

Please check the examination details below before entering your candidate information

Candidate surname

Other names

**Pearson Edexcel  
Level 3 GCE**

Centre Number

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Candidate Number

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**Thursday 08 October 2020**

Afternoon

Paper Reference **8FM0/25**

## **Further Mathematics**

**Advanced Subsidiary**

**Further Mathematics options**

**25: Further Mechanics 1**

**(Part of options C, E, H and J)**

**You must have:**

Mathematical Formulae and Statistical Tables (Green), calculator

Total Marks

**Candidates may use any calculator allowed by Pearson regulations.**

**Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

### **Instructions**

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
  - *there may be more space than you need.*
- You should show sufficient working to make your methods clear.  
Answers without working may not gain full credit.
- Unless otherwise indicated, whenever a value of  $g$  is required, take  $g = 9.8 \text{ m s}^{-2}$  and give your answer to either 2 significant figures or 3 significant figures.

### **Information**

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- The total mark for this part of the examination is 40. There are 4 questions.
- The marks for **each** question are shown in brackets
  - *use this as a guide as to how much time to spend on each question.*

### **Advice**

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

**Turn over** ►

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**Pearson**

1. Two particles  $P$  and  $Q$  have masses  $m$  and  $4m$  respectively. The particles are at rest on a smooth horizontal plane. Particle  $P$  is given a horizontal impulse, of magnitude  $I$ , in the direction  $PQ$ . Particle  $P$  then collides directly with  $Q$ . Immediately after this collision,  $P$  is at rest and  $Q$  has speed  $w$ . The coefficient of restitution between the particles is  $e$ .

(a) Find  $I$  in terms of  $m$  and  $w$ . (2)

(b) Show that  $e = \frac{1}{4}$  (1)

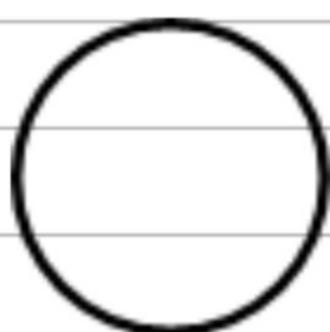
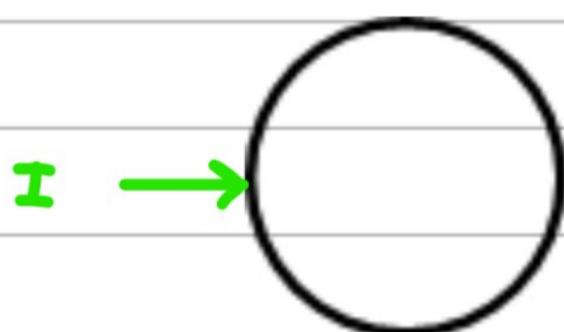
(c) Find, in terms of  $m$  and  $w$ , the total kinetic energy lost in the collision between  $P$  and  $Q$ . (2)

**BEFORE**

$$\frac{I}{m} = \frac{4mw}{m} = 4w \text{ ms}^{-1}$$

$$0 \text{ ms}^{-1}$$

**AFTER**



**IMPULSE = CHANGE IN MOMENTUM**

= MASS × CHANGE IN VELOCITY

$$I = m(\frac{I}{m} - 0)$$

$$\text{CLM: } (m)(\frac{I}{m}) + (4m)(0) = (m)(0) + (4m)(w)$$

$$\therefore I = 4mw$$

**(b) NLR :  $e = \frac{\text{SPEED OF SEPARATION}}{\text{SPEED OF APPROACH}}$**

$$= \frac{w}{4w}$$

$$= \frac{1}{4}$$

**(c) KE BEFORE =  $\frac{1}{2}(m)(4w)^2$**



**Question 1 continued**

$$= 8m\omega^2 \text{ J}$$

$$\text{KE AFTER} = \frac{1}{2}(4m)(\omega)^2$$

$$= 2m\omega^2 \text{ J}$$

$$\therefore \text{KE LOST} = 8m\omega^2 - 2m\omega^2$$

$$= 6m\omega^2$$

(Total for Question 1 is 5 marks)



2. A car of mass 1000 kg moves along a straight horizontal road.

In all circumstances, when the speed of the car is  $v \text{ m s}^{-1}$ , the resistance to the motion of the car is modelled as a force of magnitude  $cv^2 \text{ N}$ , where  $c$  is a constant.

The maximum power that can be developed by the engine of the car is 50 kW.

At the instant when the speed of the car is  $72 \text{ km h}^{-1}$  and the engine is working at its maximum power, the acceleration of the car is  $2.25 \text{ m s}^{-2}$

- (a) Convert  $72 \text{ km h}^{-1}$  into  $\text{m s}^{-1}$  (1)

- (b) Find the acceleration of the car at the instant when the speed of the car is  $144 \text{ km h}^{-1}$  and the engine is working at its maximum power. (7)

The maximum speed of the car when the engine is working at its maximum power is  $V \text{ km h}^{-1}$ .

- (c) Find, to the nearest whole number, the value of  $V$ . (4)

$$(a) 72 \frac{\text{km}}{\text{hr}} = 72 \times \frac{1000}{3600} = 20 \frac{\text{m}}{\text{s}}$$

$$(b) 144 \frac{\text{km}}{\text{hr}} = 144 \times \frac{1000}{3600} = 40 \frac{\text{m}}{\text{s}}$$



$$P = Fv : 50000 = 20F \therefore F = 2500 \text{ N}$$

$$\sum \text{FORCES} = ma : F - cv^2 = ma$$

$$2500 - c(20)^2 = 1000 \times 2.25$$

$$2500 - 400c = 2250$$

$$400c = 250 \therefore c = \frac{5}{8}$$

$$P = Fv : 50000 = 40F \therefore F = 1250$$



Question 2 continued

$$\sum \text{FORCES} = m\alpha : 1250 - \frac{5}{8}(40)^2 = 1000 \alpha$$

$$250 = 1000 \alpha \quad \therefore \alpha = 0.25 \text{ ms}^{-2}$$

$$V \frac{\text{Km}}{\text{hr}} = \frac{1000V}{3600} = \frac{5V}{18} \frac{\text{m}}{\text{s}}$$

$$P = Fv : 50000 = F \times \frac{5V}{18} \quad \therefore F = \frac{50000}{5V/18} = \frac{180000}{V}$$

MAXIMUM SPEED IMPLIES  $\alpha = 0$

$$\sum \text{FORCES} = m\alpha : \frac{180000}{V} - \frac{5}{8} \left( \frac{5V}{18} \right)^2 = 1000 \times 0$$

$$\frac{180000}{V} = \frac{125V^2}{2592}$$

$$V^3 = 3732480 \quad \therefore V = 155 \text{ (NEAREST WHOLE NUMBER)}$$



3. Three particles  $A$ ,  $B$  and  $C$  are at rest on a smooth horizontal plane. The particles lie along a straight line with  $B$  between  $A$  and  $C$ .

Particle  $B$  has mass  $4m$  and particle  $C$  has mass  $km$ , where  $k$  is a positive constant. Particle  $B$  is projected with speed  $u$  along the plane towards  $C$  and they collide directly.

The coefficient of restitution between  $B$  and  $C$  is  $\frac{1}{4}$

(a) Find the range of values of  $k$  for which there would be no further collisions.

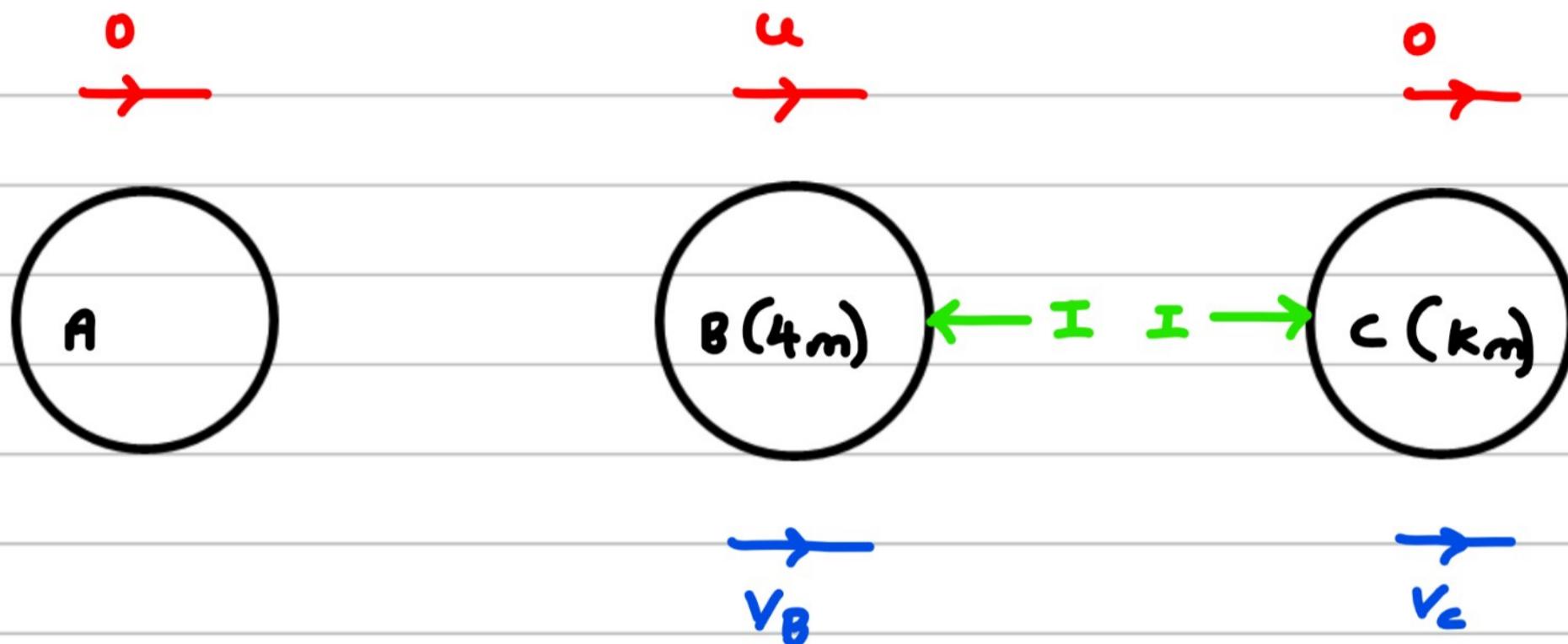
(8)

The magnitude of the impulse on  $B$  in the collision between  $B$  and  $C$  is  $3mu$

(b) Find the value of  $k$ .

(4)

(a)



$$\text{CLM} : (4m)(u) + (km)(0) = (4m)(v_B) + (km)(v_C)$$

$$4mu = 4mv_B + kmv_C$$

$$4u = 4v_B + kv_C \quad \textcircled{1}$$

$$\text{NLR} : e = \frac{\text{SPEED OF SEPARATION}}{\text{SPEED OF APPROACH}}$$

$$\frac{v_C - v_B}{u} = \frac{1}{4}$$

$$v_C - v_B = \frac{u}{4} \quad \textcircled{2}$$

$$4v_C - 4v_B = u \quad \textcircled{3}$$

$$\textcircled{1} + \textcircled{3} : 5u = kv_C + 4v_C$$

Question 3 continued

$$5u = V_c(k + 4)$$

$$\therefore V_c = \frac{5u}{k+4} \quad \textcircled{4}$$

$$\text{From } \textcircled{2}: V_B = V_c - \frac{u}{4} \quad \textcircled{5}$$

$$\textcircled{4} \text{ INTO } \textcircled{5}: V_B = \frac{5u}{k+4} - \frac{u}{4}$$

$$= \frac{4(5u) - u(k+4)}{4(k+4)}$$

$$= \frac{20u - uk - 4u}{4(k+4)}$$

$$= \frac{16u - uk}{4(k+4)}$$

$$\therefore V_B = \frac{u(16-k)}{4(k+4)} \quad \textcircled{6}$$

$$\text{as } V_B \geq 0, \frac{u(16-k)}{4(k+4)} \geq 0 \quad \therefore k \leq 16$$

$$\therefore 0 < k \leq 16$$

IMPULSE ON C BY B IS  $I = 3mu$

$$\text{i.e. } 3mu = km(V_c - 0)$$

$$3mu = km\left(\frac{5u}{k+4}\right)$$



Question 3 continued

$$3 = \frac{5k}{k+4}$$

$$3(k+4) = 5k$$

$$3k + 12 = 5k$$

$$2k = 12 \therefore k = 6$$

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4. A small ball, of mass  $m$ , is thrown vertically upwards with speed  $\sqrt{8gH}$  from a point  $O$  on a smooth horizontal floor. The ball moves towards a smooth horizontal ceiling that is a vertical distance  $H$  above  $O$ . The coefficient of restitution between the ball and the ceiling is  $\frac{1}{2}$

In a model of the motion of the ball, it is assumed that the ball, as it moves up or down, is subject to air resistance of constant magnitude  $\frac{1}{2}mg$ .

Using this model,

- (a) use the work-energy principle to find, in terms of  $g$  and  $H$ , the speed of the ball immediately before it strikes the ceiling,

(5)

- (b) find, in terms of  $g$  and  $H$ , the speed of the ball immediately before it strikes the floor at  $O$  for the first time.

(5)

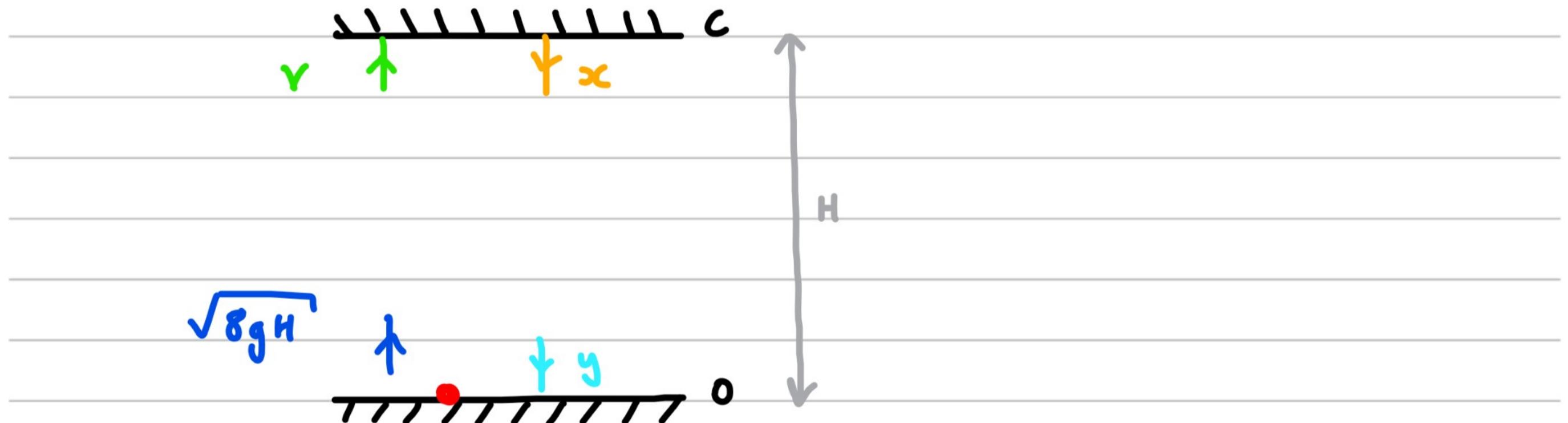
In a simplified model of the motion of the ball, it is assumed that the ball, as it moves up or down, is subject to no air resistance.

Using this simplified model,

- (c) explain, without any detailed calculation, why the speed of the ball, immediately before it strikes the floor at  $O$  for the first time, would still be less than  $\sqrt{8gH}$

(1)

(a)



$$\text{INITIAL KE} = \text{FINAL KE} + \text{FINAL GPE} + \text{WORK DONE AGAINST RES.}$$

$$\frac{1}{2} \times m \times \sqrt{8gH}^2 = \frac{1}{2} m v^2 + mgH + \frac{1}{2} m g H$$

$$\frac{1}{2} \times 8gH = \frac{1}{2} v^2 + gH + \frac{1}{2} g H$$

$$v^2 = 5gH \quad \therefore v = \sqrt{5gH}$$

(b)

$$\text{NLR: } e = \frac{\text{SPEED OF REBOUND}}{\text{SPEED OF APPROACH}}$$

Question 4 continued

$$\frac{1}{2} = \frac{x}{\sqrt{5gH}}$$

$$\therefore x = \frac{1}{2}\sqrt{5gH}$$

INITIAL KE + INITIAL GPE = FINAL KE + WORK DONE AGAINST RES.

$$\frac{1}{2}mv^2 + mgH = \frac{1}{2}mv^2 + \frac{1}{2}mgH$$

$$\frac{1}{2} \cdot \frac{5}{4}gH + gH = \frac{1}{2}v^2 + \frac{1}{2}gH$$

$$v^2 = \frac{1}{4}gH \quad \therefore v = \frac{1}{2}\sqrt{gH}$$

(c) NLR: SPEED OF REBOUND = e × SPEED OF APPROACH

AS  $e < 1$ , SPEED OF REBOUND < SPEED OF APPROACH

$$\therefore x < v$$

$\therefore$  KE LOST WHEN BALL HITS CEILING

$$\therefore v < \sqrt{8gH}$$

