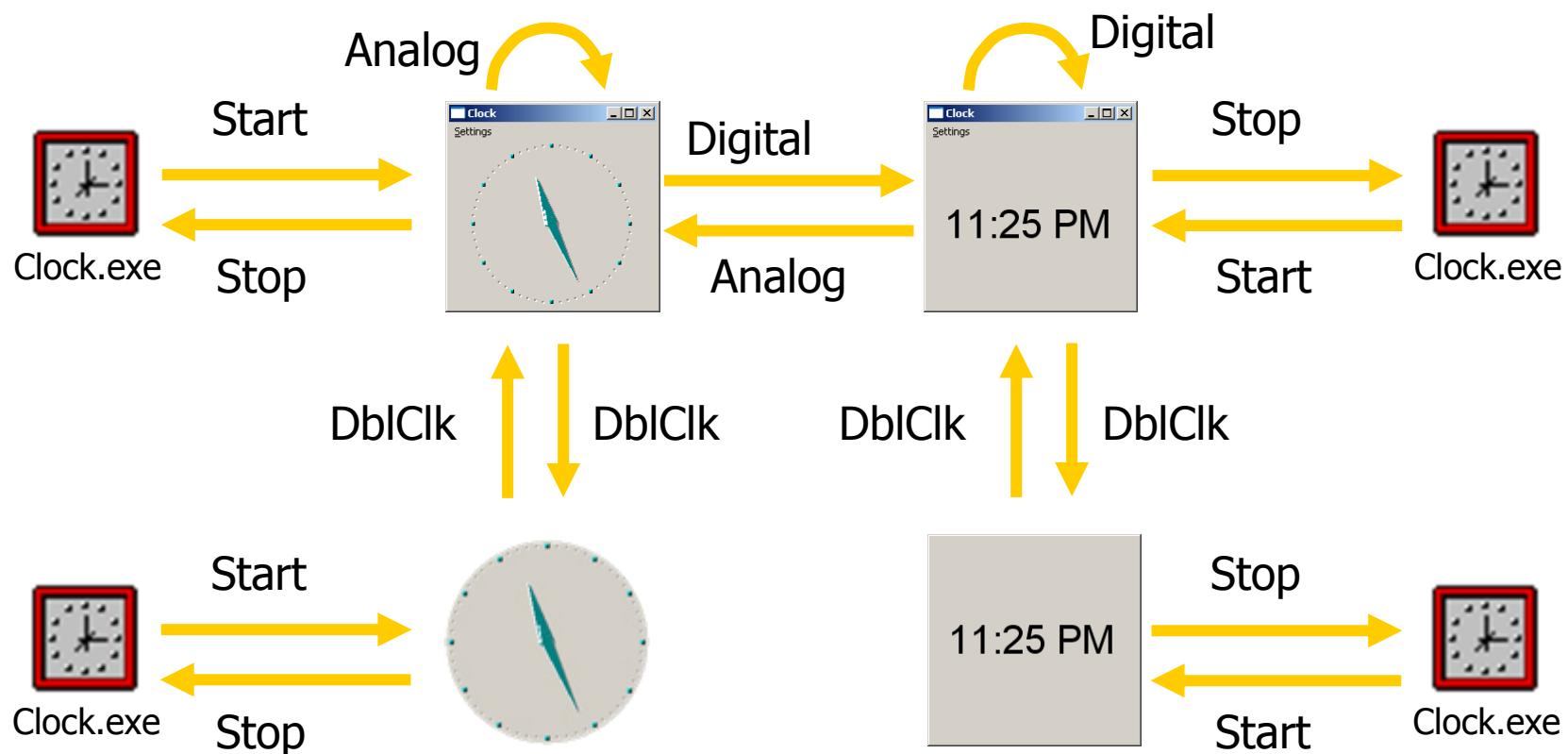
Running  
**Analog**  
Framed



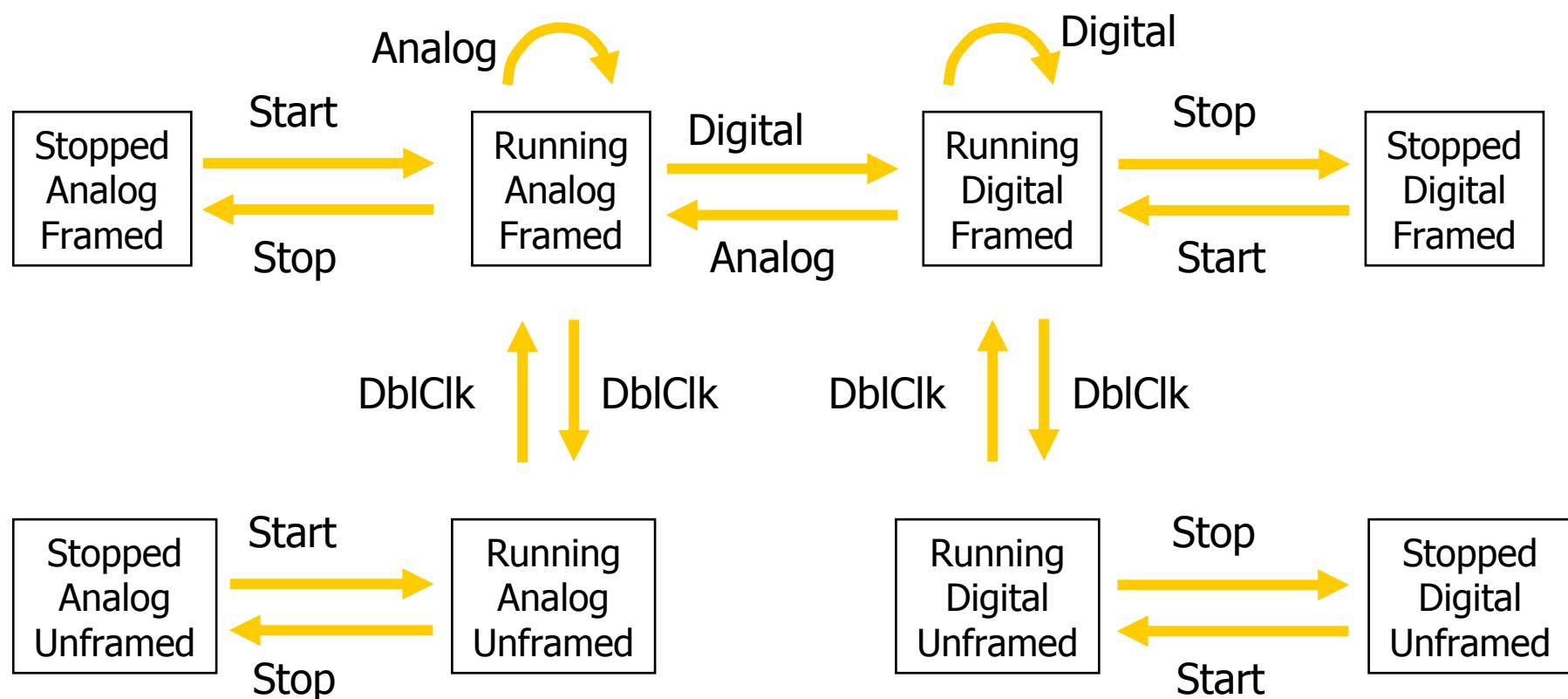
Running  
**Digital**  
Framed



# So, we can replace this model ...

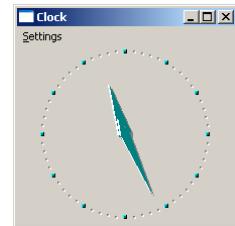


# ... with a state variable model

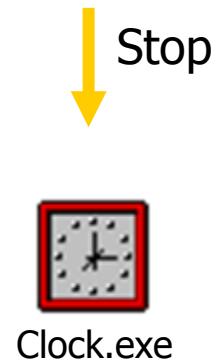


# Rules for the Stop action

- If the Clock is Running, then the user can execute the 'Stop' action.
- The 'Stop' action puts you in Stopped mode



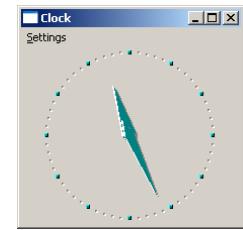
```
static void Stop()  
requires (AppStatus == AppValues.Running);  
{  
    AppStatus = AppValues.Stopped;  
}
```



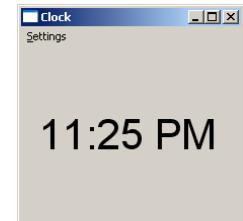
# Rules for the SelectDigital action

- If the Clock is Running and Framed, then the user can execute the 'SelectDigital' action
- The 'SelectDigital' action puts you in Digital mode

```
static void SelectDigital()  
requires (AppStatus == AppValues.Running)  
  && (FrameStatus == FrameValues.Framed);  
{  
  ModeStatus = ModeValues.Digital;  
}
```



↓  
Select  
Digital



# A generated state table!

## STARTSTATE

Stopped Analog Framed  
Running Digital Framed  
Running Digital Framed  
Running Digital Framed  
Running Digital Framed  
Running Analog Unframed  
Running Analog Unframed  
Stopped Digital Framed  
Running Digital Unframed  
Running Digital Unframed  
Stopped Analog Unframed  
Stopped Digital Unframed

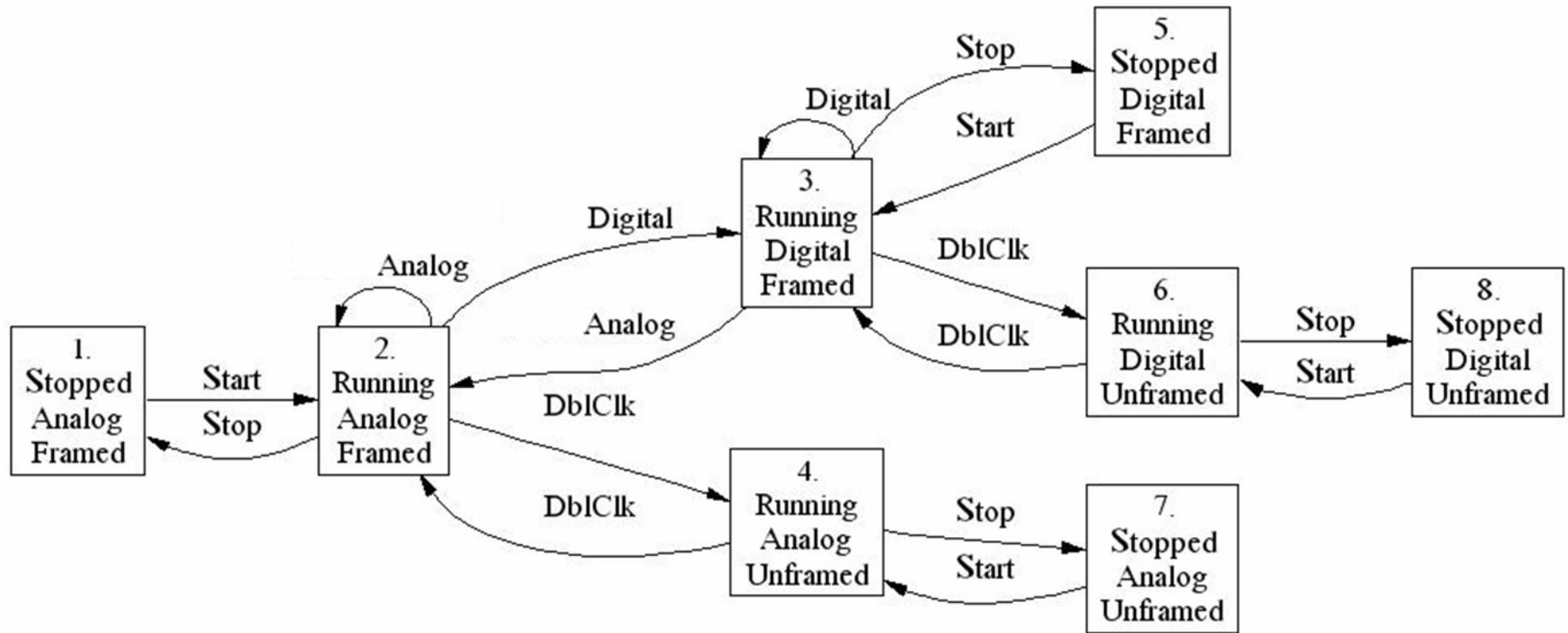
## ACTION

Start  
Stop  
SelectAnalog  
SelectDigital  
DblClk  
Stop  
SelectAnalog  
SelectDigital  
DblClk  
Stop  
DblClk  
Start  
Stop  
DblClk  
Start  
Start

## ENDSTATE

Running Analog Framed  
Stopped Analog Framed  
Running Analog Framed  
Running Digital Framed  
Running Analog Unframed  
Stopped Digital Framed  
Running Analog Framed  
Running Analog Framed  
Running Digital Framed  
Running Digital Unframed  
Stopped Analog Unframed  
Running Analog Framed  
Running Digital Framed  
Stopped Digital Unframed  
Running Digital Framed  
Running Analog Unframed  
Running Digital Unframed

# A state diagram



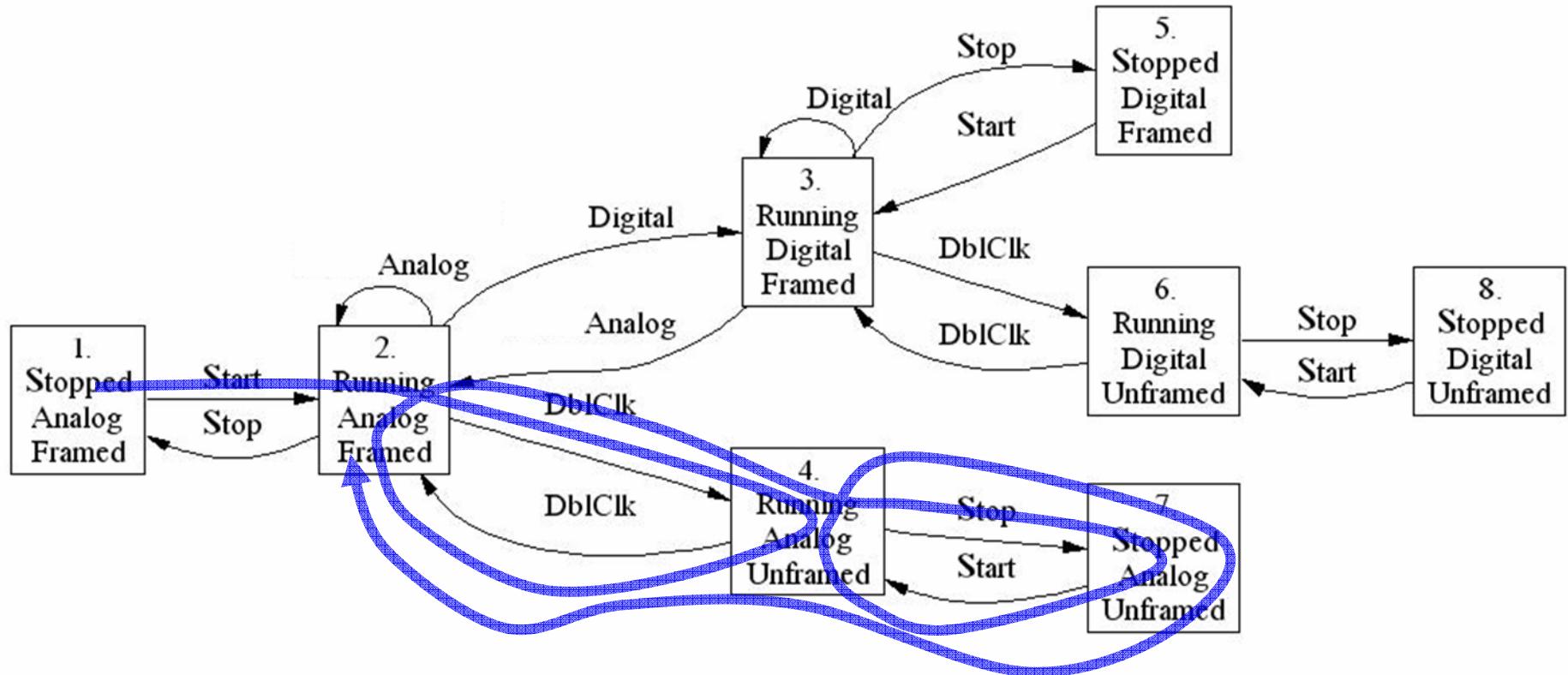
# Generating Tests from a Model

# Generating Test Sequences

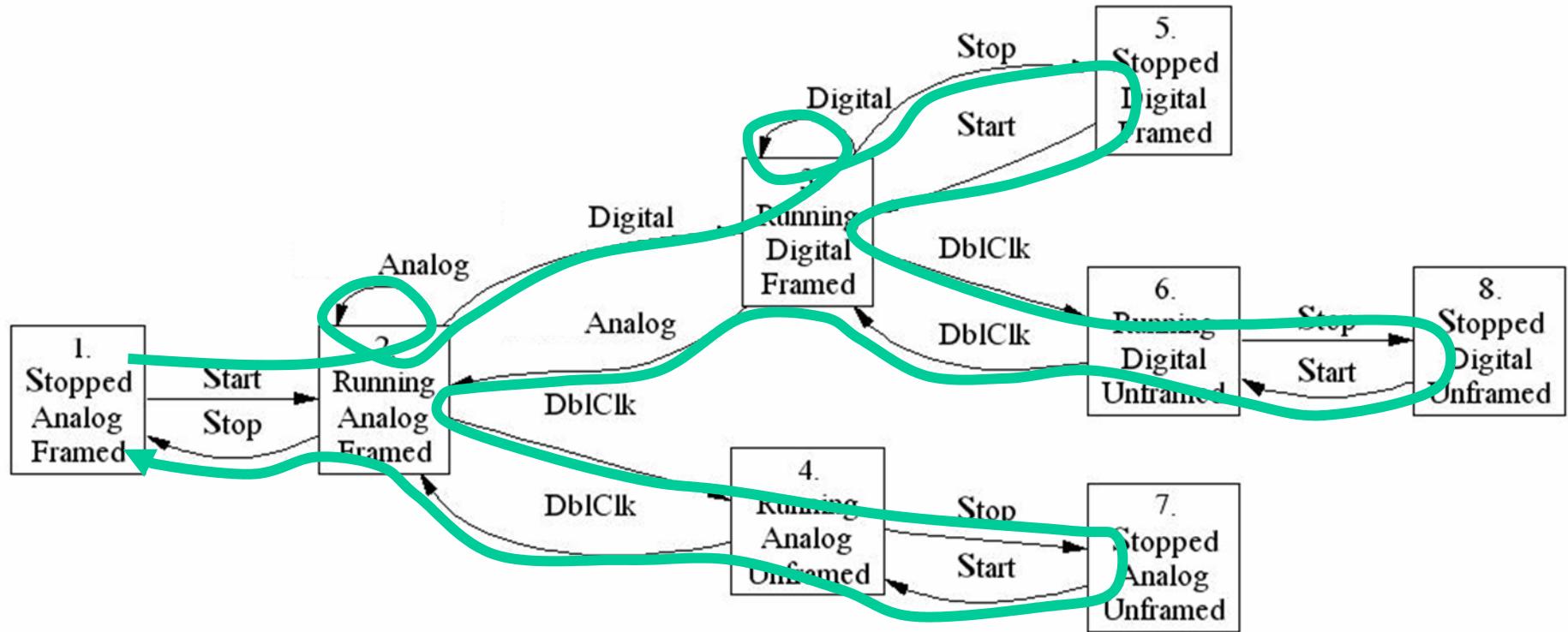
We can use the machine-readable model to create test sequences:

- Random walk
- All transitions
- Shortest paths first
- Most likely paths first

# A Random Walk



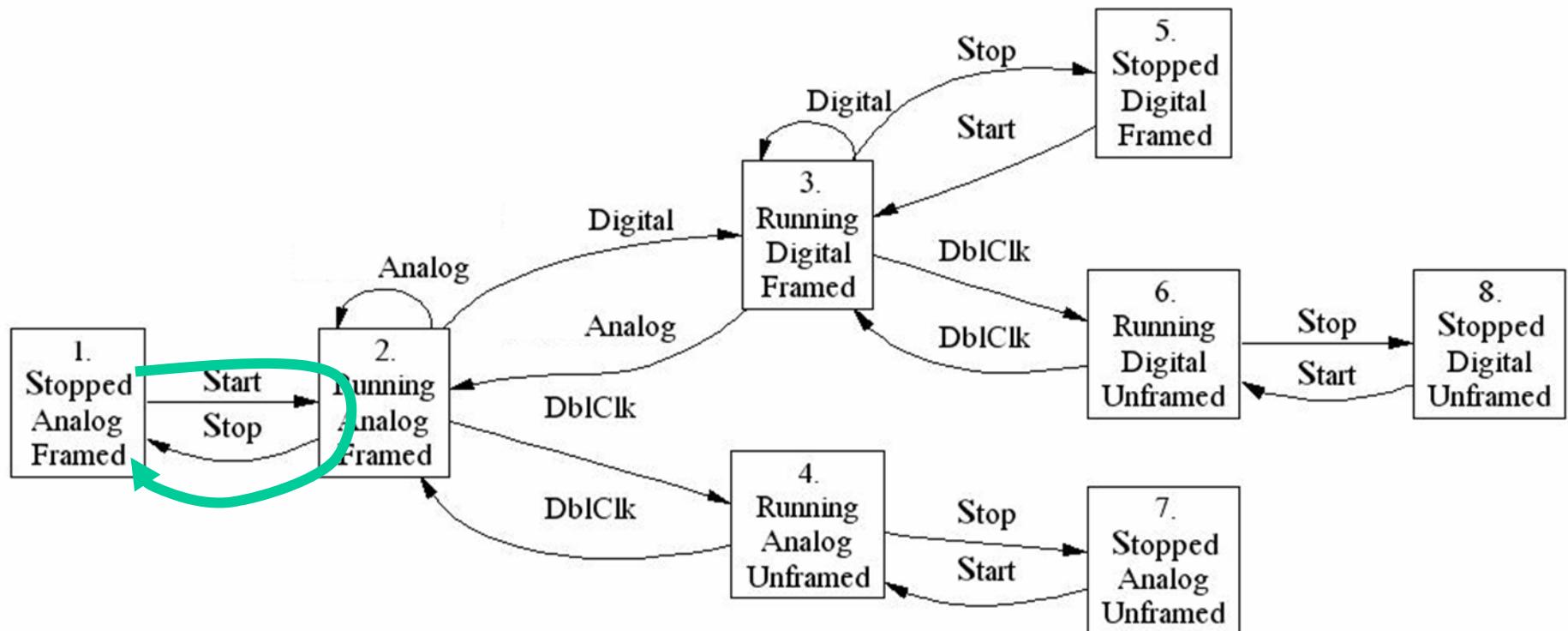
# A sequence that hits all transitions



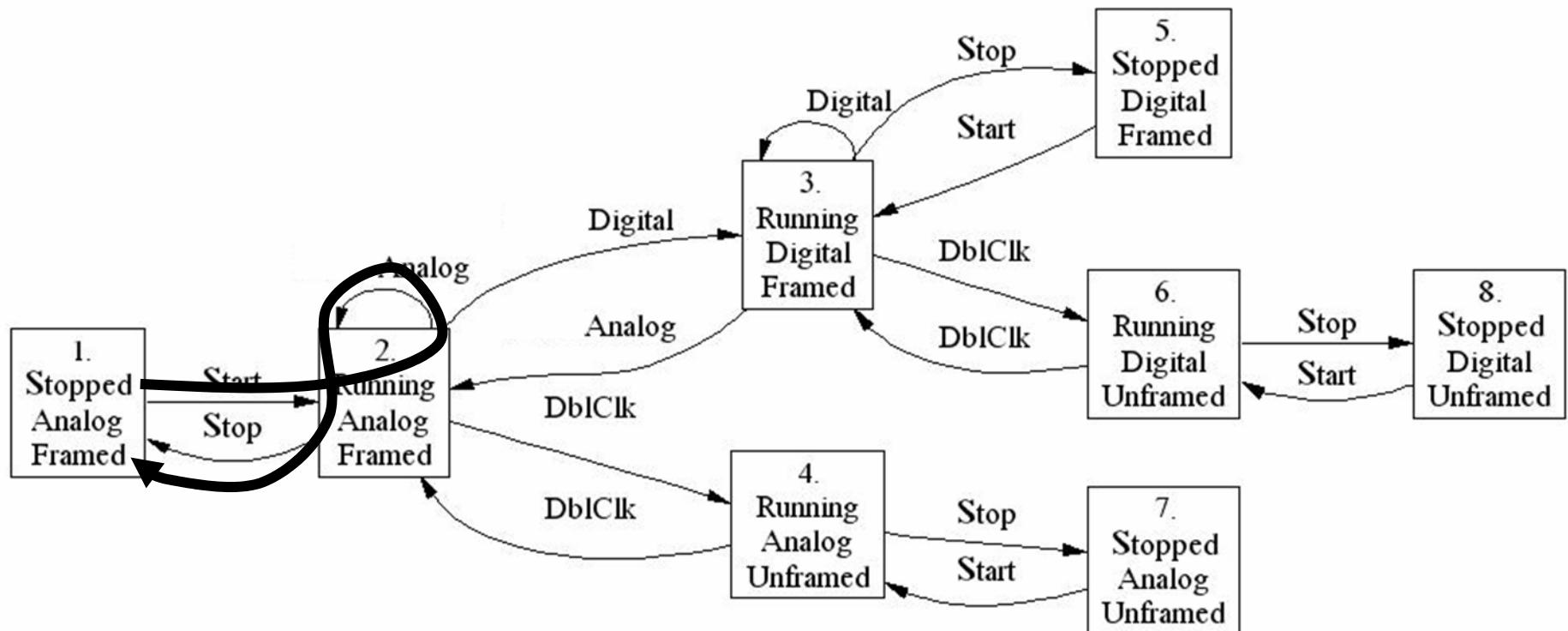
# An all-transitions sequence

- |                 |                  |
|-----------------|------------------|
| 1. Start        | 9. Start         |
| 2. Analog       | 10. Double Click |
| 3. Digital      | 11. Analog       |
| 4. Digital      | 12. Double Click |
| 5. Stop         | 13. Stop         |
| 6. Start        | 14. Start        |
| 7. Double Click | 15. Double Click |
| 8. Stop         | 16. Stop         |

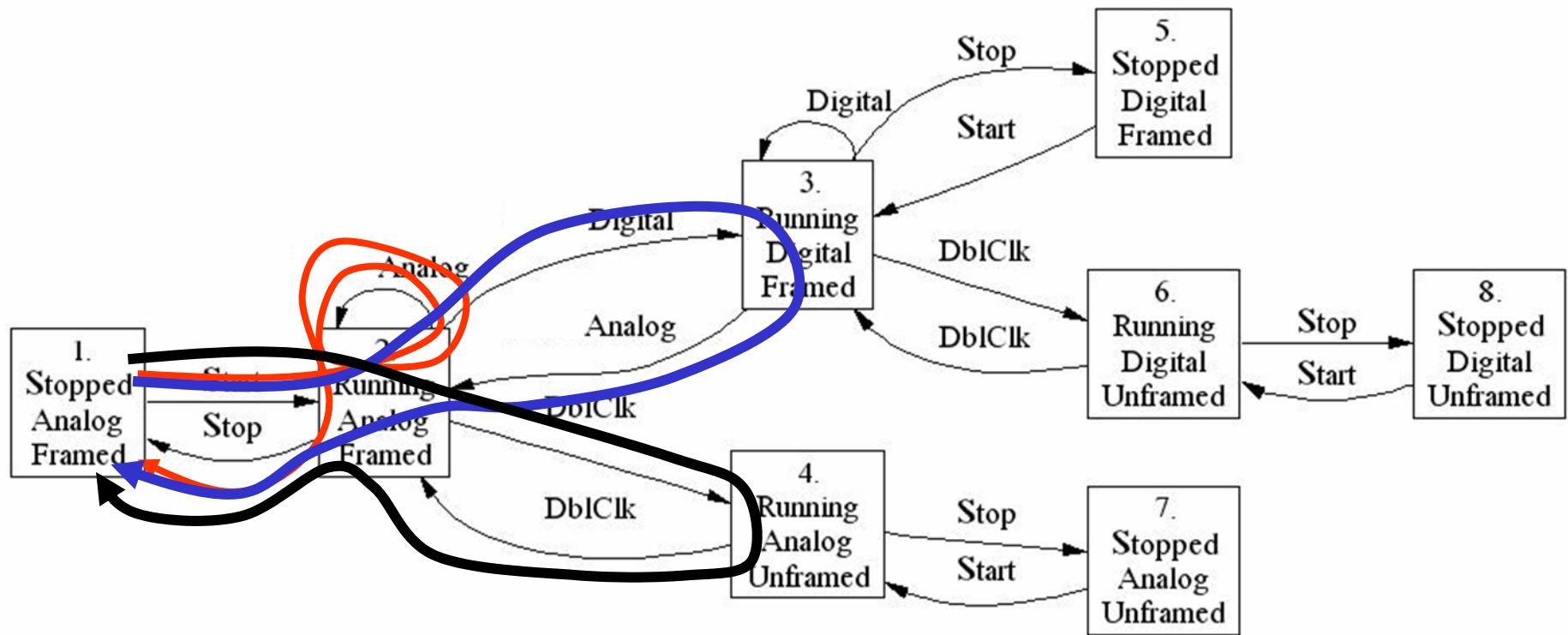
# All paths of length 2



# All paths of length 3



# All paths of length 4



# All paths of length < 5

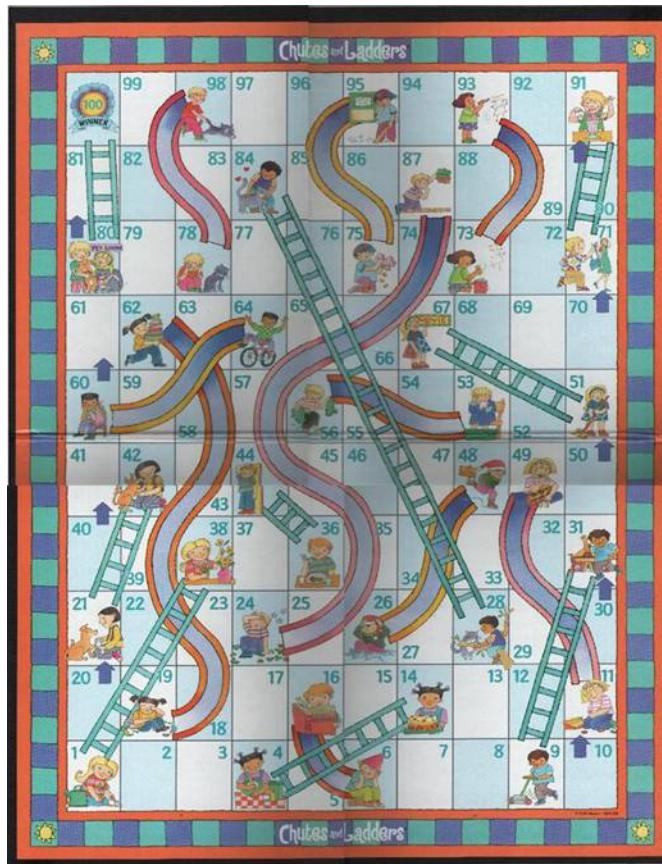
1. Start, Stop
2. Start, Analog, Stop
3. Start, Analog, Analog, Stop
4. Start, Digital, Analog, Stop
5. Start, Double Click, Double Click, Stop

## Exercise 5

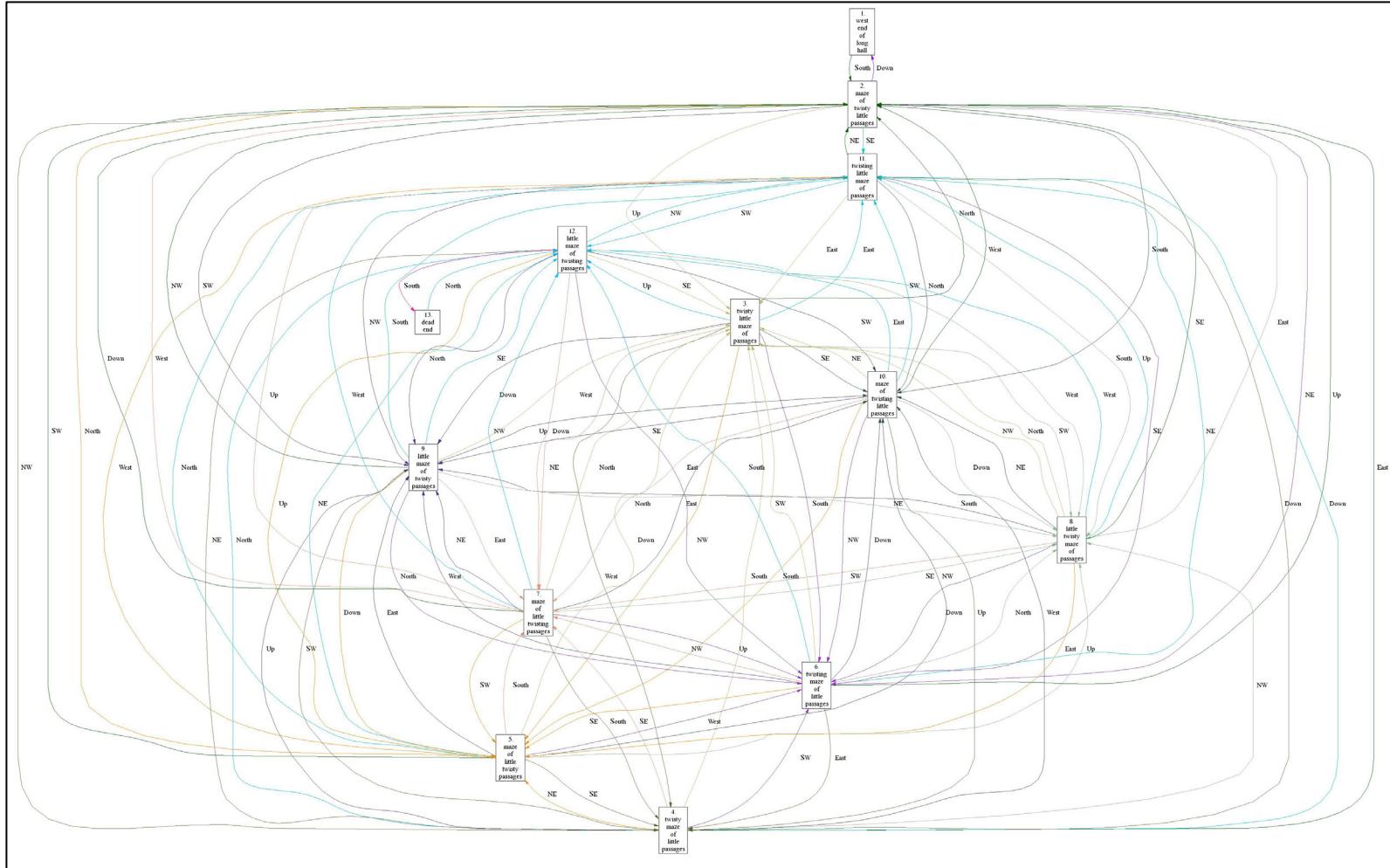
# Brainstorming Traversals



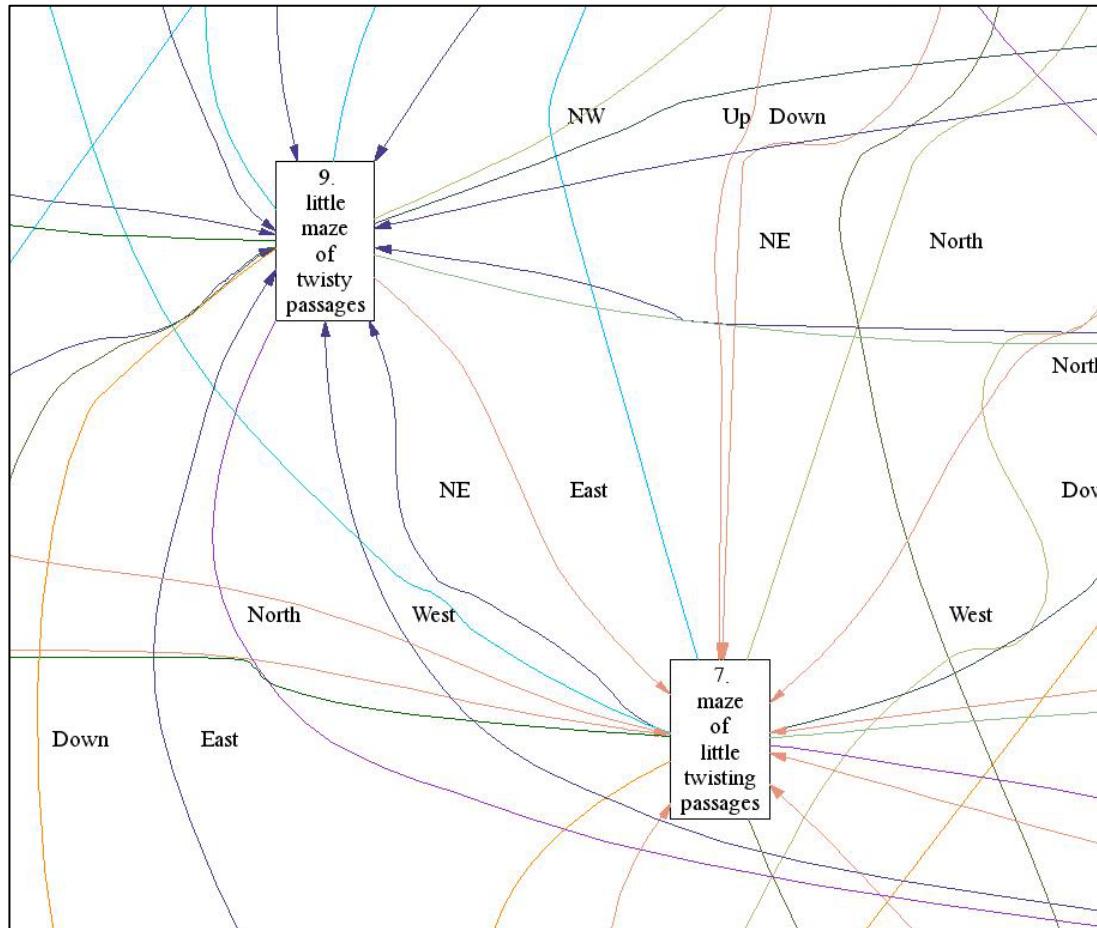
# How would you test this?



# Pathological



# Closer in ...

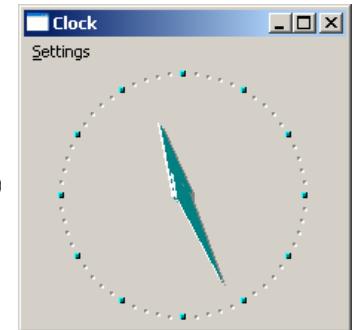
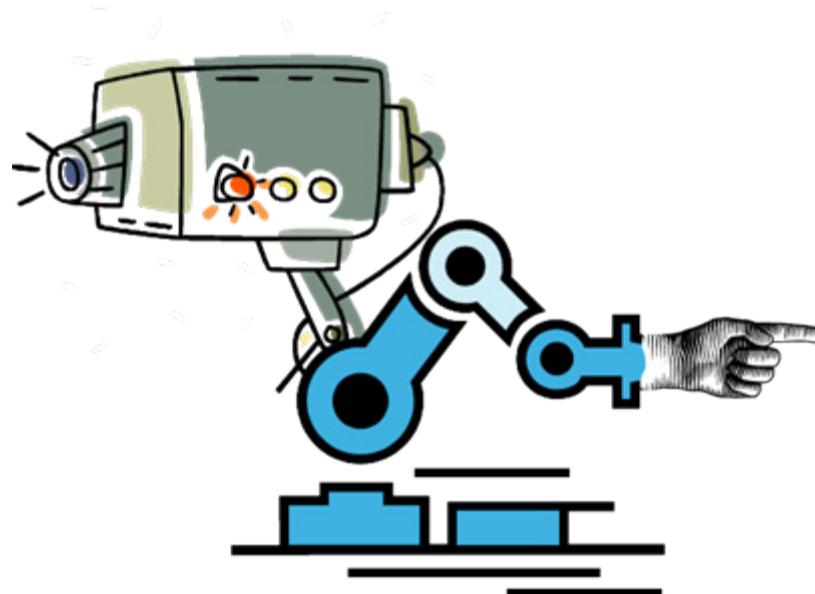


# Partial state table for the maze

*west end of long hall	South	maze of twisty little passages
maze of twisty little passages	Up	twisty little maze of passages
maze of twisty little passages	NW	twisty maze of little passages
maze of twisty little passages	North	maze of little twisty passages
maze of twisty little passages	NE	twisting maze of little passages
maze of twisty little passages	West	maze of little twisting passages
maze of twisty little passages	East	little twisty maze of passages
maze of twisty little passages	SW	little maze of twisty passages

# Executing the Test Actions

1. Start
2. Analog
3. Digital
4. Digital
5. Stop
6. Start
7. Double Click
8. Stop



# Exercise 6

# Modeling from a Spec

To Sustain Everyday Life: UMCOR Kits Are Another Way to Give  
UMCOR Sager Brown Material Resources Specifications

**Kits to Sustain Everyday Life**  
The following kit is used in places where people do not have ready access to many essential supplies for everyday life. Please follow the directions exactly. Include all items; do not add items that are not on the lists. Extra gifts, though given with the best of intentions, render a kit unusable and must be removed. Note: All items sent must be new!

**Health Kit**  
(Item #001-12-0200)  
Health kits provide basic necessities to people who have been forced to leave their homes because of human conflict or natural disaster. Health kits are also used as learning tools in personal hygiene, literacy, nutrition and cooking classes. When people gain the knowledge and materials to maintain personal hygiene, their overall health improves.

I send towel (15" x 25" up to 17" x 27")  
I washcloth  
I comb (large and sturdy, not pocket-sized)  
I nail file or fingernail clippers (no emery boards or toenail clippers)  
I bottle size tube of soap (3 oz. and up)  
I toothbrush (sooty bristles, no original wrapper)  
I large tube of toothpaste (expiration date must be 6 months or longer in advance of the date of shipment to UMCOR Sager Brown)  
6 adhesive plastic strip sterile bandages

Place these items inside a sealed one-gallon plastic bag.

Value: \$12 per kit  
In a separate envelope, please send a check for at least \$1 for each kit, to help UMCOR Sager Brown with the costs of processing and shipping kits around the world.

**Important:** Please do not include any religious, political or patriotic notes or emblems in any kit.

Thank you for your donations. You are helping to make a difference in people's lives.

You can download or print this page at <http://pgm-umc.org/umcor/print/kits/>

# “Accessing an Account”

1. customer needs to log in to use the system
2. customer stays logged in to the system until she logs out
3. customer starts with no account
4. customer can create an account
5. customer can delete her account
6. customer can open an existing account
7. customer can close an existing account

# Verifying the Outcomes

# Oracles

- Crashes
- Prediction
- Checking
- Pre-oracleing
- Heuristics
- Filtering + Humans
- Assertions

## Exercise 7

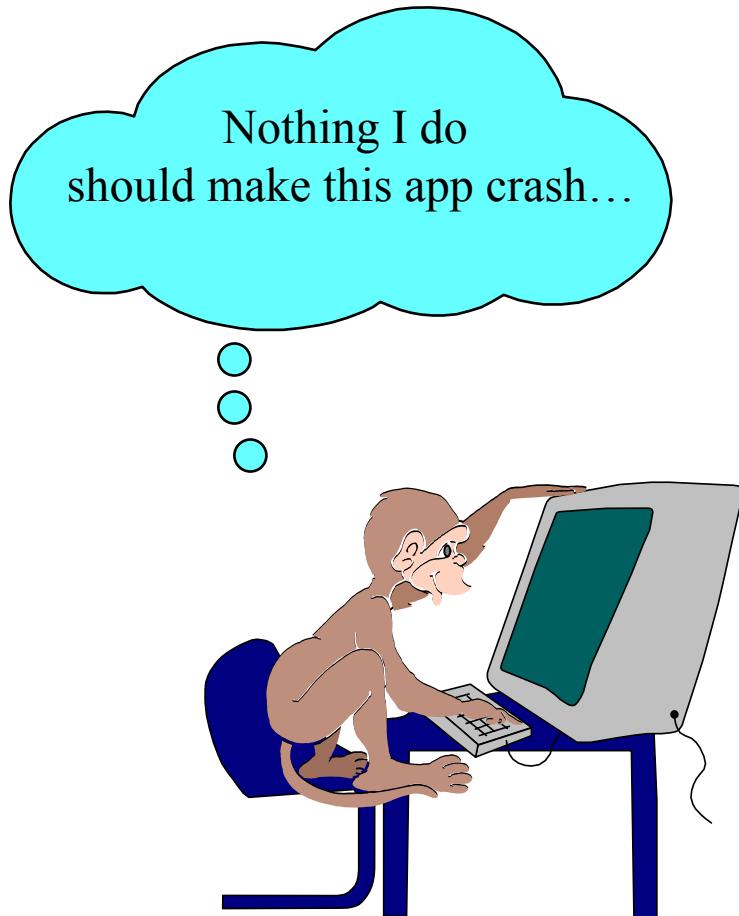
# Monkeying an Input Field



Inspired by Noel Nyman's article "Using Monkey Test Tools"

© 2006 Harry Robinson, Google

# Monkey Models



1.2

a P, a P, ab P, ab P 2, abc P, P, P, P,  
\scbuild1

Type 5

containing message laurie Bill's October  
? A

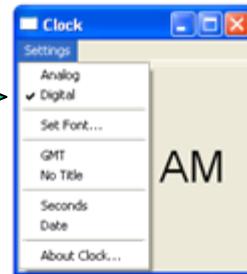
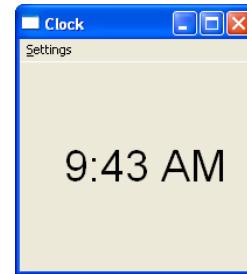
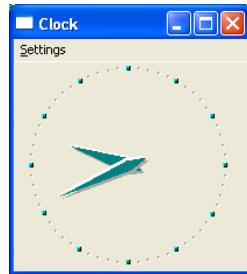
? v?-0Qrg+ 'cQ?\_<\$ ` Z`i7c} oV? E1X ...  
nov 31, 2000 Oct, 2000 dates Wednesday ...  
alike. In Word documents, for example ...

3 M note

RNL in Office 10

# Predicting the Outcome

StartState	Action	EndState
Analog	Digital	Digital



## Exercise 8

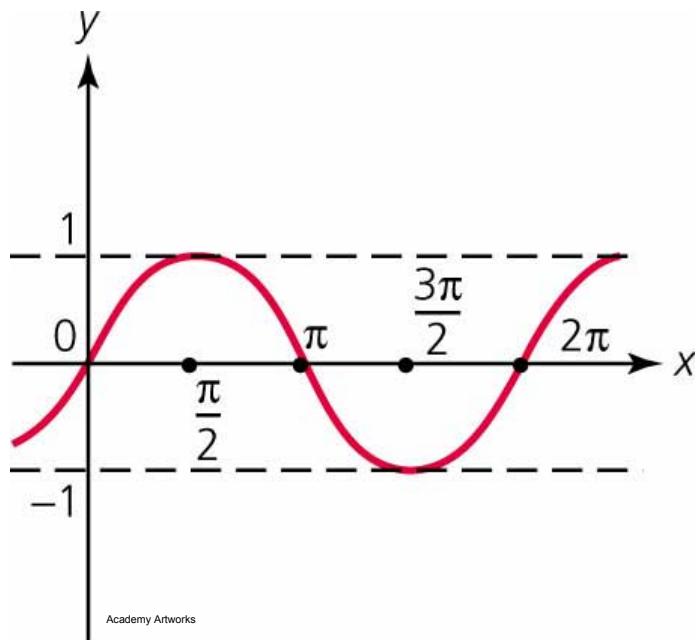
# Oracling the Square Root Function

$$\sqrt{a}$$

$$\sqrt{a} * \sqrt{a} = a$$

## Exercise 9

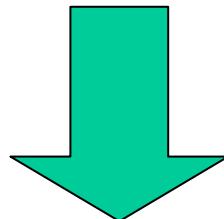
# Oracling the Sine Function



Inspired by Doug Hoffman's article "Heuristic Test Oracles"

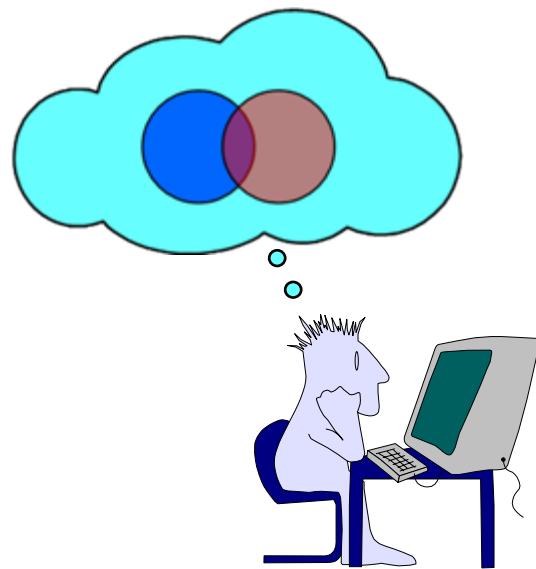
$$\sin^2(x) + \cos^2(x) = 1$$

$$\cos(x) = \sin(x-\pi)$$



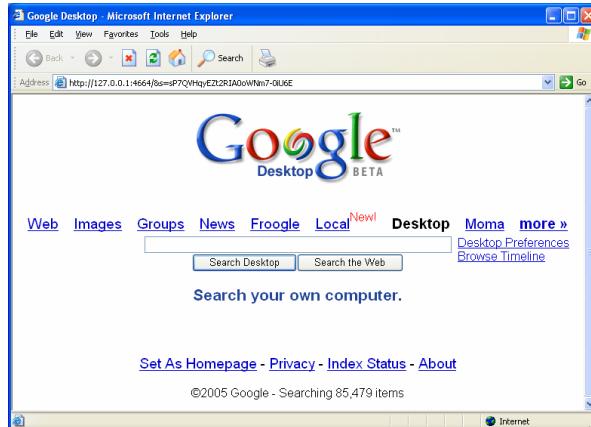
$$\sin^2(x) + \sin^2(x-\pi) = 1$$

# Modeling with Sets



# Exercise 10

# Modeling Search



+pragmatic - Google Desktop - Microsoft Internet Explorer

File Edit View Favorites Tools Help

Back Search

Address <http://127.0.0.1:4664/search?q=%2Bpragmatic&flags=8&num=10&s=5fpaN3KLbmRP56yMidOFhjyYKU> Go

**Google Desktop** BETA Web Images Groups News Froogle Local Desktop Moma more »

+pragmatic  Desktop Preferences  
Browse Timeline

Desktop: All - 0 emails - **82 files** - 0 web history - 0 chats - 0 other 1-10 of about 82 (0.)

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[Software Testing Analysis Review \(STARWEST 2005\)](#)  
Inc. bio) W7 Testing Dialogues -Technical Issues Wednesday,  
November 16, 2005, 1:45 PM T6 The Value-added Manager: Five  
**Pragmatic Practices** Thursday, November 17, 2005  
Desktop\051128 cleanup\proceedings\HTML\speakers.html - [Open folder](#) - 1 cached - Nov 16

Done Internet

+ruby - Google Desktop - Microsoft Internet Explorer

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Address [http://127.0.0.1:4664/search?q=%2Bruby&flags=8&num=10&s=NCLEGhSCGxxI3CfDdKzmCx\\_CxM](http://127.0.0.1:4664/search?q=%2Bruby&flags=8&num=10&s=NCLEGhSCGxxI3CfDdKzmCx_CxM) Go

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Browse Timeline

Desktop: All - 0 emails - **3,513 files** - 0 web history - 0 chats - 0 other 1-10 of about 3,513

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[Microsoft PowerPoint - W9](#)  
data-centric tests where each test does the same kind of thing to different kinds of data. Available in different languages (Java, C+ C# Python, Perl, **Ruby**, FitNesse, a [Desktop\051128 cleanup\proceedings\pdf\W9.pdf](#) - [Open folder](#) - [1 cached](#) - Nov 16)

Internet

+ruby +pragmatic - Google Desktop - Microsoft Internet Explorer

File Edit View Favorites Tools Help

Back Search

Address <http://127.0.0.1:4664/search?q=%2Bruby+%2Bpragmatic&flags=8&num=10&s=-llwZ2oLAc5BB-6eU5z9BIuajk8> Go

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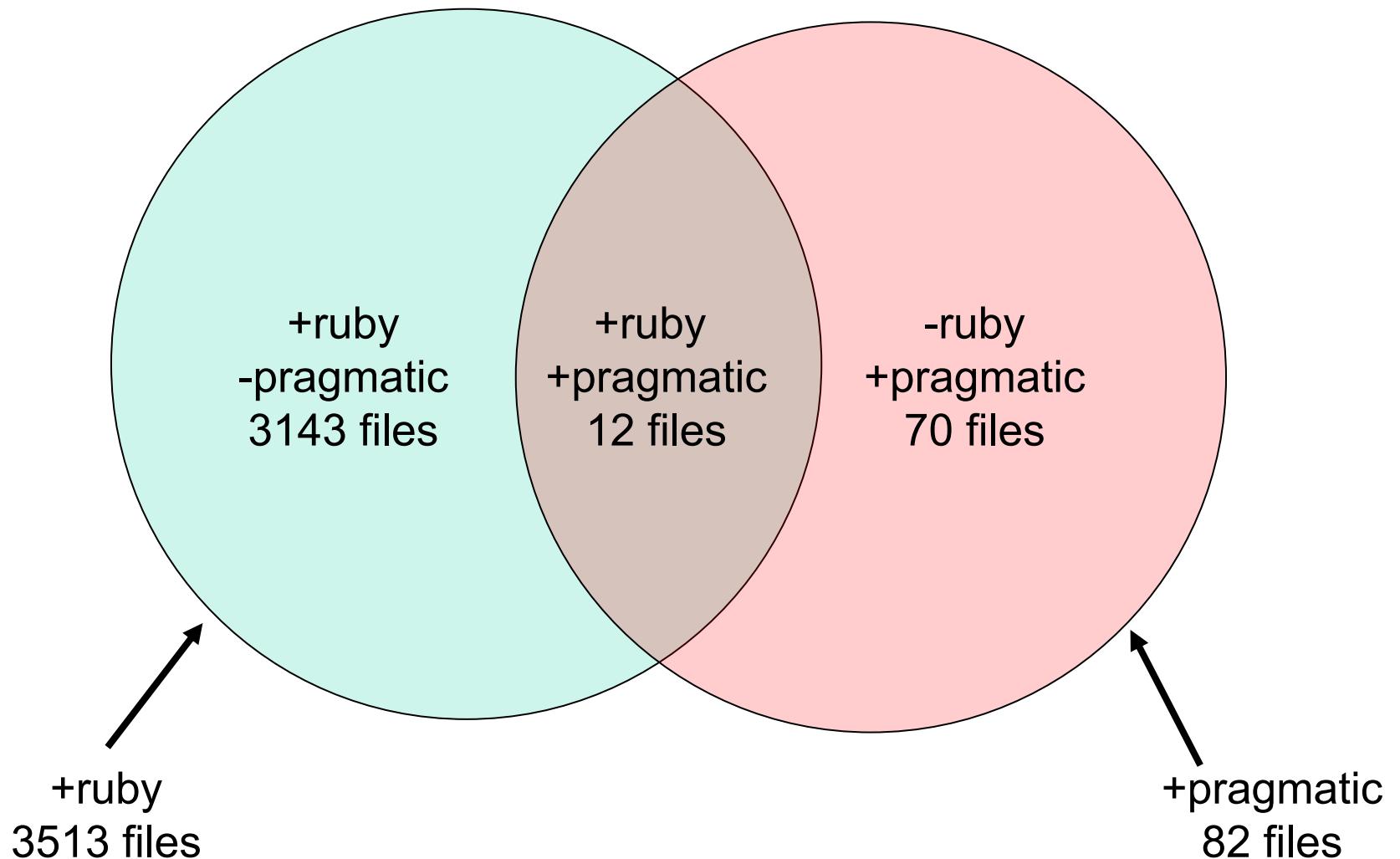
+ruby +pragmatic  Desktop Preferences  
Browse Timeline

Desktop: All - 0 emails - **12 files** - 0 web history - 0 chats - 0 other 1-10 of about 12 (0.)

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[Oct 12](#)

Internet



A Venn diagram illustrating the intersection of two file filters: '+ruby' and '-pragmatic'. The total count of files is 3513. The intersection of both filters contains 12 files. The files that are '+ruby' but not '-pragmatic' (the light green region) total 3143. The files that are '-pragmatic' but not '+ruby' (the pink region) total 70. An additional 82 files are '+pragmatic' but not '+ruby'.

$$3513 - 12 = ?$$

+ruby  
-pragmatic  
3143 files

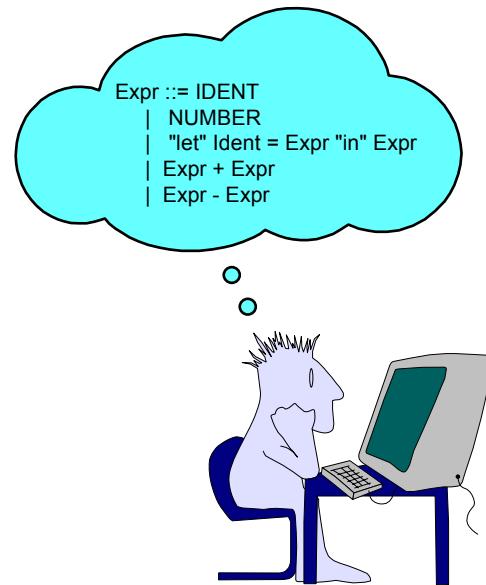
+ruby  
+pragmatic  
12 files

-ruby  
+pragmatic  
70 files

+ruby  
3513 files

+pragmatic  
82 files

# Modeling with Grammars

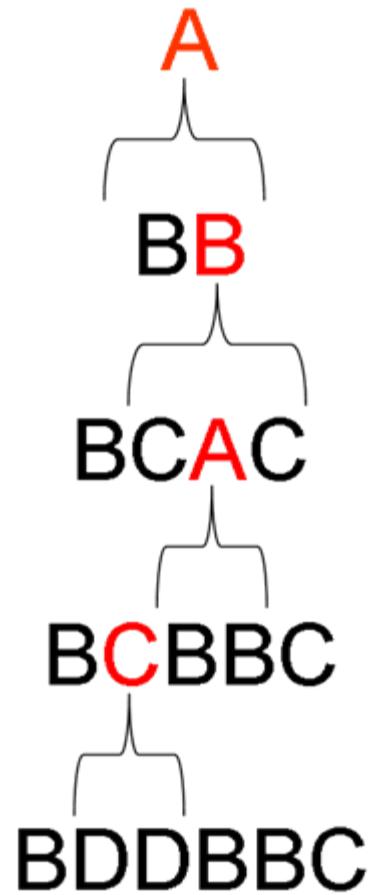


# How a Production Grammar Works

$A \rightarrow BB$

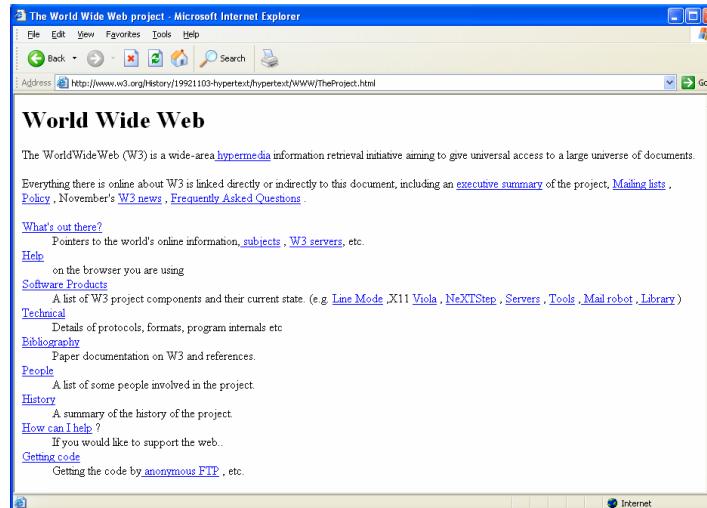
$B \rightarrow CAC$

$C \rightarrow DD$



# Exercise 11

## Modeling HTML



# A mini-html grammar

{seed}:=<html>{body}</html>;

{body}:={body}<P>{body}|<H1>{body2}</H1>|<H4>{body2}</H4>;

{body2}:=<font color="red"> {body3} </font>|<font color="blue"> {body3} </font>;

{body3}:=<U>{body4}</U>|{body4};

{body4}:=<I> {body5} </I> | {body5};

{body5}:=the quick brown fox;

# Grammar Example 1

## Modeling Arithmetic Expressions

100 \* 5 / (6 - 5.01 \* 3.14159)

Inspired by Pete TerMaat's article "Adventures in Automated Testing"

# Evaluate the following expressions

1.  $10 * 1.0 * 0.1 * 6.0 * 1.16666666667 * 1.0 * 1.14285714286 * 5.25$
2.  $2 * 2.5 * 0.4 * 4.0 * 1.25 * 1.0 * 0.8 * 5.25$
3.  $4 * 0.5 * 3.5 * 1.0 * 0.285714285714 * 3.0 * 0.166666666667 * 42.0$
4.  $2 * 5.0 * 0.2 * 1.5 * 1.0 * 2.66666666667 * 1.125 * 4.66666666667$
5.  $5 * 1.6 * 1.0 * 0.5 * 1.75 * 0.428571428571 * 0.333333333333 * 42.0$
6.  $4 * 2.0 * 0.75 * 1.5 * 0.444444444444 * 0.75 * 2.66666666667 * 5.25$
7.  $6 * 1.5 * 0.777777777778 * 0.428571428571 * 1.333333333333 * 0.25 * 7.0 * 6.0$
8.  $2 * 1.5 * 0.333333333333 * 10.0 * 0.5 * 0.8 * 1.5 * 7.0$
9.  $5 * 0.6 * 1.66666666667 * 0.2 * 1.0 * 1.0 * 10.0 * 4.2$

# 42

$$\begin{aligned} & 5 * 8.4 \\ & \downarrow \\ & 5 * 1.0 * 8.4 \\ & \downarrow \\ & 1 * 5.0 * 1.0 * 8.4 \\ & \downarrow \\ & 1 * 1.0 * 5.0 * 1.0 * 8.4 \\ & \downarrow \\ & 10 * 0.1 * 1.0 * 5.0 * 1.0 * 8.4 \\ & \downarrow \\ & 8 * 1.25 * 0.1 * 1.0 * 5.0 * 1.0 * 8.4 \\ & \downarrow \\ & 7 * 1.14285714286 * 1.25 * 0.1 * 1.0 * 5.0 * 1.0 * 8.4 \end{aligned}$$

# Evaluate the following expression

```
10 * 0.6 * 1.5 * 0.666666666667 * 1.0 * 1.0 * 0.833333333333 * 1.2 * 1.5 * 0.666666666667 *
1.333333333333 * 0.375 * 1.666666666667 * 1.0 * 2.0 * 1.0 * 0.9 * 0.777777777778 * 1.0 *
0.428571428571 * 3.0 * 0.666666666667 * 1.5 * 0.222222222222 * 0.5 * 5.0 * 2.0 * 0.4 * 2.0 *
0.5 * 0.75 * 1.33333333333 * 0.75 * 2.33333333333 * 1.42857142857 * 0.7 * 1.0 *
1.28571428571 * 1.0 * 0.33333333333 * 2.0 * 0.83333333333 * 0.2 * 6.0 * 1.33333333333 *
0.375 * 0.666666666667 * 1.0 * 2.0 * 2.25 * 0.222222222222 * 4.5 * 0.888888888889 * 0.125
* 4.0 * 2.0 * 0.75 * 1.0 * 1.5 * 0.33333333333 * 2.33333333333 * 0.428571428571 * 3.0 *
0.888888888889 * 0.625 * 0.2 * 8.0 * 0.375 * 0.33333333333 * 7.0 * 1.42857142857 * 0.1 *
3.0 * 3.33333333333 * 1.0 * 0.6 * 0.33333333333 * 4.0 * 0.5 * 2.5 * 0.5 * 1.4 *
1.14285714286 * 0.25 * 0.5 * 7.0 * 0.428571428571 * 2.0 * 1.0 * 0.5 * 0.666666666667 * 4.5 *
0.33333333333 * 2.33333333333 * 0.571428571429 * 1.75 * 0.428571428571 * 2.0 * 0.5 *
14.0
```

# Grammar Example 2

## Modeling C Code

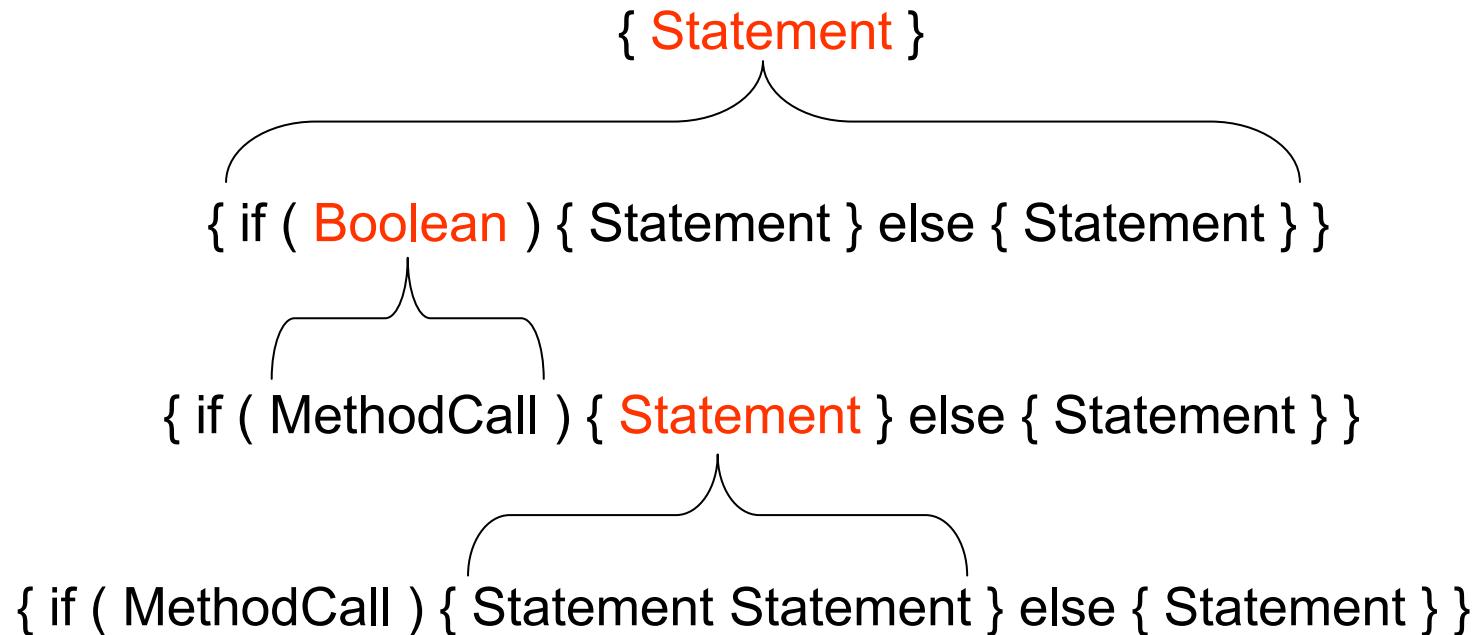
```
static void TestCase(){
    while( Fun("L21")){
        L22: break; }
    else {
        L3:{}
        L31:   goto L22;
        L32:   goto L31; }}
```

# Grammar Model for a Subset of C

```
Statement :: if ( BooleanCondition ) { Statement } else { Statement }
Statement :: while ( BooleanCondition ) { Statement }
Statement :: { Statement Statement }
Statement :: break;
Statement :: goto Label;
Statement :: Label : Statement
Statement :: ExpressionStatement;
ExpressionStatement :: MethodCall
BooleanExpression :: MethodCall
MethodCall :: Fun(Label)
```

Based on “A High-Level Modular Definition of the Semantics of C#”  
- Boerger, Fruja, Gervasi, Stark

# Deriving Programs from the Grammar



# Tests Generated from the Grammar

suite123.cs

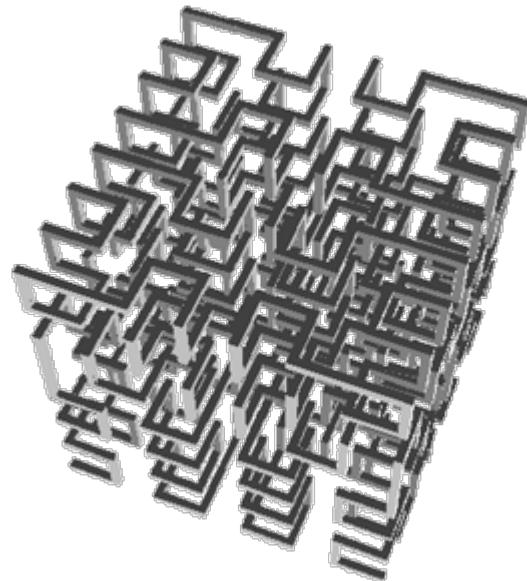
```
static void TestCase(){
L:
if ( Fun("L1") ){
L2:
if ( Fun("L21") ){
L22: goto L;
}
else{
L23: goto L;
}}
else{
L3:
{
L31: goto L32;
L32: goto L;
}}}
```

suite321.cs

```
static void TestCase(){
L:
if ( Fun("L1") ){
L2:
while( Fun("L21") ){
L22:
break;
}}
else{
L3:
{
L31: goto L;
L32: goto L31;
}}}}
```

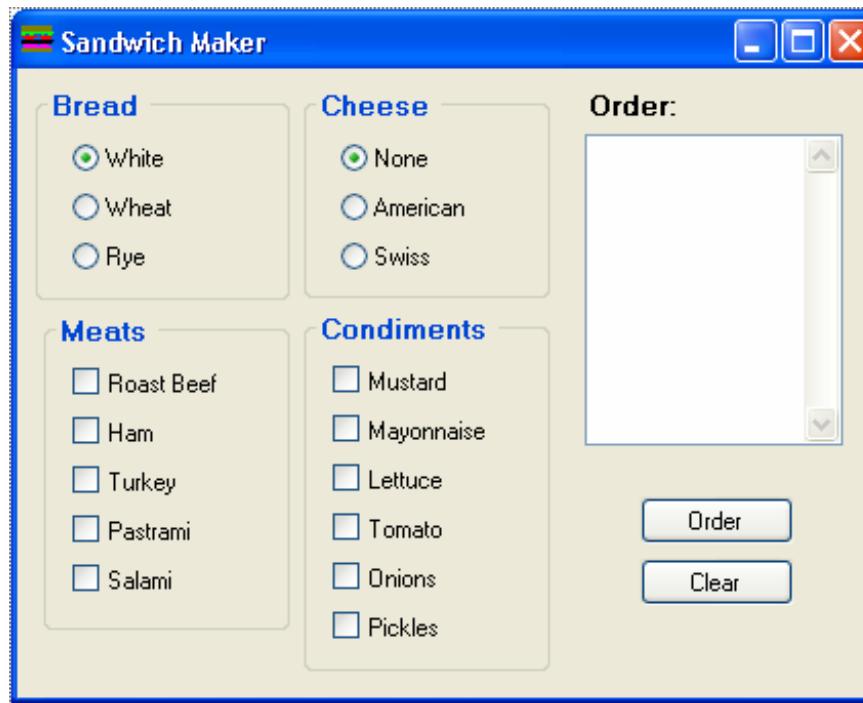
## Exercise 12

# Modeling Combinations



# Exercise 13

## Selecting Sandwiches



Inspired by an example in Lou Tylee's book "Visual C# Express for Kids"

# Setting Up the Combinations

<b>Bread</b>	<b>Cheese</b>	<b>H</b>	<b>MU</b>	<b>MA</b>	<b>L</b>	<b>T</b>
white	none	ham	mustard	mayo	lettuce	tomato
wheat	american	no_ham	no_must	no_mayo	no_lett	no_tom
rye	swiss					

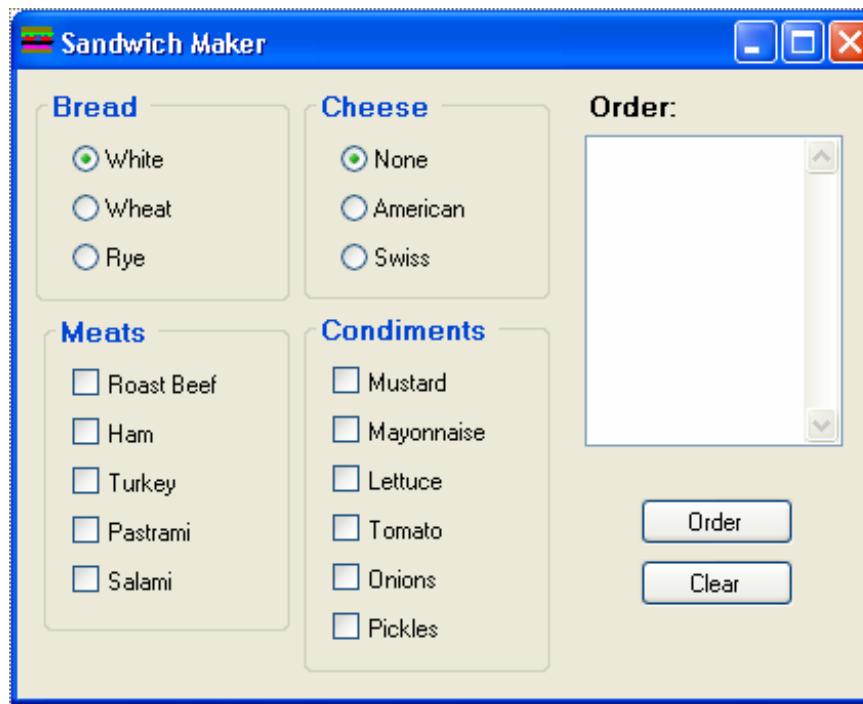
Using James Bach's AllPairs program from [www.satisfice.com](http://www.satisfice.com)

# Generating the Pairs

## TEST CASES

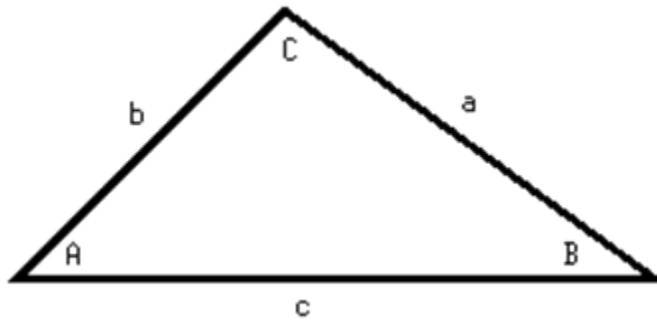
case	Bread	Cheese	H	M	MA	L	T
1	white	none	ham	mustard	mayo	lettuce	tomato
2	white	american	no_ham	no_must	no_mayo	no_lett	no_tom
3	wheat	none	no_ham	mustard	no_mayo	lettuce	no_tom
4	wheat	american	ham	no_must	mayo	no_lett	tomato
5	rye	swiss	ham	mustard	no_mayo	no_lett	tomato
6	rye	swiss	no_ham	no_must	mayo	lettuce	no_tom
7	white	none	ham	no_must	no_mayo	no_lett	no_tom
8	white	american	no_ham	mustard	mayo	lettuce	tomato
9	wheat	swiss	ham	mustard	mayo	no_lett	no_tom
10	rye	none	no_ham	no_must	no_mayo	lettuce	tomato
11	rye	american	ham	mustard	no_mayo	lettuce	no_tom
12	white	swiss	no_ham	no_must	no_mayo	no_lett	tomato

# But, did we miss any behavior of interest?



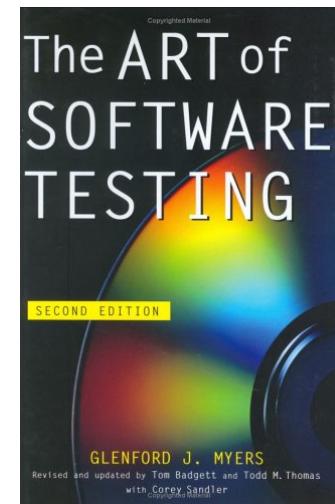
## Exercise 14

# Modeling the Triangle



Inspired by B J Rollison's conference paper "Dissecting the Triangle Problem"

triangle test cases for the triangle program, that in no way guarantees the correct detection of all equilateral triangles. The program could contain a special check for values 3842,3842,3842 and denote such a triangle as a scalene triangle. Since the program is a black box, the only way to be sure of detecting the presence of such a statement is by trying every input condition.

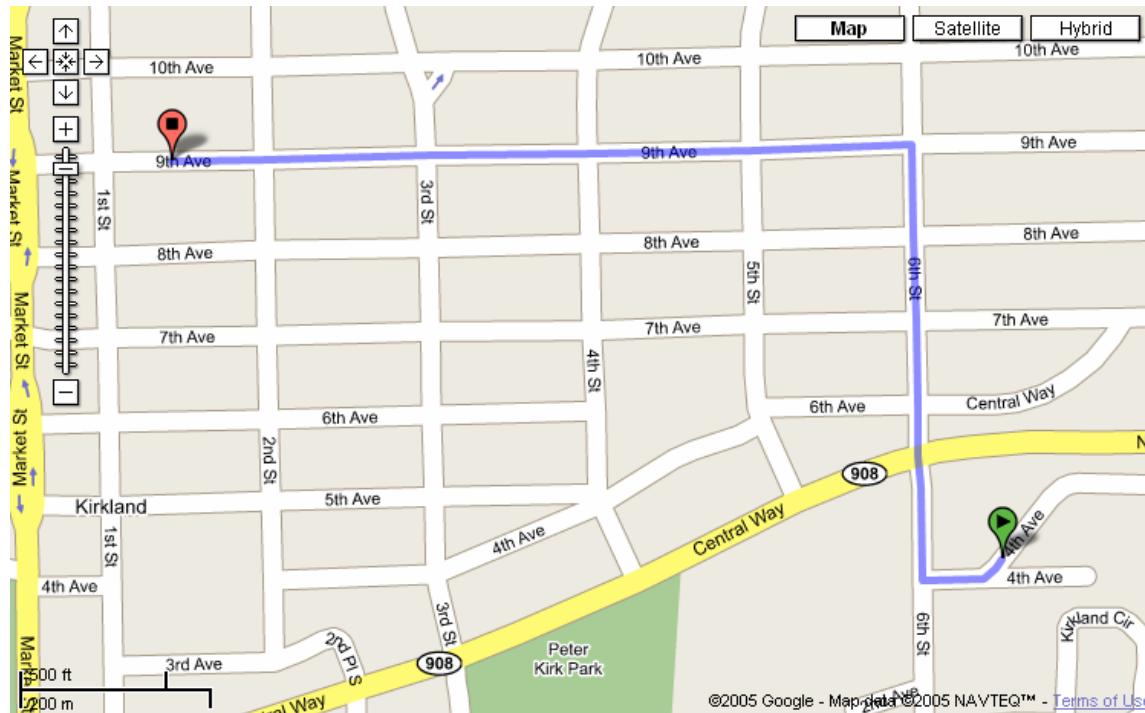


# Exhaustion?

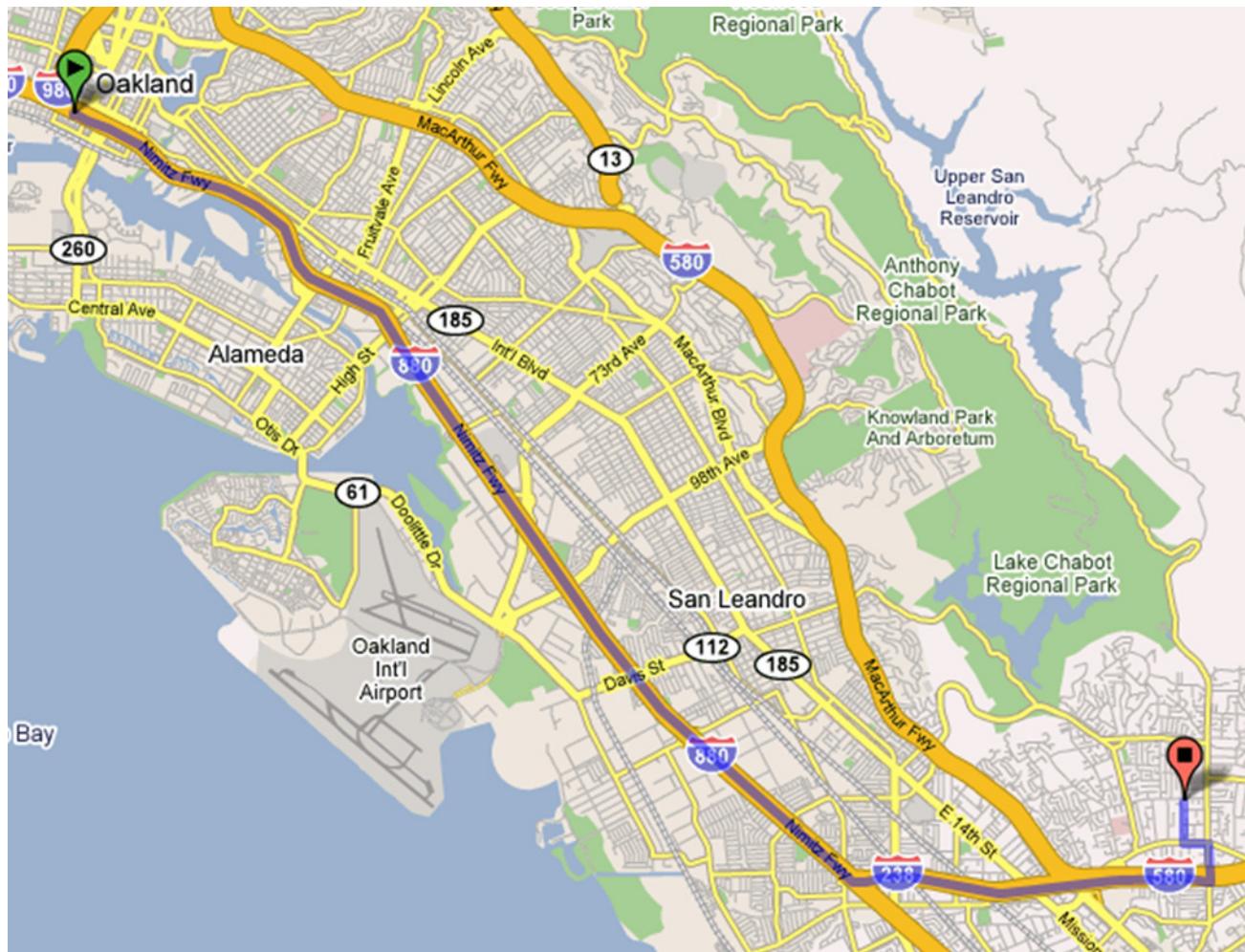
```
for ( a=0; a<=32767; a++)  
  for ( b=0; b<=32767; b++)  
    for ( c=0; c<=32767; c++)  
      evaluate( a, b, c);
```

# Exercise 15

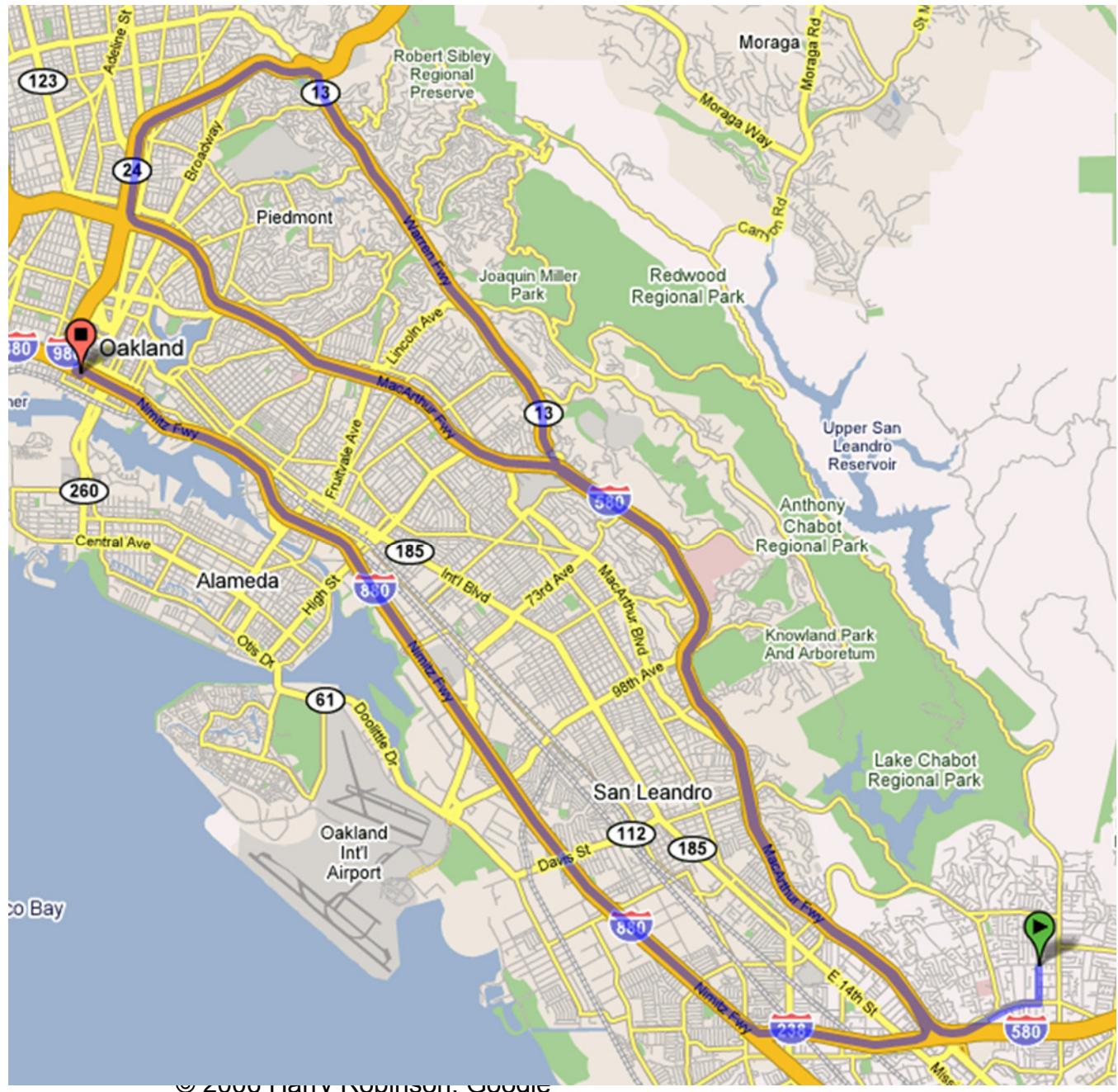
## Modeling Google Maps

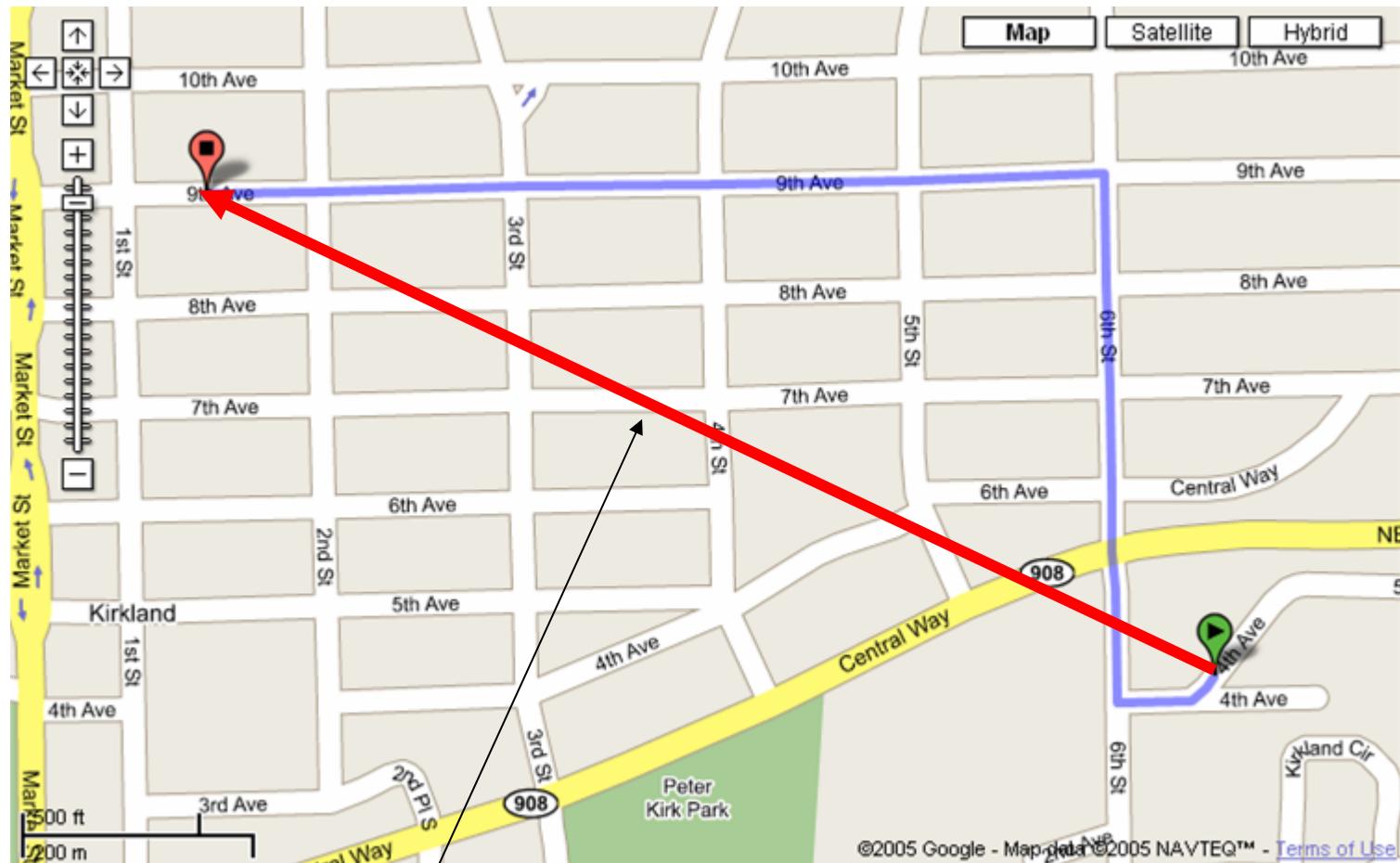


<u>Start address:</u>	Clay St Oakland, CA 94607
<u>End address:</u>	CA 94546
Distance:	15.6 mi (about 21 mins)



<u>Start address:</u>	CA 94546
<u>End address:</u>	Clay St Oakland, CA 94607
<u>Distance:</u>	45.8 mi (about 54 mins)





0.60 miles

<u>Start address:</u>	720 4th Ave Kirkland, WA 98033
<u>End address:</u>	Kirkland, WA
<u>Distance:</u>	0.9 mi (about 1 min)

Trip #115

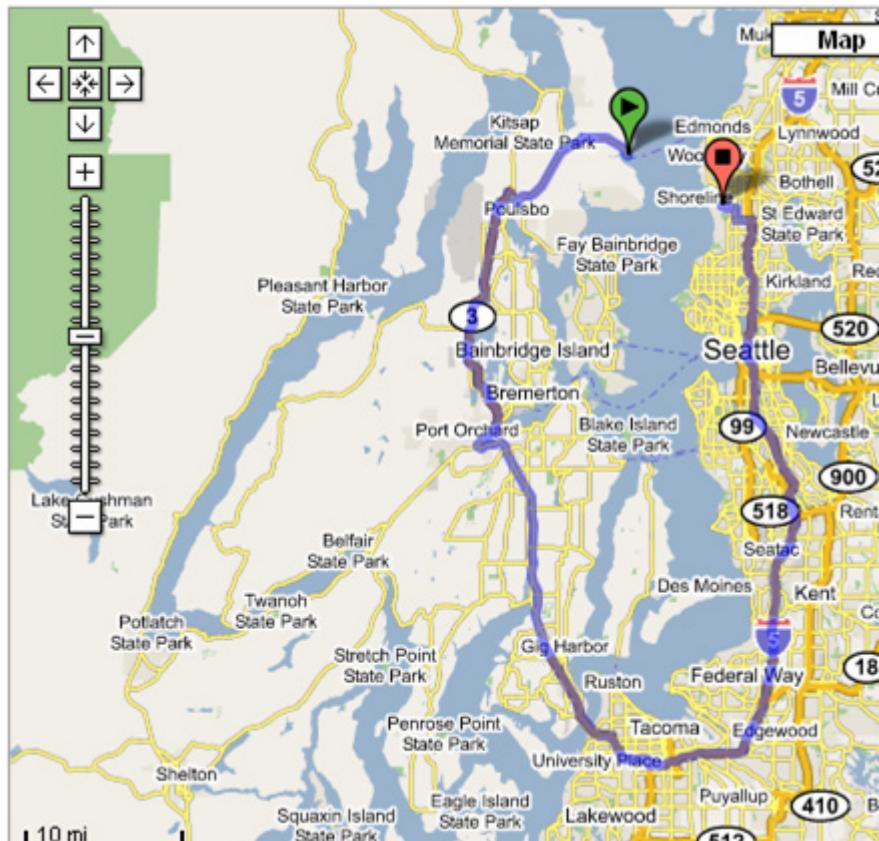
Trip start: 47.7945, -122.493

Trip end: 47.74753 -122.36585

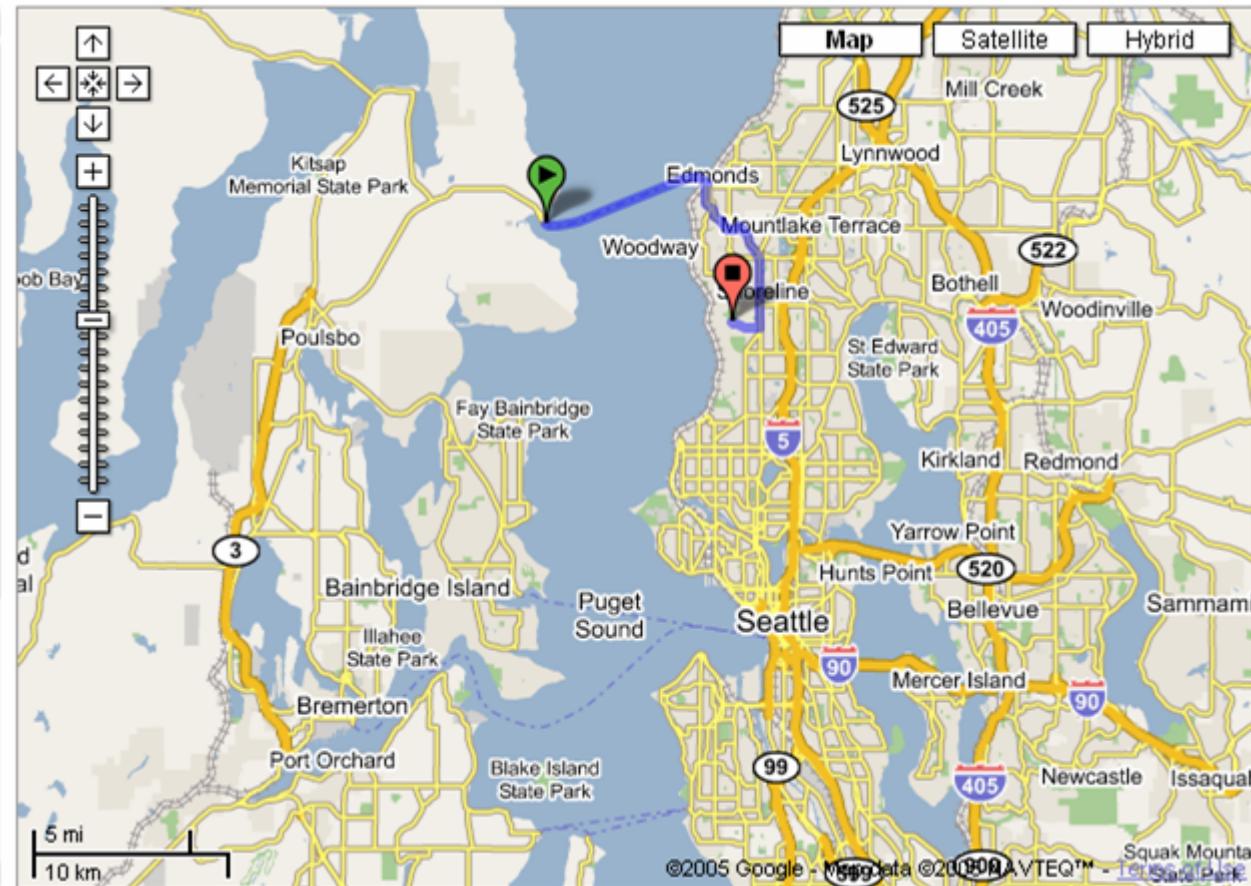
Google route distance is 102.0 miles

Straightline distance is 6.7 miles

Ratio is 15.2 ----- SUSPICIOUS...



<u>Start address:</u>	<b>47.794500, -122.493000</b> +47° 47' 40.20", -122° 29' 34.80"
<u>End address:</u>	<b>47.747530, -122.365850</b> +47° 44' 51.11", -122° 21' 57.06"
Distance:	102 mi (about 2 hours 25 mins)

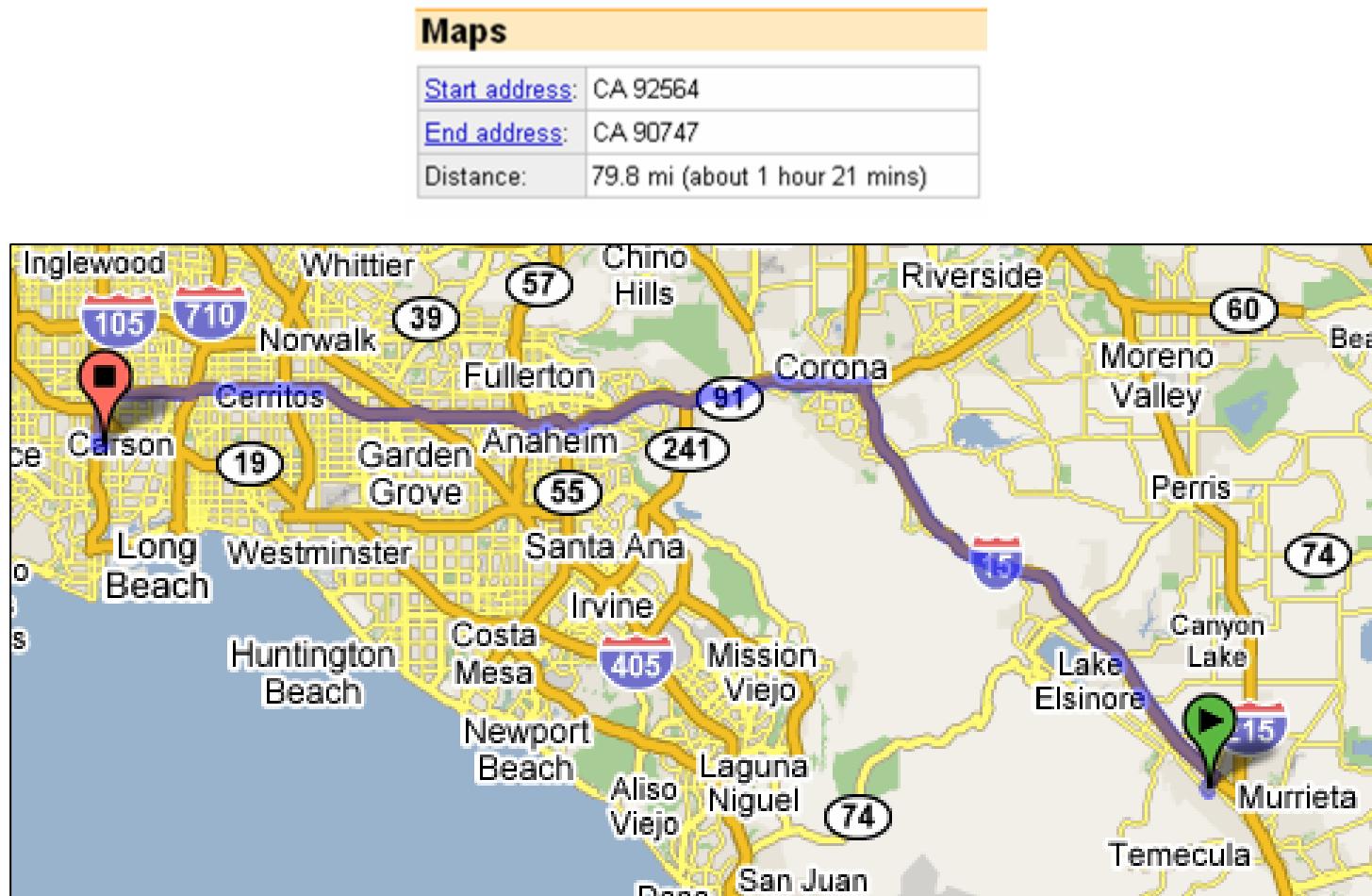


<u>Start address:</u>	47.794500, -122.492000 +47° 47' 40.20", -122° 29' 31.20"
<u>End address:</u>	47.747530, -122.365850 +47° 44' 51.11", -122° 21' 57.06"
Distance:	12.3 mi (about 2 hours 20 mins)

<u>Start address:</u>	<b>47.794500, -122.493000</b> +47° 47' 40.20", -122° 29' 34.80"
<u>End address:</u>	<b>47.747530, -122.365850</b> +47° 44' 51.11", -122° 21' 57.06"
Distance:	102 mi (about 2 hours 25 mins)

<u>Start address:</u>	<b>47.794500, -122.492000</b> +47° 47' 40.20", -122° 29' 31.20"
<u>End address:</u>	<b>47.747530, -122.365850</b> +47° 44' 51.11", -122° 21' 57.06"
Distance:	12.3 mi (about 2 hours 20 mins)

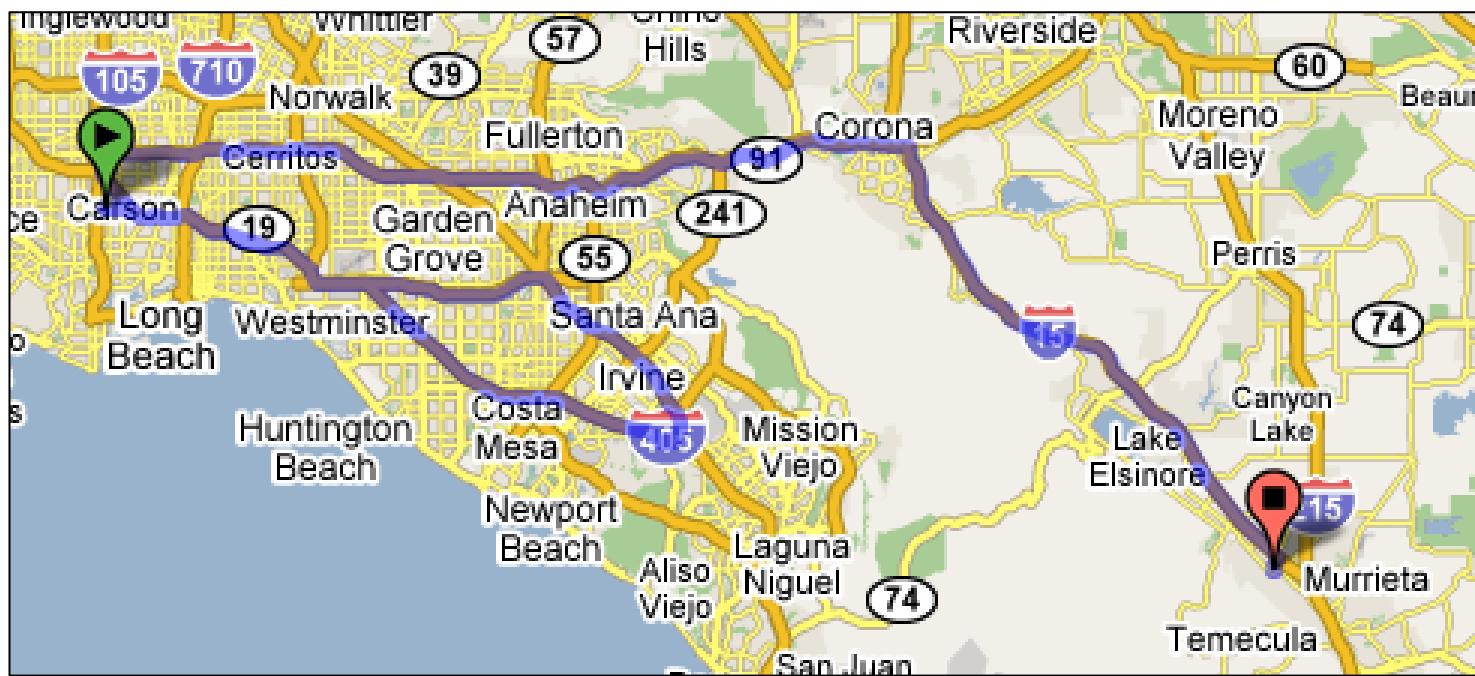
# Checking Driving Directions



# Checking Driving Directions

## Maps

<a href="#">Start address:</a>	CA 90747
<a href="#">End address:</a>	CA 92564
Distance:	149 mi (about 2 hours 29 mins)

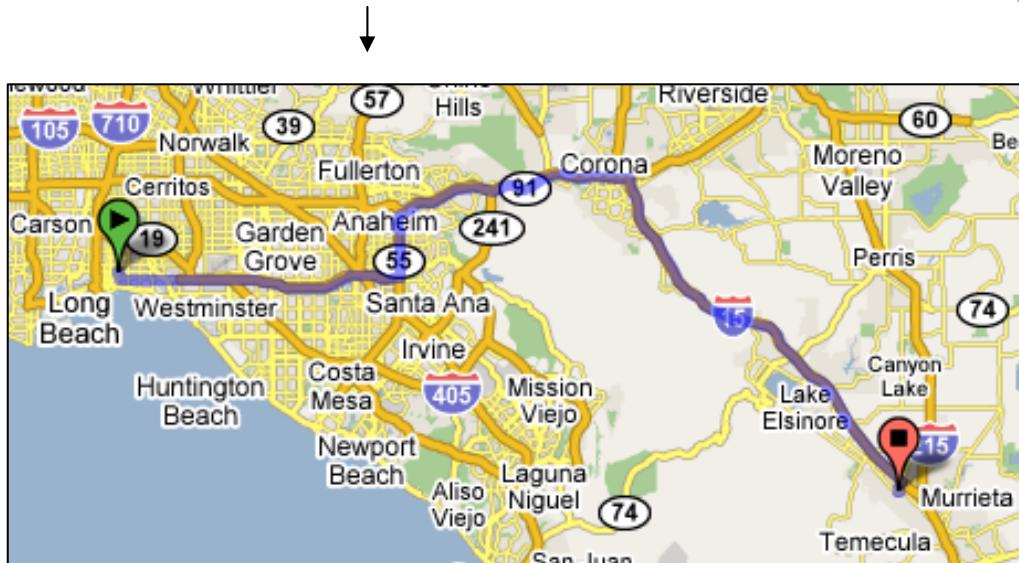


# The Long Road Home

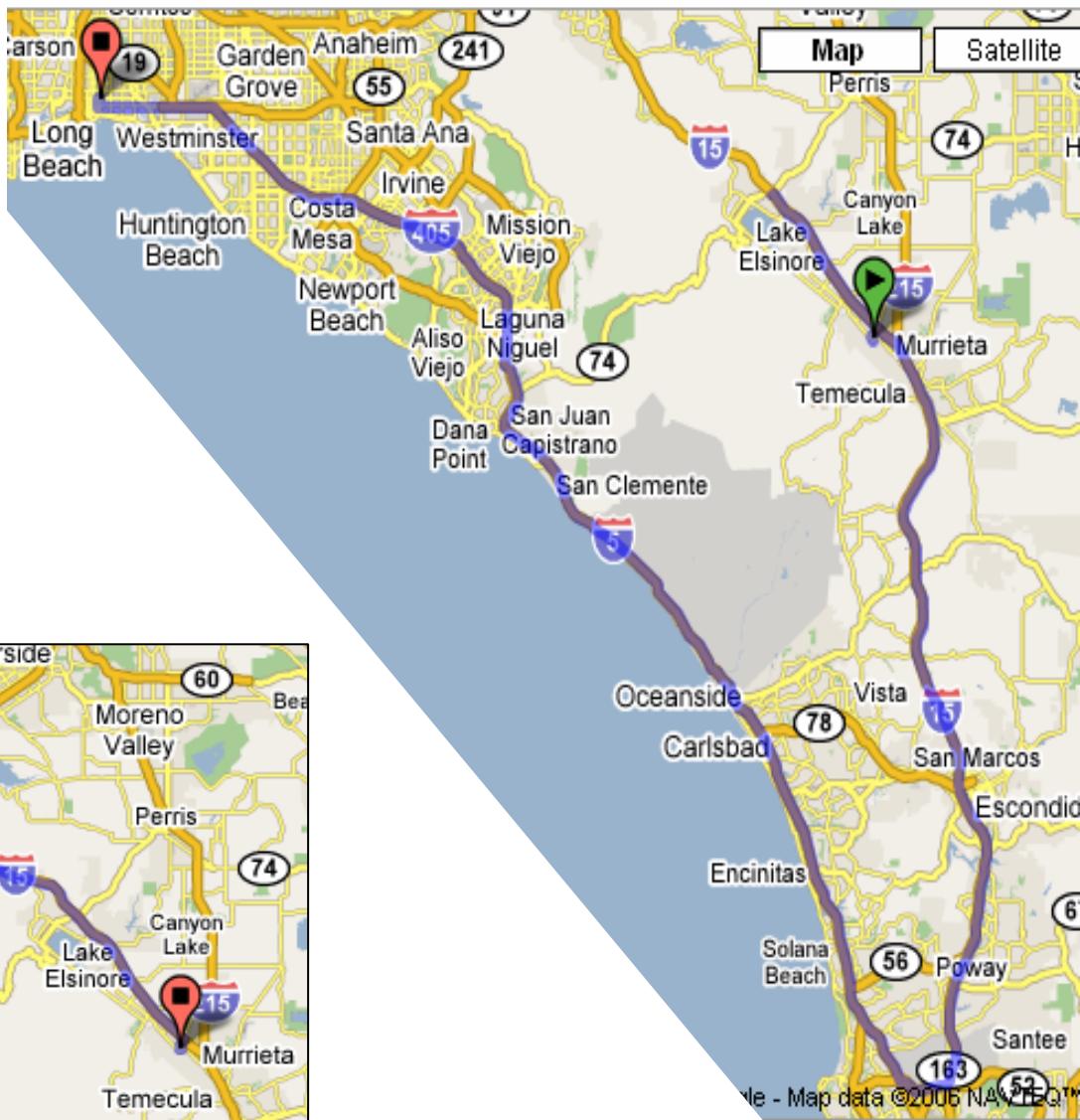
<a href="#">Start address:</a>	CA 92564
<a href="#">End address:</a>	Long Beach, CA 90813
Distance:	180 mi (about 3 hours 3 mins)



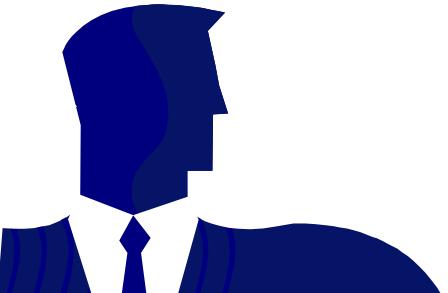
<a href="#">Start address:</a>	Long Beach, CA 90813
<a href="#">End address:</a>	CA 92564
Distance:	75.1 mi (about 1 hour 21 mins)



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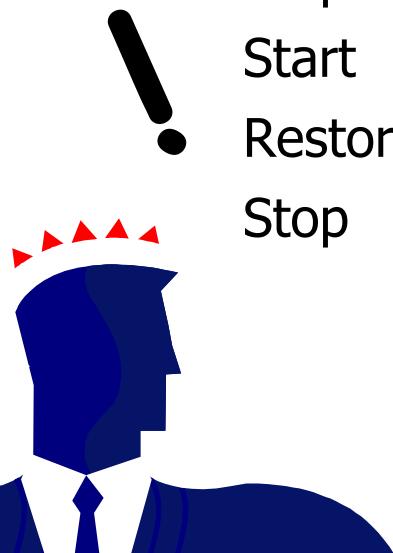
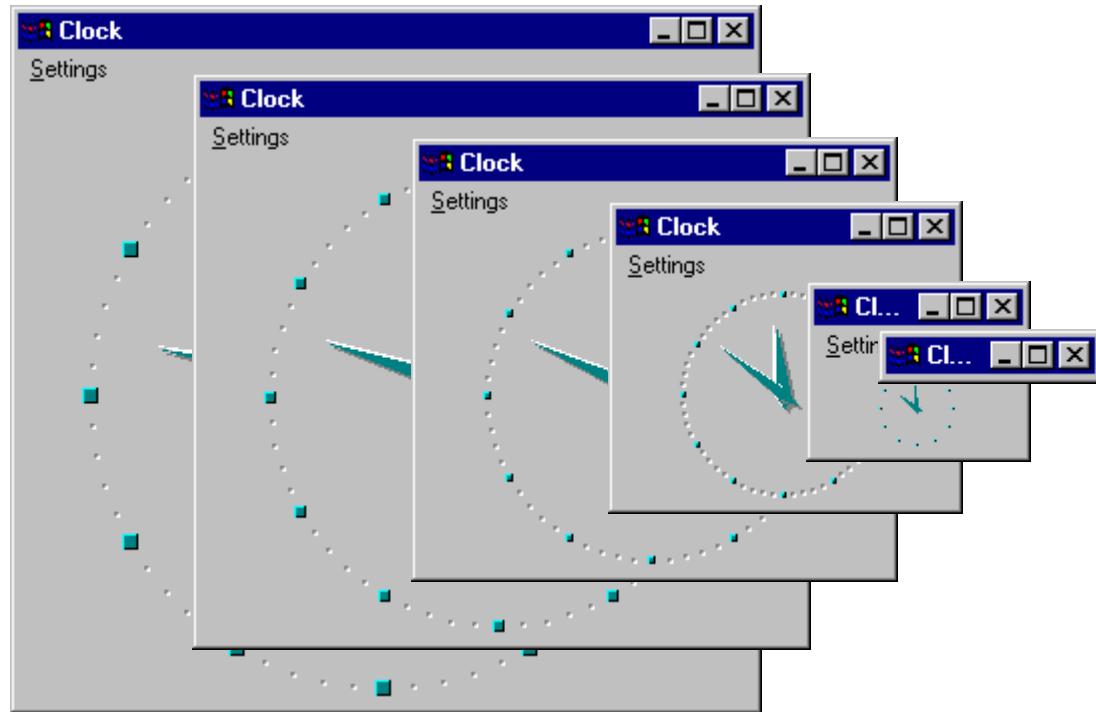


# What Kinds of Bugs do Models Find?



# The Incredible Shrinking Clock

Start  
Maximize  
Stop  
Start  
Minimize  
Stop  
Start  
Restore  
Stop



# That Was the Year that Wasn't

Start

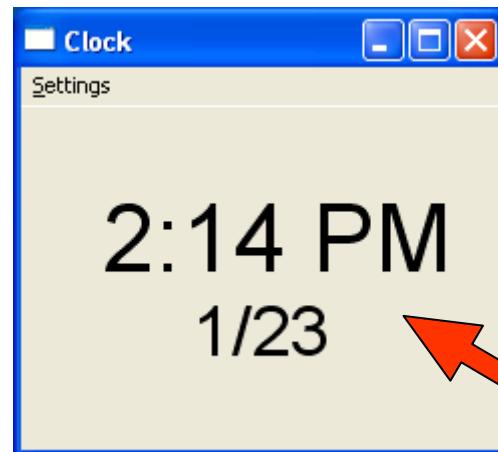
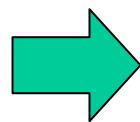
Minimize

Stop

Start

Restore

Date



bug

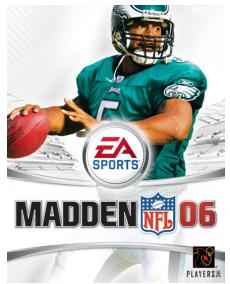


# What Kinds of Bugs do Models **NOT** Find?

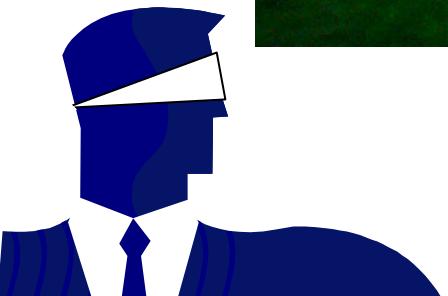




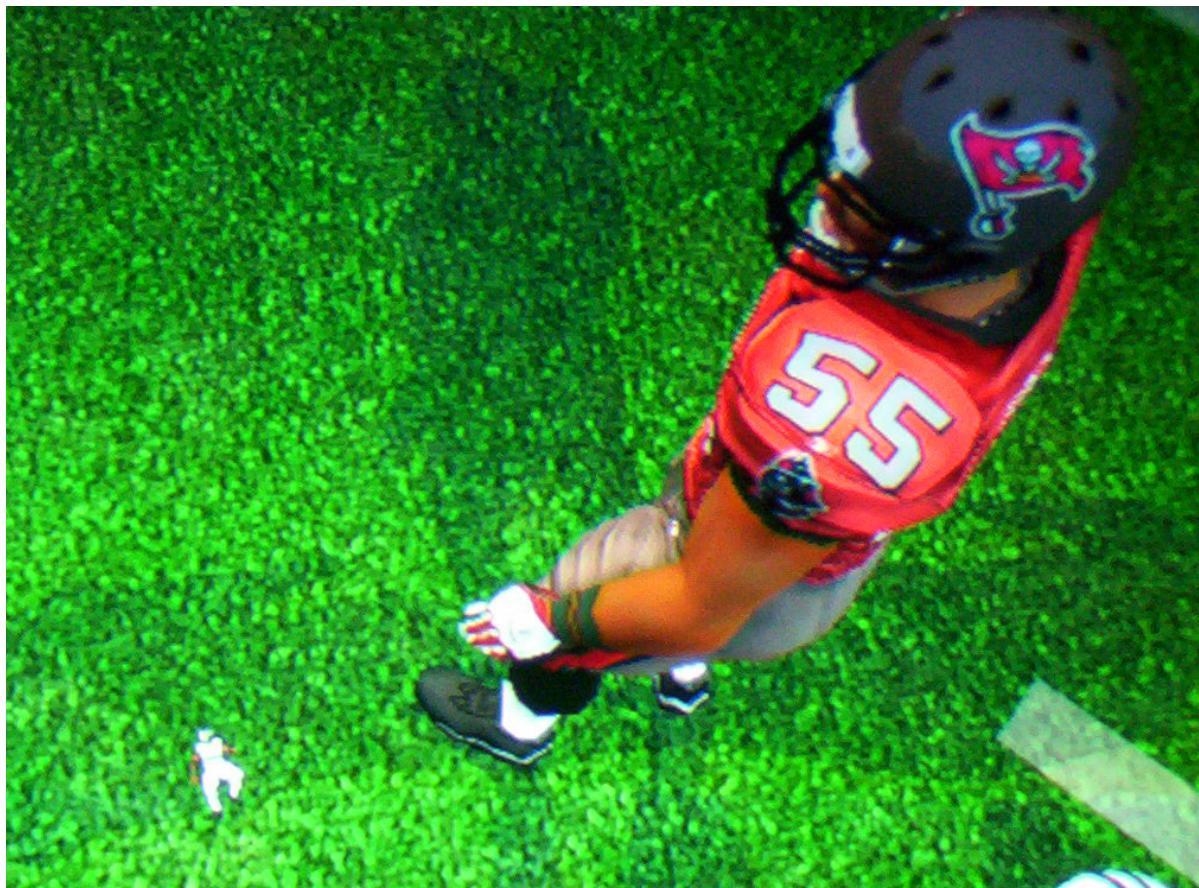
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# Where is Model-Based Testing Heading?

1. Security Testing
2. Shortening Bug Repro Scenarios
3. Meaningful Regression Testing
4. Machine Learning?

# Security Testing

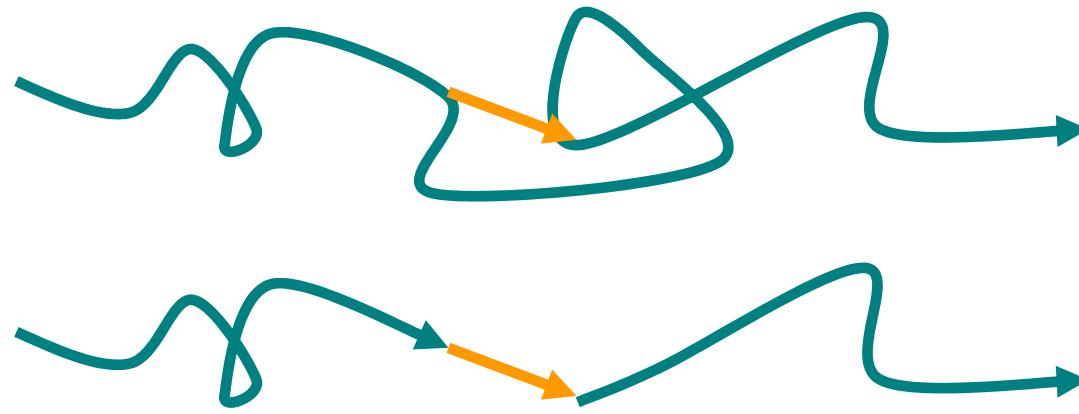
“The testing method developed in the PROTOS project is uniquely practical .... Tests are conducted by bombing software with illegally formatted or unexpected input.”

**Tekes - National Technology Agency of Finland**

## CERT Advisories

- CA-2001-18 Multiple vulnerabilities in LDAP Implementations
- CA-2002-03 Multiple vulnerabilities in SNMP Implementations
- CA-2003-06 Multiple vulnerabilities in SIP Implementations
- CA-2003-11 Multiple vulnerabilities in Lotus Notes and Domino

# Shortening Repro Scenarios



# The Motivation

"The fewer steps that it takes to reproduce a bug,  
the fewer places the programmer has to look (usually).

If you make it easier to find the cause and test the change,  
you reduce the effort required to fix the problem.  
Easy bugs gets fixed even if they are minor."

- from Testing Computer Software

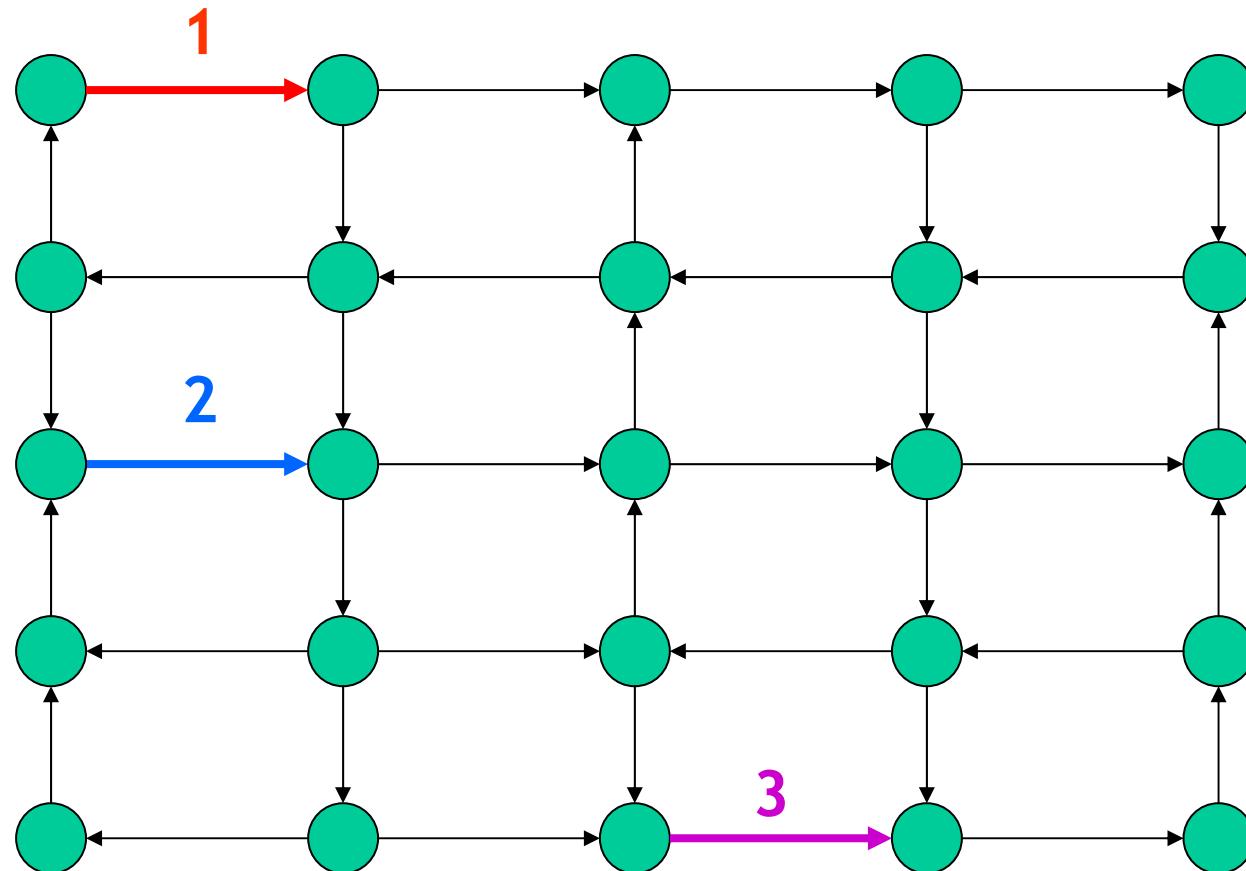


# The Beeline Approach

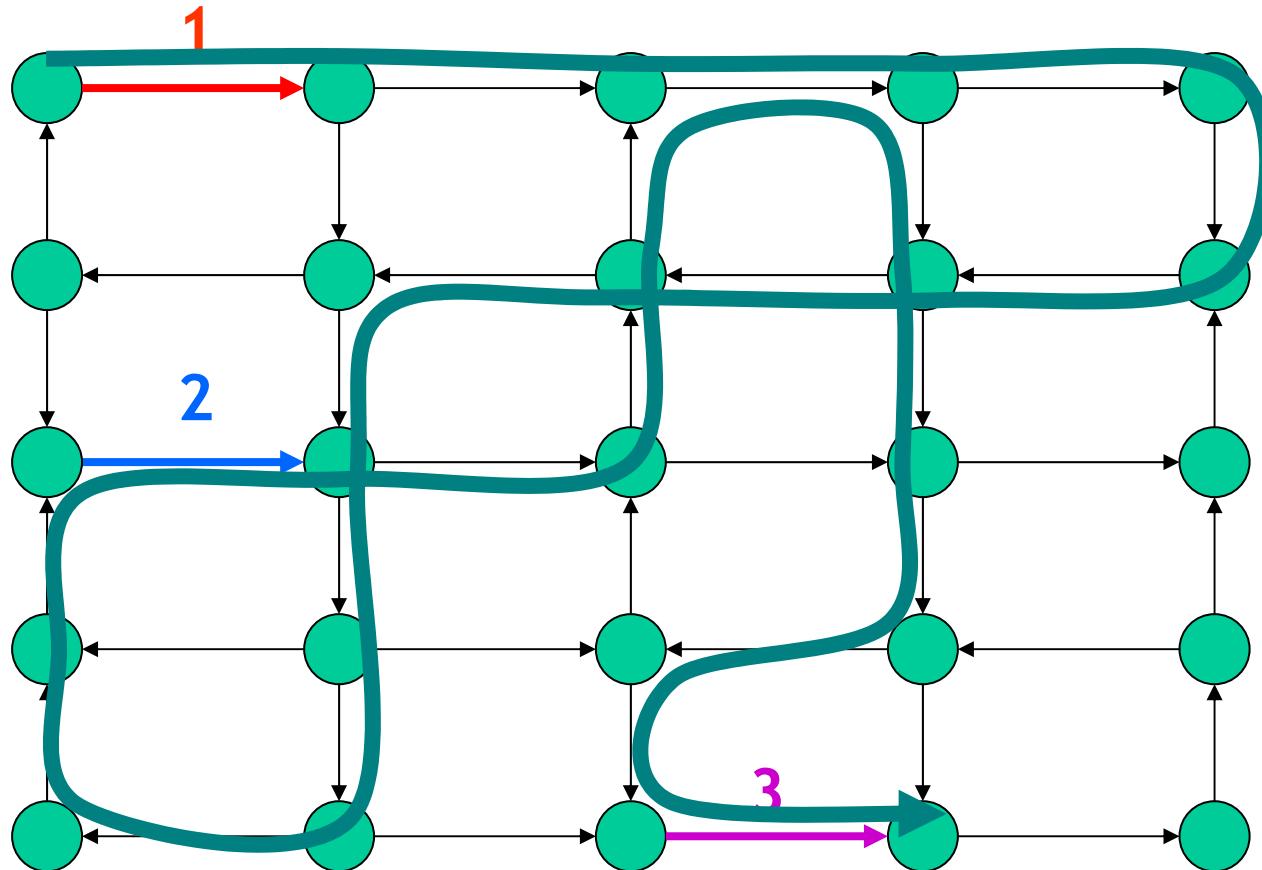
A repro path is simply another traversal through the state model, so ...

1. Choose any 2 nodes in the repro path
2. Find the shortest path between them
3. Execute the spliced 'shortcut' path
4. Evaluate the results and repeat

# The repro path reduction problem

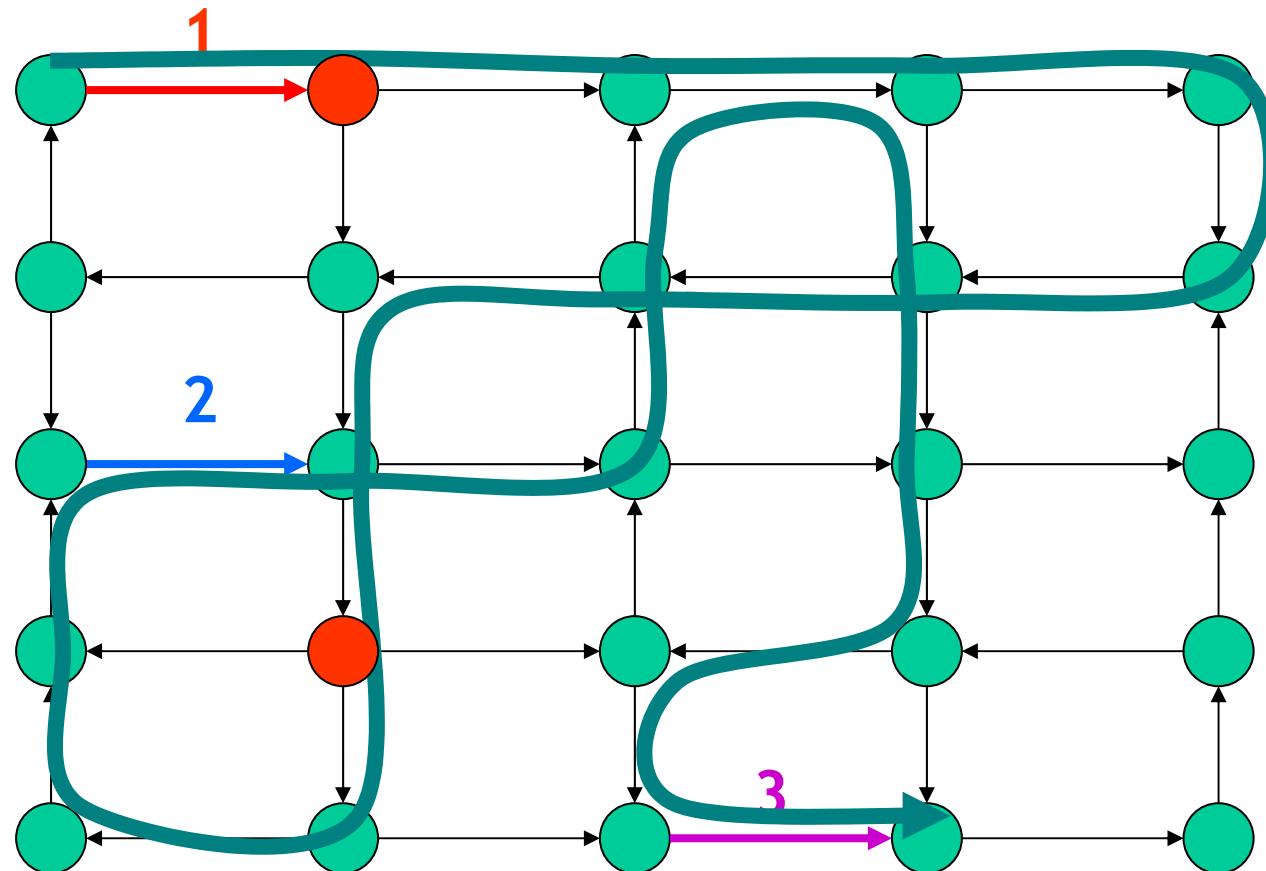


# Random walk finds a bug

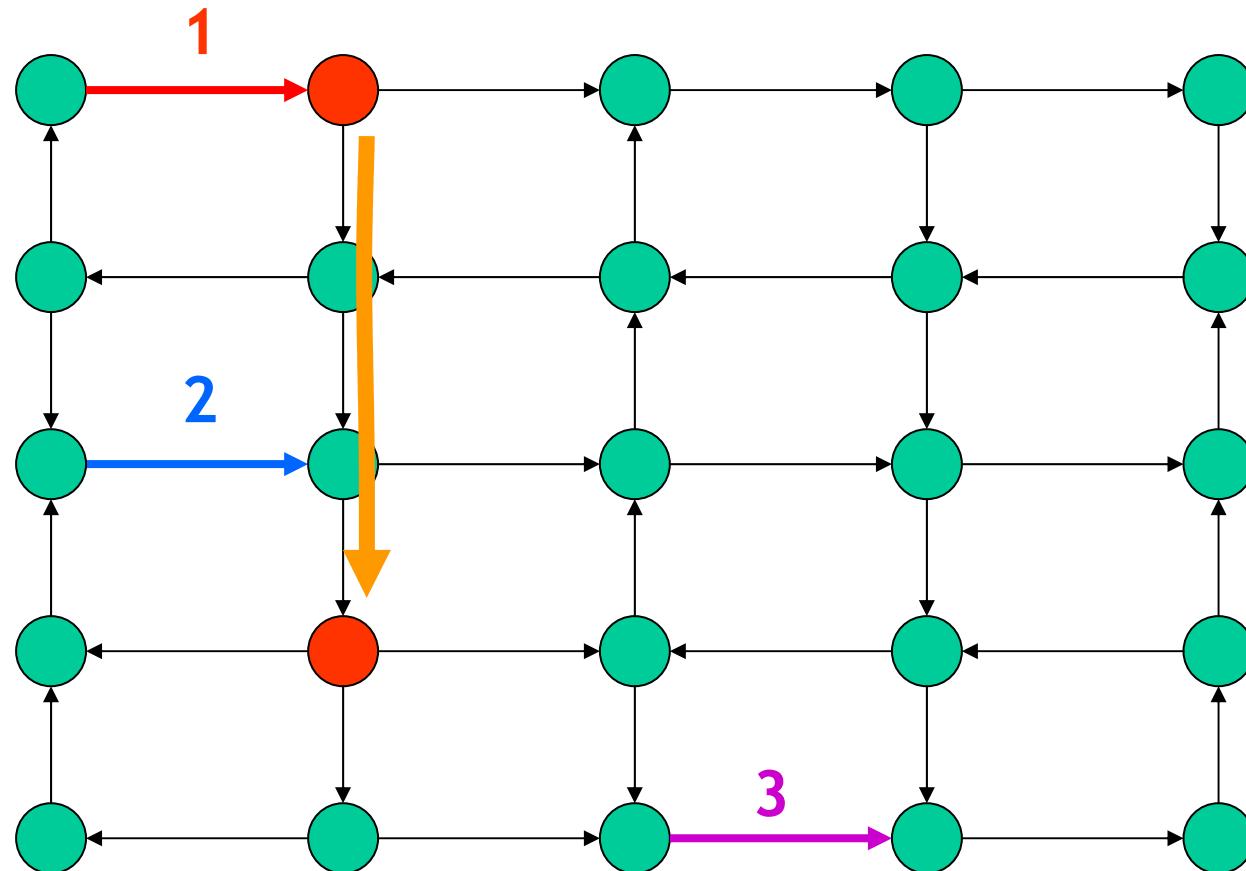


... but the repro path is inconveniently long

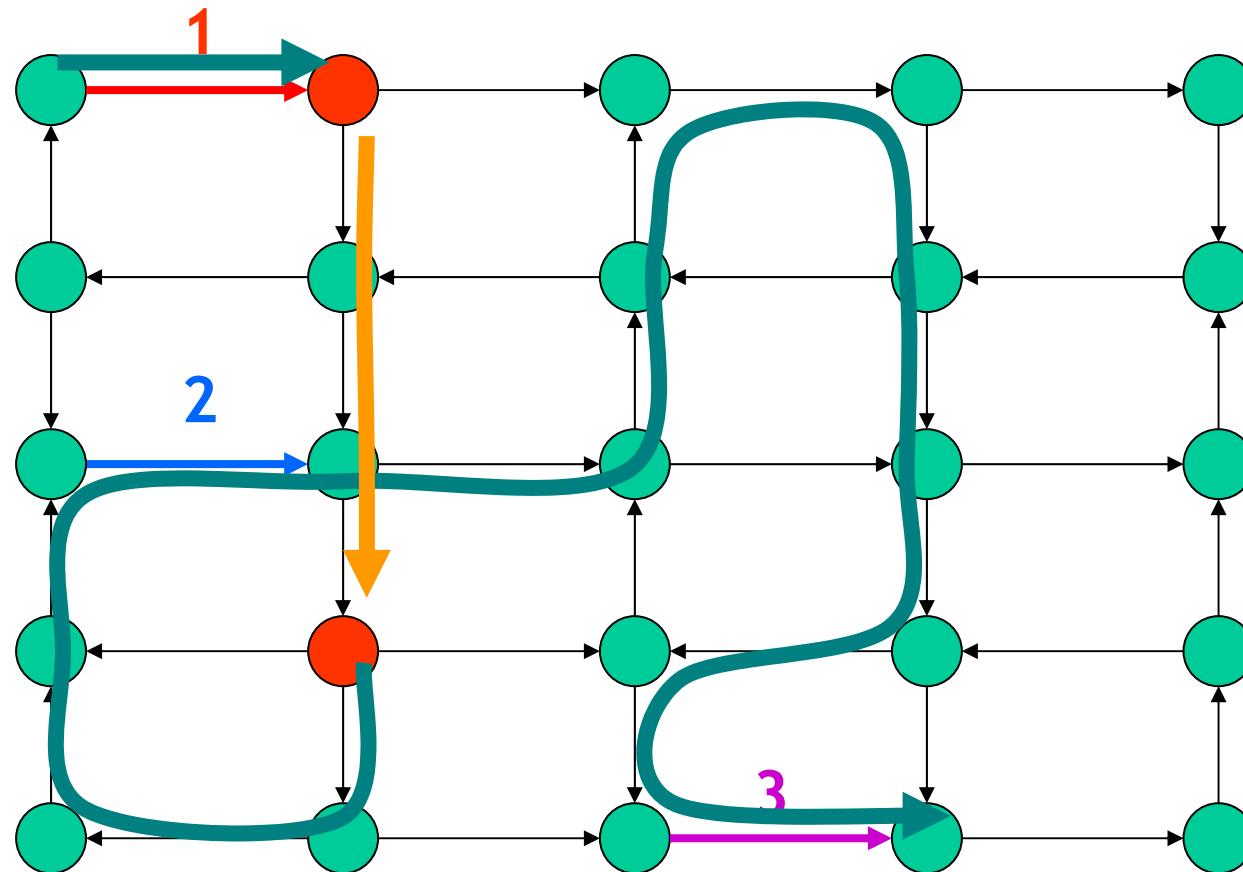
# 1. Choose any 2 nodes in the path



## 2. Find shortest path between them

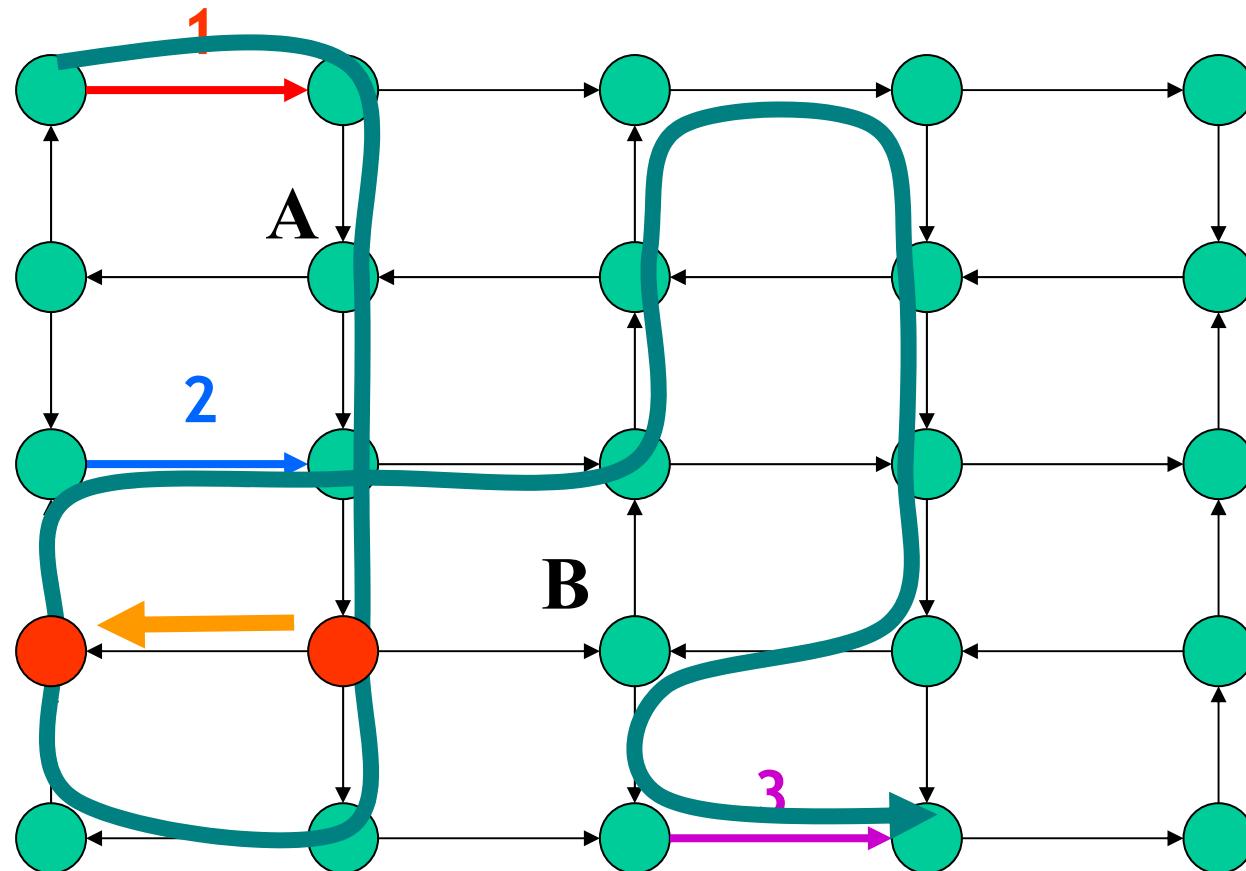


### 3. Execute the spliced shortcut path

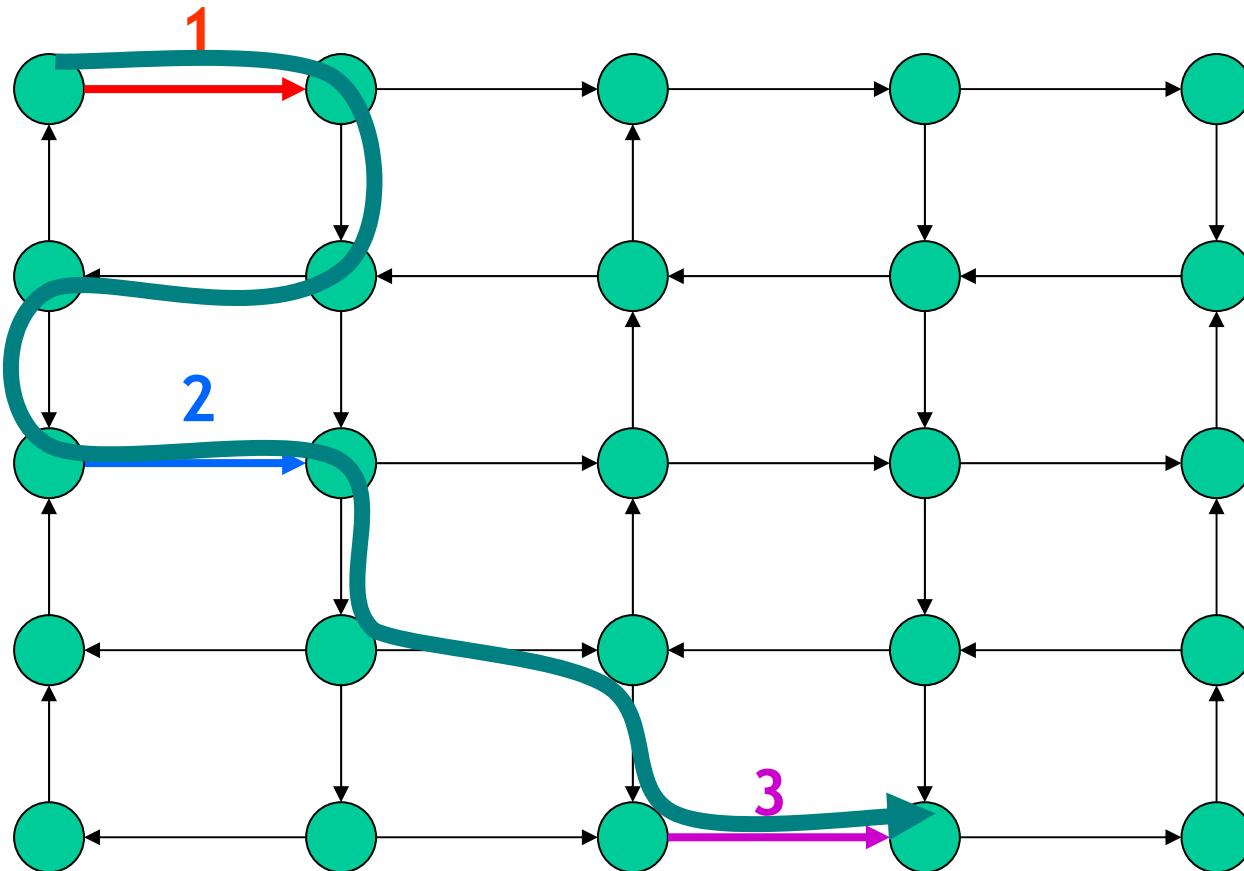


The bug repro'ed - this is the new shortest path

# Continue trimming ...



... until you stop.

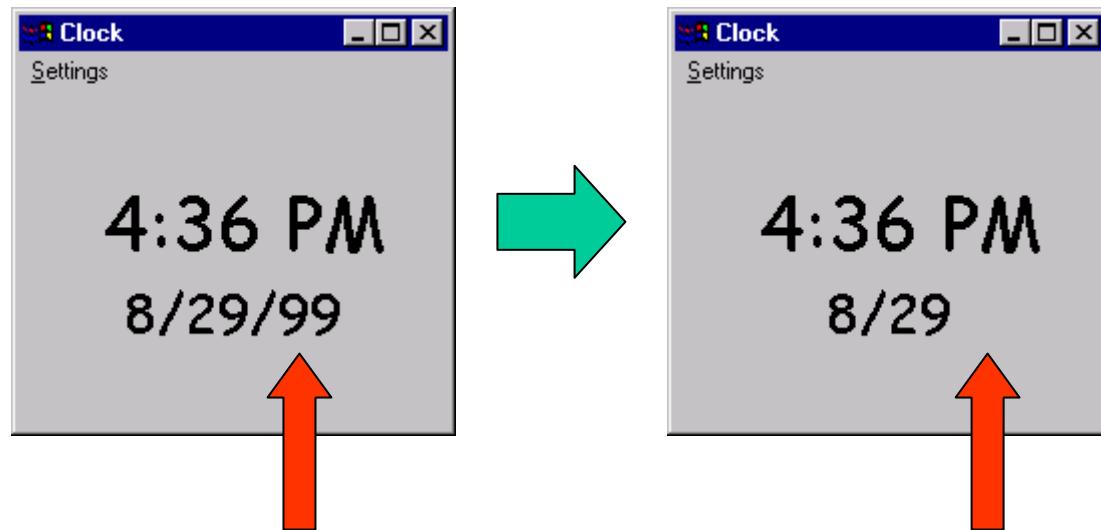


# Why Use a Model for Reducing?

- The model can detect (and therefore reduce) both crashing AND non-crashing bugs.
- Finding a shortcut is simple in a model, so the reduction is more efficient.
- Finding bugs is good. Getting them fixed is better.

# That Was The Year That Wasn't

Start  
Minimize  
Stop  
Start  
Restore  
Date



bug

# An 84-step repro sequence

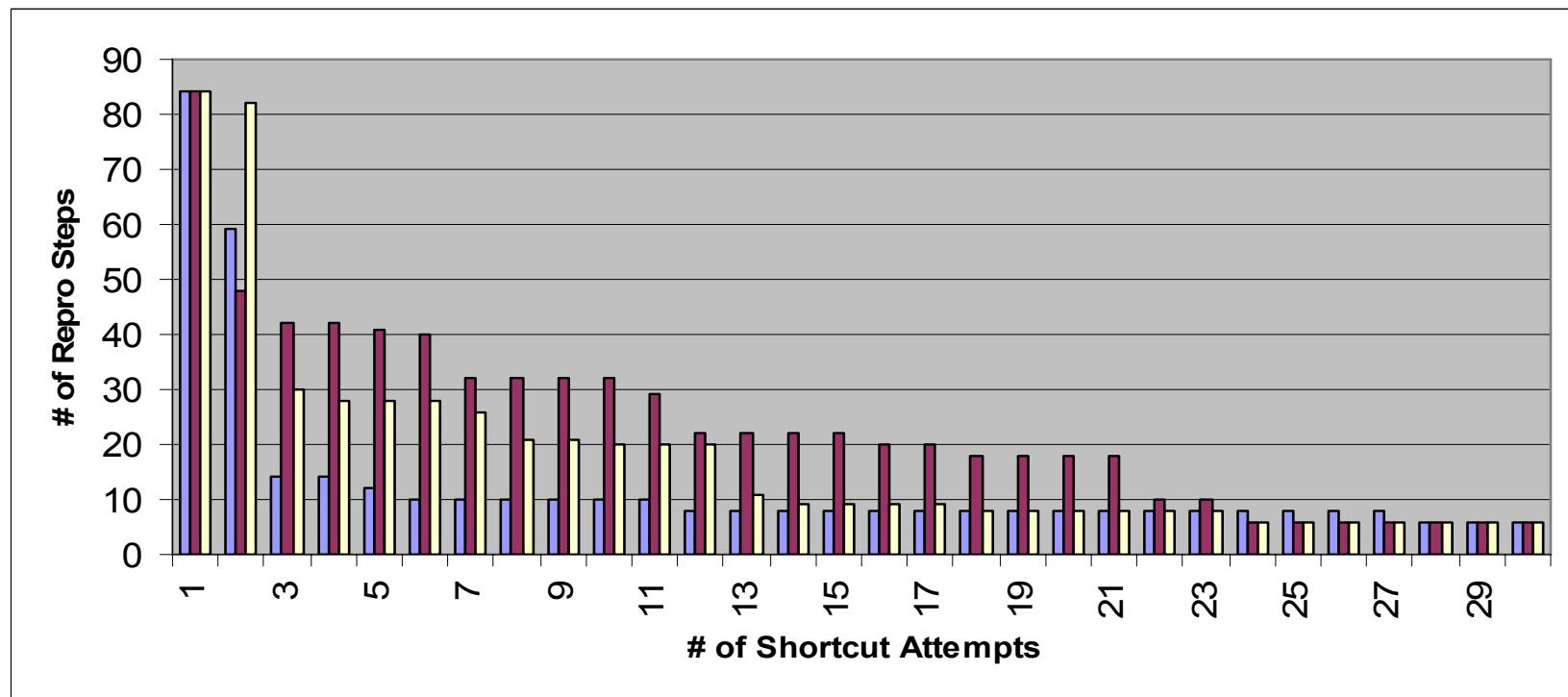
**invoke** about ok\_about no\_title doubleclick seconds restore  
seconds doubleclick doubleclick date about ok\_about restore  
gmt maximize doubleclick doubleclick date seconds date  
close\_clock invoke close\_clock invoke close\_clock invoke  
seconds date restore about ok\_about no\_title doubleclick  
digital doubleclick doubleclick no\_title doubleclick no\_title  
doubleclick seconds restore restore doubleclick doubleclick gmt  
analog maximize date digital minimize restore **minimize**  
**close\_clock invoke restore** digital date minimize close\_clock  
invoke maximize gmt digital restore doubleclick doubleclick  
about ok\_about maximize digital digital digital seconds analog  
about ok\_about about ok\_about minimize close\_clock invoke  
restore **date**



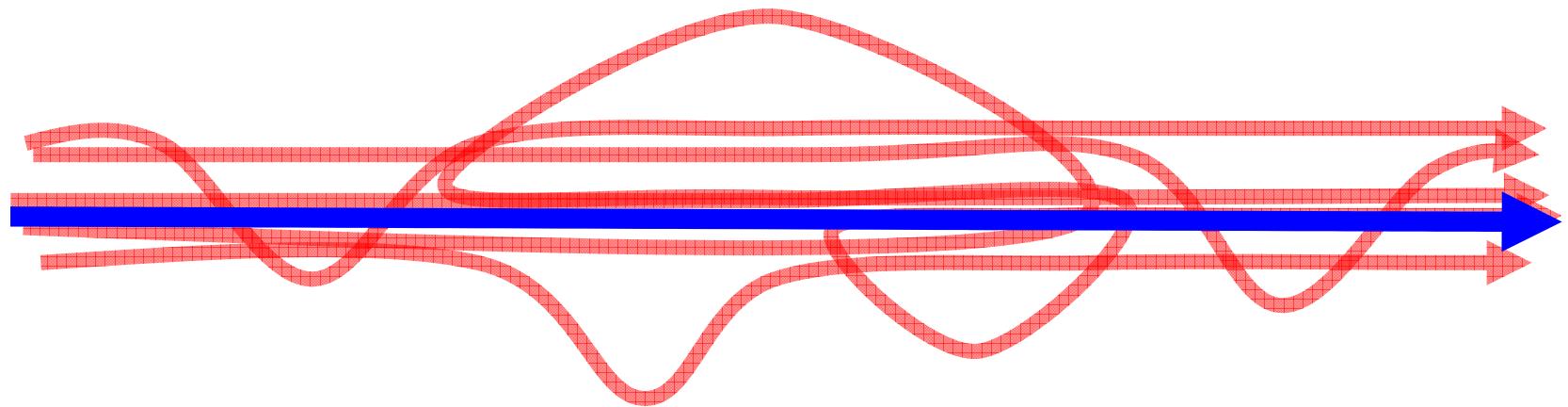
# Reducing the Sequence:

- Initial path length: 84 steps
- Shortcut attempt 2 : repro sequence: 83 steps
- Shortcut attempt 3 : repro sequence: 64 steps
- Shortcut attempt 4 : repro sequence: 37 steps
- Shortcut attempt 5 : repro sequence: 11 steps
- Shortcut attempt 7 : repro sequence: 9 steps
- Shortcut attempt 20 : repro sequence: 8 steps
- Shortcut attempt 29 : repro sequence: 6 steps

# # Repro Steps Over Time



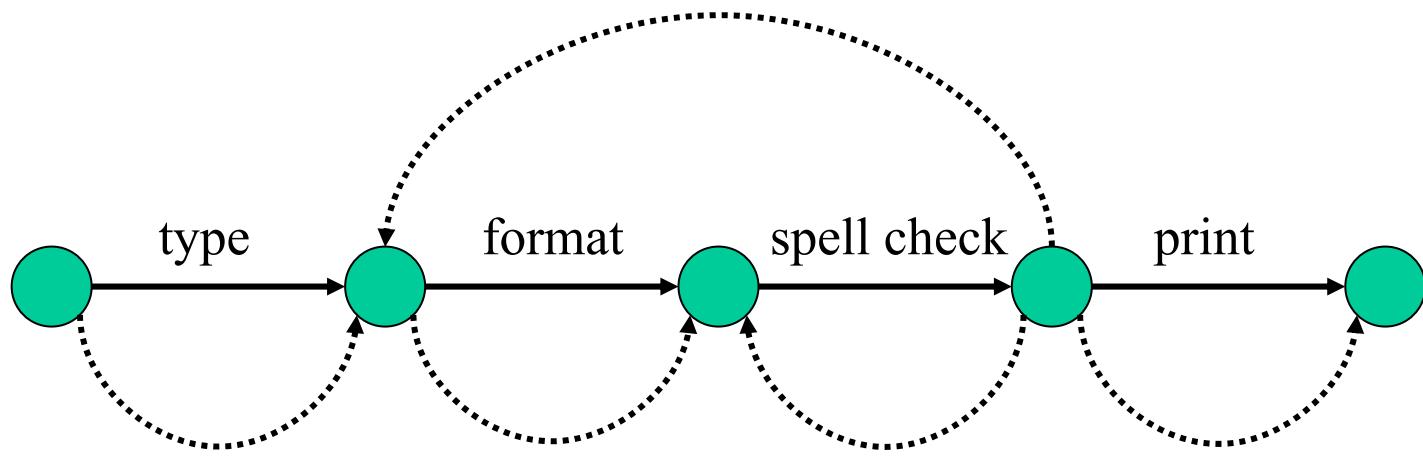
# Useful Regression Testing



# The Motivation

Q: What scenario does a developer use to test a fix?

A: The repro scenario you provided!

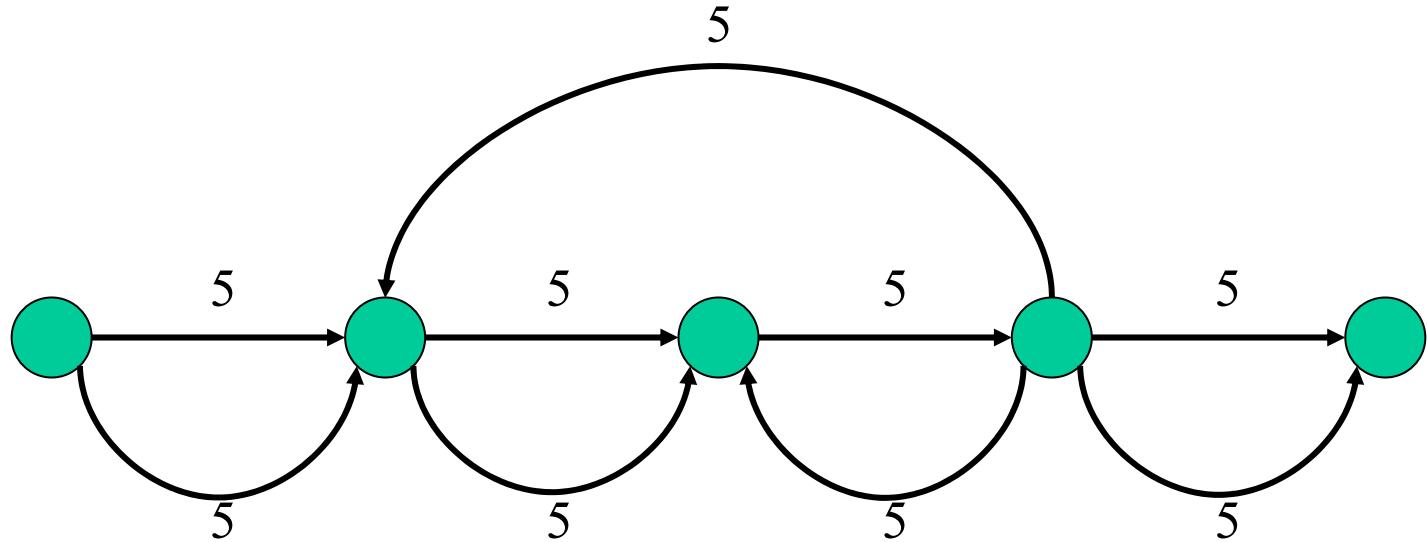


# The Gawain\* Approach

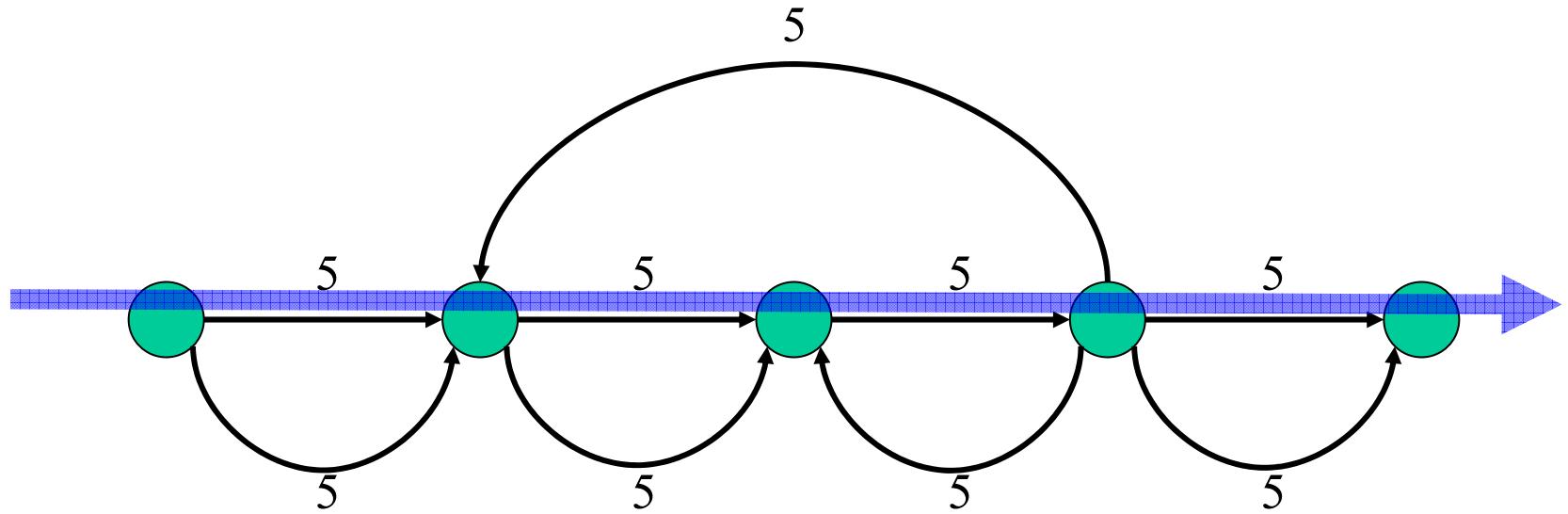
1. Assign the same weight to each arc in a graph
2. Choose a path through the graph
3. Assign a low weight to each arc in that path
4. Exercise paths in graph in weight-increasing order

\* Graph Algorithm Without An Interesting Name

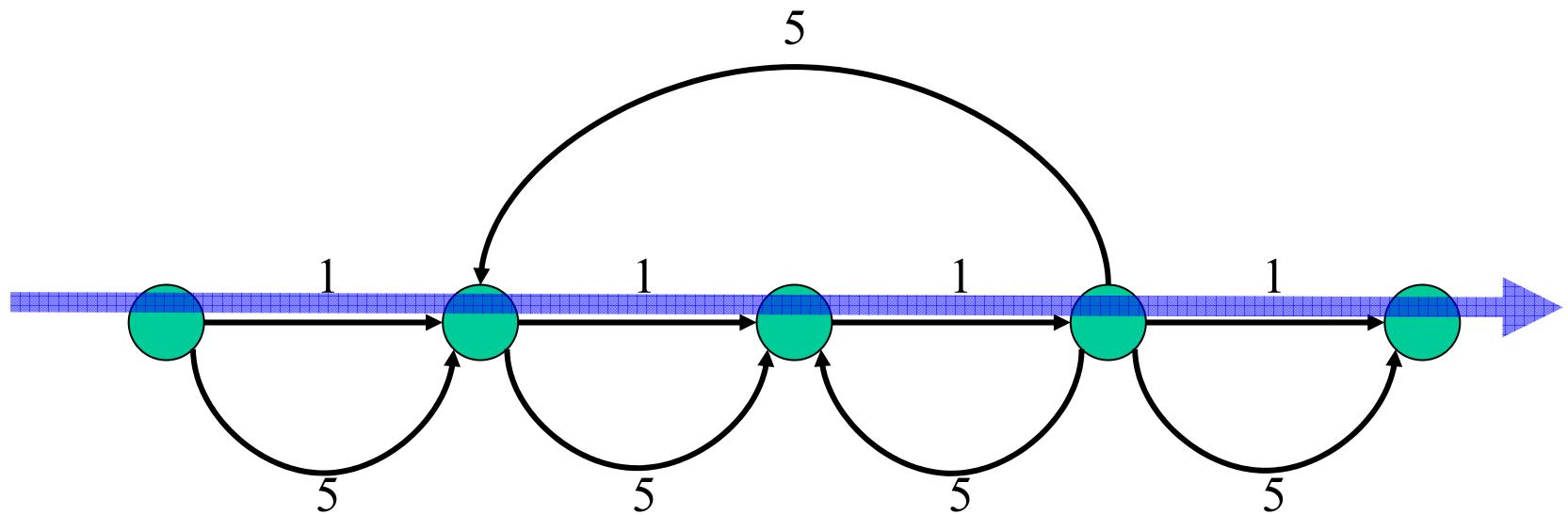
Assign the same weight to each arc



# Choose a path through the graph

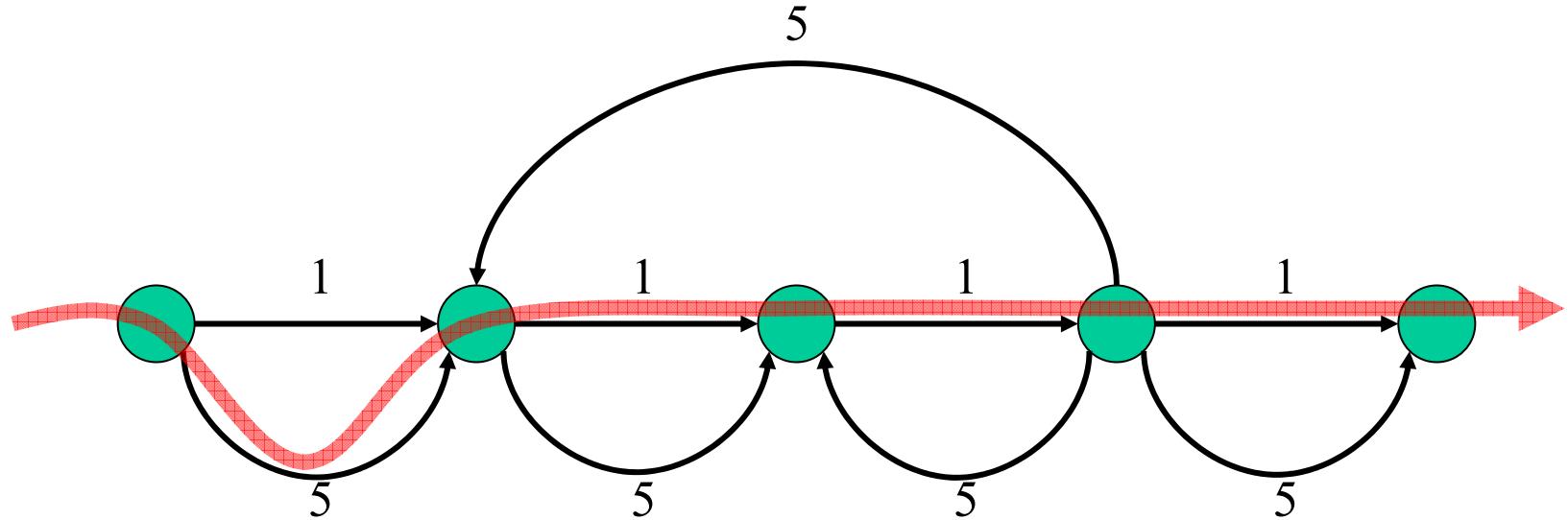


Assign a lower weight to each arc  
in that path

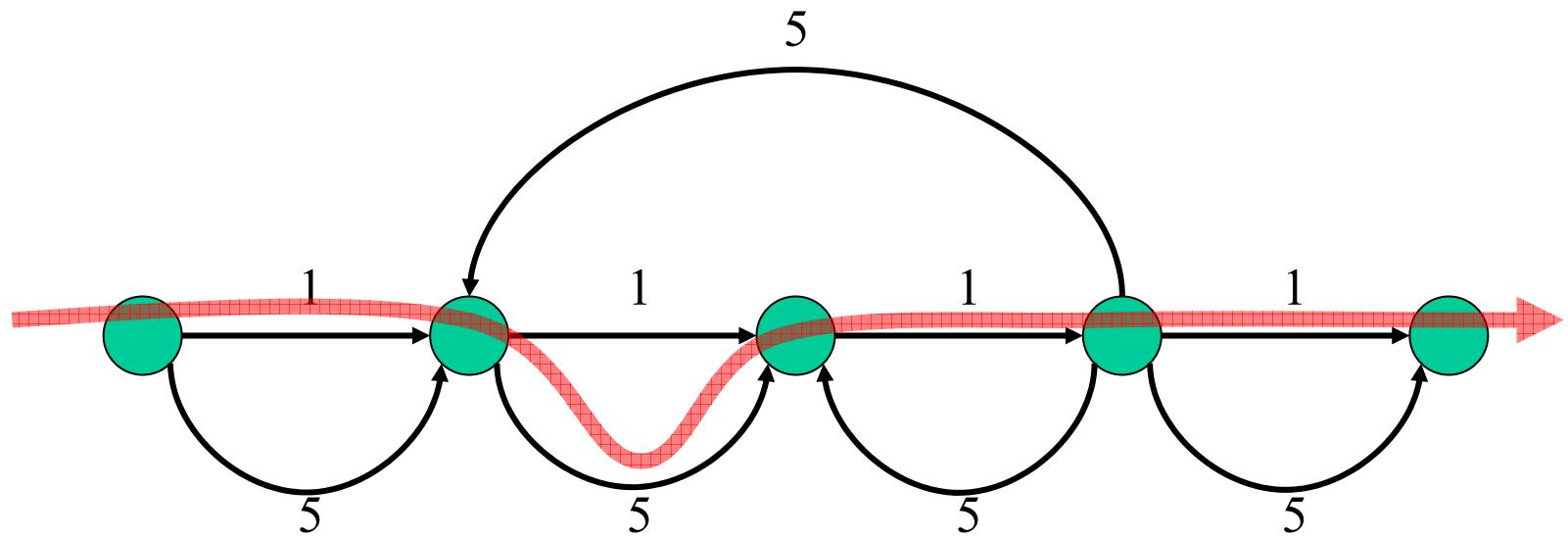


Weight of this path = 4

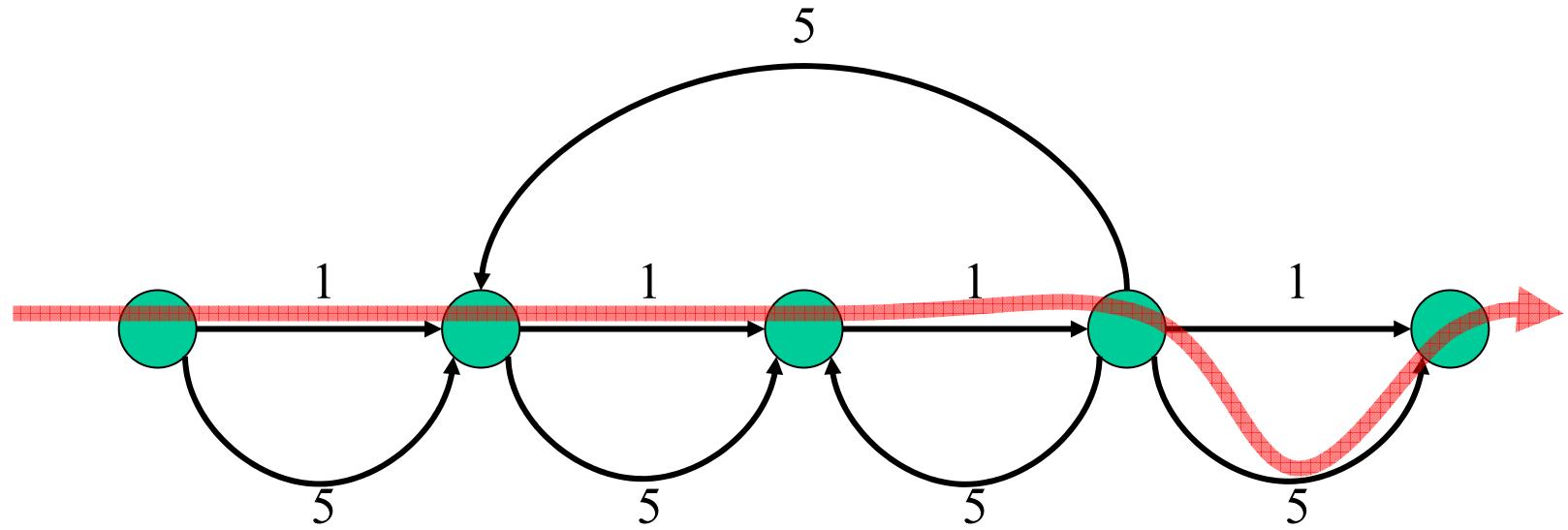
Execute all paths with total weight less than some amount "X"



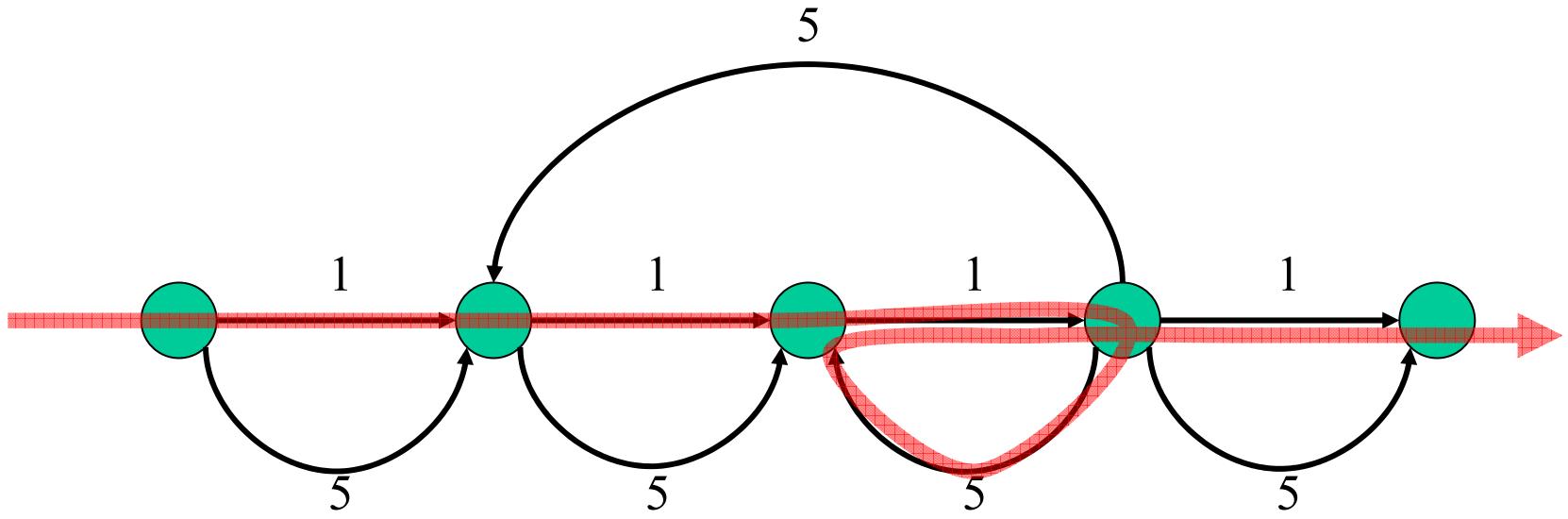
E.g., weight of this path = 8



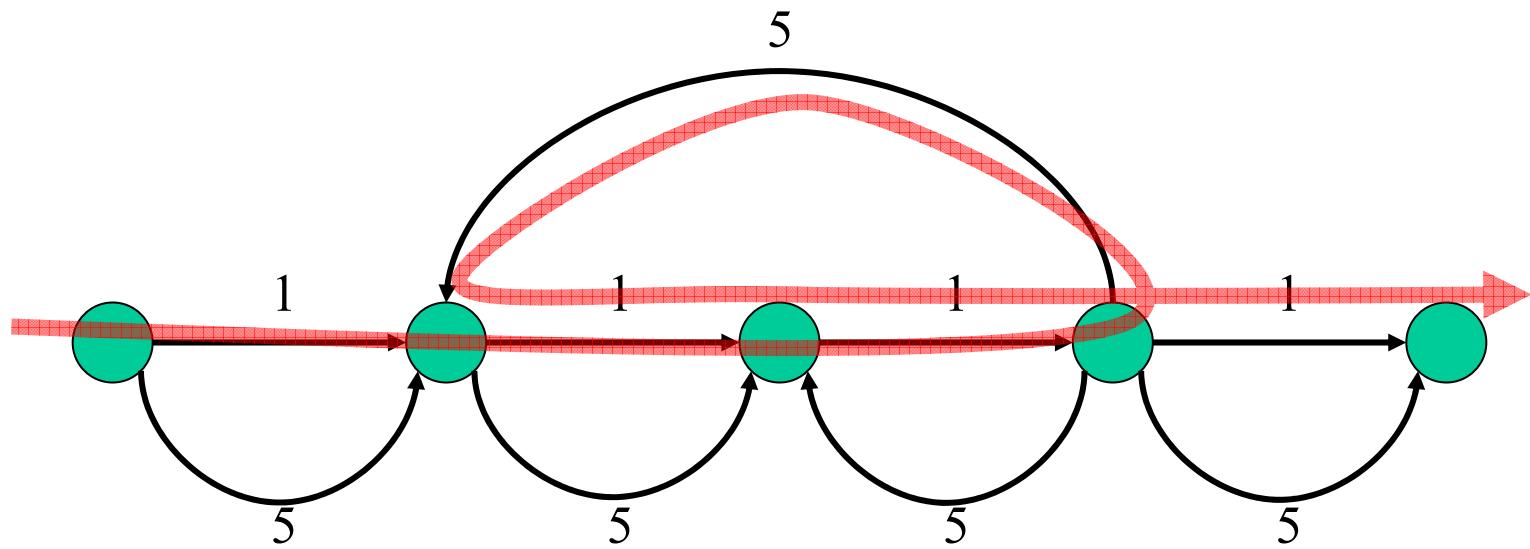
Weight of this path = 8



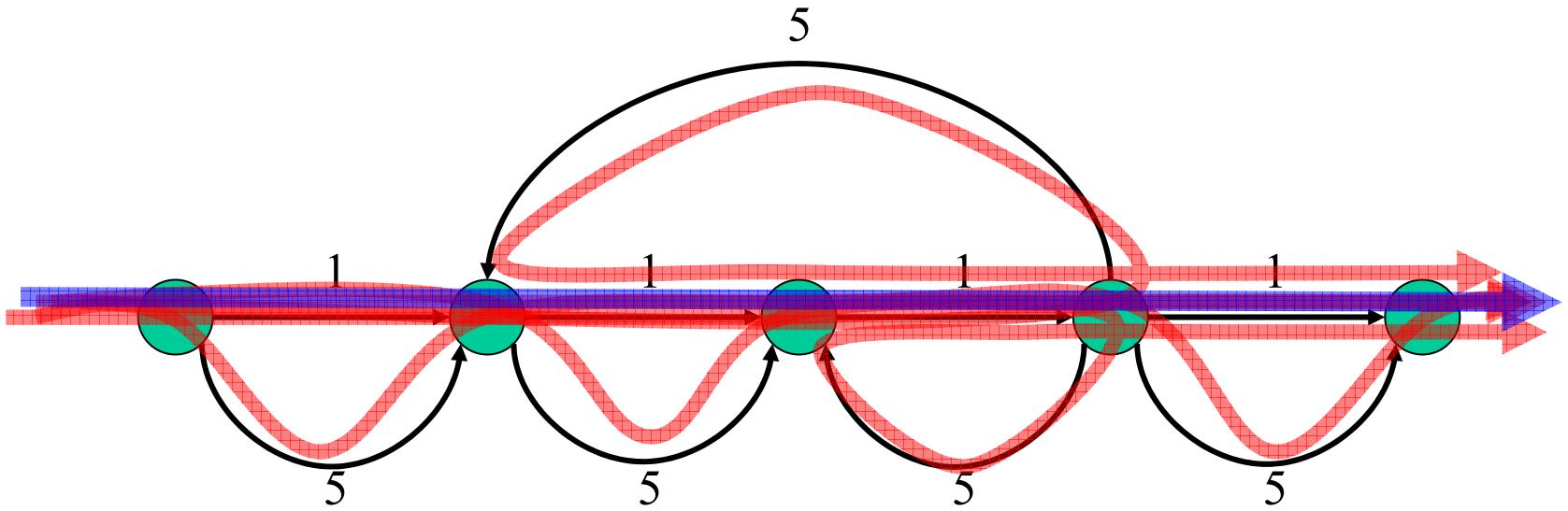
Weight of this path = 8



Weight of this path = 9

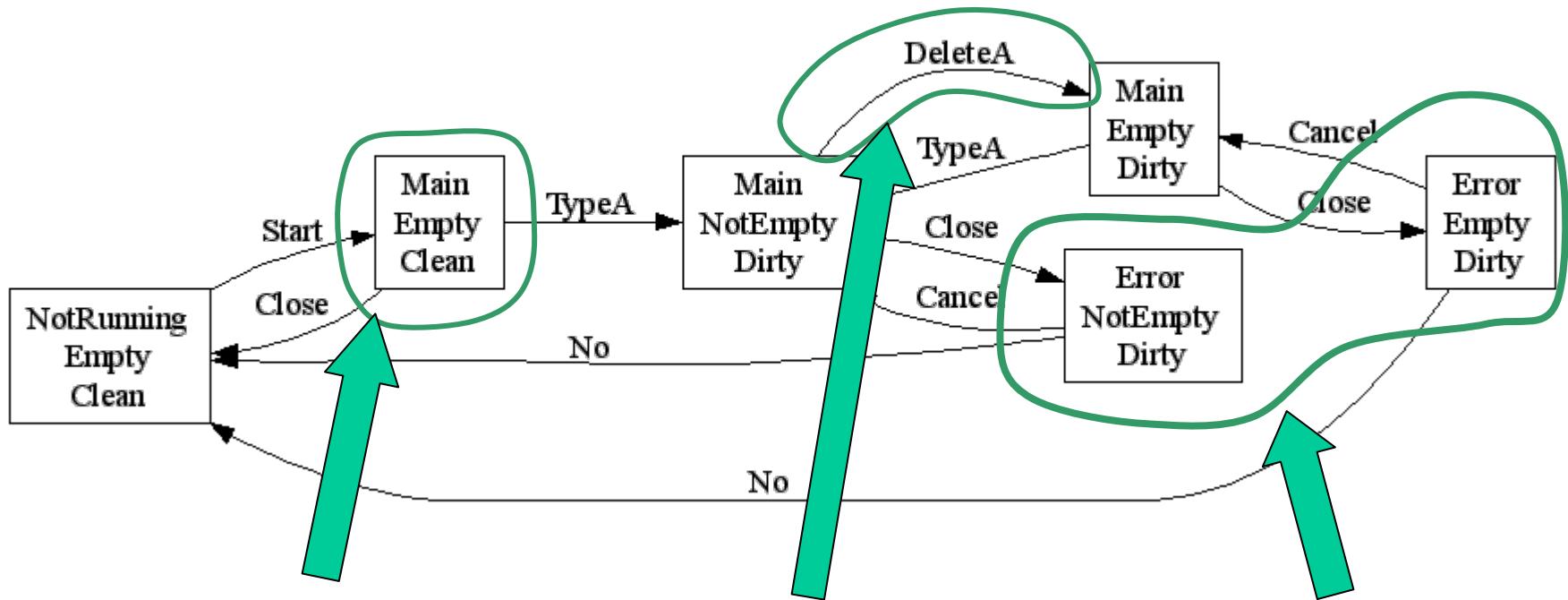


Weight of this path = 11



You end up “Cocooning” the regression path

# Machine Learning?



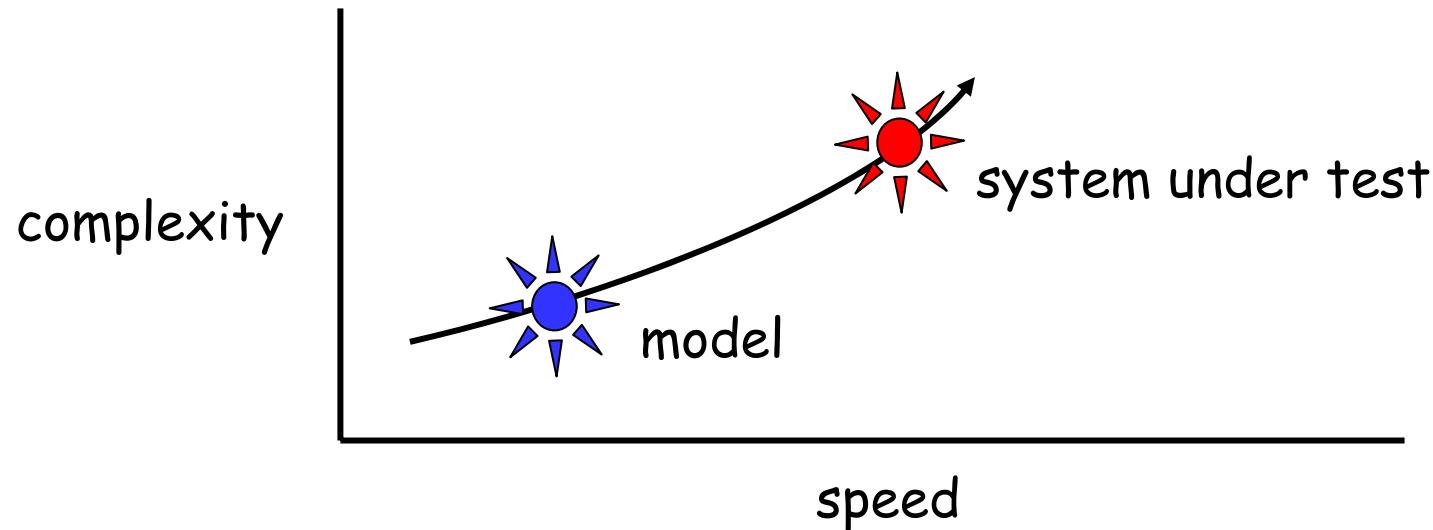
This developer  
is new.

New bug  
fix here.

This feature  
is new.

# Observations on Model-Based Testing

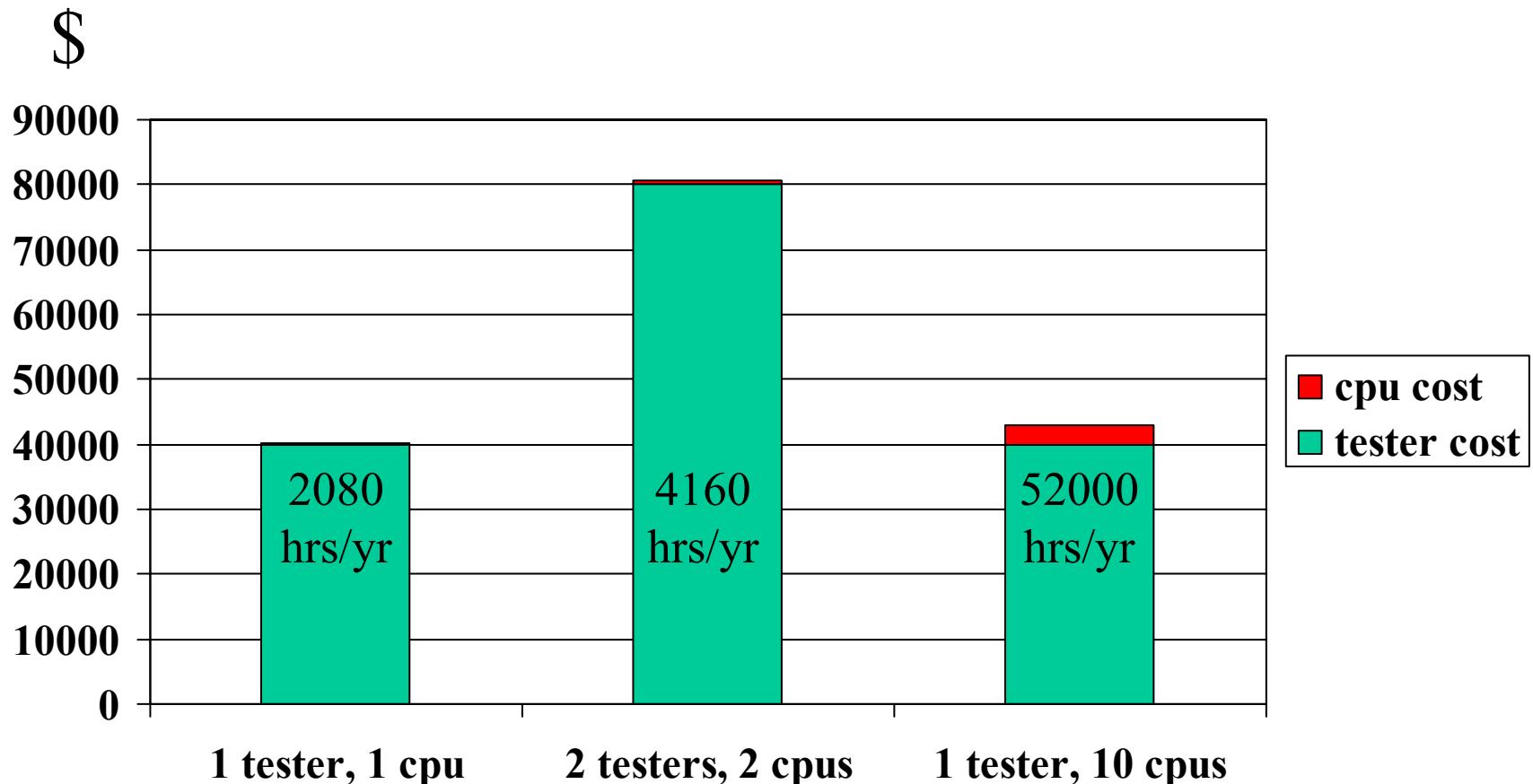
# Why Does Model-Based Testing Work?



"... I think that less than 10 percent of most programs' code is specific to the application. Furthermore, that 10 percent is often the easiest 10 percent. Therefore, it is not unreasonable to build a model program to use as an oracle."

-Boris Beizer, Black Box Testing, p.63

# Economics of Model-Based Testing

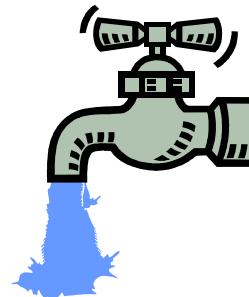


# Metrics Issues

Should you count bugs you prevented?



Should you count how many test cases you've generated?



# Benefits of Model-Based Testing

- Easy test case maintenance
- Reduced costs
- More test cases
- Early bug detection
- Increased bug count
- Time savings
- Time to address bigger test issues
- Improved tester job satisfaction

# Obstacles to Model-Based Testing

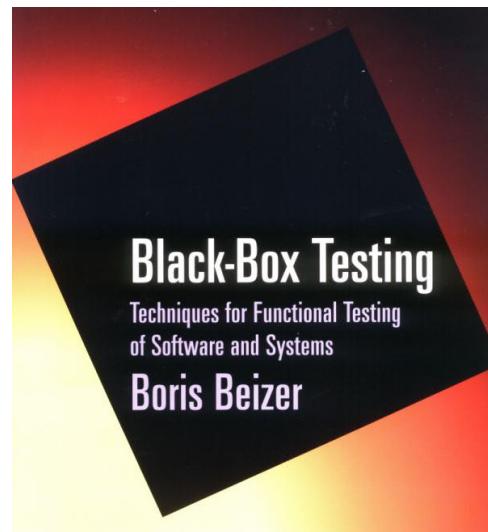
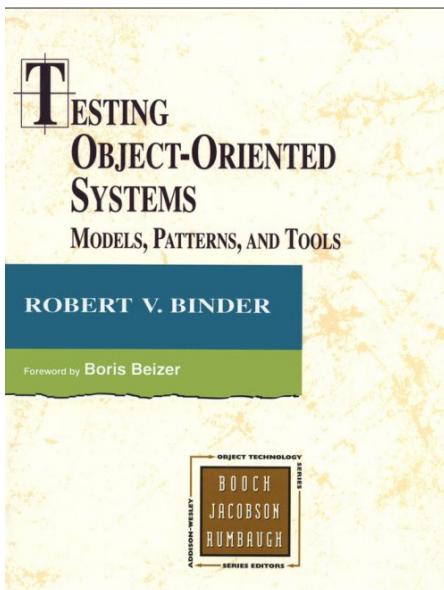
- Comfort factor
  - This is not your parents' test automation
- Skill sets
  - Need testers who can design
- Expectations
  - Models can be a significant upfront investment
  - Will never catch all the bugs
- Metrics
  - Bad metrics: bug counts, number of test cases
  - Better metrics: spec coverage, code coverage

# A Useful Resource

The Model-Based Testing Home Page

[www.model-based-testing.org](http://www.model-based-testing.org)

# Recommended reading



Thank  
you!

