# DATA STRUCTURES AND ALGORITHMS LECTURE 2

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#### In Lecture 1...

Course Organization

Abstract Data Types and Data Structures

Algorithm Analysis

## Today

- Algorithm Analysis
- 2 Arrays
- 3 Iterators

## Algorithm Analysis for Recursive Functions

 How can we compute the time complexity of a recursive algorithm?

## Recursive Binary Search

```
function BinarySearchR (array, elem, start, end) is:
//array - an ordered array of integer numbers
//elem - the element we are searching for
//start - the beginning of the interval in which we search (inclusive)
//end - the end of the interval in which we search (inclusive)
   if start > end then
      BinarySearchR \leftarrow False
   end-if
   middle \leftarrow (start + end) / 2
   if array[middle] = elem then
      BinarySeachR \leftarrow True
   else if elem < array[middle] then
      BinarySearchR \leftarrow BinarySearchR(array, elem, start, middle-1)
   else
      BinarySearchR \leftarrow BinarySearchR(array, elem, middle+1, end)
   end-if
end-function
```

## Recursive Binary Search

• First call to the *BinarySearchR* algorithms for an ordered array of *nr* elements:

BinarySearchR(array, elem, 1, nr)

• How do we compute the complexity of the BinarySearchR algorithm?

## Recursive Binary Search

- We will denote the length of the sequence that we are checking at every iteration by n (so n = end - start)
- We need to write the recursive formula of the solution

$$T(n) = egin{cases} 1, & ext{if } n \leq 1 \ T(rac{n}{2}) + 1, & ext{otherwise} \end{cases}$$

#### Master method

 The master method can be used to compute the time complexity of algorithms having the following general recursive formula:

$$T(n) = a * T(\frac{n}{b}) + f(n)$$

• where  $a \ge 1$ , b > 1 are constants and f(n) is an asymptotically positive function.

#### Master method

 Advantage of the master method: we can determine the time complexity of a recursive algorithm without further computations.

 Disadvantage of the master method: we need to memorize the three cases of the method.

# Computing the time complexity without the master method

- If we don't want to memorize the cases from the master method we can always compute the time complexity in the following way:
- Recall, the recursive formula for BinarySearchR was:

$$T(n) = egin{cases} 1, & ext{if } n \leq 1 \ T(rac{n}{2}) + 1, & ext{otherwise} \end{cases}$$

• We suppose that  $n = 2^k$  and rewrite the second branch of the recursive formula:

$$T(2^k) = T(2^{k-1}) + 1$$

• Now, we write what the value of  $T(2^{k-1})$  is (based on the recursive formula)

$$T(2^{k-1}) = T(2^{k-2}) + 1$$

• Next, we add what the value of  $T(2^{k-2})$  is (based on the recursive formula)

$$T(2^{k-2}) = T(2^{k-3}) + 1$$



ullet The last value that can be written is the value of  $\mathcal{T}(2^1)$ 

$$T(2^1) = T(2^0) + 1$$

 Now, we write all these equations together and add them (and we will see that many terms can be simplified, because they appear on the left hand side of an equation and the right hand side of another equation):

$$T(2^{k}) = T(2^{k-1}) + 1$$

$$T(2^{k-1}) = T(2^{k-2}) + 1$$

$$T(2^{k-2}) = T(2^{k-3}) + 1$$
...
$$T(2^{1}) = T(2^{0}) + 1$$

$$T(2^{k}) = T(2^{0}) + 1 + 1 + 1 + \dots + 1 = 1 + k$$

- We started from the notation  $n = 2^k$ .
- We want to go back to the notation using n. If  $n = 2^k \Rightarrow k = log_2 n$

$$T(2^k) = 1 + k$$
  
 
$$T(n) = 1 + \log_2 n \in \Theta(\log_2 n)$$

#### Another example

 Let's consider the following pseudocode and compute the time complexity of the algorithm:

```
subalgorithm operation(n, i) is:
//n and i are integer numbers, n is positive
  if n > 1 then
      i \leftarrow 2 * i
      m \leftarrow n/2
      operation(m, i-2)
      operation(m, i-1)
      operation(m, i+2)
      operation(m, i+1)
   else
      write i
   end-if
end-subalgorithm
```

• The first step is to write the recursive formula:

$$T(n) = egin{cases} 1, & ext{if } n \leq 1 \ 4 * T(rac{n}{2}) + 1, & ext{otherwise} \end{cases}$$

• We suppose that  $n = 2^k$ .

$$T(2^k) = 4 * T(2^{k-1}) + 1$$

• This time we need the value of  $4 * T(2^{k-1})$ 

$$T(2^{k-1}) = 4 * T(2^{k-2}) + 1 \Rightarrow$$
  
 $4 * T(2^{k-1}) = 4^2 * T(2^{k-2}) + 4$ 



• And the value of  $4^2 * T(2^{k-2})$ 

$$4^2 * T(2^{k-2}) = 4^3 * T(2^{k-3}) + 4^2$$

• The last value we can compute is  $4^{k-1} * T(2^1)$ 

$$4^{k-1} * T(2^1) = 4^k * T(2^0) + 4^{k-1}$$

• We write all the equations and add them:

$$T(2^{k}) = 4 * T(2^{k-1}) + 1$$

$$4 * T(2^{k-1}) = 4^{2} * T(2^{k-2}) + 4$$

$$4^{2} * T(2^{k-2}) = 4^{3} * T(2^{k-3}) + 4^{2}$$
...
$$\frac{4^{k-1} * T(2^{1}) = 4^{k} * T(2^{0}) + 4^{k-1}}{T(2^{k}) = 4^{k} * T(1) + 4^{0} + 4^{1} + 4^{2} + \dots + 4^{k-1}}$$

• T(1) is 1 (first case from recursive formula)

$$T(2^k) = 4^0 + 4^1 + 4^2 + ... + 4^{k-1} + 4^k$$



$$\sum_{i=0}^{n} p^{i} = \frac{p^{n+1} - 1}{p - 1}$$

$$T(2^k) = \frac{4^{k+1} - 1}{4 - 1} = \frac{4^k * 4 - 1}{3} = \frac{(2^k)^2 * 4 - 1}{3}$$

• We started from  $n = 2^k$ . Let's change back to n

$$T(n) = \frac{4n^2 - 1}{3} \in \Theta(n^2)$$

#### Records

- A record (or struct) is a static data structure.
- It represents the reunion of a fixed number of components (which can have different types) that form a logical unit together.
- We call the components of a record fields.
- For example, we can have a record to denote a *Person* formed of fields for *name*, *date of birth*, *address*, etc.

#### Person:

name: String dob: String address: String

etc.

#### **Arrays**

- An array is one of the simplest and most basic data structures.
- An array can hold a fixed number of elements and these elements occupy a contiguous memory block.
- Arrays are often used as representation for other (more complex) data structures.

#### **Arrays**

- When a new array is created, the maximum number of elements that can be stored in the array has to be specified (capacity of the array).
- The memory occupied by the array will be the capacity times the size of one element.
- The array itself is memorized by the address of the first element.

## Arrays - Example 1

An array of boolean values (boolean values occupy one byte)

```
Address of array: 00B5FBD4
Address of 0th elemet: 00B5FBD4
Address of 1th elemet: 00B5FBD5
Address of 2th elemet: 00B5FBD6
Address of 3th elemet: 00B5FBD7
Address of 4th elemet: 00B5FBD7
Address of 5th elemet: 00B5FBD9
Address of 5th elemet: 00B5FBD9
Address of 6th elemet: 00B5FBDA
Address of 7th elemet: 00B5FBDA
Address of 8th elemet: 00B5FBDC
Address of 9th elemet: 00B5FBDD
...
Press any key to continue . . .
```

• Can you guess the address of the 10th element?



## Arrays - Example 2

An array of integer values (integer values occupy 4 bytes)

```
Address of array: 0133FE10
Address of 0th elemet: 0133FE10
Address of 1th elemet: 0133FE14
Address of 2th elemet: 0133FE18
Address of 3th elemet: 0133FF1C
Address of 4th elemet: 0133FE20
Address of 5th elemet: 0133FE24
Address of 6th elemet: 0133FE28
Address of 7th elemet: 0133FE2C
Address of 8th elemet: 0133FE30
Address of 9th elemet: 0133FE34
Press any key to continue . . .
```

• Can you guess the address of the 10th element?

## Arrays - Example 3

 An array of fraction record values (the fraction record is composed of two integers)

```
Address of array: 008FF804
Address of 0th elemet: 008FF804
Address of 1th elemet: 008FF80C
Address of 2th elemet: 008FF814
Address of 3th elemet: 008FF81C
Address of 4th elemet: 008FF82C
Address of 5th elemet: 008FF82C
Address of 6th elemet: 008FF83C
Address of 7th elemet: 008FF83C
Address of 8th elemet: 008FF84C
Address of 9th elemet: 008FF84C
...
Press any key to continue . . . .
```

• Can you guess the address of the 10th element?



#### **Arrays**

• The main advantage of arrays is that any element of the array can be accessed in constant time  $(\Theta(1))$ , because the address of the element can simply be computed (considering that the first element is at position 0):

Address of  $i^{th}$  element = address of array + i \* size of an element

#### **Arrays**

- An array is a static structure: once the capacity of the array is specified, you cannot add or delete slots from it (you can add and delete elements from the slots, but the number of slots remains the same)
- This leads to an important disadvantage: we need to know/estimate from the beginning the number of elements
  - if the capacity is too small: we cannot store every element we want to
  - if the capacity is too big: we waste memory

## Dynamic Array

- There are arrays whose size can grow or shrink, depending on the number of elements that need to be stored in the array: they are called *dynamic arrays* (or *dynamic vectors*).
- Dynamic arrays are still arrays, the elements are still kept at contiguous memory locations.

## Dynamic Array - Representation

- In general, for a Dynamic Array we need the following fields:
  - cap denotes the number of slots allocated for the array (its capacity)
  - len denotes the actual number of elements stored in the array
  - elems denotes the actual array with capacity slots for TElems allocated

#### DynamicArray:

cap: Integer len: Integer

elems: TElem[]



## Dynamic Array - Resize

- When the value of *len* equals the value of *capacity*, we say
  that the array is full. If more elements need to be added, the *capacity* of the array is increased (usually doubled) and the
  array is *resized*.
- During the resize operation a new, bigger array is allocated and the existing elements are copied from the old array to the new one.
- Optionally, resize can be performed after delete operations as well: if the dynamic array becomes "too empty", a resize operation can be performed to shrink its size (to avoid occupying unused memory).



## Dynamic Array - Interface I

- Although a Dynamic Array can be implemented in a single way (using an array that occupies a contiguous memory block, but which can grow and shrink), we can present it in an abstract way, as the ADT DynamicArray.
- Domain of ADT DynamicArray

$$\mathcal{DA} = \{ \mathbf{da} | da = (cap, len, e_1e_2e_3...e_{len}), cap, len \in N, len \leq cap, e_i \text{ is of type TElem} \}$$



## Dynamic Array - Interface II

 Interface of the ADT Dynamic Array (interface of an ADT contains the set of operations that should exist for the ADT, together with the specifications, pre- and postconditions, for each operation)

## Dynamic Array - Interface III

- init(da, cp)
  - description: creates a new, empty DynamicArray with initial capacity cp (constructor)
  - pre: *cp* ∈ *N*
  - post:  $da \in \mathcal{DA}$ , da.cap = cp, da.n = 0
  - throws: an exception if cp is negative

# Dynamic Array - Interface IV

- destroy(da)
  - description: destroys a DynamicArray (destructor)
  - pre:  $da \in \mathcal{DA}$
  - **post**: *da* was destroyed (the memory occupied by the dynamic array was freed)

## Dynamic Array - Interface V

- size(da)
  - description: returns the size (number of elements) of the DynamicArray
  - pre:  $da \in \mathcal{DA}$
  - **post:** len ← the size of *da* (the number of elements)

## Dynamic Array - Interface VI

- getElement(da, i, e)
  - description: returns the element from a position from the DynamicArray
  - pre:  $da \in \mathcal{DA}$ ,  $1 \le i \le da.len$
  - **post:**  $e \in TElem$ ,  $e = da.e_i$  (the element from position i)
  - throws: an exception if i is not a valid position

# Dynamic Array - Interface VII

- setElement(da, i, e)
  - description: changes the element from a position to another value
  - pre:  $da \in \mathcal{DA}$ ,  $1 \le i \le da.len$ ,  $e \in TElem$
  - **post:**  $da' \in \mathcal{DA}, da'.e_i = e$  (the  $i^{th}$  element from da' becomes e)
  - throws: an exception if i is not a valid position

## Dynamic Array - Interface VIII

- addToEnd(da, e)
  - **description:** adds an element to the end of a DynamicArray. If the array is full, its capacity will be increased
  - pre:  $da \in \mathcal{DA}, e \in TElem$
  - **post:**  $da' \in \mathcal{DA}$ , da'.len = da.len + 1;  $da'.e_{da'.len} = e (da.cap = da.len <math>\Rightarrow da'.cap \leftarrow da.cap * 2)$

## Dynamic Array - Interface IX

- addToPosition(da, i, e)
  - description: adds an element to a given position in the DynamicArray. If the array is full, its capacity will be increased
  - **pre**:  $da \in \mathcal{DA}$ ,  $1 \leq i \leq da$ .len,  $e \in TE$ lem
  - **post:**  $da' \in \mathcal{DA}$ , da'.len = da.len + 1,  $da'.e_i = da.e_{i-1} \forall j = da'.len$ , da'.len 1, ..., i + 1,  $da'.e_i = e$  ( $da.cap = da.len \Rightarrow da'.cap \leftarrow da.cap * 2$ )
  - **throws:** an exception if *i* is not a valid position (da.len+1 is a valid position when adding a new element)

# Dynamic Array - Interface X

- deleteFromEnd(da, e)
  - description: deletes an element from the end of the DynamicArray. Returns the deleted element
  - pre:  $da \in \mathcal{DA}$ , da.len > 0
  - post:

```
e \in TElem, \ e = da.e_{da.len}, \ da' \in \mathcal{DA}, \ da'.len = da.len - 1
```

• throws: an exception if da is empty

# Dynamic Array - Interface XI

- deleteFromPosition(da, i, e)
  - description: deletes an element from a given position from the DynamicArray. Returns the deleted element
  - pre:  $da \in \mathcal{DA}$ ,  $1 \le i \le da.len$
  - **post:**  $e \in TElem\ e = da.e_i,\ da' \in \mathcal{DA},\ da'.len = da.len 1,\ da'.e_i = da.e_{i+1} \forall i \leq j \leq da'.len$
  - throws: an exception if i is not a valid position

# Dynamic Array - Interface XII

- iterator(da, it)
  - **description:** returns an iterator for the DynamicArray
  - pre:  $da \in \mathcal{DA}$
  - **post:**  $it \in \mathcal{I}$ , it is an iterator over da

## Dynamic Array - Interface XIII

- Other possible operations:
  - Delete all elements from the Dynamic Array (make it empty)
  - Verify if the Dynamic Array is empty
  - Delete an element (given as element, not as position)
  - Check if an element appears in the Dynamic Array
  - etc.

### Dynamic Array - Implementation

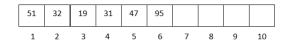
- Most operations from the interface of the Dynamic Array are very simple to implement.
- In the following we will discuss the implementation of two operations: addToEnd and addToPosition
- For the implementation we are going to use the representation discussed earlier:

```
DynamicArray:
cap: Integer
len: Integer
```

elems: TElem[]

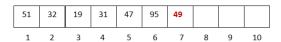


# Dynamic Array - addToEnd



- capacity (cap): 10
- length (len): 6

 Add the element 49 to the end of the dynamic array



- capacity (cap): 10
- length (len): 7



# Dynamic Array - addToEnd

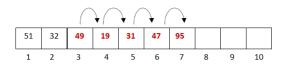
```
subalgorithm addToEnd (da, e) is:
   if da.len = da.cap then
   //the dynamic array is full. We need to resize it
      da.cap \leftarrow da.cap * 2
      newElems \leftarrow 0 an array with da.cap empty slots
      //we need to copy existing elements into newElems
      for index \leftarrow 1, da.len execute
         newElems[index] \leftarrow da.elems[index]
      end-for
      //we need to replace the old element array with the new one
      //depending on the prog. lang., we may need to free the old elems array
      da.elems \leftarrow newElems
   end-if
   //now we certainly have space for the element e
   da.len \leftarrow da.len + 1
   da.elems[da.len] \leftarrow e
end-subalgorithm
```

# Dynamic Array - addToPosition



- · capacity (cap): 10
- length (len): 6

Add the element 49 to position 3



- capacity (cap): 10
- length (len): 7

. Add the element 49 to position 3



# Dynamic Array - addToPosition

```
subalgorithm addToPosition (da, i, e) is:
  if da.len = da.cap then
   //the dynamic array is full. We need to resize it
      da.cap \leftarrow da.cap * 2
      newElems ← @ an array with da.cap empty slots
      for index \leftarrow 1, da.len execute
         newElems[index] \leftarrow da.elems[index]
      end-for
      da.elems ← newElems
   end-if
   //now we certainly have space for the element e
   da.len \leftarrow da.len + 1
   //move the elements to the right to free position i
   for index \leftarrow da.len, i+1, -1 execute
      da.elems[index] \leftarrow da.elems[index-1]
   end-for
   da.elems[i] \leftarrow e
end-subalgorithm
```

### Dynamic Array

#### Observations:

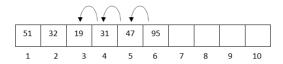
- If the capacity of a Dynamic Array can be 0, then da.cap ← da.cap \* 2 + 1 can be used at resize.
- While it is not mandatory to double the capacity, it is important to define the new capacity as a product of the old one with a constant number greater than 1 (just adding one new slot, or a constant number of new slots is not OK - you will see later why).
- After a resize operation the elements of the Dynamic Array will still occupy a contiguous memory zone, but it will be a different one than before.

### Dynamic Array

```
Address of DynamicArray structure: 00EFF78C
   Length: 3 and capacity: 3
   Address of the array from DA: 0115E1F8
     Address of the 1th element: 0115F1F8
     Address of the 2th element: 0115E1FC
     Address of the 3th element: 0115E200
Address of DynamicArray structure: 00EFF78C
   Length: 6 and capacity: 6
  Address of the array from DA: 011607A0
     Address of the 1th element: 011607A0
     Address of the 2th element: 011607A4
     Address of the 3th element: 011607A8
     Address of the 4th element: 011607AC
     Address of the 5th element: 011607B0
     Address of the 6th element: 011607B4
Address of DynamicArray structure: 00EFF78C
   Length: 7 and capacity: 12
   Address of the array from DA: 0115EB58
     Address of the 1th element: 0115EB58
     Address of the 2th element: 0115EB5C
     Address of the 3th element: 0115EB60
     Address of the 4th element: 0115EB64
     Address of the 5th element: 0115EB68
     Address of the 6th element: 0115FB6C
     Address of the 7th element: 0115EB70
Press any key to continue . . . _
```

## Dynamic Array - delete operations

- There are two operations to delete an element from a Dynamic Array:
  - To delete the element from the end of the array.
  - To delete an element from a given position *i*. In this case the elements after position *i* need to be moved one position to the left (element from position *j* is moved to position *j*-1).



- capacity (cap): 10
  - length (len): 5

Delete the element from position 3

# Dynamic Array - Complexity of operations

- Usually, we can discuss the complexity of an operation for an ADT only after we have chosen the representation. Since the ADT Dynamic Array can be represented in a single way, we can discuss the complexity of its operations:
  - size  $\Theta(1)$
  - getElement  $\Theta(1)$
  - setElement  $\Theta(1)$
  - iterator  $\Theta(1)$
  - addToEnd  $\Theta(1)$  amortized
  - addToPosition O(n)
  - deleteFromEnd  $\Theta(1)$
  - deleteFromPosition O(n)

- In asymptotic time complexity analysis we consider a single run of an algorithm.
  - addToEnd should have complexity O(n) when we have to resize the array, we need to move every existing element, so the number of instructions is proportional to the length of the array
  - Consequently, a sequence of n calls to the addToEnd operation would have complexity  $O(n^2)$
- In amortized time complexity analysis we consider a sequence of operations and compute the average time for these operations.
  - In amortized time complexity analysis we will consider the total complexity of *n* calls to the *addToEnd* operation and divide this by *n*, to get the *amortized* complexity of the algorithm.

- We can observe that we rarely have to resize the array if we consider a sequence of n operations.
- Specifically (considering that we double the capacity at each resize operation), at the *i*th operation we perform a resize if *i*-1 is a pover of 2. So, the cost of operation *i*, c<sub>i</sub>, is:

$$c_i = \begin{cases} i, & \text{if i-1 is an exact power of 2} \\ 1 & \text{otherwise} \end{cases}$$

Cost of n operations is:

$$\sum_{i=1}^{n} c_i \le n + \sum_{j=0}^{\lceil \log_2 n \rceil} 2^j < n + 2n = 3n$$

- The sum contains at most n values of 1 (this is where the n term comes from) and at most (integer part of) log<sub>2</sub>n terms of the form 2<sup>j</sup>.
- Since the total cost of *n* operations is 3*n*, we can say that the cost of one operation is 3, which is constant.

- While the worst case time complexity of addToEnd is still O(n), the amortized complexity is  $\Theta(1)$ .
- The amortized complexity is no longer valid, if the resize operation just adds a constant number of new slots.
- In case of the addToPosition operation, both the worst case and the amortized complexity of the operation is O(n) even if resize is performed rarely, we need to move elements to empty the position where we put the new element.

- In order to avoid having a Dynamic Array with too many empty slots, we can resize the array after deletion as well, if the array becomes "too empty".
- How empty should the array become before resize? Which of the following two strategies do you think is better? Why?
  - Wait until the table is only half full (da.len  $\approx$  da.cap/2) and resize it to the half of its capacity
  - Wait until the table is only a quarter full (da.len  $\approx$  da.cap/4) and resize it to the half of its capacity

#### **I**terator

- An iterator is a structure that is used to iterate through the elements of a container.
- Containers can be represented in different ways, using different data structures. Iterators are used to offer a common and generic way of moving through all the elements of a container, independently of the representation of the container.
- Every container that can be iterated, has to contain in the interface an operation called *iterator* that will create and return an iterator over the container.

#### **Iterator**

- An iterator usually contains:
  - a reference to the container it iterates over
  - a reference to a current element from the container
- Iterating through the elements of the container means actually moving this current element from one element to another until the iterator becomes invalid
- The exact way of representing the current element from the iterator depends on the data structure used for the implementation of the container. If the representation/ implementation of the container changes, we need to change the representation/ implementation of the iterator as well.



### Iterator - Interface I

• Domain of an Iterator

 $\mathcal{I} = \{\textbf{it} | \text{it is an iterator over a container with elements of type TElem } \}$ 

### Iterator - Interface II

• Interface of an Iterator:

### Iterator - Interface III

- init(it, c)
  - description: creates a new iterator for a container
  - **pre:** c is a container
  - **post:**  $it \in \mathcal{I}$  and it points to the first element in c if c is not empty or it is not valid

### Iterator - Interface IV

- getCurrent(it, e)
  - description: returns the current element from the iterator
  - **pre**:  $it \in \mathcal{I}$ , it is valid
  - post:  $e \in TElem$ , e is the current element from it

### Iterator - Interface V

- next(it)
  - description: moves the current element from the container to the next element or makes the iterator invalid if no elements are left
  - **pre:**  $it \in \mathcal{I}$ , it is valid
  - post: the current element from it points to the next element from the container

### Iterator - Interface VI

- valid(it)
  - description: verifies if the iterator is valid
  - pre:  $it \in \mathcal{I}$
  - post:

$$valid \leftarrow \begin{cases} True, & \text{if it points to a valid element from the container} \\ False & \text{otherwise} \end{cases}$$

### Types of iterators I

- The interface presented above describes the simplest iterator: unidirectional and read-only
- A unidirectional iterator can be used to iterate through a container in one direction only (usually forward, but we can define a reverse iterator as well).
- A bidirectional iterator can be used to iterate in both directions. Besides the next operation it has an operation called previous.

### Types of iterators II

- A random access iterator can be used to move multiple steps (not just one step forward or one step backward).
- A read-only iterator can be used to iterate through the container, but cannot be used to change it.
- A read-write iterator can be used to add/delete elements to/from the container.

### Using the iterator

 Since the interface of an iterator is the same, independently of the exact container or its representation, the following subalgorithm can be used to print the elements of any container.

```
subalgorithm printContainer(c) is:
//pre: c is a container
//post: the elements of c were printed
//we create an iterator using the iterator method of the container
  iterator(c, it)
  while valid(it) execute
     //get the current element from the iterator
     getCurrent(it, elem)
     print elem
     //go to the next element
     next(it)
   end-while
end-subalgorithm
```

### Iterator for a Dynamic Array

- How can we define an iterator for a Dynamic Array?
- How can we represent that current element from the iterator?
- In case of a Dynamic Array, the simplest way to represent a current element is to retain the position of the current element.

#### IteratorDA:

da: DynamicArray current: Integer

 Let's see how the operations of the iterator can be implemented.



# Iterator for a Dynamic Array - init

• What do we need to do in the *init* operation?

```
\begin{array}{l} \textbf{subalgorithm} \  \, \text{init(it, da)} \  \, \textit{is:} \\ //\textit{it is an IteratorDA, da is a Dynamic Array} \\ \quad \text{it.da} \leftarrow \text{da} \\ \quad \text{it.current} \leftarrow 1 \\ \textbf{end-subalgorithm} \end{array}
```

# Iterator for a Dynamic Array - getCurrent

• What do we need to do in the getCurrent operation?

# Iterator for a Dynamic Array - next

• What do we need to do in the *next* operation?

```
\begin{array}{l} \textbf{subalgorithm} \ \ \text{next(it)} \ \textit{is:} \\  \  \  \  \text{it.current} \leftarrow \text{it.current} + 1 \\ \textbf{end-subalgorithm} \end{array}
```

## Iterator for a Dynamic Array - valid

• What do we need to do in the valid operation?

```
function valid(it) is:

if it.current <= it.da.len then

valid ← True

else

valid ← False

end-if

end-function
```

## Iterator for a Dynamic Array

- We can print the content of a Dynamic Array in two ways:
  - Using an iterator (as present above for a container)
  - Using the positions (indexes) of elements

```
subalgorithm printDA(da) is:

//pre: da is a Dynamic Array

//post: the elements of da were printed

for i ← 1, size(da) execute

getElement(da, i, elem)

print elem

end-for

end-subalgorithm
```

### Iterator for a Dynamic Array

- In case of a Dynamic Array both printing algorithms have  $\Theta(n)$  complexity
- For other data structures/containers we need iterator because
  - there are no positions in the data structure/container
  - the time complexity of iterating through all the elements is smaller