

Functional and logic programming

- written exam -

Important:

1. Subjects are graded as follows: of - 1p; A – 1.5p; B - 2.5p; C - 2.5p; D - 2.5p.
2. Prolog problems will be resolved using SWI Prolog. The following are required: (1) explanation of the code and of the reasoning behind it; (2) recursive model that solves the problem, for all the predicates used; (3) specification of every predicate (parameters and their meaning, flow model, type of the predicate - deterministic/non-deterministic).
3. Lisp problems will be resolved using Common Lisp. The following are required: (1) explanation of the code and of the reasoning behind it; (2) recursive model that solves the problem, for each function used; (3) specification of every function (parameters and their meaning).

A. The following function definition in LISP is given

```
(DEFUN F(L)
  (COND
    ((NULL L) 0)
    (> (F (CAR L)) 2) (+ (F (CDR L)) (F (CAR L))))
    (T (+ (F (CAR L)) 1))
  )
)
```

Rewrite the definition in order to avoid the repeated recursive call **(F (CAR L))**. Do NOT redefine the function. Do NOT use SET, SETQ, SETF. Justify your answer.

B. Given a list composed of only sublists that contain positive digits, write a SWI-Prolog program that computes the greatest even number that can be formed picking one digit from each sublist. The digits in the resulted number must be in the same order as in the sublists they come from. Each sublist will contain at least one even digit. For example, for the list `[[2,5,1,9], [7,2,1], [9,4,6,5], [2,6,0,7]]` the result will be 9796.

C. Write a PROLOG program that generates the list of all combinations of k elements with the value of sum of each combination even number, from a list of integers. Write the mathematical models and flow models for the predicates used. For example, for the list $L[6, 5, 3, 4]$, $k=2 \Rightarrow [[6,4],[5,3]]$ (not necessarily in this order).

D. Given a nonlinear list, write a Lisp function to return the list with all non-numerical atoms on even levels removed. The superficial level is assumed 1. **A MAP function shall be used.**

Example for the list (a (1 (2 b)) (c (d))) the result is (a (1 (2 b)) ((d)))