

STRUCTURI DE DATE SI ALGORITMI

CURS I, II
INTRODUCERE, ALGORITM, ANALIZA ALGORITMILOR,
LISTE, STIVE, COZI

AGENDA

- Prezentare curs, echipa, reguli
- Putin despre algoritmi ...
- Structuri de date
 - Abstracte: Lista, stiva, coada
 - Implementari: lista simplu/dublu inlantuita, etc.

STRUCTURI DE DATE SI ALGORITMI

- Echipa:
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 - Pagina curs:
 - Moodle: <https://moodle.cs.utcluj.ro/>

OBJECTIVE

- Familiarizarea cu structuri de date fundamentale si algoritmi care opereaza pe acestea
- Familiarizarea cu diferite proprietati ale structurilor de date si algoritmilor
- Dezvoltarea capacitatii de a analiza comparativ algoritmii (proprietati, timp de rulare, memorie folosita, etc)
- Dezvoltarea capacitatii de a identifica structuri de date si algoritmi potriviti, atunci cand acestia sunt disponibili
- Dezvoltarea capacitatii de a dezvolta algoritmi si structuri de date noi, atunci cand nu exista disponibile

ORGANIZARE

- Cursuri
 - participare, implicare prin intrebari
- Sesiuni de laborator
 - Lucrarea de laborator parcursa inaintea sesiunii de laborator!!!
 - 3 tipuri de sarcini:
 - obligatorii (depunctare!)
 - aditionale (optionale, de fixare a cunostintelor)
 - extra credit (bonus, 9->10)
 - Cadrul didactic de la laborator este acolo in primul rand sa va ajute, in al doilea rand sa va evalueze

EVALUARE

- Activitate practica – 30% (laborator)
 - $0.45 * \text{Test1} + 0.45 * \text{Test2} + 0.1 * \text{Extra credit}$
 - extra credit maxim \rightarrow min 4 probleme extra credit
 - probleme extra credit - max 2 saptamani pt a fi prezentate
- Evaluare pe parcursul semestrului - 20%
 - Partial, in timpul cursului
 - Dupa curs 6?
- Evaluare finala - 50%
 - sesiunea de vara

BIBLIOGRAFIE RECOMANDATA

- Aho, Hopcroft, Ullman [AHU]: Data Structures and Algorithms, Addison-Wesley, 427 pages, 1987.
 - Cartea clasică se SDA, introductivă, valoroasă, nu acopera exhaustiv tematica; Pascal extins
- Cormen, Leiserson, Rivest, (Stein) [CLR, CLRS]: Introduction to Algorithms. MIT Press / McGraw Hill, (2nd edition), 1028 pages, 1990 (2002).
 - BIBLIA de Algoritmi Fundamentali (anul II), scrisă pentru toate nivelele, cu capitole introductive, dar și detaliate (în a doua parte a cărții); pseudocod

BIBLIOGRAFIE EXTINSA

- Preiss. Data Structures and Algorithms with object-Oriented Design Patterns in C++, John Wiley and Sons, 660 pages, 1999.
- Knuth. The Art of Computer Programming, Addison Wesley, 3 volume, multiple editii.
- Skiena. The Algorithm Design Manual. <http://sist.sysu.edu.cn/~isslxm/DSA/textbook/Skiena.-.TheAlgorithmDesignManual.pdf>
(recomandata de recruiterii Google, DAR!! nu suficient de teoretica)

RESURSE ADITIOANALE

- visualgo.net
 - vizualizare, unealta interactiva
- <http://algoviz.org/>
- coursera.org
 - Data structures: Measuring and Optimizing Performance (U.C. San Diego) - in desfasurare
- ...

CUPRINS CURS

- Introducere. Algoritm. Structura abstracta de date. Analiza eficientei
- Liste. Stive. Cozi
- *ADT* pentru colectii: dictionare, tabele de dispersie, cozi de prioritati
- Arbori. Arbori binari. Arbori binari de cautare
- Arbori binari de cautare echilibrati: AVL, rosu si negru, arbori perfect echilibrati
- Grafuri: reprezentare; definitii, proprietati, problematici, traversari
- Tehnici de dezvoltare a algoritmilor / generale de cautare: backtracking, branch and bound, greedy, divide et impera, programare dinamica

REZOLVAREA UNEI PROBLEME

- **Model exact** al soluțiilor valide
 - gasirea unui astfel de model - 50% problema rezolvata
 - experienta, cunostinte de matematica, inginerie software, algoritmica, etc.
- Dupa ce dispunem de modelul matematic, putem **specifica o solutie in termenii aceluia model**

CONSTRUIREA MODELULUI

- Provocari:
 - cum modelam **obiectele reale** ca si **entitati matematice**
 - definirea **multimii de operatii** care manipuleaza entitatile
 - modalitatea de **stocare in memorie** (cum le agregam, cum le stocam propriu-zis) - **STRUCTURI DE DATE!**
 - **algoritmii** care realizeaza operatiile - **ALGORITMI!**

DEFINITII

- **Problema computatională:** O specificare în termeni generali a *intrărilor* și *ieșirilor* și relația dorită dintre acestea.
- **Instanță de problemă:** O colecție particulară de intrare pentru problema dată.
- **Algoritm:** O metodă de rezolvare a unei probleme care poate fi implementată de un calculator.
- **Program:** Implementarea explicită a unui algoritm

EXEMPLU - SORTAREA

- Problema:
 - *Intrare:* O secventa/sir de n numere $\langle a_1, a_2, \dots, a_n \rangle$
 - *Iesire:* O permutare a numerelor $\langle a_1, a_2, \dots, a_n \rangle$ a.i. $a_i \leq a_j, i < j$
- Instanta: sirul $\langle 7, 5, 4, 10, 5 \rangle$
- Algoritmi:
 - sortare prin selectie
 - sortare prin insertie
 - sortare rapida (Quick sort)
 - etc

UN ALGORITHM....

- trebuie sa fie:
 - corect
 - eficient
 - *usor de implementat*

PROIECTAREA ALGORITMULUI

ALGORITHMDESIGN(informal problem)

- 1 formalize problem (mathematically) [Step 0]
- 2 **repeat**
 - 3 devise algorithm [Step 1]
 - 4 analyze correctness [Step 2]
 - 5 analyze efficiency [Step 3]
 - 6 refine
- 7 **until** algorithm good enough
- 8 **return** algorithm

EXEMPLU DE ALGORITHM - ROBOT TOUR OPTIMIZATION

- Problema: *Robot Tour Optimization*
- Intrare: O multime S de n puncte in plan.
- Iesire: Care este *cel mai scurt tur ciclu* (e. cycle tour) care viziteaza fiecare punct din multimea S ?

ROBOT TOUR OPTIMIZATION

NearestNeighbor(P)

Pick and visit an initial point p_0 from P

$p = p_0$

$i = 0$

While there are still unvisited points

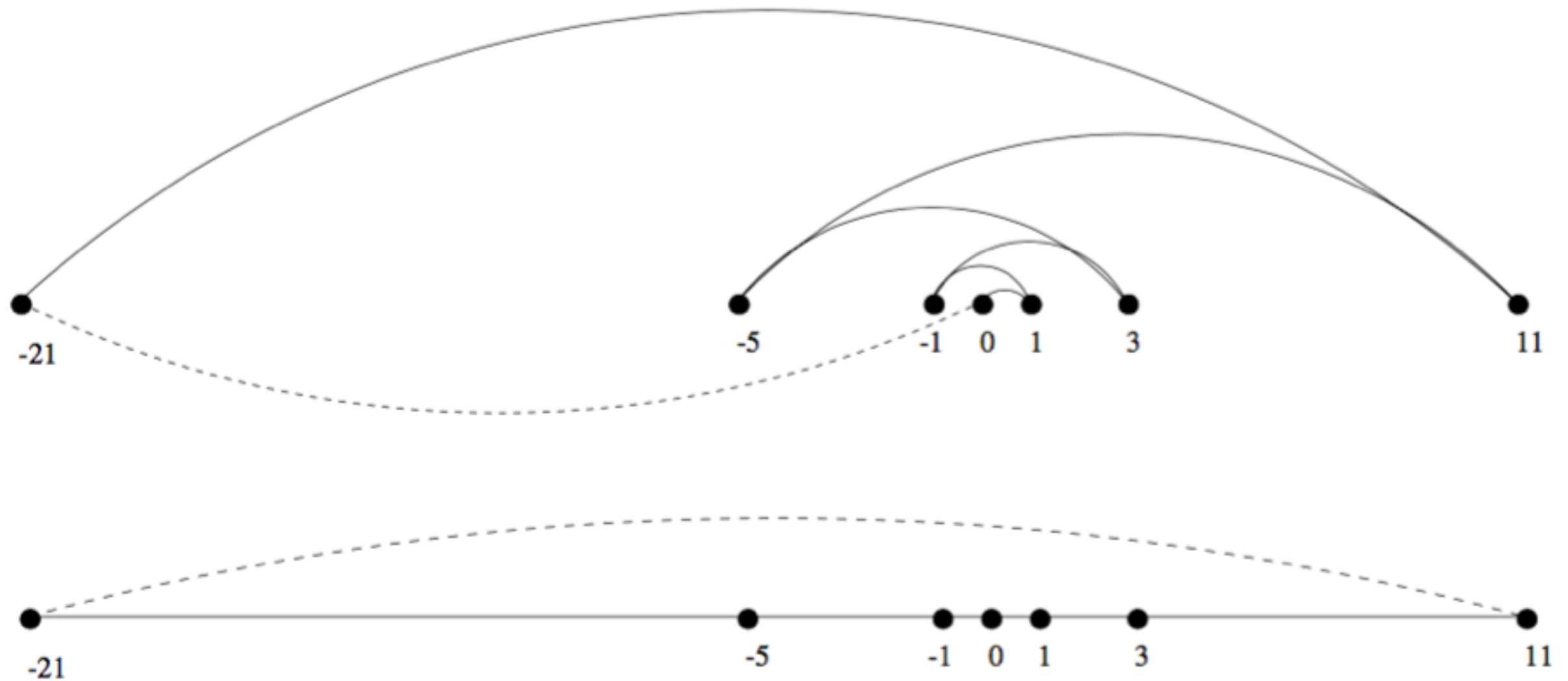
$i = i + 1$

Select p_i to be the closest unvisited
point to p_{i-1}

Visit p_i

Return to p_0 from p_{n-1}

NearestNeighbor



Algoritmul nu gaseste neaparat turul de lungime minima!

ROBOT TOUR OPTIMIZATION

ClosestPair(P)

Let n be the number of points in set P

For $i = 1$ to $n - 1$ do

$d = \infty$

 For each pair of endpoints (s, t) from
 distinct vertex chains

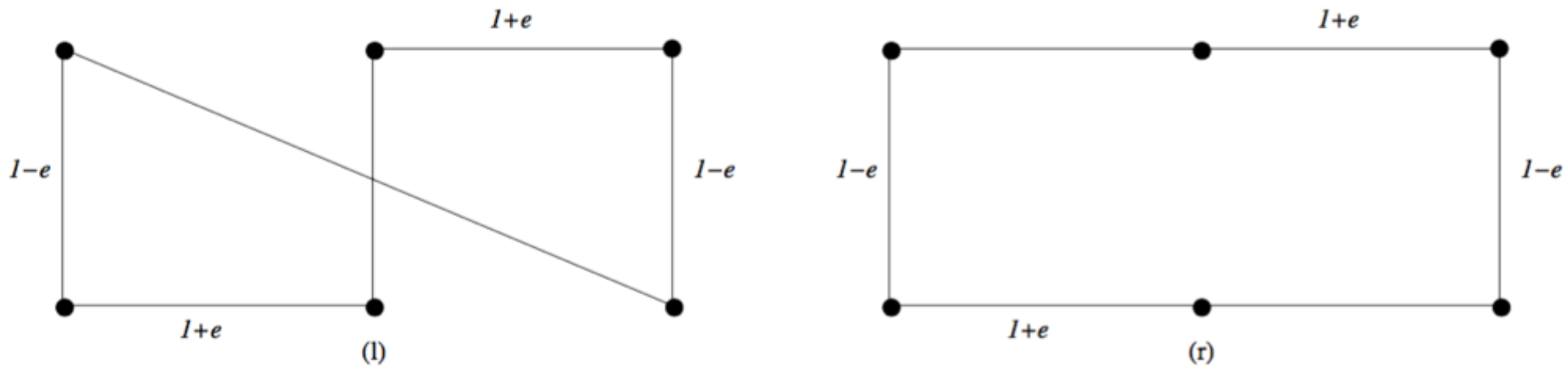
 if $\text{dist}(s, t) \leq d$ then

$s_m = s, t_m = t$, and $d = \text{dist}(s, t)$

 Connect (s_m, t_m) by an edge

Connect the two endpoints by an edge

ClosestPair



Nici acest algoritm nu gaseste neaparat turul de lungime minima!

ROBOT TOUR OPTIMIZATION

OptimalTSP(P)

$d = \infty$

For each of the $n!$ permutations P_i of point set P

 If ($\text{cost}(P_i) \leq d$) then

$d = \text{cost}(P_i)$ and $P_{\min} = P_i$

Return P_{\min}

DETINUT MINTE...

- Esenta unui algoritm este o idee!
- Este important ca algoritmul sa fie exprimat clar!
(pseudocod, limbaj natural, limbaj de programare)
- Corectitudinea trebuie demonstrata! Incorectitudinea -
contra-exemplu (verificabilitate, simplitate)
- Contra-exemple: dimensiune mica, exhaustiv, slabiciuni ->
egalitate, extreme

ANALIZA ALGORITMILOR

- Stabilirea cantitatilor de **resurse** necesare rularii algoritmului (de regula in functie de **dimensiunea** intrarii).
- Resurse:
 - timp
 - memorie (spatiu)
 - numar de accese la memoria secundara
 - numar de operatii aritmetice de baza
 - traficul de retea
- Formal, se defineste timpul de rulare al unui algoritm pe o intrare particulara ca fiind numarul de operatii de baza (atribuiri, comparatii) efectuate de algoritm pe acea intrare.

ANALIZA ALGORITMILOR - ESENTA

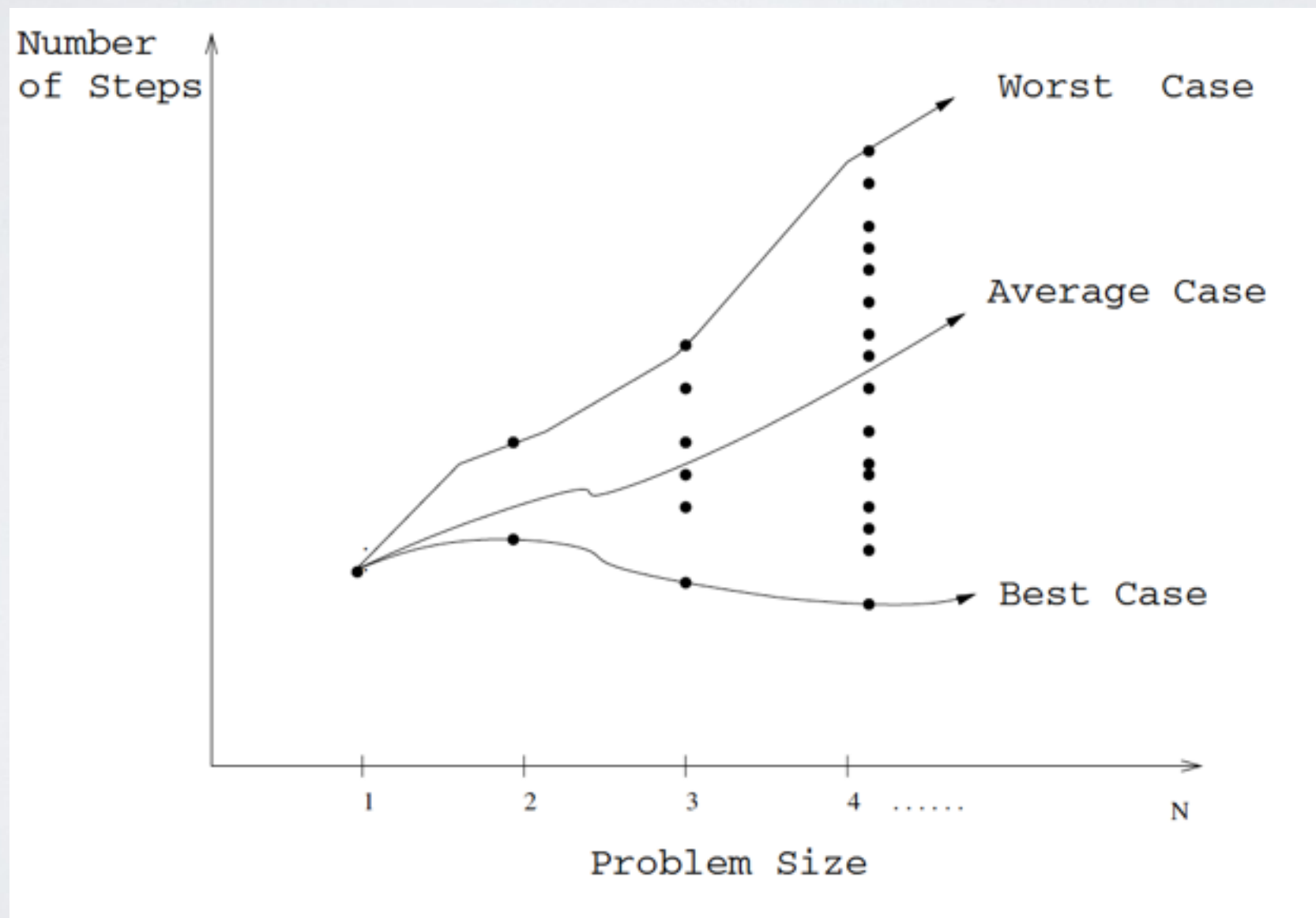
- maniera independenta de masina si limbaj
- unelte:
 - Modelul de calcul RAM
 - Analiza asimptotica a cazului defavorabil

MODELUL RAM DE CALCUL

- orice operatie simpla se executa intr-o unitate de timp
- buclele si sub-rutinele nu sunt operatii simple
(compozitie de mai multe operatii simple)
- accesul la memorie se executa intr-o unitate de timp
(memorie nelimitata, nu se face diferenta intre cache si disc)

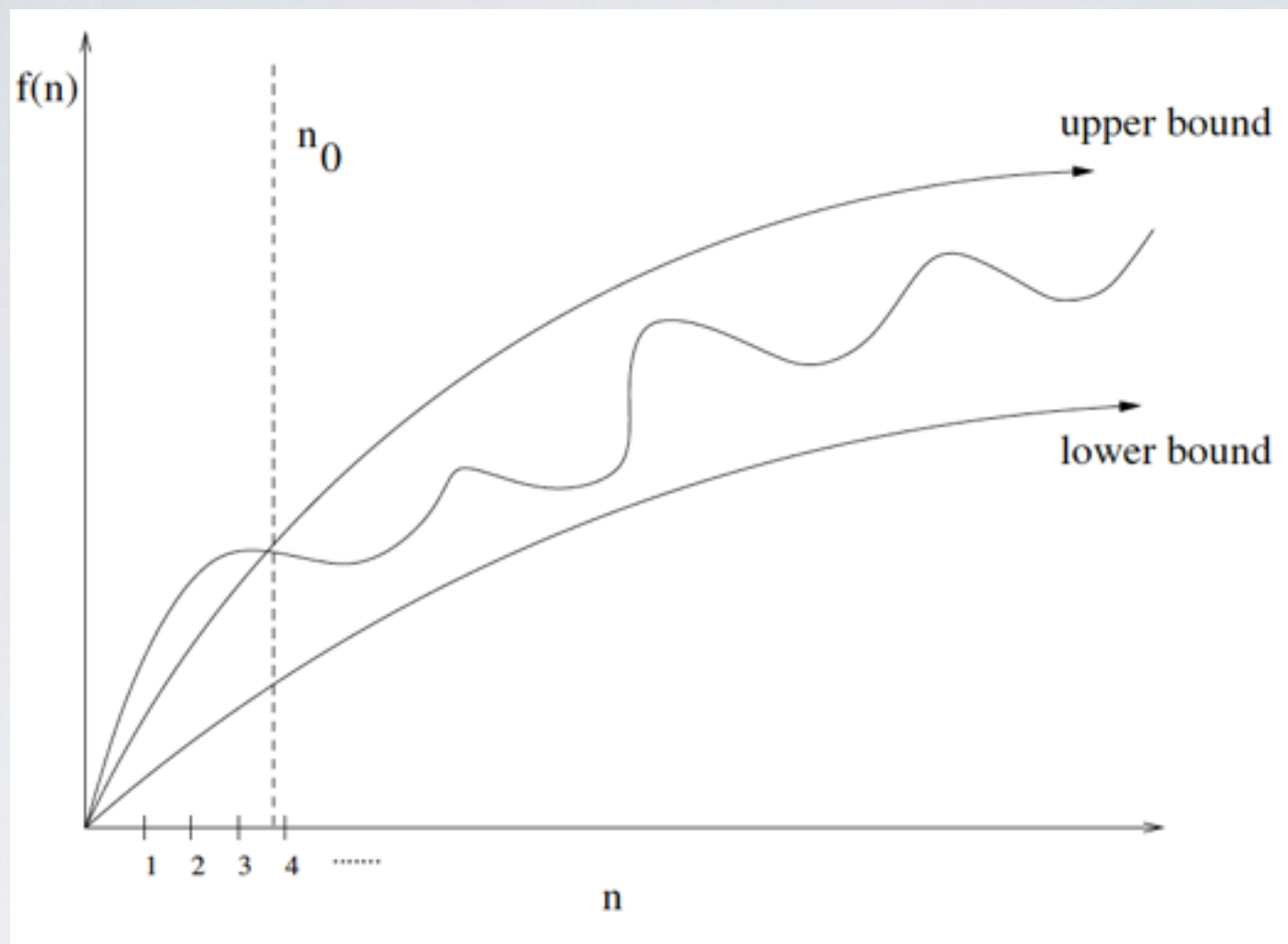
CAZ FAVORABIL, DEFAVORABIL, MEDIU STATISTIC

- modelul RAM aplicat pe TOATE instantele posibile (e.g. sortare)



O (BIG OH)

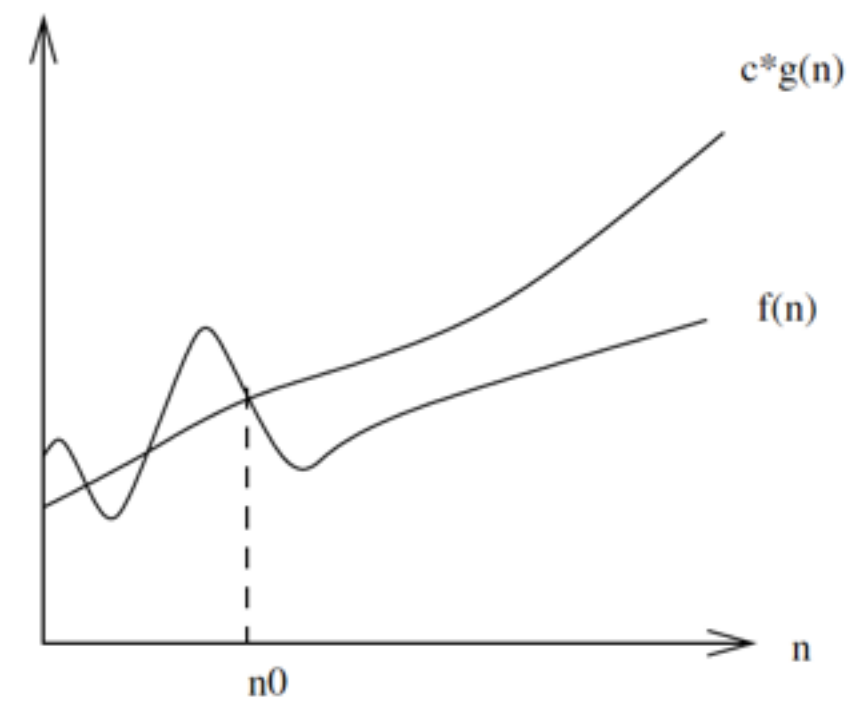
- extrem de greu de specificat funcțiile de complexitate exact!
- prea multe “spykes/bumps”
- prea multe detalii pentru a putea fi specificate exact (detalii neinteresante de cod)
- \Rightarrow limite superioare/inferioare



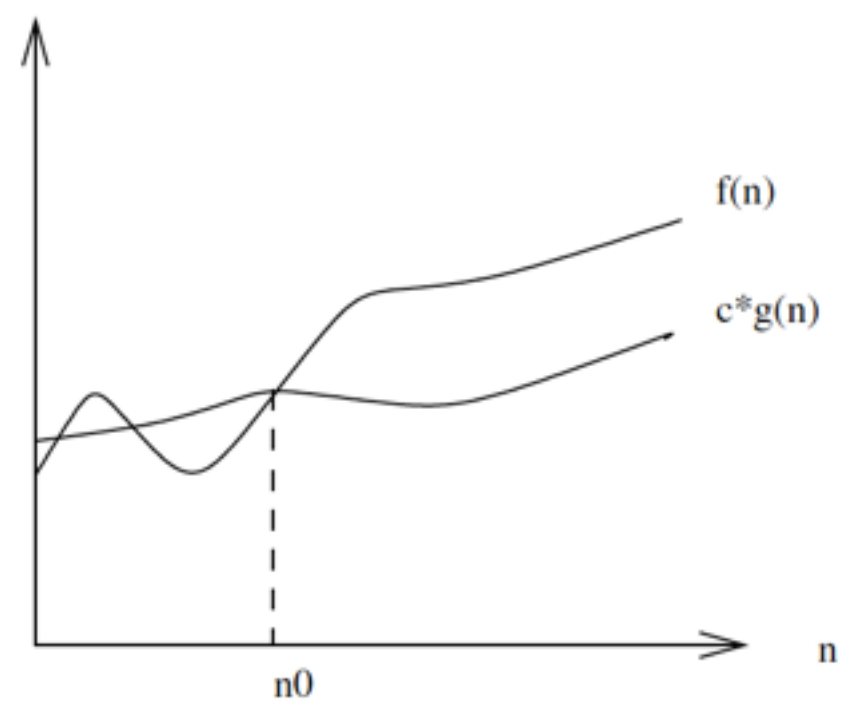
Upper bound: $f(n) = O(g(n)), \exists c, n_0 \text{ s.t. } f(n) < c \cdot g(n), \forall n > n_0$

Lower bound: $f(n) = \Omega(g(n)), \exists c, n_0 \text{ s.t. } f(n) \geq c \cdot g(n), \forall n > n_0$

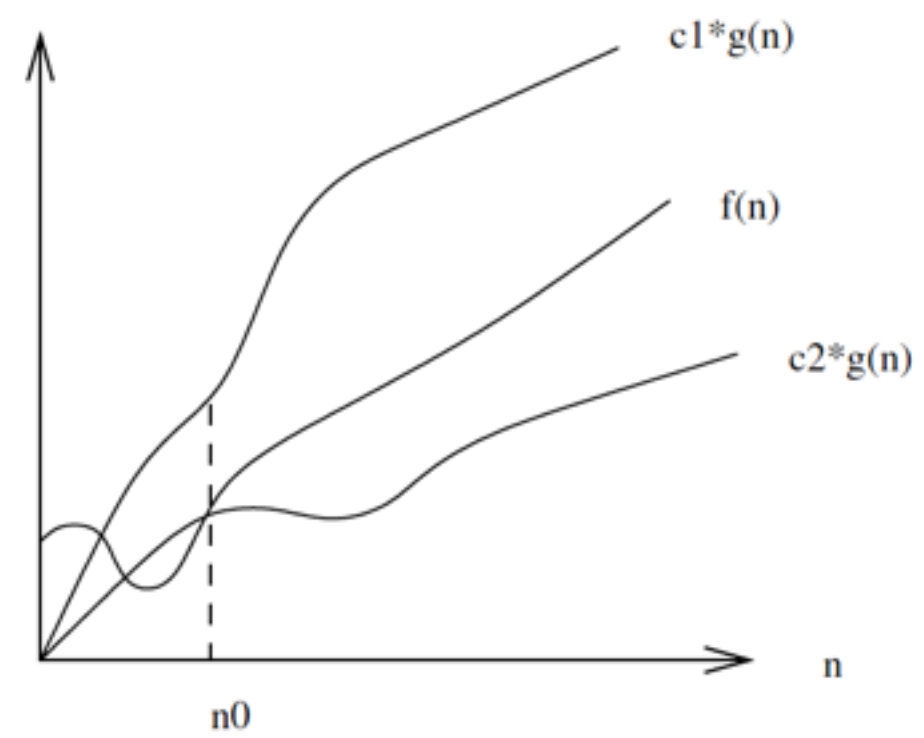
Tight bound: $f(n) = \Theta(g(n)), \exists c_1, c_2, n_0 \text{ s.t. } f(n) \geq c_1 \cdot g(n) \text{ and } f(n) < c_2 \cdot g(n), \forall n > n_0$



(a)



(b)



(c)

TIP DE DATA ABSTRACT (ADT) vs STRUCTURI DE DATE (DS)

- sinonime?
- ADT - model matematic pentru *tipuri de date*
 - semantica d.p.d.v. utilizator (valori posibile, operatii) -> **comportament!**
- DS - reprezentari concrete ale datelor
 - **implementare**

ADT vs DS

- *Lista* - o colectie *ordonata* de elemente, posibil duplicate (container)
 - *ordonata* nu inseamna neaparat *sortata* in acest context! (elementele apar unul dupa celalalt, acces secvential)
- O lista poate fi implementata fie folosind un *vector (array)*, fie o *lista simplu/dublu inlantuita*
- *particular* - *java.util.ArrayList*, *java.util.LinkedList*, sau o *biblioteca specifica C++* (din *Standard Template Library*).

LISTA (ADT)

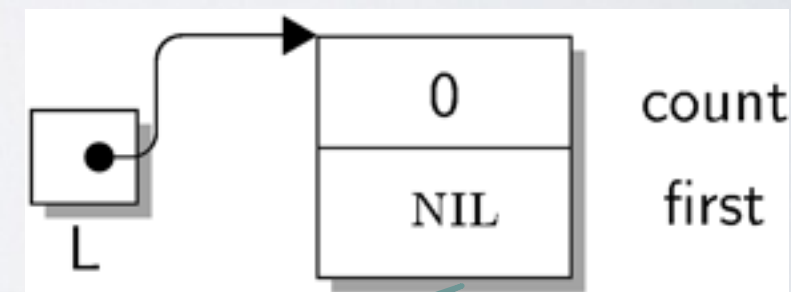
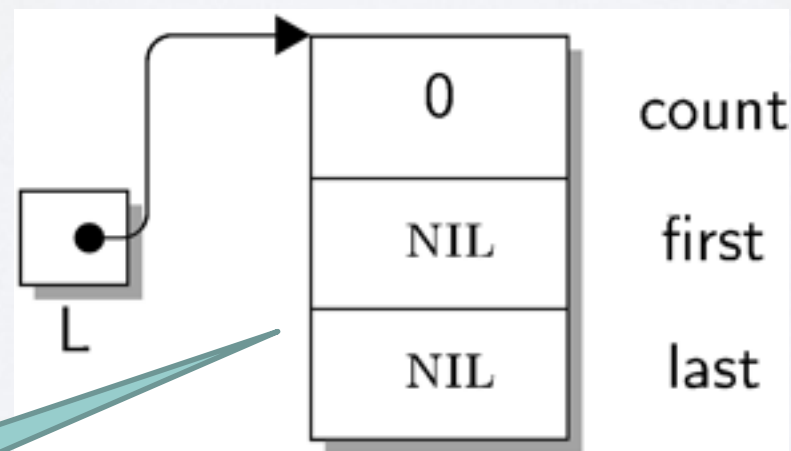
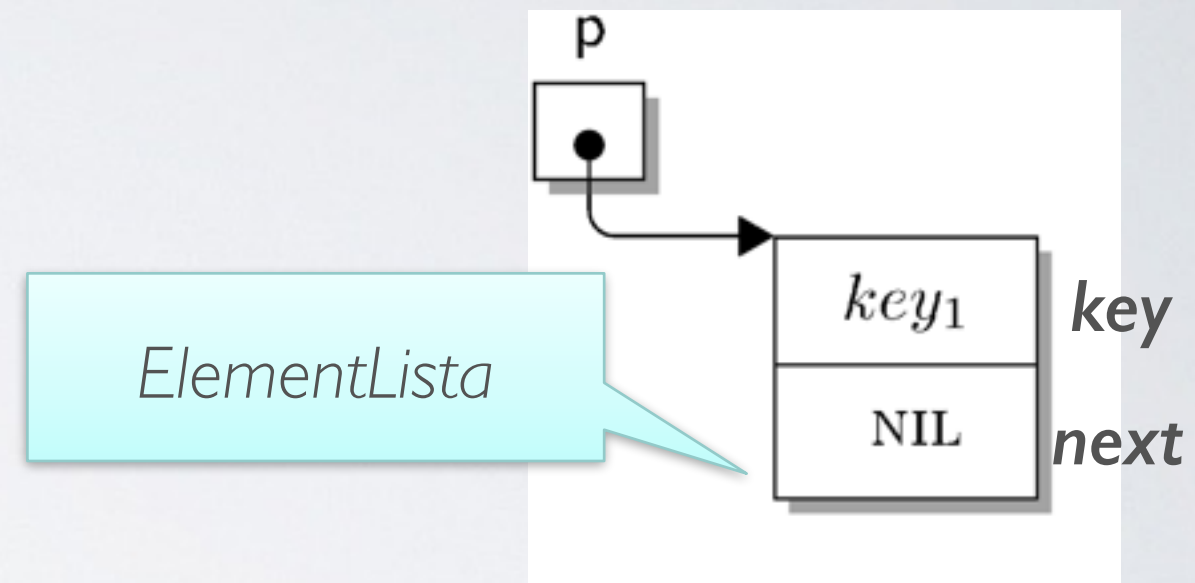
- O colectie de elemente (*ElementLista*), poate contine duplicate
- Operatii fundamentale:
 - insert(x): Adauga *ElementLista* x la inceputul listei (poate si la sfarsit, in ordine)
 - Intrare: *ElementLista*; lesire: nimic
 - delete(x): Sterge *ElementLista* x; eroare daca lista e goala
 - Input: pointer catre elementul de sters; lesire: nimic
 - search(k): cauta *ElementLista* care are cheia k
 - Intrare: cheia de cautat; lesire: pointer catre *ElementLista* sau nil daca nu s-a gasit
- Operatii aditionale:
 - size(): returneaza numarul de operatii din lista
 - Intrare: nimic; lesire: intreg
 - isEmpty(): returneaza valoare booleana care semnaleaza daca lista e goala
 - Intrare: nimic; lesire: boolean
 - first(): returneaza, fara a sterge, primul element din lista; eroare daca lista este goala (head())
 - Intrare: none; lesire: *ElementLista*
 - last(): returneaza, fara a sterge, ultimul element din lista; eroare daca lista este goala
 - Intrare: none; lesire: *ElementLista*
 - prev(x), next(x): returneaza *ElementLista* care precede/succede *ElementLista* x
 - tail(): returneaza restul listei, fara primul element
 - createEmpty()

LISTA SIMPLU INLANTUITA

- Inlantuire intr-o singura directie
- Elementele listei - structura separata (*ElementLista*)
- Structura *Lista* (capul listei):

- 2 (3) campuri:

- count
- first
- (last)

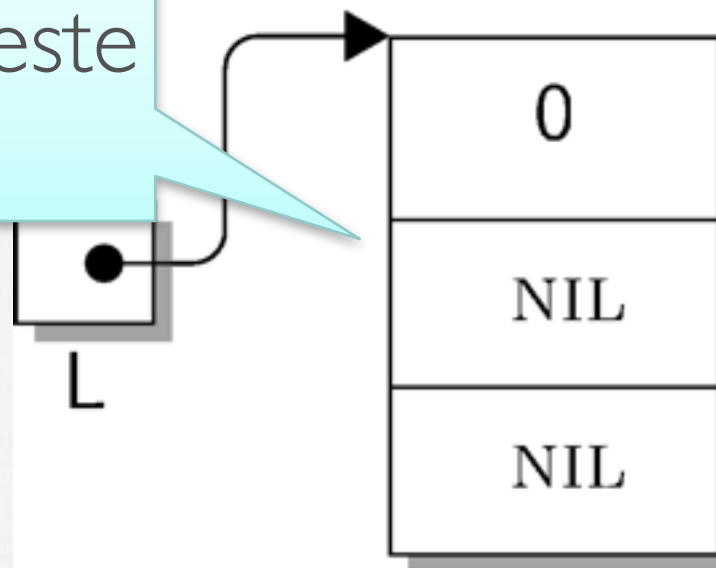


LISTA SIMPLU INLANTUITA

CREARE

- *createEmpty()*:
 - Creeaza capul listei
 - Seteaza *L* sa pointeze catre capul listei

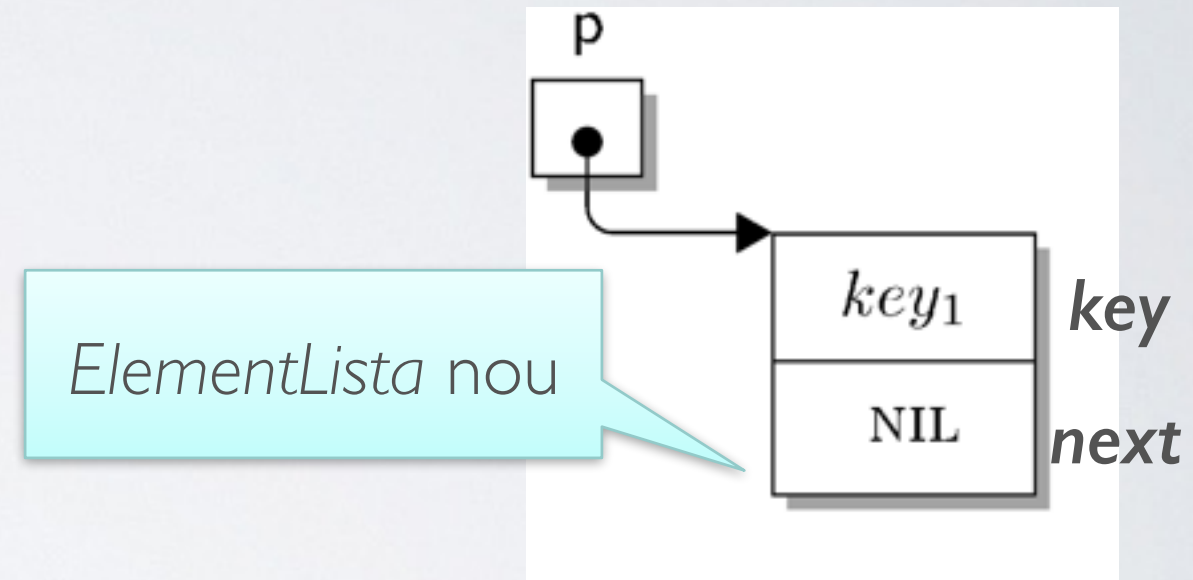
Capul listei. Lista este goala!



LISTA SIMPLU INLANTUITA

INSERT

- *Insert* - optiuni
 1. (intotdeauna) la inceput
 2. la ambele capete (inceput si sfarsit)
 3. la pozitia k
 4. ordonata
- Trebuie creat intai elementul de inserat !!!



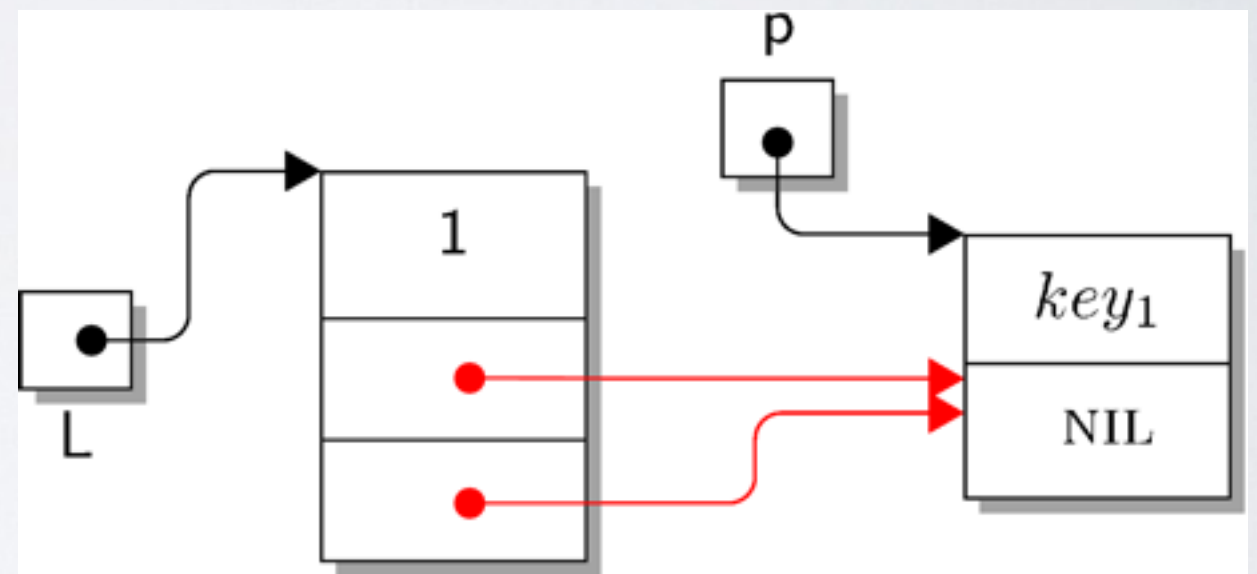
- Caz 1: adaugare la inceput, el va fi noul *head*
- Caz 2: adaugare la sfarsit (noul *last*?)
- Caz 3 & 4:
 - cautare loc
 - refacere legaturi

LISTA SIMPLU INLANTUITA

INSERT

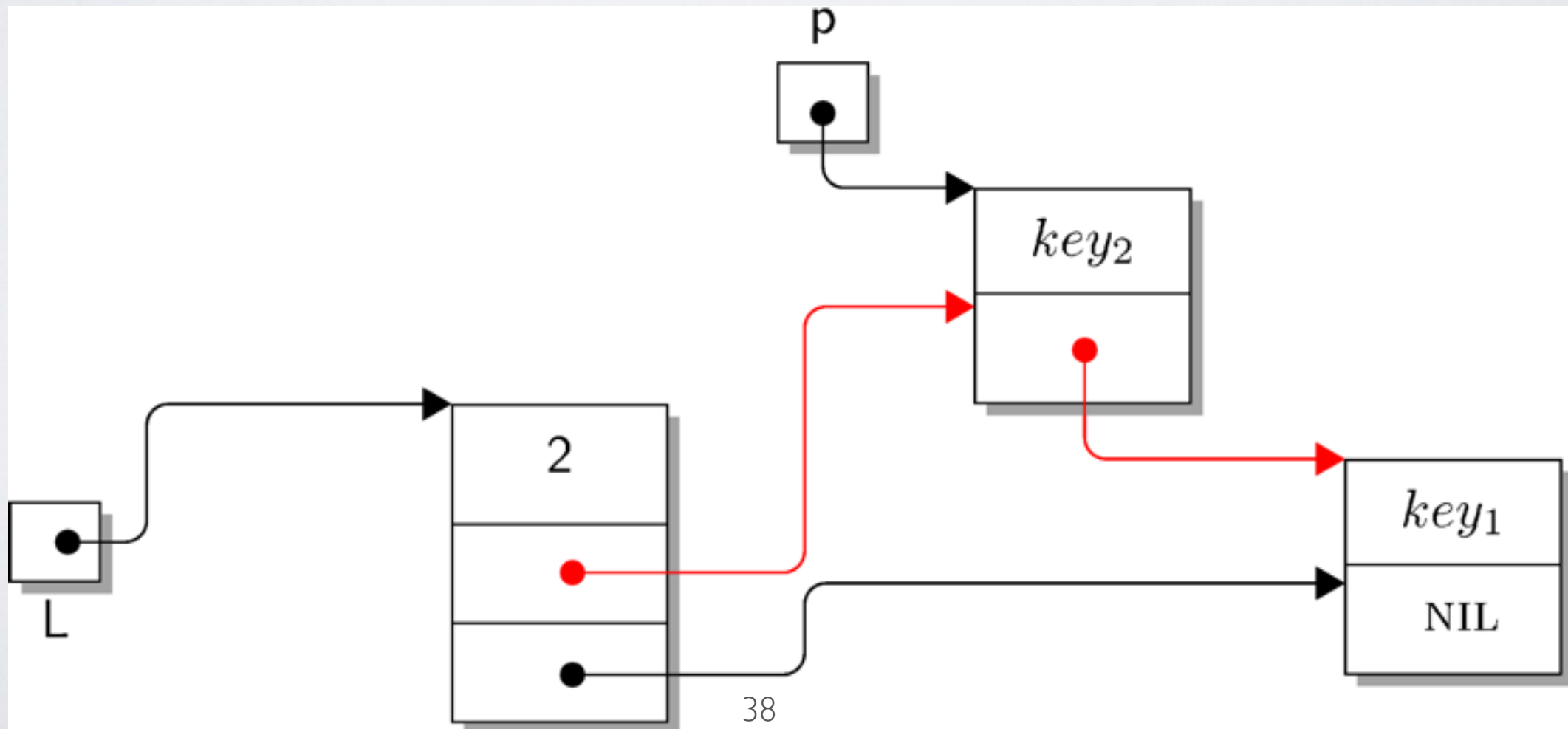
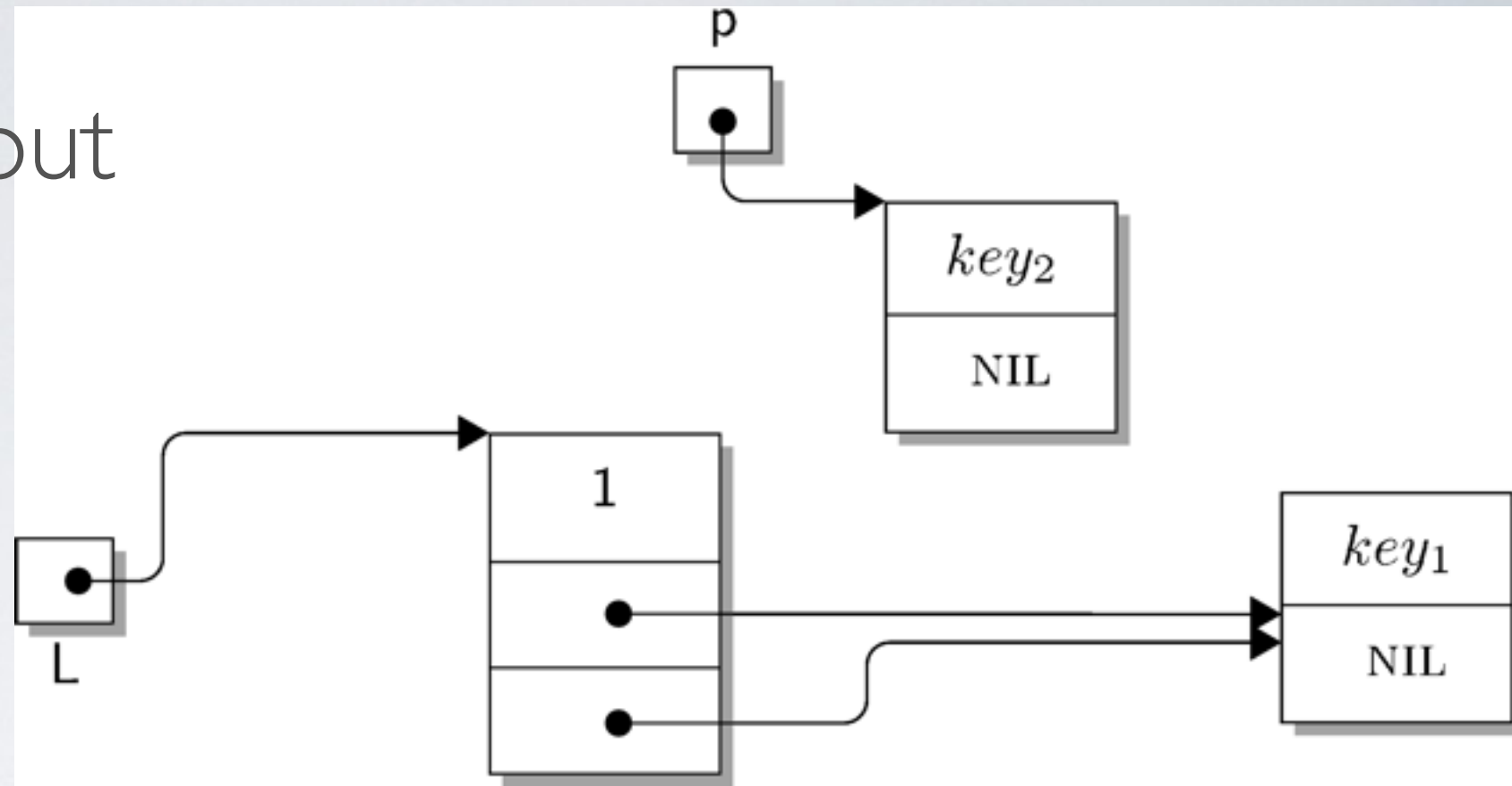
I. Adaugare la inceput

- Daca lista e goala
 - Similar adaugare la final (append)



I. Adaugare la inceput

- Lista nu e goala

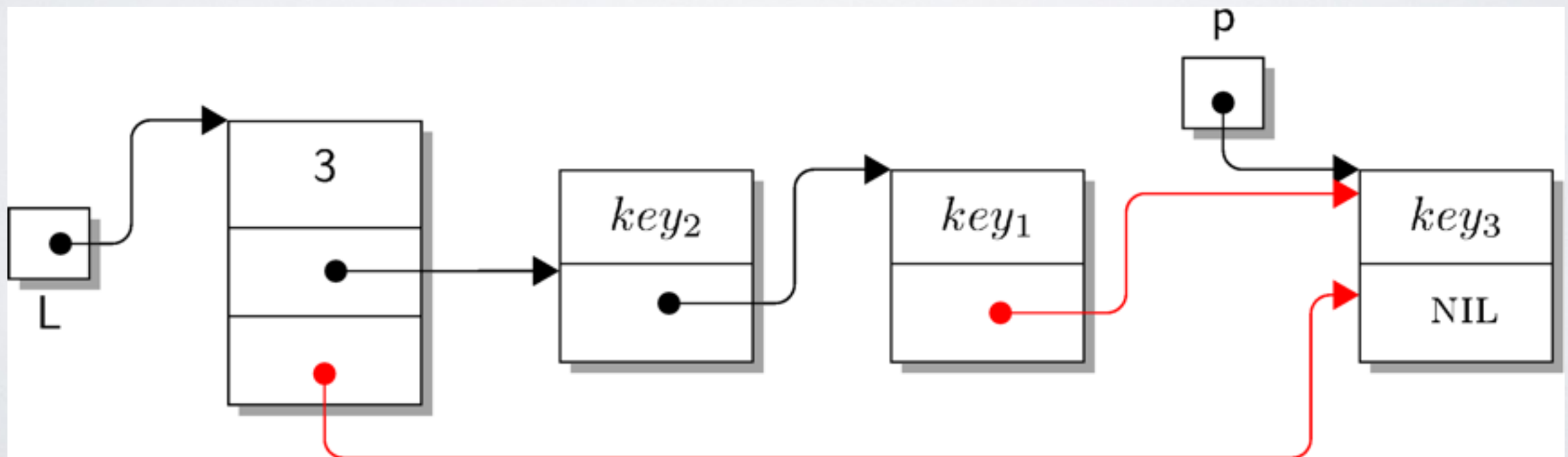


LISTA SIMPLU INLANTUITA

INSERT

2. Adaugare la final (*append*)

- Lista goala: la fel ca si la inserare la inceput
- Lista care contine elemente:



LISTA SIMPLU INLANTUITA

INSERT

3. Inserare in lista *ordonata* sau la pozitia k :

- Lista goala: ca si mai inainte
- Lista cu elemente:
 - Inainte de primul nod (i.e. inserare la inceput)
 - Dupa ultimul nod (i.e. append)
 - **In interiorul listei**
 - trebuie traversata lista, si stabiliti doi pointeri:
 - nodul curent (va deveni *next* pt nodul inserat)
 - nodul anterior (al carui pointer *next* va referi nodul nou inserat)
- Exerciitiu!!!!

EXEMPLU COD: *INSERT FIRST*

```
void insert_first(list **first, item_type x)
{
    list *p; /* temporary pointer */
    p = malloc( sizeof(list) );
    p->item = x;
    p->next = *first;
    *first = p;
}
```

SEARCH

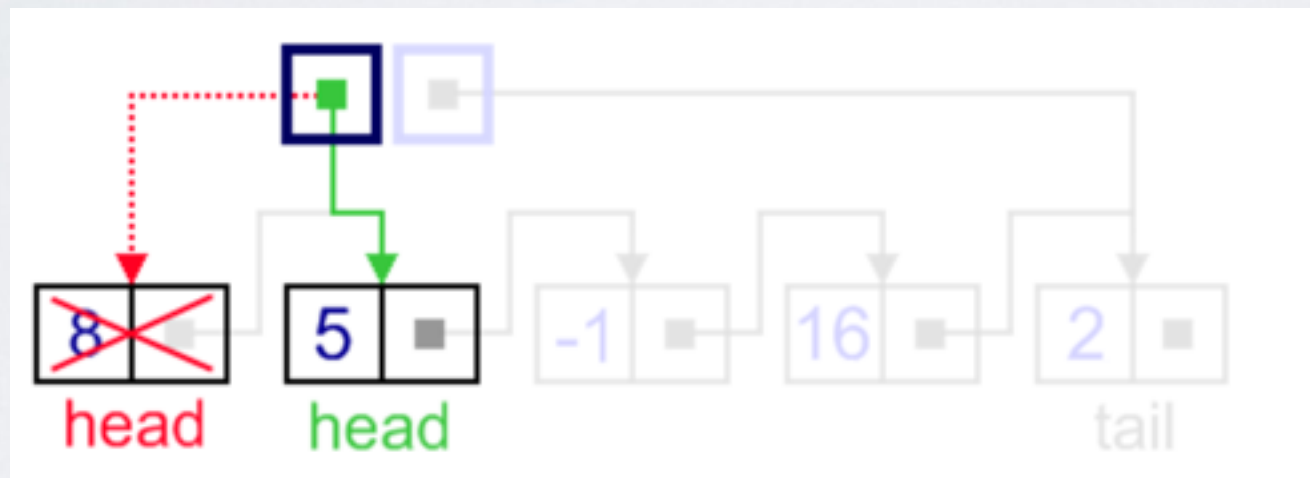
```
list *search_list(list *l, item_type x){
    if (l == NULL) return(NULL);
    if (l->item == x)
        return(l);
    else
        return( search_list(l->next, x) );
}
```

LISTA SIMPLU INLANTUITA

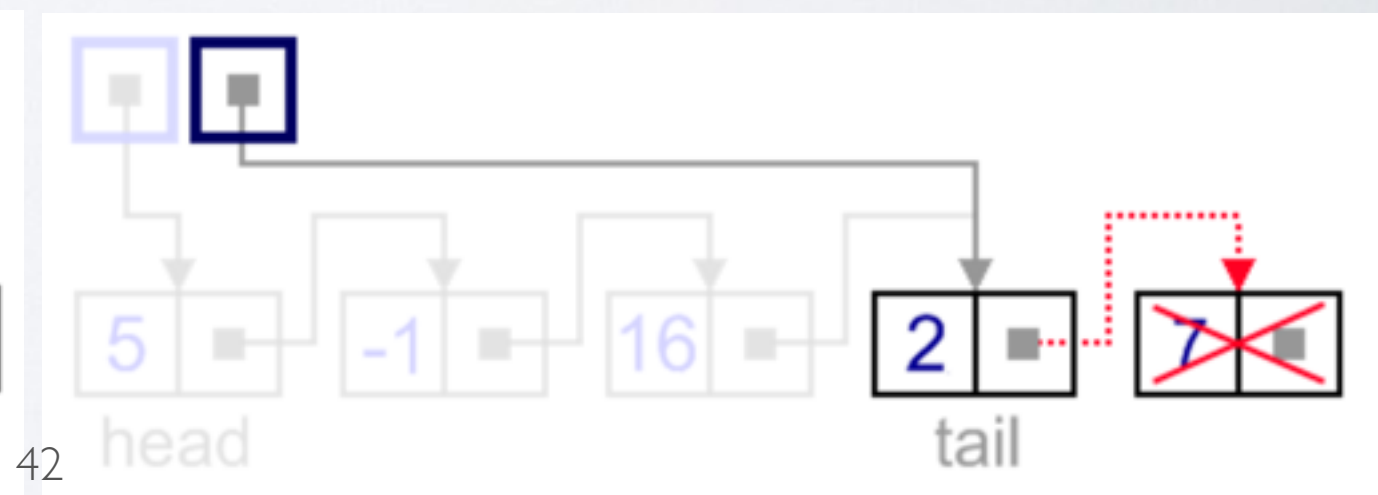
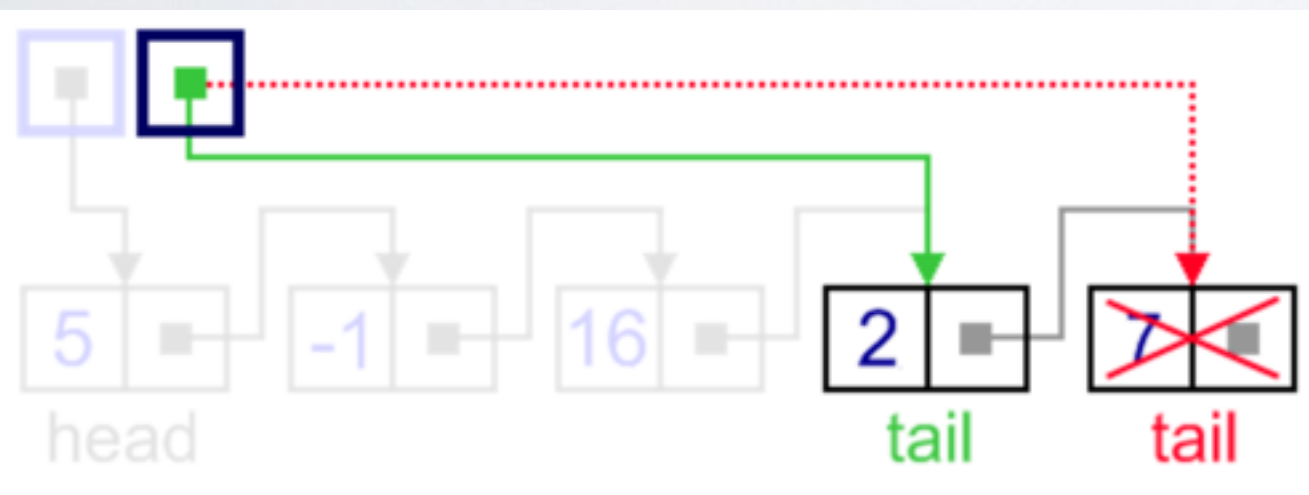
DELETE

- *Delete* - cazuri speciale

1. primul element



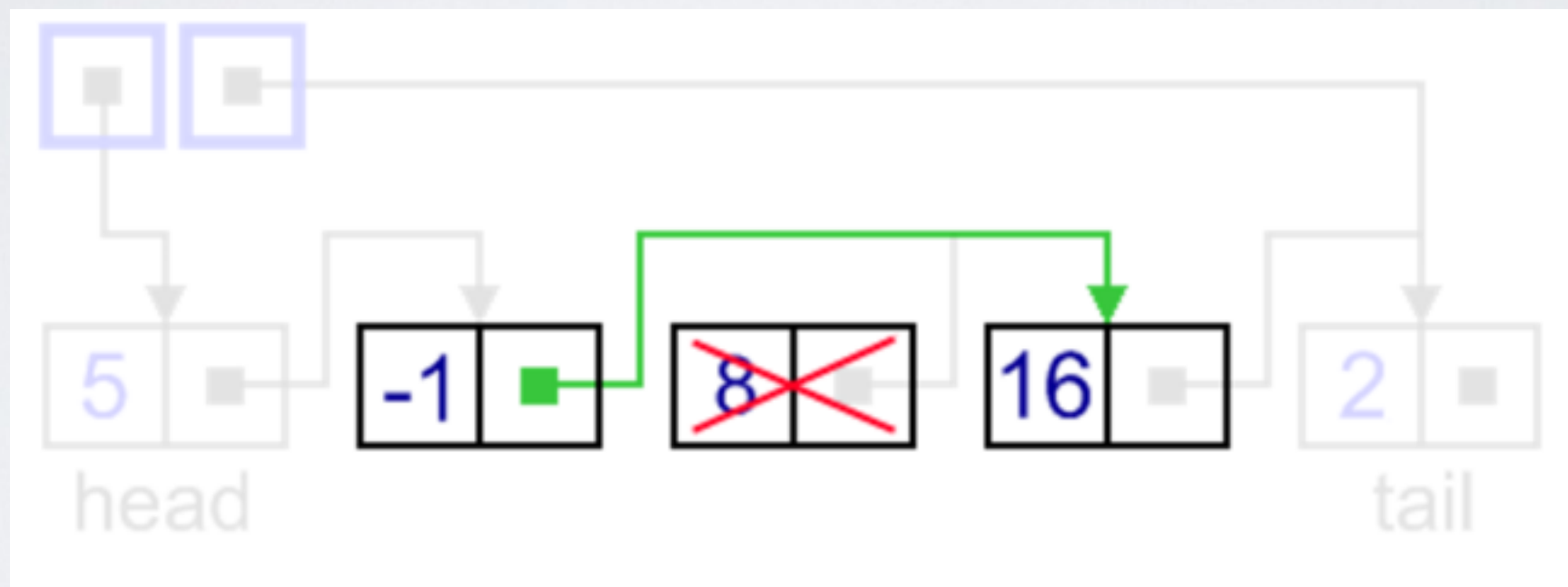
2. ultimul element



LISTA SIMPLU INLANTUITA

DELETE

- *Delete* - cazul general



```

list *predecessor_list(list *l, item_type x){
    if ((l == NULL) || (l->next == NULL)) {
        printf("Error: predecessor sought on null list.\n");
        return(NULL);
    }
    if ((l->next)->item == x)
        return(l);
    else
        return(predecessor_list(l->next, x));
}

```

DELETE

```

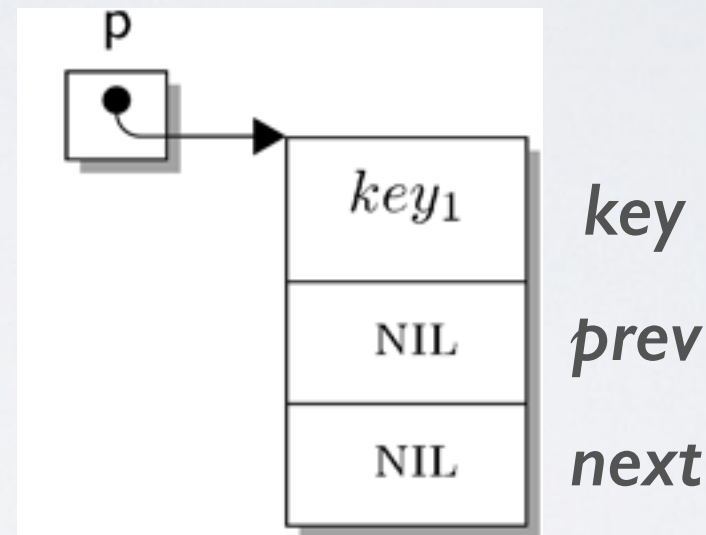
delete_list(list **l, item_type x){
    list *p; /* item pointer */
    list *pred; /* predecessor pointer */
    p = search_list(*l,x);
    if (p != NULL) {
        pred = predecessor_list(*l,x);
        if (pred == NULL) /* update head */
            *l = p->next;
        else
            pred->next = p->next;
        free(p); /* free memory used by node */
    }
}

```

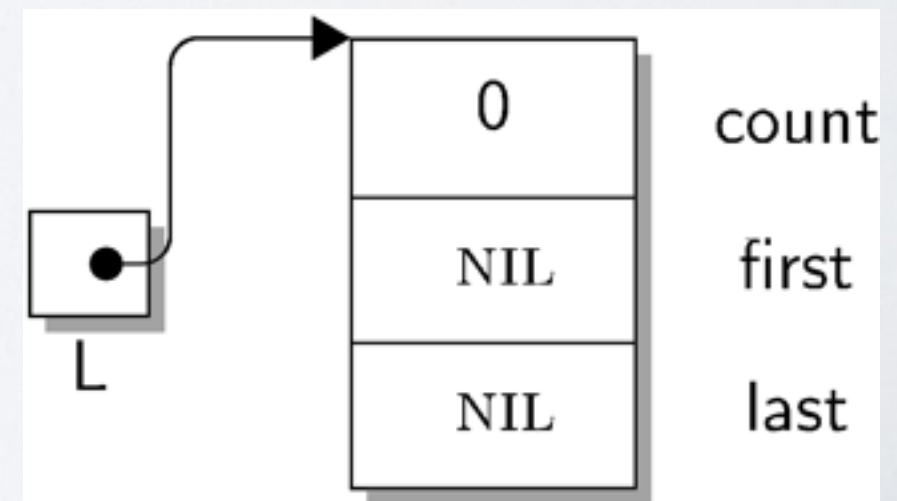
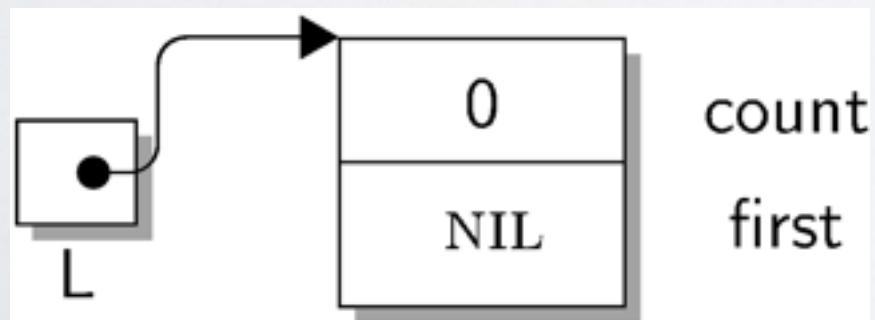

LISTA DUBLU INLANTUITA

- Inlantuire bi-directionala

- *ElementLista*:

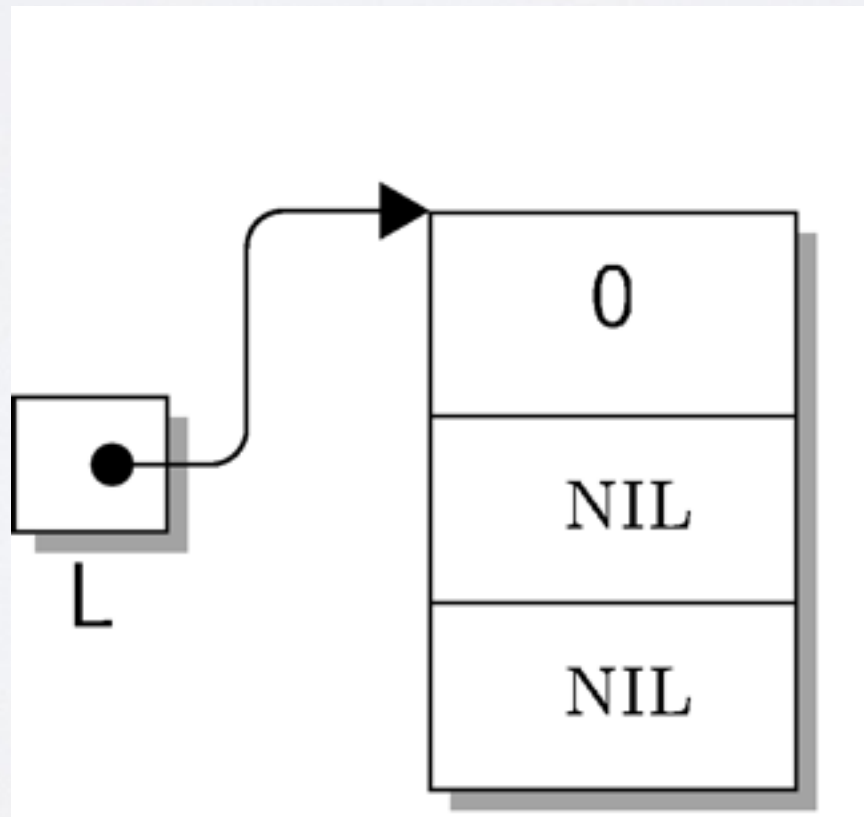


- Capul listei (*Lista*):



LISTA DUBLU INLANTUITA

- *createEmpty()*:
 - Creeaza capul listei
 - Seteaza *L* sa pointeze catre capul listei



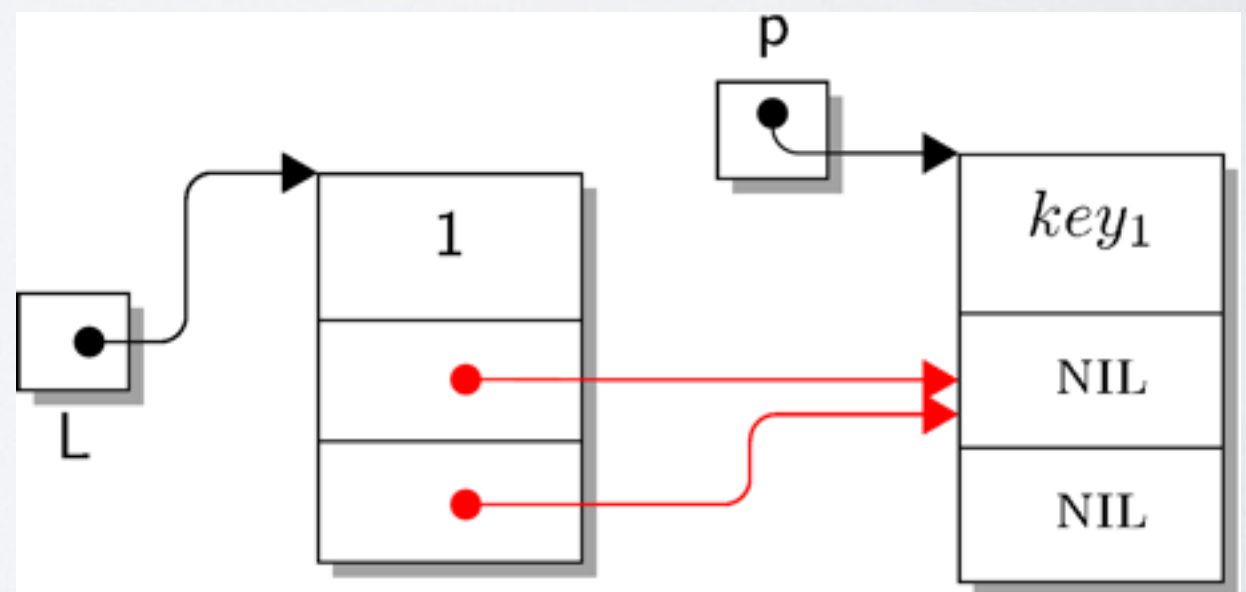
LISTA DUBLU INLANTUITA

INSERT

Ca si la liste simplu inlantuite, initial trebuie creat nodul de inserat (ElementLista) !!

I. Inserare la inceput:

- Lista goala
 - La fel si la *append*

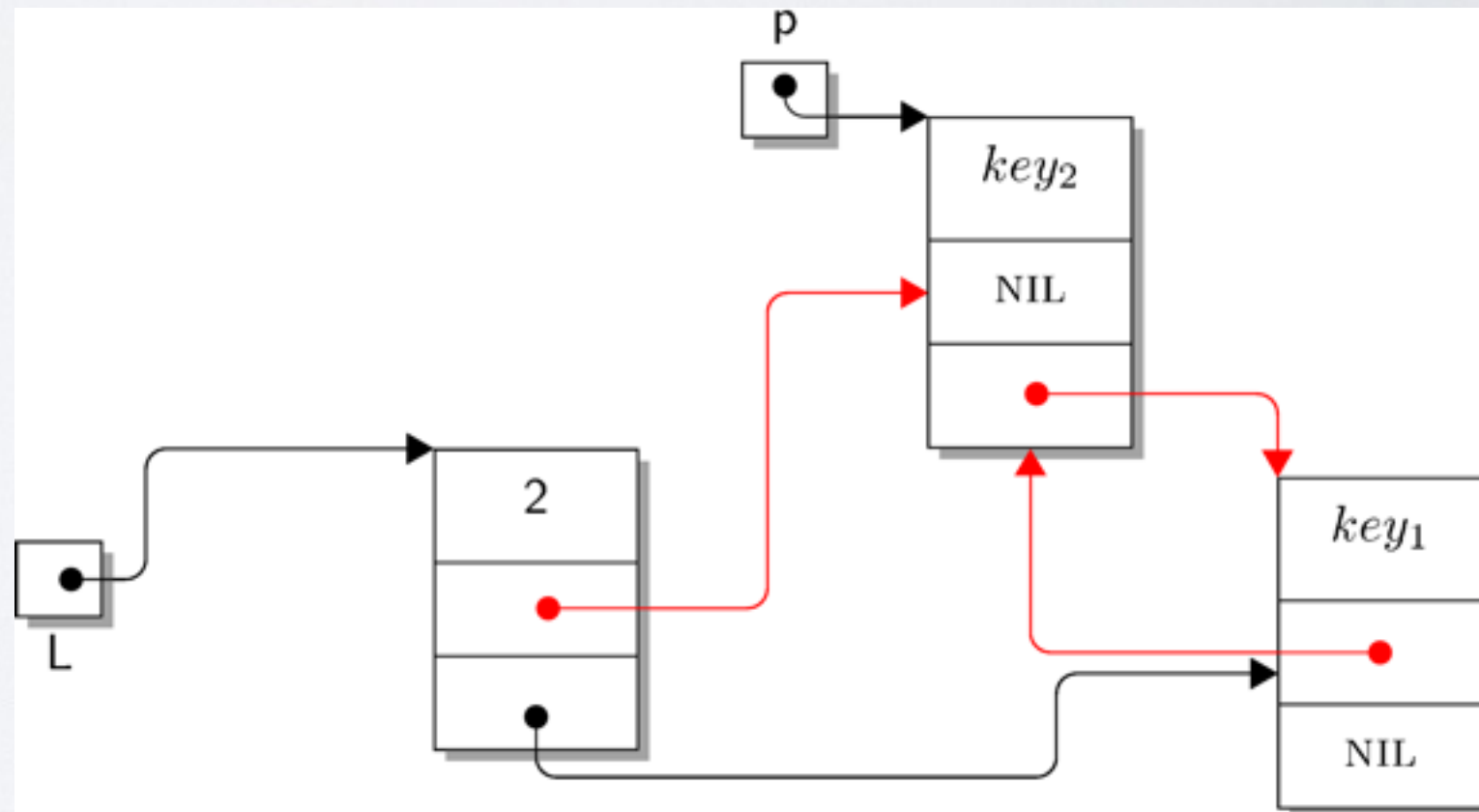
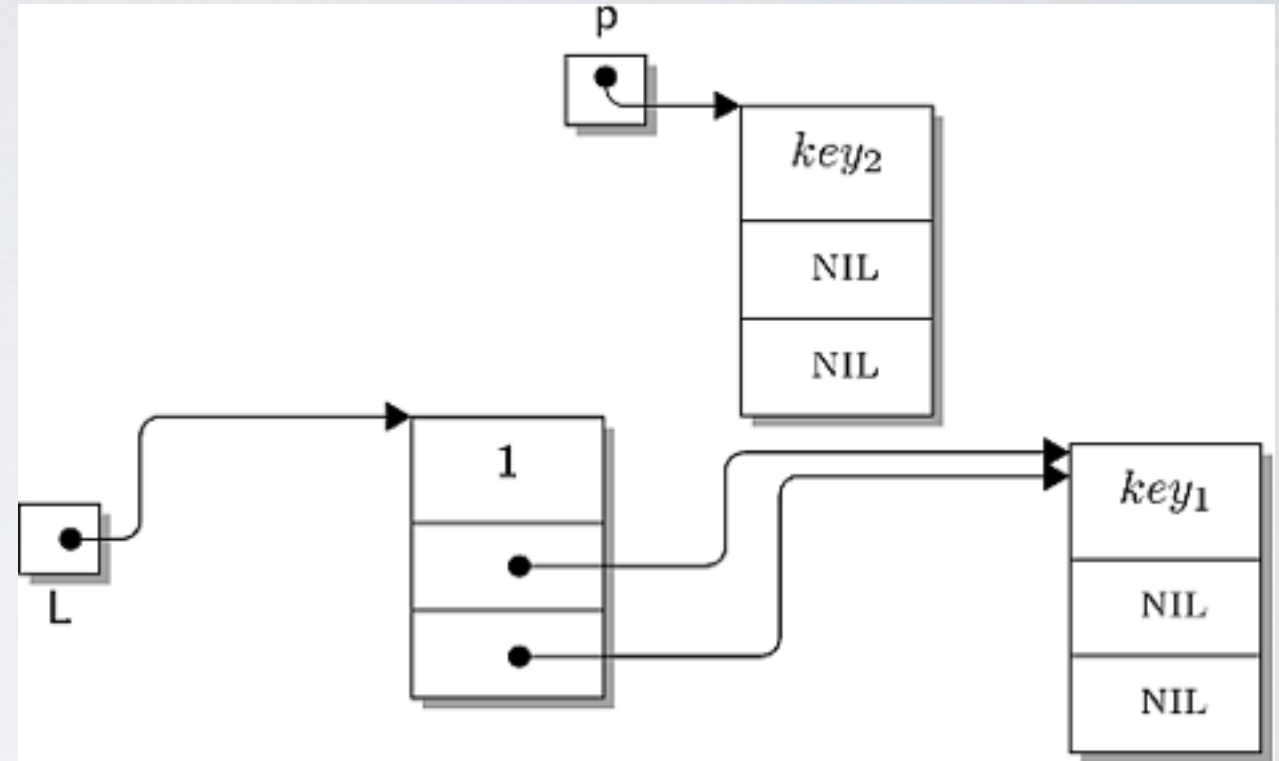


LISTA DUBLU INLANTUITA

INSERT

1. Inserare la inceput:

- Lista nu e goala

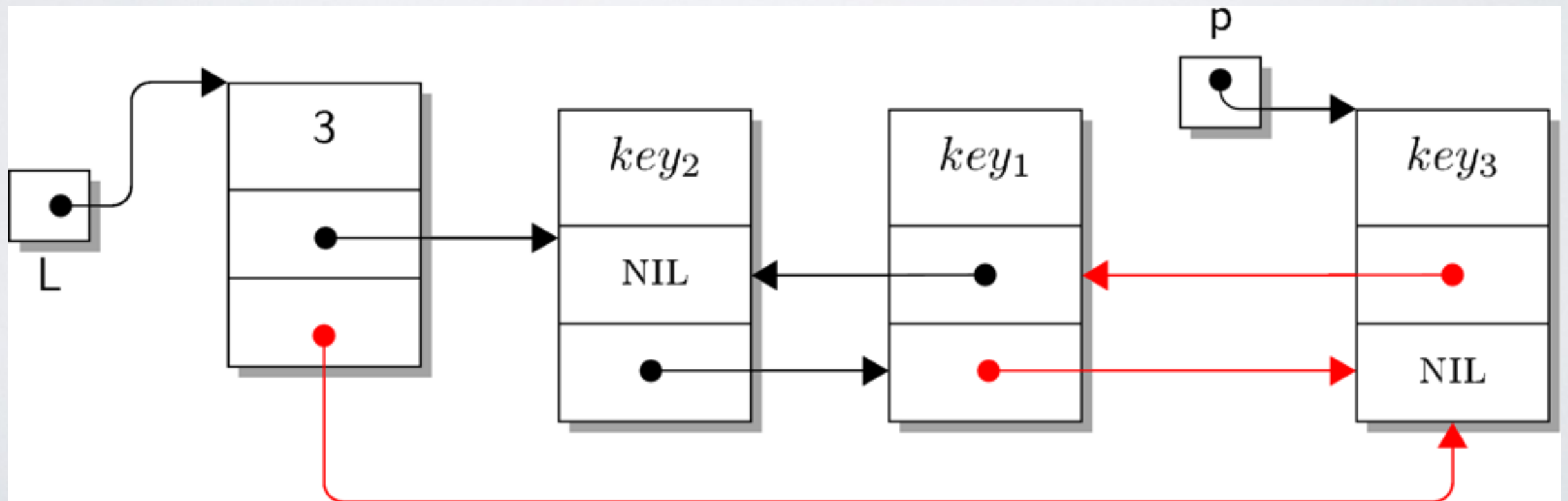


LISTA DUBLU INLANTUITA

INSERT

2. Inserare la final (append):

- Lista goala - ca si la insertFirst
- Lista nu e goala



LISTA DUBLU INLANTUITA

INSERT

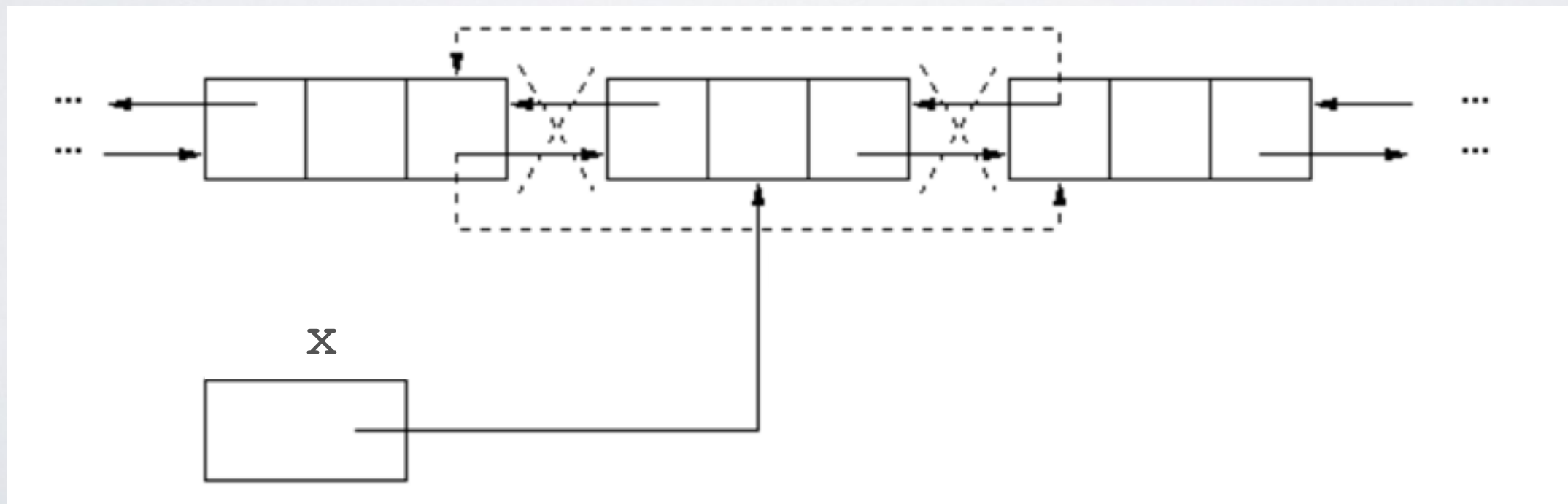
3. Inserare in lista ordonata, sau a pozitia k

- Lista goala: ca si mai inainte
- Lista cu elemente:
 - Inainte de primul nod (i.e. inserare la inceput)
 - Dupa ultimul nod (i.e. append)
 - **In interiorul listei**
 - trebuie traversata lista, si stabilit un pointer (*de ce nu 2?*):
 - nodul curent (va deveni *next* pt nodul inserat)
 - nodul inserat va deveni *prev* pentru nodul curent
- **Exercitiu!!!!**

LISTA DUBLU INLANTUITA DELETE

```
delete(L, x)
  if prev[x] != NIL then
    next[prev[x]] = next[x]
  else
    head[L] = next[x]
  if next[x] != NIL then
    prev[next[x]] = prev[x]
```

*Obs: lista are doar first (head),
nu si last*



LISTE INLANTUITE CU SANTINELA

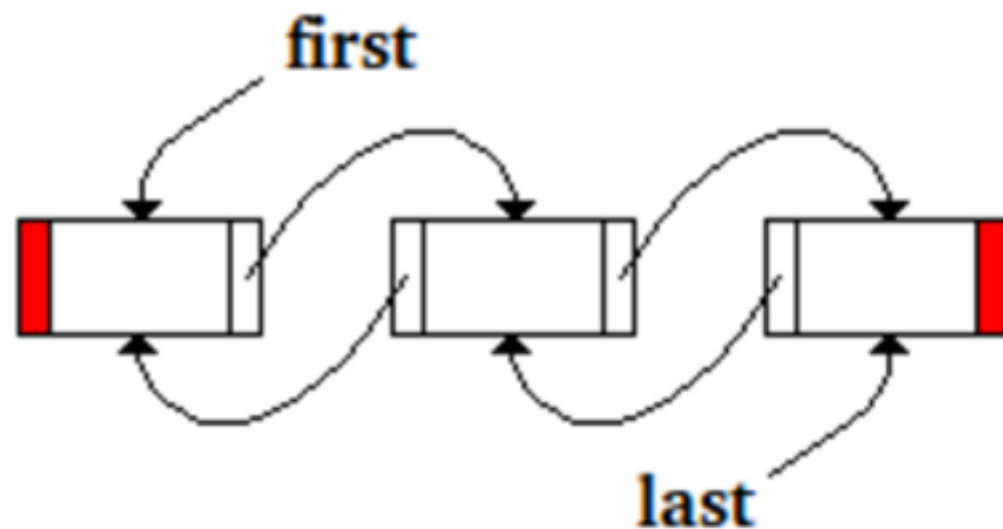
- ○ **santinela** este un element de lista *dummy* care ne permite sa eliminam cazurile speciale (NIL).
 - nu contine informatie
 - contine toate campurile celorlalte elemente de lista

LISTA DUBLU INLANTUITA: INSERT, DELETE CU SANTINELA

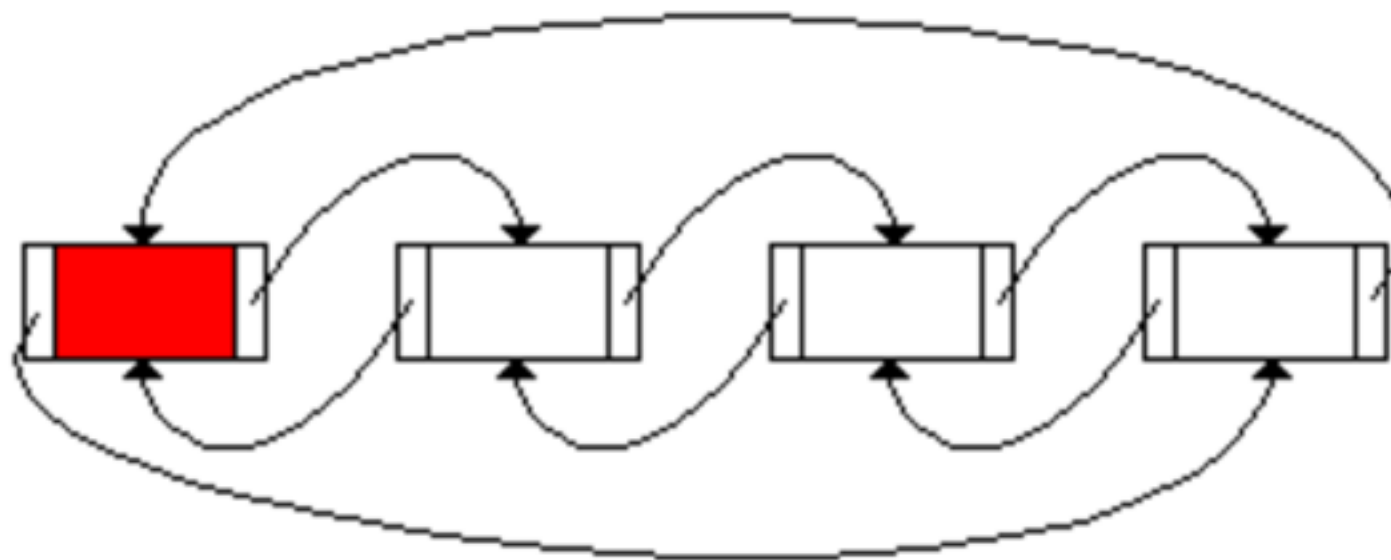
```
//insert nod n inaintea lui x
n->next = x;
n->prev = x ? x->prev : last;
if (n->prev) n->prev->next = n;
    else first = n;
if (n->next) n->next->prev = n;
    else last = n;
```

```
delete(L, x)
    if prev[x] != NIL then
        next[prev[x]] = next[x]
    else
        head[L] = next[x]
    if next[x] != NIL then
        prev[next[x]] = prev[x]
```

LISTA DUBLU INLANTUITA - FARA/CU SANTINELA



Using **NULL** to
mark end of list



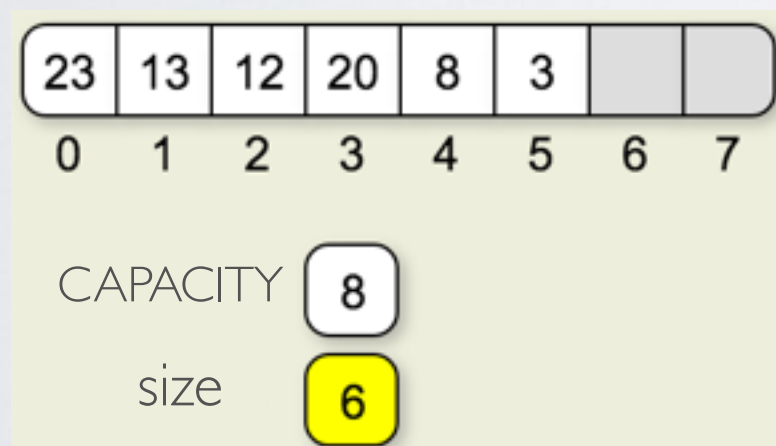
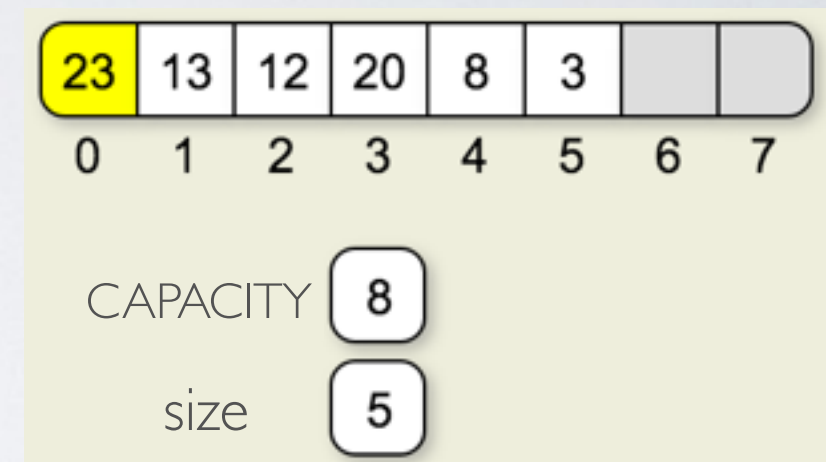
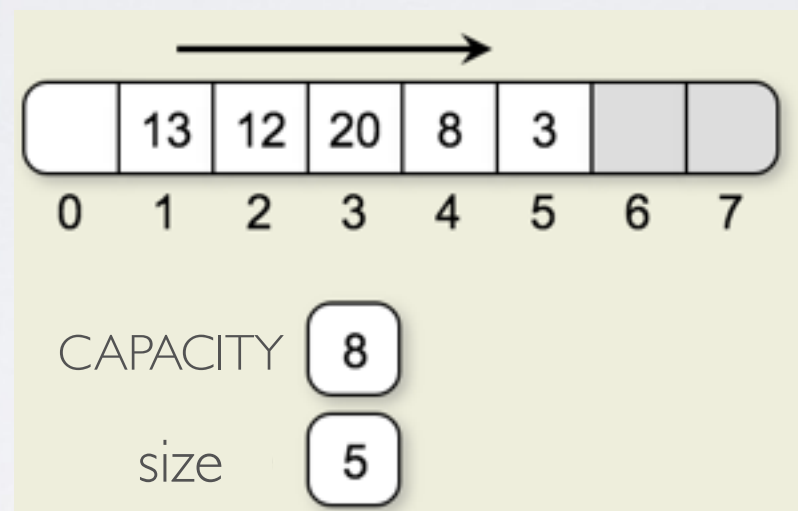
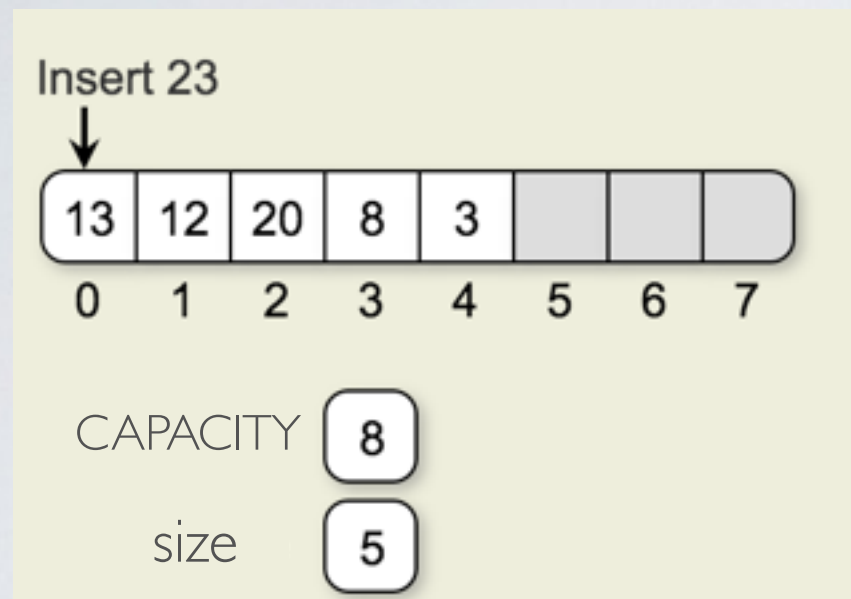
Using a special
dummy node

LISTA - IMPLEMENTARE VECTOR

- Structura:
 - `vector: int myList[CAPACITY]`
 - `dimensiune: int size`
- Operatii:
 - `search(k)`
 - `insertFirst(x)`, `insertLast(x)`, `insertK(x, k)`, `insertOrd(x)`
 - `delete(x)`
 - `size()`, `capacity()`,

LISTA - IMPLEMENTARE

VECTOR - **INSERT**

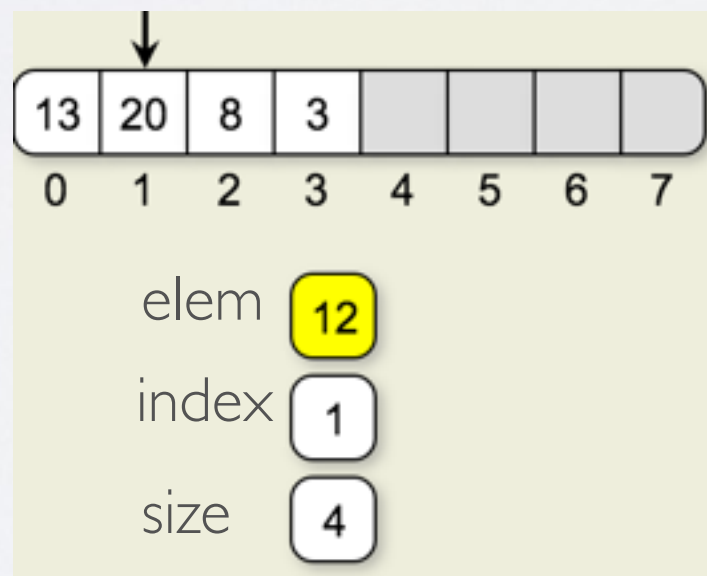
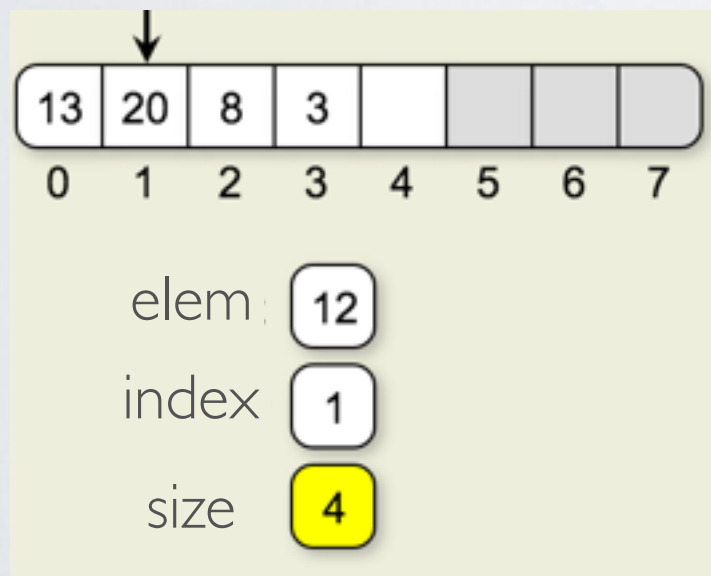
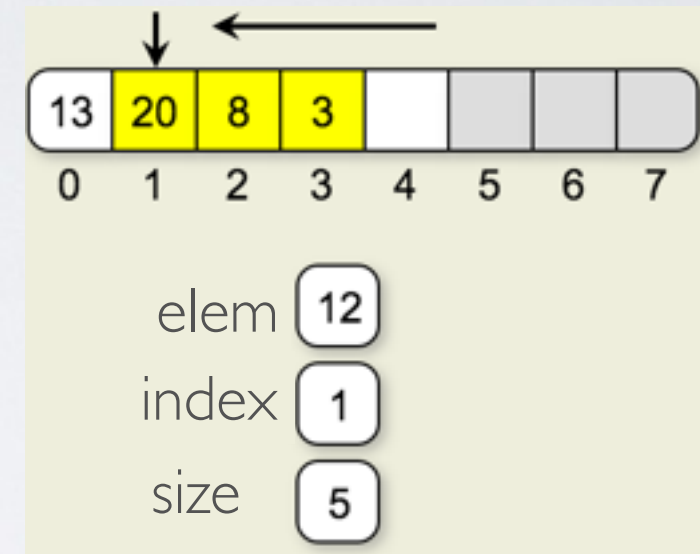
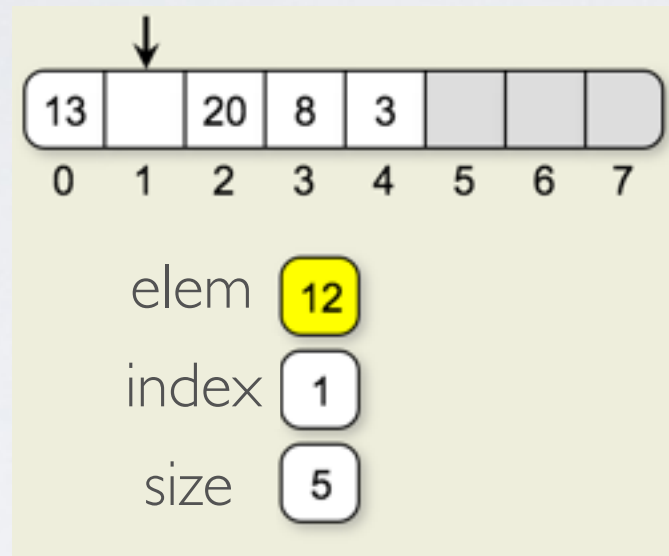
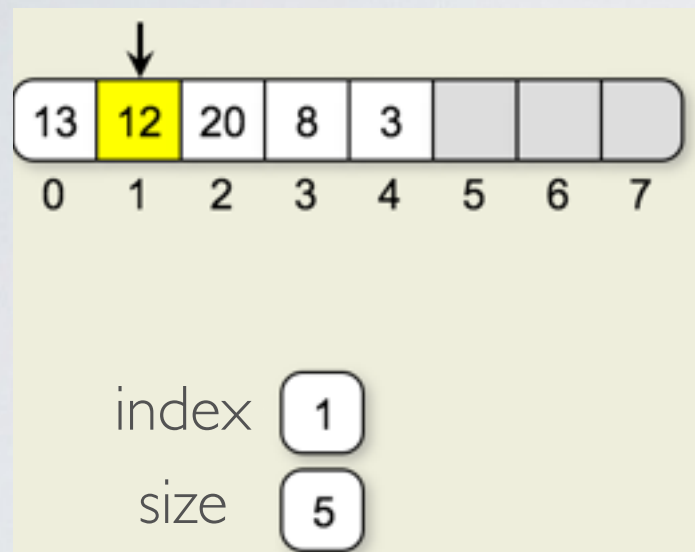


$insertK(x, pos)$ - mutata toate elementele aflate
dupa pozitia de inserare catre dreapta

- pus elementul x pe pozitia pos
- $size++$

??? Ce se intampla daca $size = CAPACITY$

LISTA - IMPLEMENTARE VECTOR - DELETE



VECTOR VS LISTA INLANTUITA

	VECTOR	LISTA INLANTUITA
+	<ul style="list-style-type: none"> timp de acces constant, dupa index (acces direct) eficienta memorie (nu exista legaturi, alte info aditionale) localitatea memoriei (memoria cache) 	<ul style="list-style-type: none"> <i>no overflow</i> (decat daca memoria e plina) inserare si stergere eficienta cu inregistrari mari, mutarea de pointeri este mai eficienta decat mutarea intregii inregistrari
-	<ul style="list-style-type: none"> <i>overflow</i> - dimensiune fixa (vectori <i>dinamici</i>, analiza amortizata) 	<ul style="list-style-type: none"> memorie aditionala pt. stocarea pointerilor accesul aleator nu e eficient accesarea pe baza de pointeri inlantuiti nu exploateaza principiile memoriei cache

STIVA

- o colectie de elemente cu politica de acces (inserare/stergere) de tip *LIFO* (*Last-In-First-Out*)
 - elementele sunt inserate astfel incat, la orice moment, doar cel mai recent element inserat poate fi eliminat
- Inserare - la **inceptut** - “push” *onto the stack*
- Stergere - de la **inceptut** - “pop” *off the stack*

STIVA (ADT)

- Operatii fundamentale:
 - push(x): insereaza elementul *x* in varful stivei (en. *top, stack pointer*)
 - Intrare: ElementStiva; lesire: nimic
 - pop(): Sterge elementul aflat in varful stivei, si il returneaza; daca stiva e goala, mesaj de eroare
 - Intrare: nimic; lesire: ElementStiva
- Operatii aditionale (nu sunt fundamentale, dar utile):
 - size(): returneaza numarul de elemente din stiva
 - Intrare: nimic; lesire: intreg
 - isEmpty(): semnaleaza daca stiva este goala
 - Intrare: nimic; lesire: boolean
 - top(): returneaza elementul din varful stivei, fara a-l sterge; daca stiva este goala, mesaj de eroare.
 - Intrare: nimic; lesire: ElementStiva

STIVA

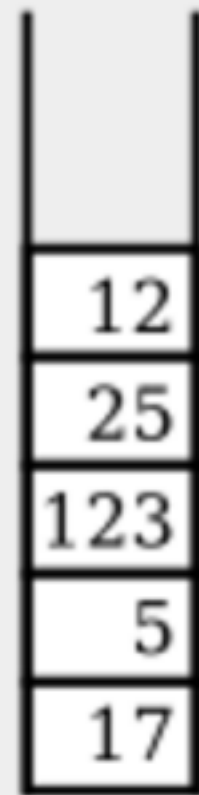
PUSH(S, x)

- 1 $top[S] \leftarrow top[S] + 1$
- 2 $S[top[S]] \leftarrow x$

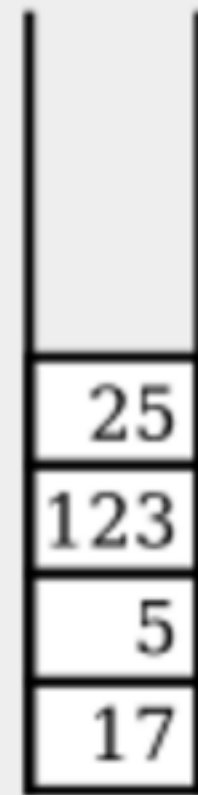
POP(S)

- 1 **if** STACK-EMPTY(S)
- 2 **then error** “underflow”
- 3 **else** $top[S] \leftarrow top[S] - 1$
- 4 **return** $S[top[S] + 1]$

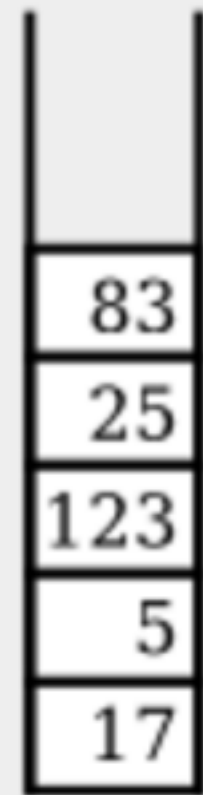
STIVA - Implementare cu vector



Original stack.



After pop().



After push(83).

STIVA - Implementare cu lista simplu inlantuita:

- first
- push(x) -> insertFirst(x)
- pop() -> delete head element

STIVA - RELEVANTA

- Stiva apare in programe
 - Mecanism cheie in apelul/iesirea functii/proceduri
 - Recursivitatea - stiva
 - Apel: *push stack frame*
 - Iesire: *pop stack frame*
- *Stack frame*
 - argumente functie
 - variabile locale
 - adresa de iesire

COADA

- o colectie de elemente cu politica de acces (inserare/stergere) de tip *FIFO* (*First-In-First-Out*)
- elementele sunt inserate astfel incat, la orice moment, elementul care a fost inserat la cel mai indepartat moment poate fi eliminat (cel mai *vechi*)
- Inserare: la ***sfarsit*** - “*enqueue*”
- Stergere: de la ***inceput*** - “*dequeue*”

COADA (ADT)

- Operatii fundamentale:
 - enqueue(o): Insereaza elementul o la sfarsitul cozii
 - Intrare: ElementCoada; lesire: nimic
 - dequeue(): Sterge elementul aflat la inceputul cozii si il returneaza; eroare daca nu exista elemente in coada
 - Intrare: nimic; lesire: ElementCoada
- Operatii aditionale (nu sunt fundamentale, dar utile):
 - size(): returneaza numarul de elemente din coada
 - Intrare: nimic; lesire: intreg
 - isEmpty(): semnaleaza daca coada este goala
 - Intrare: nimic; lesire: boolean
 - front(): returneaza elementul din varful cozii, fara a-l sterge; daca coada este goala, mesaj de eroare.
 - Intrare: nimic; lesire: ElementCoada

Coada circulara implementata ca vector

ENQUEUE(Q, x)

```
1   $Q[rear(Q)] \leftarrow x$ 
2  if  $rear[Q] = length[Q]$ 
3      then  $rear[Q] \leftarrow 1$ 
4      else  $rear[Q] \leftarrow rear[Q] + 1$ 
```

DEQUEUE(Q, x)

```
1   $x \leftarrow Q[front(Q)]$ 
2  if  $front[Q] = length[Q]$ 
3      then  $front[Q] \leftarrow 1$ 
4      else  $front[Q] \leftarrow front[Q] + 1$ 
5  return  $x$ 
```

1	10	
2	12	$\leftarrow rear[Q]$
3	10	
4	2	
5	7	
6	22	$\leftarrow front[Q]$
7	15	
8	33	

Coada implementata ca lista
simplu inlantuita:

- first, last
- enqueue(x) \rightarrow InsertLast
- dequeue() \rightarrow deleteFirst

DE RETINUT...

- SD - organiza, accesa si manipula date
- SD potrivita -> algoritm eficient
- ADT vs DS (abstractizare, separare what/how)
 - Lista, Stiva, Coada
 - Lista simplu/dublu inlantuita, vector

STRUCTURI CONTIGUE VS INLANTUITE

- Structura contigue - vectori, matrici (graf reprezentat cu matrice de adiacenta), heap-uri, tabele de dispersie.
- Structuri inlantuite - liste, arbori, grafuri reprezentate prin liste de adiacenta

STRUCTURI LINIARE VS IERARHICE

- Structura liniara - vector, lista
- Structuri ierarhice - heap-uri, arbori, grafuri,