MODEL ANSWERS

Write your name here		
Surname		Other names
Pearson Edexcel Level 3 GCE	Centre Number	Candidate Number
Further M Advanced Subsidiary Further Mathematics of 25: Further Mechanics (Part of options C, E, F)	options 3 1	matics
Thursday 17 May 2018 – Af	ternoon	Paper Reference 8FM0-25
You must have: Mathematical Formulae and Sta	atistical Tables, ca	Total Marks alculator

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use black ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer all questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
 there may be more space than you need.
- You should show sufficient working to make your methods clear.
 Answers without working may not gain full credit.
- Answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- The total mark for this part of the examination is 40. There are 4 questions.
- The marks for each question are shown in brackets
 use this as a guide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ▶



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Whenever a numerical value of g is required, take $g = 9.8 \,\mathrm{m\,s^{-2}}$ and give your answer to either 2 significant figures or 3 significant figures.

Answer ALL questions. Write your answers in the spaces provided.

1. A small ball of mass 0.3 kg is released from rest from a point 3.6 m above horizontal ground. The ball falls freely under gravity, hits the ground and rebounds vertically upwards.

In the first impact with the ground, the ball receives an impulse of magnitude 4.2 Ns. The ball is modelled as a particle.

(a) Find the speed of the ball immediately after it first hits the ground.

(5)

(b) Find the kinetic energy lost by the ball as a result of the impact with the ground.

(3)

(a)	To find speed	of ball just before
1 (0.3 kg)	hitting the gr	of ball just before ound (v)
	0 ()	(is tve)
	S = 3.6	
3.6m	u = 0	$V^2 = u^2 + 2as$
	∨ = ?	$\sqrt{2} = 0^2 + 2 \times 9.8 \times 3.6$
	$\alpha = 9.8$	$V = \sqrt{70.56}$
	t =	$= 8.4 \text{ ms}^{-1}$
7///////	/ /	

To find speed of ball just after hitting the ground (
$$\omega$$
)

Change in momentum = $I = m\omega - m\nu$ (\uparrow is + ν e)

 $4.2 = 0.3\omega - 0.3 \times (-8.4)$
 $\omega = 1.68 = 5.6 \text{ ms}^{-1}$

b) KE lost during impact =
$$\frac{1}{2}mv^2 - \frac{1}{2}m\omega^2$$

= $\frac{1}{2} \times 0.3 (8.4^2 - 5.6^2)$
= 5.88 J

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Question 1 continued	
	(Total for Question 1 is 8 marks)
	(Total for Question 1 is 6 marks)



2.

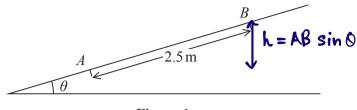


Figure 1

Figure 1 shows a ramp inclined at an angle θ to the horizontal, where $\sin \theta = \frac{2}{7}$

A parcel of mass 4 kg is projected, with speed 5 m s⁻¹, from a point A on the ramp. The parcel moves up a line of greatest slope of the ramp and first comes to instantaneous rest at the point B, where AB = 2.5 m.

The parcel is modelled as a particle.

The total resistance to the motion of the parcel from non-gravitational forces is modelled as a constant force of magnitude R newtons.

(a) Use the work-energy principle to show that R = 8.8

(4)

After coming to instantaneous rest at *B*, the parcel slides back down the ramp. The total resistance to the motion of the particle is modelled as a constant force of magnitude 8.8 N.

(b) Find the speed of the parcel at the instant it returns to A.

(3)

(c) Suggest two improvements that could be made to the model.

(2)

$$\frac{1}{2} \times 4 \times 5^2 = 4 \times 9.8 \times 2.5 \times \frac{2}{7} + 2.5 R$$

$$2.5R = 22$$

b) Using the Work-Energy Principle for pared sliding down

CIPE at B = KE at A + Work done by non-grav. forces

PMT

Question 2 continued

$$mg \times AB \sin 0 = \frac{1}{2}mv^2 + 8.8 \times AB$$

$$4 \times 9.8 \times 2.5 \times \frac{2}{7} = \frac{1}{2} \times 4 \times v^2 + 8.8 \times 2.5$$

$$2v^{2} = 6$$

 $v = \sqrt{3}$
 $v \approx 1.7 \text{ ms}^{-1}$ (To 2 s.f.)

A drag force (air resistance) proportional to the parcel's speed can be included



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Question 2 continued

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Question 2 continued	
	(Total for Question 2 is 9 marks)
	(20mi ioi Question 2 is / marks)



3. A van of mass 750 kg is moving along a straight horizontal road. At the instant when the van is moving at $v \, \text{m s}^{-1}$, the resistance to the motion of the van is modelled as a force of magnitude $\lambda v \, \text{N}$, where λ is a constant.

The engine of the van is working at a constant rate of 18 kW. At the instant when v = 15, the acceleration of the van is $0.6 \,\text{m}\,\text{s}^{-2}$

(a) Show that $\lambda = 50$

(4)

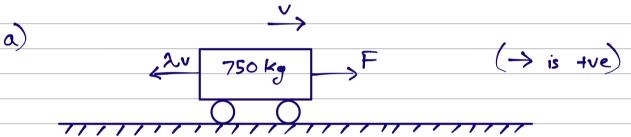
The van now moves up a straight road inclined at an angle to the horizontal, where $\sin \alpha = \frac{1}{15}$

At the instant when the van is moving at $v \, \text{m s}^{-1}$, the resistance to the motion of the van from non-gravitational forces is modelled as a force of magnitude $50v \, \text{N}$. When the engine of the van is working at a constant rate of $12 \, \text{kW}$ the van is moving at

When the engine of the van is working at a constant rate of 12 kW, the van is moving at a constant speed $V \, \mathrm{m} \, \mathrm{s}^{-1}$

(b) Find the value of V.

(5)



Let F be the forward force on the van generated by the engine (of Power P)

$$P = F_V$$

 $F = P$

Ising Newton's 2nd Law:

$$\frac{P}{V} - \lambda V = ma$$

When
$$v=15$$
, $\alpha=0.6$

$$\frac{18000}{15} = 750 \times 0.6$$

Question 3 continued

$$1200 - 15\lambda = 450$$

$$\lambda = 50$$

b) / / is +ve)

Using Newton's 2nd Law, resolving up the ramp

$$F - 50 V - mg sin x = ma$$

$$\frac{12000 - 50V - 750 \times 9.8 \times 1}{V} = 0$$

$$50V^2 + 490V - 12000 = 0$$

$$5V^2 + 49V - 1200 = 0$$

$$V = -49 \pm \sqrt{49^2 + 4 \times 5 \times 1200}$$

$$2 \times 5$$

Since van is going up hill, take positive root
$$\Rightarrow V = 11.3$$

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Question 3 continued	
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Question 3 continued	
	(Total for Question 3 is 9 marks)
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4. A particle P of mass 3m is moving in a straight line on a smooth horizontal floor. A particle Q of mass 5m is moving in the opposite direction to P along the same straight line.

The particles collide directly.

Immediately before the collision, the speed of P is 2u and the speed of Q is u. The coefficient of restitution between P and Q is e.

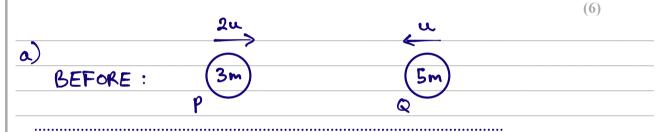
- (a) Show that the speed of Q immediately after the collision is $\frac{u}{8}(9e+1)$
- (b) Find the range of values of *e* for which the direction of motion of *P* is not changed as a result of the collision.

(2)

When P and Q collide they are at a distance d from a smooth fixed vertical wall, which is perpendicular to their direction of motion. After the collision with P, particle Q collides directly with the wall and rebounds so that there is a second collision between P and Q. This second collision takes place at a distance x from the wall.

Given that $e = \frac{1}{18}$ and the coefficient of restitution between Q and the wall is $\frac{1}{3}$

(c) find x in terms of d.





$$3mV_1 + 5mV_2 = 6mu - 5mu$$

$$3V_1 + 5V_2 = u \longrightarrow 1$$

$$e = \frac{V_2 - V_1}{2u + u} \Rightarrow V_2 - V_1 = 3eu \longrightarrow 2$$



Question 4 continued

To solve this system of linear equations.

$$1 + 3 \times 2 : 5 = 4 + 9 = 4$$

$$1 + 3 \times 2 : 5 = 4 + 9 = 4$$

$$1 + 3 \times 2 : 5 = 4 + 9 = 4$$

$$1 + 3 \times 2 : 5 = 4 + 9 = 4$$

= Speed of Q just after collision

$$=\frac{9}{8}eu + u - 3eu$$

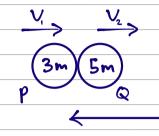
= $u (1-15e)$

If direction of Pis unchanged,

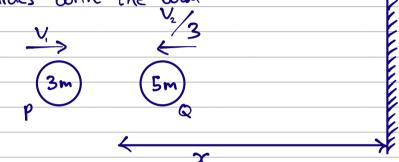
Since u #0 (or else the collision would not have happened

Question 4 continued

Just after 1st collision:



After Q collides with the wall:



d

In the time taken for Q to travel d+x, P travels d-x

Time elapsed = Time elapsed for Q for P

$$\frac{d}{\sqrt{2}} + \frac{x}{\sqrt{2}/3} = \frac{d-x}{\sqrt{1}}$$

$$\frac{d+3x}{\sqrt{3}} = \frac{d-x}{\sqrt{3}}$$

$$\frac{\sqrt{3}}{\sqrt{3}} = \frac{d-x}{\sqrt{3}}$$

Since
$$e = \frac{1}{18}$$
,

$$\frac{d+3x}{\left(\frac{1}{2}+1\right)} = \frac{d-x}{\left(1-\frac{15}{18}\right)}$$

$$\frac{d+3x}{3/2} = \frac{d-x}{3/18}$$

Question 4 continued

$$2d+6x = 18d-18x$$

 $24x = 16d$
 $x = \frac{2}{3}d$

Question 4 continued
(Total for Question 4 is 14 marks)
TOTAL FOR FURTHER MECHANICS 1 IS 40 MARKS