

Mathematical Logic – Proofs by Resolution (recap)

$$P \rightarrow Q \equiv \neg P \vee Q$$
$$\neg(P \rightarrow Q) \equiv P \wedge \neg Q$$

The method:

- negate the statement
- Pg 42 - convert to prenex form
 - move quantifiers as prefix
- Pg 43 - convert to skolem form
 - remove quantifiers and replace with functions
 - convert to clausal form = conj NF = $(\dots \vee \dots) \wedge (\dots \vee \dots) \dots$
- Pg 58 - resolve by resolution (via unifications and substitutions)

- Pg 37 - resolution for propositions
- Pg 38-40 - examples
- Pg 60 - ex 37, example of predicates resolution
 - $P \wedge Q \rightarrow R$ processed as a whole
 - or process separately P , Q and $\neg R$
 - why?

- Pg 61 - Prolog computation
- Pg 62 - example, the English succession
- Pg 64 - Prolog execution of above

fact	$B.$	$\{B\}$
definite clause	$B \leftarrow A_1, \dots, A_n.$	$\{\neg A_1, \dots, \neg A_n, B\}$
goal	$\leftarrow A_1, \dots, A_n.$	$\{\neg A_1, \dots, \neg A_n\}$