

# DATA STRUCTURES AND ALGORITHMS

## LECTURE 7

Lect. PhD. Oneț-Marian Zsuzsanna

Babeș - Bolyai University  
Computer Science and Mathematics Faculty

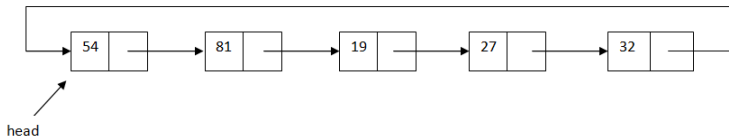
2020 - 2021

- Linked Lists
- Sorted Linked List

- Linked List
  - Circular Lists
  - XOR Lists
  - Skip Lists
- Linked List on Array

# Circular Lists

- For a SLL or a DLL the last node has as *next* the value *NIL*. In a *circular list* no node has *NIL* as next, since the last node contains the address of the first node in its next field.



# Circular Lists

- We can have singly linked and doubly linked circular lists, in the following we will discuss the singly linked version.
- In a circular list each node has a successor, and we can say that the list does not have an end.
- We have to be careful when we iterate through a circular list, because we might end up with an infinite loop (if we set as stopping criterion the case when *currentNode* or *[currentNode].next* is *NIL*).
- There are problems where using a circular list makes the solution simpler (for example: Josephus circle problem, rotation of a list)

- Operations for a circular list have to consider the following two important aspects:
  - The *last* node of the list is the one whose *next* field is the *head* of the list.
  - Inserting before the head, or removing the head of the list, is no longer a simple  $\Theta(1)$  complexity operation, because we have to change the *next* field of the last node as well (and for this we have to find the last node).

# Circular Lists - Representation

- The representation of a circular list is exactly the same as the representation of a simple SLL. We have a structure for a *Node* and a structure for the *Circular Singly Linked Lists - CSLL*.

## CSLLNode:

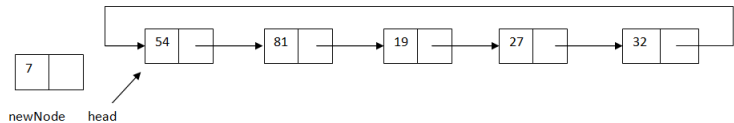
info: TElem

next: ↑ CSLLNode

## CSLL:

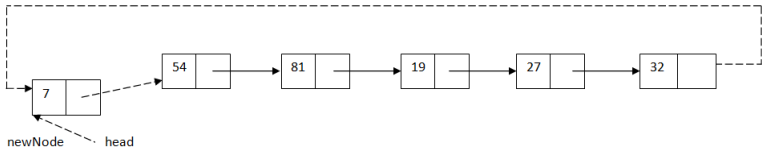
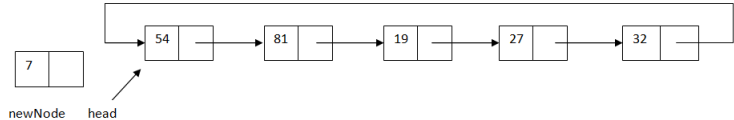
head: ↑ CSLLNode

# CSLL - InsertFirst





# CSLL - InsertFirst



**subalgorithm** insertFirst (csll, elem) **is:**

*//pre: csll is a CSLL, elem is a TElem*

*//post: the element elem is inserted at the beginning of csll*

newNode  $\leftarrow$  allocate()

[newNode].info  $\leftarrow$  elem

[newNode].next  $\leftarrow$  newNode

**if** csll.head = NIL **then**

    csll.head  $\leftarrow$  newNode

**else**

    lastNode  $\leftarrow$  csll.head

**while** [lastNode].next  $\neq$  csll.head **execute**

        lastNode  $\leftarrow$  [lastNode].next

**end-while**

*//continued on the next slide...*

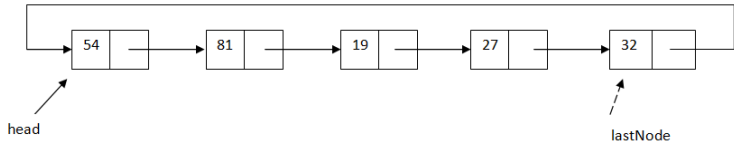
```
[newNode].next ← csll.head  
[lastNode].next ← newNode  
csll.head ← newNode
```

**end-if**

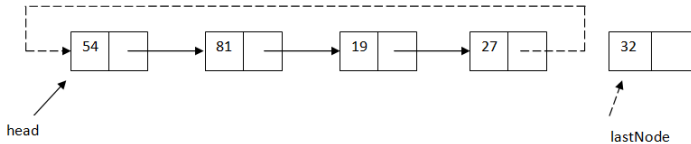
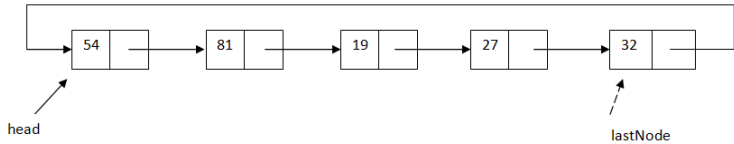
**end-subalgorithm**

- Complexity:  $\Theta(n)$
- Note: inserting a new element at the end of a circular list looks exactly the same, but we do not modify the value of *csll.head* (so the last instruction is not needed).

# CSLL - DeleteLast



# CSLL - DeleteLast



# CSLL - DeleteLast

```
function deleteLast(csll) is:  
  //pre: csll is a CSLL  
  //post: the last element from csll is removed and the node  
  //containing it is returned  
  deletedNode  $\leftarrow$  NIL  
  if csll.head  $\neq$  NIL then  
    if [csll.head].next = csll.head then  
      deletedNode  $\leftarrow$  csll.head  
      csll.head  $\leftarrow$  NIL  
    else  
      prevNode  $\leftarrow$  csll.head  
      while [[prevNode].next].next  $\neq$  csll.head execute  
        prevNode  $\leftarrow$  [prevNode].next  
      end-while  
  //continued on the next slide...
```

```
    deletedNode  $\leftarrow$  [prev].next  
    [prev].next  $\leftarrow$  csll.head  
end-if  
end-if  
[deletedNode].next  $\leftarrow$  NIL  
deleteLast  $\leftarrow$  deletedNode  
end-function
```

- Complexity:  $\Theta(n)$

- How can we define an iterator for a CSLL? What do you think is the most challenging part of implementing the iterator?



- How can we define an iterator for a CSLL? What do you think is the most challenging part of implementing the iterator?
- The main problem with the *standard* SLL iterator is its *valid* method. For a SLL *valid* returns false, when the value of the *currentElement* becomes *NIL*. But in case of a circular list, *currentElement* will never be *NIL*.
- We have finished iterating through all elements when the value of *currentElement* becomes equal to the *head* of the list.
- However, writing that the iterator is invalid when *currentElement* equals the *head*, will produce an iterator which is invalid the moment it was created.

# CSLL - Iterator - Possibilities

- We can say that the iterator is invalid, when the *next* of the *currentElement* is equal to the *head* of the list.
- This will stop the iterator when it is set to the last element of the list, so if we want to print all the elements from a list, we have to call the *element* operation one more time when the iterator becomes invalid (or use a do-while loop instead of a while loop - but this causes problems when we iterate through an empty list).
- As a second problem, this violates the precondition that *element* should only be called when the iterator is valid.

- We can add a boolean flag to the iterator besides the *currentElement*, something that shows whether we are at the *head* for the first time (when the iterator was created), or whether we got back to the *head* after going through all the elements.
- For this version, standard iteration code remains the same.

- Similarly, if the CSLL contains a field for the size of the list, we can add a counter in the iterator (besides the current node), which counts how many times we called next. If it is equal to the size + 1, the iterator is invalid. It is a combination of how we represent current element for a dynamic array and a linked list.
- For this version, standard iteration code remains the same.

# CSLL - Iterator - Possibilities

- Depending on the problem we want to solve, we might need a read/write iterator: one that can be used to change the content of the CSLL.
- We can have *insertAfter* - insert a new element after the current node - and *delete* - delete the current node
- We can say that the iterator is invalid when there are no elements in the circular list (especially if we delete from it).

# The Josephus circle problem

- There are  $n$  men standing a circle waiting to be executed. Starting from one person we start counting into clockwise direction and execute the  $m^{th}$  person. After the execution we restart counting with the person after the executed one and execute again the  $m^{th}$  person. The process is continued until only one person remains: this person is freed.
- Given the number of men,  $n$ , and the number  $m$ , determine which person will be freed.
- For example, if we have 5 men and  $m = 3$ , the  $4^{th}$  man will be freed.

# Circular Lists - Variations

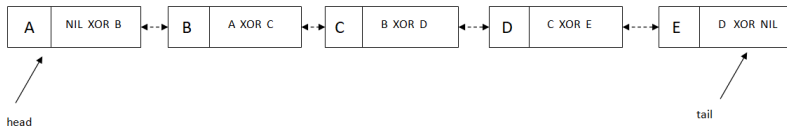
- There are different possible variations for a circular list that can be useful, depending on what we use the circular list for.
  - Instead of retaining the *head* of the list, retain its *tail*. In this way, we have access both to the *head* and the *tail*, and can easily insert before the head or after the tail. Deleting the head is simple as well, but deleting the tail still needs  $\Theta(n)$  time.
  - Use a *header* or *sentinel* node - a special node that is considered the *head* of the list, but which cannot be deleted or changed - it is simply a separation between the head and the tail. For this version, knowing when to stop with the iterator is easier.

# XOR Linked List

- Doubly linked lists are better than singly linked lists because they offer better complexity for some operations
- Their disadvantage is that they occupy more memory, because you have two links to memorize, instead of just one.
- A memory-efficient solution is to have a *XOR Linked List*, which is a doubly linked list (we can traverse it in both directions), where every node retains one single link, which is the XOR of the previous and the next node.

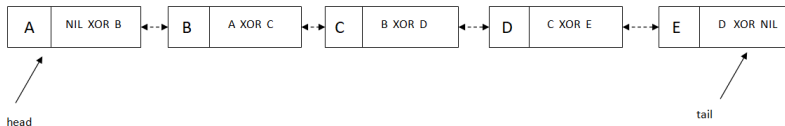


# XOR Linked List - Example



- How do you traverse such a list?

# XOR Linked List - Example



- How do you traverse such a list?
  - We start from the head (but we can have a backward traversal starting from the tail in a similar manner), the node with A
  - The address from node A is directly the address of node B ( $\text{NIL XOR B} = \text{B}$ )
  - When we have the address of node B, its link is  $\text{A XOR C}$ . To get the address of node C, we have to XOR B's link with the address of A (it's the previous node we come from):  $\text{A XOR C XOR A} = \text{A XOR A XOR C} = \text{NIL XOR C} = \text{C}$

# XOR Linked List - Representation

- We need two structures to represent a XOR Linked List: one for a node and one for the list

## XORNode:

info: TELeM

link: ↑ XORNode

## XORList:

head: ↑ XORNode

tail: ↑ XORNode

# XOR Linked List - Traversal

**subalgorithm** printListForward(xorl) **is:**

*//pre: xorl is a XORList*

*//post: true (the content of the list was printed)*

prevNode  $\leftarrow$  NIL

currentNode  $\leftarrow$  xorl.head

**while** currentNode  $\neq$  NIL **execute**

**write** [currentNode].info

    nextNode  $\leftarrow$  prevNode XOR [currentNode].link

    prevNode  $\leftarrow$  currentNode

    currentNode  $\leftarrow$  nextNode

**end-while**

**end-subalgorithm**

- Complexity:  $\Theta(n)$

# XOR Linked List - addToBeginning

- How can we add an element to the beginning of the list?

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- How can we add an element to the beginning of the list?

**subalgorithm** addToBeginning(xorl, elem) **is:**

*//pre: xorl is a XORList*

*//post: a node with info elem was added to the beginning of the list*

newNode  $\leftarrow$  allocate()

[newNode].info  $\leftarrow$  elem

[newNode].link  $\leftarrow$  xorl.head

**if** xorl.head = NIL **then**

    xorl.head  $\leftarrow$  newNode

    xorl.tail  $\leftarrow$  newNode

**else**

    [xorl.head].link  $\leftarrow$  [xorl.head].link XOR newNode

    xorl.head  $\leftarrow$  newNode

**end-if**

**end-subalgorithm**

- Complexity:

# XOR Linked List - addToBeginning

- How can we add an element to the beginning of the list?

**subalgorithm** addToBeginning(xorl, elem) **is:**

*//pre: xorl is a XORList*

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newNode  $\leftarrow$  allocate()

[newNode].info  $\leftarrow$  elem

[newNode].link  $\leftarrow$  xorl.head

**if** xorl.head = NIL **then**

    xorl.head  $\leftarrow$  newNode

    xorl.tail  $\leftarrow$  newNode

**else**

    [xorl.head].link  $\leftarrow$  [xorl.head].link XOR newNode

    xorl.head  $\leftarrow$  newNode

**end-if**

**end-subalgorithm**

- Complexity:  $\Theta(1)$

# Skip Lists

- Assume that we want to memorize a sequence of sorted elements. The elements can be stored in:
  - dynamic array
  - linked list (let's say doubly linked list)
- We know that the most frequently used operation will be the insertion of a new element, so we want to choose a data structure for which insertion has the best complexity. Which one should we choose?



- We can divide the insertion operation into two steps: *finding where to insert* and *inserting the elements*

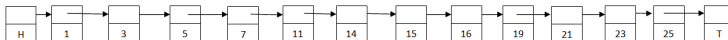
- We can divide the insertion operation into two steps: *finding where to insert* and *inserting the elements*
  - For a dynamic array finding the position can be optimized (binary search  $O(\log_2 n)$ ), but the insertion is  $O(n)$
  - For a linked list the insertion is optimal ( $\Theta(1)$ ), but finding where to insert is  $O(n)$

# Skip List

- A skip list is a data structure that allows *fast search* in an ordered sequence.
- How can we do that?

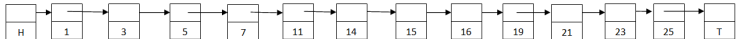
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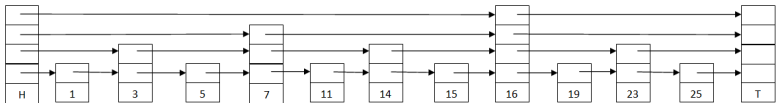
# Skip List

- A skip list is a data structure that allows *fast search* in an ordered sequence.
- How can we do that?



- Starting from an ordered linked list, we add to every second node another pointer that skips over one element.
- We add to every fourth node another pointer that skips over 3 elements.
- etc.

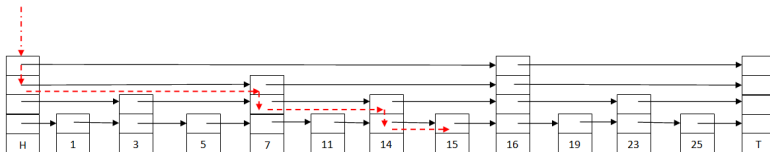
# Skip List



- H and T are two special nodes, representing *head* and *tail*. They cannot be deleted, they exist even in an empty list.

# Skip List - Search

- Search for element 15.



- Start from head and from highest level.
- If possible, go right.
- If cannot go right (next element is greater), go down a level.

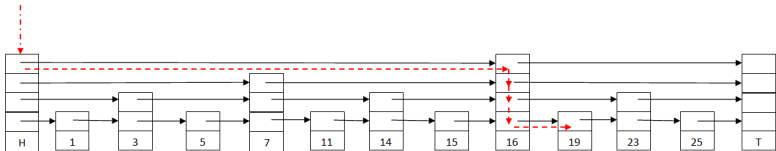
# Skip List

- Lowest level has all  $n$  elements.
- Next level has  $\frac{n}{2}$  elements.
- Next level has  $\frac{n}{4}$  elements.
- etc.
- $\Rightarrow$  there are approx  $\log_2 n$  levels.
- From each level, we check at most 2 nodes.
- Complexity of search:  $O(\log_2 n)$



# Skip List - Insert

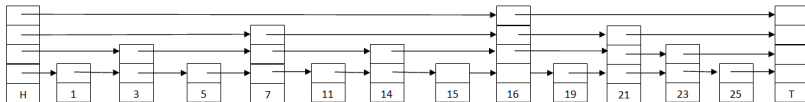
- Insert element 21.



- How *high* should the new node be?

# Skip List - Insert

- *Height* of a new node is determined *randomly*, but in such a way that approximately half of the nodes will be on level 2, a quarter of them on level 3, etc.



- Assume we randomly generate the height 3 for the node with 21.

- Skip Lists are *probabilistic* data structures, since we decide randomly the height of a newly inserted node.
- There might be a worst case, where every node has height 1 (so it is just a linked list).
- In practice, they function well.

# Linked Lists on Arrays

- What if we need a linked list, but we are working in a programming language that does not offer pointers (or references)?
- We can still implement linked data structures, without the explicit use of pointers or memory addresses, simulating them using arrays and array indexes.

# Linked Lists on Arrays

- Usually, when we work with arrays, we store the elements in the array starting from the leftmost position and place them one after the other (no empty spaces in the middle of the list are allowed).
- The order of the elements is given by the order in which they are placed in the array.

elems

|    |    |    |   |    |    |  |  |  |  |
|----|----|----|---|----|----|--|--|--|--|
| 46 | 78 | 11 | 6 | 59 | 19 |  |  |  |  |
|----|----|----|---|----|----|--|--|--|--|

- Order of the elements: 46, 78, 11, 6, 59, 19

# Linked Lists on Arrays

- We can define a linked data structure on an array, if we consider that the order of the elements is not given by their relative positions in the array, but by an integer number associated with each element, which shows the index of the next element in the array (thus we have a singly linked list).

|       |    |    |    |    |    |    |  |  |  |  |
|-------|----|----|----|----|----|----|--|--|--|--|
| elems | 46 | 78 | 11 | 6  | 59 | 19 |  |  |  |  |
| next  | 5  | 6  | 1  | -1 | 2  | 4  |  |  |  |  |

head = 3

- Order of the elements: 11, 46, 59, 78, 19, 6

# Linked Lists on Arrays

- Now, if we want to delete the number 46 (which is actually the second element of the list), we do not have to move every other element to the left of the array, we just need to modify the links:

|       |  |    |    |    |    |    |  |  |  |  |
|-------|--|----|----|----|----|----|--|--|--|--|
| elems |  | 78 | 11 | 6  | 59 | 19 |  |  |  |  |
| next  |  | 6  | 5  | -1 | 2  | 4  |  |  |  |  |

head = 3

- Order of the elements: 11, 59, 78, 19, 6

# Linked Lists on Arrays

- If we want to insert a new element, for example 44, at the 3<sup>rd</sup> position in the list, we can put the element anywhere in the array, the important part is setting the links correctly:

|       |  |    |    |    |    |    |  |    |  |  |
|-------|--|----|----|----|----|----|--|----|--|--|
| elems |  | 78 | 11 | 6  | 59 | 19 |  | 44 |  |  |
| next  |  | 6  | 5  | -1 | 8  | 4  |  | 2  |  |  |

head = 3

- Order of the elements: 11, 59, 44, 78, 19, 6



# Linked Lists on Arrays

- When a new element needs to be inserted, it can be put to any empty position in the array. However, finding an empty position has  $O(n)$  complexity, which will make the complexity of any insert operation (anywhere in the list)  $O(n)$ . In order to avoid this, we will keep a linked list of the empty positions as well.

|       |   |    |    |    |    |    |   |    |    |    |
|-------|---|----|----|----|----|----|---|----|----|----|
| elems |   | 78 | 11 | 6  | 59 | 19 |   | 44 |    |    |
| next  | 7 | 6  | 5  | -1 | 8  | 4  | 9 | 2  | 10 | -1 |

head = 3

firstEmpty = 1

# Linked Lists on Arrays

- In a more formal way, we can simulate a singly linked list on an array with the following:
  - an array in which we will store the elements.
  - an array in which we will store the links (indexes to the next elements).
  - the capacity of the arrays (the two arrays have the same capacity, so we need only one value).
  - an index to tell where the *head* of the list is.
  - an index to tell where the first empty position in the array is.

# SLL on Array - Representation

- The representation of a singly linked list on an array is the following:

SLLA:

```
elems: TElem[]  
next: Integer[]  
cap: Integer  
head: Integer  
firstEmpty: Integer
```

- We can implement for a SLLA any operation that we can implement for a SLL:
  - insert at the beginning, end, at a position, before/after a given value
  - delete from the beginning, end, from a position, a given element
  - search for an element
  - get an element from a position

**subalgorithm** `init(slla)` **is:**

*//pre: true; post: slla is an empty SLLA*

`slla.cap`  $\leftarrow$  `INIT_CAPACITY`

**subalgorithm** init(slla) **is:**

*//pre: true; post: slla is an empty SLLA*

slla.cap  $\leftarrow$  INIT\_CAPACITY

slla.elems  $\leftarrow$  @an array with slla.cap positions

slla.next  $\leftarrow$  @an array with slla.cap positions

slla.head  $\leftarrow$  -1

**for**  $i \leftarrow 1, \text{slla.cap}-1$  **execute**

    slla.next[i]  $\leftarrow$  i + 1

**end-for**

slla.next[slla.cap]  $\leftarrow$  -1

slla.firstEmpty  $\leftarrow$  1

**end-subalgorithm**

- Complexity:

**subalgorithm** init(slla) **is:**

*//pre: true; post: slla is an empty SLLA*

slla.cap  $\leftarrow$  INIT\_CAPACITY

slla.elems  $\leftarrow$  @an array with slla.cap positions

slla.next  $\leftarrow$  @an array with slla.cap positions

slla.head  $\leftarrow$  -1

**for**  $i \leftarrow 1, \text{slla.cap}-1$  **execute**

    slla.next[i]  $\leftarrow$  i + 1

**end-for**

slla.next[slla.cap]  $\leftarrow$  -1

slla.firstEmpty  $\leftarrow$  1

**end-subalgorithm**

- Complexity:  $\Theta(n)$  -where n is the initial capacity

**function** search (slla, elem) **is:**

*//pre: slla is a SLLA, elem is a TElem*

*//post: return True is elem is in slla, False otherwise*

current  $\leftarrow$  slla.head

**while** current  $\neq$  -1 **and** slla.elems[current]  $\neq$  elem **execute**

current  $\leftarrow$  slla.next[current]

**end-while**

**if** current  $\neq$  -1 **then**

search  $\leftarrow$  True

**else**

search  $\leftarrow$  False

**end-if**

**end-function**

- Complexity:



**function** search (slla, elem) **is:**

*//pre: slla is a SLLA, elem is a TElem*

*//post: return True is elem is in slla, False otherwise*

current  $\leftarrow$  slla.head

**while** current  $\neq$  -1 **and** slla.elems[current]  $\neq$  elem **execute**

current  $\leftarrow$  slla.next[current]

**end-while**

**if** current  $\neq$  -1 **then**

search  $\leftarrow$  True

**else**

search  $\leftarrow$  False

**end-if**

**end-function**

- Complexity:  $O(n)$

- From the *search* function we can see how we can go through the elements of a SLLA (and how similar this traversal is to the one done for a SLL):
  - We need a *current* element used for traversal, which is initialized to the index of the *head* of the list.
  - We stop the traversal when the value of *current* becomes -1
  - We go to the next element with the instruction:  $current \leftarrow slla.next[current]$ .

# SLLA - InsertFirst

**subalgorithm** insertFirst(slla, elem) **is:**

*//pre: slla is an SLLA, elem is a TElem*

*//post: the element elem is added at the beginning of slla*

**if** slla.firstEmpty = -1 **then**

newElems  $\leftarrow$  @an array with  $\text{slla.cap} * 2$  positions

newNext  $\leftarrow$  @an array with  $\text{slla.cap} * 2$  positions

**for**  $i \leftarrow 1, \text{slla.cap}$  **execute**

newElems[i]  $\leftarrow$  slla.elems[i]

newNext[i]  $\leftarrow$  slla.next[i]

**end-for**

**for**  $i \leftarrow \text{slla.cap} + 1, \text{slla.cap} * 2 - 1$  **execute**

newNext[i]  $\leftarrow i + 1$

**end-for**

newNext[slla.cap\*2]  $\leftarrow -1$

*//continued on the next slide...*

# SLLA - InsertFirst

*//free slla.elems and slla.next if necessary*

$slla.elems \leftarrow newElems$

$slla.next \leftarrow newNext$

$slla.firstEmpty \leftarrow slla.cap + 1$

$slla.cap \leftarrow slla.cap * 2$

**end-if**

$newPosition \leftarrow slla.firstEmpty$

$slla.elems[newPosition] \leftarrow elem$

$slla.firstEmpty \leftarrow slla.next[slla.firstEmpty]$

$slla.next[newPosition] \leftarrow slla.head$

$slla.head \leftarrow newPosition$

**end-subalgorithm**

- Complexity:

*//free slla.elems and slla.next if necessary*

$slla.elems \leftarrow newElems$

$slla.next \leftarrow newNext$

$slla.firstEmpty \leftarrow slla.cap + 1$

$slla.cap \leftarrow slla.cap * 2$

**end-if**

$newPosition \leftarrow slla.firstEmpty$

$slla.elems[newPosition] \leftarrow elem$

$slla.firstEmpty \leftarrow slla.next[slla.firstEmpty]$

$slla.next[newPosition] \leftarrow slla.head$

$slla.head \leftarrow newPosition$

**end-subalgorithm**

- Complexity:  $\Theta(1)$  amortized

# SLLA - DeleteElement

```
subalgorithm deleteElement(slla, elem) is:  
//pre: slla is a SLLA; elem is a TElem  
//post: the element elem is deleted from SLLA  
    nodC  $\leftarrow$  slla.head  
    prevNode  $\leftarrow$  -1  
    while nodC  $\neq$  -1 and slla.elems[nodC]  $\neq$  elem execute  
        prevNode  $\leftarrow$  nodC  
        nodC  $\leftarrow$  slla.next[nodC]  
    end-while  
    if nodC  $\neq$  -1 then  
        if nodC = slla.head then  
            slla.head  $\leftarrow$  slla.next[slla.head]  
        else  
            slla.next[prevNode]  $\leftarrow$  slla.next[nodC]  
        end-if  
//continued on the next slide...
```

# SLLA - DeleteElement

```
//add the nodC position to the list of empty spaces  
slla.next[nodC]  $\leftarrow$  slla.firstEmpty  
slla.firstEmpty  $\leftarrow$  nodC  
else  
  @the element does not exist  
end-if  
end-subalgorithm
```

- Complexity:  $O(n)$

- Iterator for a SLLA is a combination of an iterator for an array and of an iterator for a singly linked list:
- Since the elements are stored in an array, the *currentElement* will be an index from the array.
- But since we have a linked list, going to the next element will not be done by incrementing the *currentElement* by one; we have to follow the *next* links.
- Also, initialization will be done with the position of the head, not position 1.



- Obviously, we can define a doubly linked list as well without pointers, using arrays.
- For the DLLA we will see another way of representing a linked list on arrays:
  - The main idea is the same, we will use array indexes as links between elements
  - We are using the same information, but we are going to structure it differently
  - However, we can make it look more similar to linked lists with dynamic allocation

- Linked Lists with dynamic allocation are made of nodes. We can define a structure to represent a node, even if we are working with arrays.
- A node (for a doubly linked list) contains the information and links towards the previous and the next nodes:

DLLANode:

info: TElem  
next: Integer  
prev: Integer

- Having defined the *DLLANode* structure, we only need one array, which will contain *DLLANodes*.
- Since it is a doubly linked list, we keep both the head and the tail of the list.

## DLLA:

nodes: *DLLANode*[]

cap: Integer

head: Integer

tail: Integer

firstEmpty: Integer

size: Integer *//it is not mandatory, but useful*

# DLLA - Allocate and free

- To make the representation and implementation even more similar to a dynamically allocated linked list, we can define the *allocate* and *free* functions as well.

**function** allocate(dlla) **is:**

*//pre: dlla is a DLLA*

*//post: a new element will be allocated and its position returned*

newElem  $\leftarrow$  dlla.firstEmpty

**if** newElem  $\neq$  -1 **then**

    dlla.firstEmpty  $\leftarrow$  dlla.nodes[dlla.firstEmpty].next

**if** dlla.firstEmpty  $\neq$  -1 **then**

        dlla.nodes[dlla.firstEmpty].prev  $\leftarrow$  -1

**end-if**

    dlla.nodes[newElem].next  $\leftarrow$  -1

    dlla.nodes[newElem].prev  $\leftarrow$  -1

**end-if**

    allocate  $\leftarrow$  newElem

**end-function**

# DLLA - Allocate and free

**subalgorithm** free (dlla, poz) **is:**

*//pre: dlla is a DLLA, poz is an integer number*

*//post: the position poz was freed*

$\text{dlla.nodes}[\text{poz}].\text{next} \leftarrow \text{dlla.firstEmpty}$

$\text{dlla.nodes}[\text{poz}].\text{prev} \leftarrow -1$

**if**  $\text{dlla.firstEmpty} \neq -1$  **then**

$\text{dlla.nodes}[\text{dlla.firstEmpty}].\text{prev} \leftarrow \text{poz}$

**end-if**

$\text{dlla.firstEmpty} \leftarrow \text{poz}$

**end-subalgorithm**

# DLLA - InsertPosition

**subalgorithm** insertPosition(dlla, elem, poz) **is:**

*//pre: dlla is a DLLA, elem is a TElem, poz is an integer number*

*//post: the element elem is inserted in dlla at position poz*

**if** poz < 1 **OR** poz > dlla.size + 1 **execute**

    @throw exception

**end-if**

newElem  $\leftarrow$  allocate(dlla)

**if** newElem = -1 **then**

    @resize

    newElem  $\leftarrow$  allocate(dlla)

**end-if**

dlla.nodes[newElem].info  $\leftarrow$  elem

**if** poz = 1 **then**

**if** dlla.head = -1 **then**

        dlla.head  $\leftarrow$  newElem

        dlla.tail  $\leftarrow$  newElem

**else**

*//continued on the next slide...*

# DLLA - InsertPosition

```
dlla.nodes[newElem].next  $\leftarrow$  dlla.head  
dlla.nodes[dlla.head].prev  $\leftarrow$  newElem  
dlla.head  $\leftarrow$  newElem
```

**end-if**

**else**

```
nodC  $\leftarrow$  dlla.head
```

```
pozC  $\leftarrow$  1
```

**while**  $\text{nodC} \neq -1$  **and**  $\text{pozC} < \text{poz} - 1$  **execute**

```
    nodC  $\leftarrow$  dlla.nodes[nodC].next
```

```
    pozC  $\leftarrow$  pozC + 1
```

**end-while**

**if**  $\text{nodC} \neq -1$  **then** *//it should never be -1, the position is correct*

```
    nodNext  $\leftarrow$  dlla.nodes[nodC].next
```

```
    dlla.nodes[newElem].next  $\leftarrow$  nodNext
```

```
    dlla.nodes[newElem].prev  $\leftarrow$  nodC
```

```
    dlla.nodes[nodC].next  $\leftarrow$  newElem
```

*//continued on the next slide...*

# DLLA - InsertPosition

```
    if nodNext = -1 then
        dlla.tail ← newElem
    else
        dlla.nodes[nodNext].prev ← newElem
    end-if
end-if
end-if
end-subalgorithm
```

- Complexity:  $O(n)$



- The iterator for a DLLA contains as *current element* the index of the current node from the array.

DLLAIterator:

list: DLLA

currentElement: Integer

**subalgorithm** init(it, dlla) **is:**

*//pre: dlla is a DLLA*

*//post: it is a DLLAlterator for dlla*

it.list  $\leftarrow$  dlla

it.currentElement  $\leftarrow$  dlla.head

**end-subalgorithm**

- For a (dynamic) array, currentElement is set to 0 when an iterator is created. For a DLLA we need to set it to the head of the list (which might be position 0, but it might be a different position as well).
- Complexity:

**subalgorithm** init(it, dlla) **is:**

*//pre: dlla is a DLLA*

*//post: it is a DLLAlterator for dlla*

it.list  $\leftarrow$  dlla

it.currentElement  $\leftarrow$  dlla.head

**end-subalgorithm**

- For a (dynamic) array, currentElement is set to 0 when an iterator is created. For a DLLA we need to set it to the head of the list (which might be position 0, but it might be a different position as well).
- Complexity:  $\Theta(1)$

# DLLAlterator - getCurrent

**subalgorithm** getCurrent(it) **is:**

*//pre: it is a DLLAlterator, it is valid*

*//post: e is a TElem, e is the current element from it*

*//throws exception if the iterator is not valid*

**if** it.currentElement = -1 **then**

    @throw exception

**end-if**

    getCurrent  $\leftarrow$  it.list.nodes[it.currentElement].info

**end-subalgorithm**

- Complexity:

**subalgorithm** getCurrent(it) **is:**

*//pre: it is a DLLAlterator, it is valid*

*//post: e is a TElem, e is the current element from it*

*//throws exception if the iterator is not valid*

**if** it.currentElement = -1 **then**

    @throw exception

**end-if**

    getCurrent  $\leftarrow$  it.list.nodes[it.currentElement].info

**end-subalgorithm**

- Complexity:  $\Theta(1)$

**subalgorithm** next (it) **is:**

*//pre: it is a DLLAlterator, it is valid*

*//post: the current elements from it is moved to the next element*

*//throws exception if the iterator is not valid*

**if** it.currentElement = -1 **then**

    @throw exception

**end-if**

it.currentElement  $\leftarrow$  it.list.nodes[it.currentElement].next

**end-subalgorithm**

- In case a (dynamic) array, going to the next element means incrementing the *currentElement* by one. For a DLLA we need to follow the links.
- Complexity:

**subalgorithm** next (it) **is:**

*//pre: it is a DLLAlterator, it is valid*

*//post: the current elements from it is moved to the next element*

*//throws exception if the iterator is not valid*

**if** it.currentElement = -1 **then**

    @throw exception

**end-if**

it.currentElement  $\leftarrow$  it.list.nodes[it.currentElement].next

**end-subalgorithm**

- In case a (dynamic) array, going to the next element means incrementing the *currentElement* by one. For a DLLA we need to follow the links.
- Complexity:  $\Theta(1)$

**function** valid (it) **is:**

*//pre: it is a DLLAlterator*

*//post: valid return true is the current element is valid, false otherwise*

**if** it.currentElement = -1 **then**

valid  $\leftarrow$  False

**else**

valid  $\leftarrow$  True

**end-if**

**end-function**

- Complexity:



**function** valid (it) **is:**

*//pre: it is a DLLAlterator*

*//post: valid return true is the current element is valid, false otherwise*

**if** it.currentElement = -1 **then**

    valid  $\leftarrow$  False

**else**

    valid  $\leftarrow$  True

**end-if**

**end-function**

- Complexity:  $\Theta(1)$