Please check the examination deta	ils below before er	ntering your candidate information
Candidate surname		Other names
	Centre Numbe	Candidate Number
Pearson Edexcel	Centre Number	Candidate Number
Level 3 GCE		
<b>Monday 5 Oct</b>	+ 2020	
Monday 5 Oc	1 2020	
Afternoon (Time: 1 hour 40 minu	tes) Paper	Reference <b>8FM0/01</b>
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Advanced Subsidiary	matics	
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Advanced Subsidiary	matics	Total Mark:

Candidates may use any calculator allowed by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

## Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer all questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
  - there may be more space than you need.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

## Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 10 questions in this question paper. The total mark for this paper is 80.
- The marks for **each** question are shown in brackets
  - use this as a guide as to how much time to spend on each question.

## Advice

- Read each guestion carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ▶







1. A system of three equations is defined by

$$kx + 3y - z = 3$$

$$3x - y + z = -k$$

$$-16x - ky - kz = k$$

where k is a positive constant.

Given that there is no unique solution to all three equations,

(a) show that k = 2

**(2)** 

Using k = 2

(b) determine whether the three equations are consistent, justifying your answer.

**(3)** 

(c) Interpret the answer to part (b) geometrically.

**(1)** 


Question 1 continued	
(Total for Ques	tion 1 is 6 marks)



2. Given that

$$z_1 = 2 + 3i$$
$$|z_1 z_2| = 39\sqrt{2}$$
$$\arg(z_1 z_2) = \frac{\pi}{4}$$

where  $z_1$  and  $z_2$  are complex numbers,

(a) write  $z_1$  in the form  $r(\cos\theta + i\sin\theta)$ 

Give the exact value of r and give the value of  $\theta$  in radians to 4 significant figures.

**(2)** 

(b) Find  $z_2$  giving your answer in the form a + ib where a and b are integers.

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Question 2 continued
(Total for Question 2 is 8 marks)
(20mi for Question 2 is 6 marks)



Figure 1

Figure 1 shows a circle with radius r and centre at the origin.

The region R, shown shaded in Figure 1, is bounded by the x-axis and the part of the circle for which y > 0

The region R is rotated through  $360^{\circ}$  about the x-axis to create a sphere with volume V

Use integration to show that  $V = \frac{4}{3}\pi r^3$ 

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Question 3 continued	
/T-4-1	for Question 2 is 5 mayles)
(lotal	for Question 3 is 5 marks)



## All units in this question are in metres.

A lawn is modelled as a plane that contains the points L(-2, -3, -1), M(6, -2, 0) and N(2, 0, 0), relative to a fixed origin O.

(a) Determine a vector equation of the plane that models the lawn, giving your answer in the form  $\mathbf{r} = \mathbf{a} + \lambda \mathbf{b} + \mu \mathbf{c}$ 

**(3)** 

- (b) (i) Show that, according to the model, the lawn is perpendicular to the vector  $\begin{pmatrix} 1 \\ 2 \\ -10 \end{pmatrix}$ 
  - (ii) Hence determine a Cartesian equation of the plane that models the lawn.

**(4)** 

There are two posts set in the lawn.

4.

There is a washing line between the two posts.

The washing line is modelled as a straight line through points at the top of each post with coordinates P(-10, 8, 2) and Q(6, 4, 3).

(c) Determine a vector equation of the line that models the washing line.

**(2)** 

(d) State a limitation of one of the models.

**(1)** 

The point R(2, 5, 2.75) lies on the washing line.

(e) Determine, according to the model, the shortest distance from the point R to the lawn, giving your answer to the nearest cm.

**(2)** 

Given that the shortest distance from the point R to the lawn is actually 1.5 m,

(f) use your answer to part (e) to evaluate the model, explaining your reasoning.

**(1)** 

Question 4 continued



Question 4 continued

Question 4 continued	
	(Total for Question 4 is 13 marks)



Figure 2

A block has length (r+2) cm, width (r+1) cm and height r cm, as shown in Figure 2.

In a set of n such blocks, the first block has a height of 1 cm, the second block has a height of 2 cm, the third block has a height of 3 cm and so on.

(a) Use the standard results for  $\sum_{r=1}^{n} r^3$ ,  $\sum_{r=1}^{n} r^2$  and  $\sum_{r=1}^{n} r$  to show that the **total** volume, V, of all n blocks in the set is given by

$$V = \frac{n}{4}(n+1)(n+2)(n+3) \qquad n \geqslant 1$$
(5)

Given that the total volume of all *n* blocks is

$$(n^4 + 6n^3 - 11710)$$
 cm<sup>3</sup>

(b) determine how many blocks make up the set.

**(2)** 

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Question 5 continued	



Question 5 continued	

Question 5 continued	
(	Total for Question 5 is 7 marks)



**6.** (i)

$$\mathbf{A} = \begin{pmatrix} 2 & a \\ a - 4 & b \end{pmatrix}$$

where a and b are non-zero constants.

Given that the matrix A is self-inverse,

(a) determine the value of b and the possible values for a.

**(5)** 

The matrix A represents a linear transformation M.

Using the smaller value of a from part (a),

(b) show that the invariant points of the linear transformation M form a line, stating the equation of this line.

(3)

(ii)

$$\mathbf{P} = \begin{pmatrix} p & 2p \\ -1 & 3p \end{pmatrix}$$

where p is a positive constant.

The matrix  $\mathbf{P}$  represents a linear transformation U.

The triangle T has vertices at the points with coordinates (1, 2), (3, 2) and (2, 5).

The area of the image of T under the linear transformation U is 15

(a) Determine the value of p.

**(4)** 

The transformation V consists of a stretch scale factor 3 parallel to the x-axis with the y-axis invariant followed by a stretch scale factor -2 parallel to the y-axis with the x-axis invariant. The transformation V is represented by the matrix  $\mathbf{Q}$ .

(b) Write down the matrix **Q**.

**(2)** 

Given that U followed by V is the transformation W, which is represented by the matrix  $\mathbf{R}$ ,

(c) find the matrix  $\mathbf{R}$ .

**(2)** 



Question 6 continued



Question 6 continued

Question 6 continued	
	(Total for Question 6 is 16 marks)



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$$f(z) = z^4 + az^3 + bz^2 + cz + d$$

where a, b, c and d are real constants.

The equation f(z) = 0 has complex roots  $z_1, z_2, z_3$  and  $z_4$ When plotted on an Argand diagram, the points representing  $z_1$ ,  $z_2$ ,  $z_3$  and  $z_4$  form the vertices of a square, with one vertex in each quadrant. Given that  $z_1 = 2 + 3i$ , determine the values of a, b, c and d.

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Question 7 continued	
	(Total for Question 7 is 6 marks)



Q	Prove by induction that, for $n \in \mathbb{Z}^+$		
0.	There by induction that, for $n \in \mathbb{Z}$	C( ) 2n+2 + 22n+1	
	i. 41ii 1 7	$f(n) = 2^{n+2} + 3^{2n+1}$	
	is divisible by 7		(6)

Question 8 continued	
(10t	al for Question 8 is 6 marks)



9. The cubic equation

$$3x^3 + x^2 - 4x + 1 = 0$$

has roots  $\alpha$ ,  $\beta$ , and  $\gamma$ .

Without solving the cubic equation,

(a) determine the value of  $\frac{1}{\alpha} + \frac{1}{\beta} + \frac{1}{\gamma}$ 

- (3)
- (b) find a cubic equation that has roots  $\frac{1}{\alpha}$ ,  $\frac{1}{\beta}$  and  $\frac{1}{\gamma}$ , giving your answer in the form

 $x^3 + ax^2 + bx + c = 0$ , where a, b and c are integers to be determined.



Question 9 continued	
	(Total for Question 9 is 6 marks)



10. Given that there are two distinct complex numbers z that satisfy

$${z:|z-3-5i|=2r} \cap {z:arg(z-2)=\frac{3\pi}{4}}$$

determine the exact	range of values	for the real	constant r.
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Question 10 continued



Question 10 continued	
(Total for Question 10 is 7 marks)	
TOTAL FOR CORE PURE MATHEMATICS IS 80 MARKS	

