

Figure 1: (Left) A current I experiences a force F in a B -field.

2 Chapter 11: Magnetic Forces and Fields

1. Consider Fig. 1 (left). In each of the three cases, determine the direction of the B -field given that F is the Lorentz force.

- a: into page
- b: left
- c: out of page

2. Consider Fig. 1 (right). **The Hall Effect.** An E -field exists in the vertical direction and a B -field is perpendicular to the direction of charge velocity. (a) Show that if the E -field force on a charge balances the Lorentz force on a charge, that $v = E/B$. (b) If the E -field is constant, $E = \Delta V/\Delta x$. Show that

$$a) F = q\vec{v} \times \vec{B} = FB = q\vec{v} \times \vec{B} \quad \Delta V = \frac{B\Delta x I}{nq_e A} \quad (1)$$

$$FE = qB = \frac{qE}{v} = E = vB$$

where n is the charge carrier density, q_e is the electron charge, A is the cross-sectional area of the conductor, and I is the current. Plug in $B = 1.33 \text{ T}$, $\Delta x = 2 \text{ cm}$, $I = 10 \text{ A}$, $n = 2 \times 10^{28} \text{ m}^{-3}$, $A = 1 \text{ mm}^2$, and q_e is the charge of an electron.

$$B = 1.33$$

$$\Delta x = 0.02 \text{ m}$$

$$I = 10 \text{ A}$$

$$n = 2 \times 10^{28}$$

$$A = 1 \times 10^{-6}$$

$$q_e = 1.6 \times 10^{-19}$$

$$\Delta V = \frac{(1.33)(0.02)(10)}{(2 \times 10^{28})(1.6 \times 10^{-19})(1 \times 10^{-6})} = 8.3 \times 10^{-5} \text{ V}$$

3. A proton has a magnetic field due to its spin. The field is similar to that created by a circular current loop $0.65 \times 10^{-15} \text{ m}$ in radius with a current of $1.05 \times 10^4 \text{ A}$. Find the maximum torque on a proton in a 2.50-T field. (This is a significant torque on a small particle.)

$$\tau = IAB$$

$$\tau = (1.05 \times 10^4)(1.3 \times 10^{-30})(2.50) = 3.4 \times 10^{-26} \text{ N}\cdot\text{m} \quad A = \pi r^2 = 3.14(0.65 \times 10^{-15})^2 = 1.3 \times 10^{-30}$$

$$I = 1.05 \times 10^4 \text{ A}$$

$$B = 2.5 \text{ T}$$

3 Chapter 12: Sources of Magnetic Fields

1. (a) What is the B -field inside a solenoid with 500 turns per meter, carrying a current of 0.3 A ? (b) Suppose we insert a piece of metal inside the solenoid, boosting μ_0 by a factor of 5000. What is the new B -field?

$$a) B = \mu_0 n I = (4\pi \times 10^{-7})(500)(0.3) = 1.88 \times 10^{-4} \text{ T} \quad \mu_0 = 4\pi \times 10^{-7}$$

$$b) B = ((5000)(4\pi \times 10^{-7}))(500)(0.3) = 0.94 \text{ T} \quad n = 500$$

$$I = 0.3 \text{ A}$$

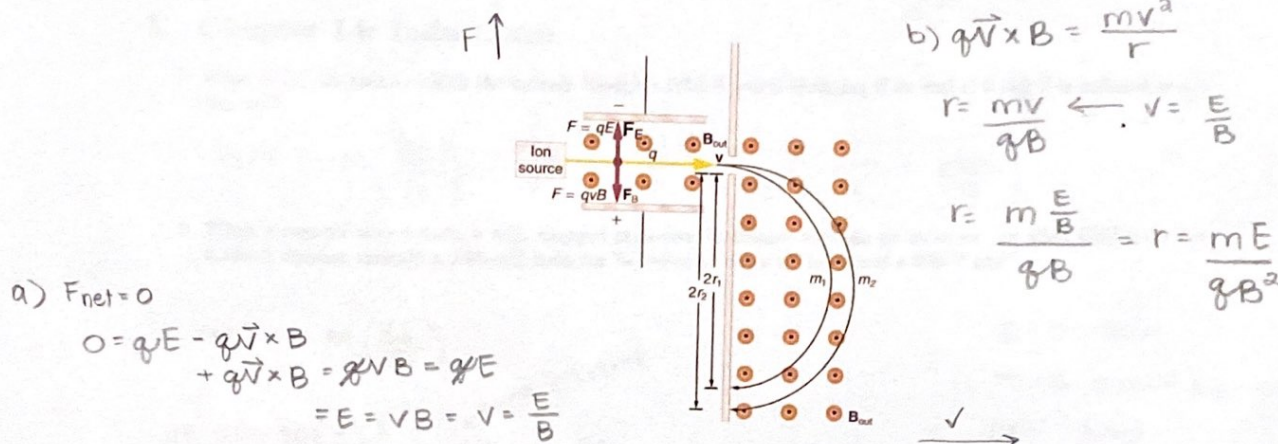


Figure 2: A basic diagram of a *toroid*, which is a solenoid wrapped into a circular tube.

2. Consider Fig. 2. **Mass spectrometer.** Suppose that the velocity of the charged particles moving to the right is $v = E/B$. (a) Show that if $v = E/B$, $F_{net} = 0$ in the region in the top left¹. (b) Recall that the centripetal force on a particle of mass m is mv^2/r . Set this equal to the magnitude of the Lorentz force to prove that

$$r = \frac{mE}{qB^2} \quad (2)$$

The mass of an oxygen nucleus is 16 times that of a proton (mass of proton: 1.67×10^{-27} kg). Suppose oxygen ions with the charge of 1 proton are sent through the mass-sepectrometer. The E-field is 10 V/m, and the B-field is 0.01 T. What is the distance r ?

$$r = \frac{(2.7 \times 10^{-26})(10)}{(1.6 \times 10^{-19})(0.01)^2} = 0.017 \text{ m}$$

$$\text{Emf} = 10 \frac{\text{V}}{\text{m}}$$

$$B = 0.01 \text{ T}$$

$$m = 16(1.67 \times 10^{-27})$$

$$= 2.7 \times 10^{-26}$$

4 Chapter 13: Electromagnetic Induction

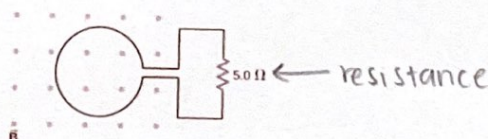


Figure 3: A voltage is induced on a loop by a changing B-field.

1. The magnetic field in Fig. 3 flows out of the page through a single ($N = 1$) loop, and changes in magnitude according to

$$\frac{\Delta B}{\Delta t} = \frac{B_0}{T_0} (\sin(2\pi ft)) \quad (3)$$

The loop has a radius r . (a) In terms of the given variables, what is the induced voltage in the circuit? (b) If $B_0 = 0.1$ T, $r = 0.1$ m, $f = 10^3$ Hz, and $T = 1$ ms, what is the induced emf at $t = 0$? (c) What about $t_1 = 0.16$ ms? (d) What is the current through the resistor at t_1 ?

a) $E = -N \left(\frac{d\Phi}{dt} \right) = -1 \left(\frac{d(BA)}{dt} \right)$

$$= E = \pi r^2 \frac{B_0}{T_0} (\sin(2\pi ft))$$

b) $\sin(2\pi ft)$
 $t = 0$
 $\text{emf} = 0$

c) $B_0 = 0.1 \text{ T}$
 $r = 0.1 \text{ m}$
 $f = 10^3$
 $T_0 = 1 \times 10^{-6}$
 $t_1 = 0.16 \times 10^{-3}$

¹ Molecules that do not have this velocity will hit the sides of this portion of the instrument.

$$\pi (0.1)^2 \left(\frac{0.1}{1 \times 10^{-6}} \right) (\sin(2\pi) (10^3) (0.16 \times 10^{-3}))$$

d) $V = IR$

$$I = \frac{V}{R} = \frac{0.055}{5} = 0.011 \text{ A}$$

$$B = 0.055 \text{ V}$$

5 Chapter 14: Inductance

1. What is (a) the rate at which the current through a 0.50-H coil is changing if an emf of 0.150 V is induced across the coil?

$$\text{emf} = -M \left(\frac{dI}{dt} \right) = \frac{dI}{dt} = \frac{\text{emf}}{-M} = \frac{0.150}{-0.50} = \boxed{0.3 \frac{\text{amps}}{\text{s}}}$$

$$\begin{aligned} \text{emf} &= 0.150 \text{ V} \\ M &= 0.50 \text{ H} \end{aligned}$$

2. When a camera uses a flash, a fully charged capacitor discharges through an inductor. In what time must the 0.100-A current through a 2.00-mH inductor be switched on or off to induce a 500-V emf?

$$\text{emf} = -M \left(\frac{dI}{dt} \right)$$

$$\frac{dt}{\text{emf}} = \frac{-M(dI)}{500} = \frac{(-0.002)(0.100)}{500} = \boxed{4 \times 10^{-7} \text{ s}}$$

no (-) time

$$I = 0.100 \text{ A}$$

$$M = 2.00 \text{ mH} = 0.002 \text{ H}$$

$$\text{emf} = 500$$