

ALGEBRA-BASED PHYSICS-2: ELECTRICITY, MAGNETISM, AND MODERN PHYSICS (PHYS135B-01): UNIT 4

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UNIT 2 REVIEW

Reading: Chapters 20 and 21

1. Current, Ohm's Law, resistors and conductors
2. DC circuits I
3. Nerve signals
4. DC circuits II

UNIT 2 REVIEW PROBLEMS

UNIT 2 REVIEW PROBLEMS

Consider a proton with mass m and charge q_p . The proton is located in a region with electric field E , and it has initial velocity v_i at time $t = 0$. What is the acceleration of the proton? What is the proton velocity v_f after a time t ?

- A: $a = \frac{m}{q_p}E$, $v_f = v_i + t$
- B: $a = \frac{m}{q_p}E$, $v_f = v_i + \frac{m}{q_p}Et$
- C: $a = \frac{q_p}{m}E$, $v_f = v_i + \frac{q_p}{m}Et$
- D: $a = \frac{q_p}{m}E$, $v_f = v_i + t$

UNIT 2 REVIEW PROBLEMS

Consider a line of charge with linear charge density λ C/m, aligned with the z-axis. What is most likely the expression for the electric field a distance r away from the line? In this coordinate system, ϕ is the angle measured counter-clockwise from the x-axis in the x-y plane, and z is the height above the x-y plane. *Hint: think about symmetry of the charge distribution.*

- A: $\frac{2k\lambda}{r} \hat{r}$
- B: $\frac{2k\lambda}{r^2} \hat{r}$
- C: $\frac{2k\lambda}{r} \cos \phi \hat{r}$
- D: $\frac{2k\lambda}{r} \sin \phi \hat{r}$

Consider a 12V battery driving current through a system with a total resistance of $1\text{ k}\Omega$. What is the current? What is the power consumption?

- A: 12 mA, 144 W
- B: 144 mA, 12 mW
- C: 12 mA, 144 mW
- D: 14.4 A, 144 W

SUMMARY

Reading: Chapter 22

1. Magnets and magnetic fields
2. Force on a moving charge in a magnetic field
3. **The Hall effect**
4. Magnetic forces on conductors
5. **Ampère's Law**

JITT - READING QUIZ RESULTS

1. List the ways in which magnetic field lines and electric field lines are similar. For example, the field direction is tangent to the line at any point in space. Also list the ways in which they differ.
2. Is the Earth's magnetic field parallel to the ground at all locations? If not, where is it parallel to the surface? Is its strength the same at all locations? If not, where is it greatest?
3. How is the Hall effect used to obtain information on the sign of the free charges in a conductor?

List the ways in which magnetic field lines and electric field lines are similar. For example, the field direction is tangent to the line at any point in space. Also list the ways in which they differ.

“They are both vector field, but the electric field lines are more like rays while the magnetic field lines are closed loops.”

“Magnetic field lines and electric field lines are similar because they never cross each other, the strength of the field is proportional to the number and closeness of field lines, and the field is unique at each point in space. However, they differ because the electric force is parallel to the field lines whereas magnetic force is perpendicular to the field lines.”

“...Magnetic field lines are continuous, while electric field lines have starting and ending points.”

Is the Earth's magnetic field parallel to the ground at all locations? If not, where is it parallel to the surface? Is its strength the same at all locations? If not, where is it greatest?

"No it is not parallel to the ground at all locations. It is parallel to the surface at/near the equator. Its strength is no the same at all locations and is the greatest at the poles."

"Earth's magnetic field is not parallel to the ground at all locations. The magnetic field is most commonly parallel in locations near the equator. Strength is not the same in all locations either. The magnetic south and north poles have the largest strength."

"The earth's magnetic field is not always parallel to the surface of the earth and may be perpendicular. The general trend is that the field is strongest near the magnetic poles and is weakest near the equator."

How is the Hall effect used to obtain information on the sign of the free charges in a conductor?

“Moving electrons feel a magnetic force toward one side of the conductor, leaving a net positive charge on the other side. This separation of charge creates a voltage. If electrons move to the left then the voltage is positive. If electrons move to the right voltage is negative.”

“The Hall effect is the creation of voltage ϵ , known as the Hall emf, across a current-carrying conductor by a magnetic field. The Hall emf is given by $\epsilon = Blv$ (B , v , and l , mutually perpendicular) for a conductor of width l through which charges move at a speed v . We can use this information to determine if the charges in a given conductor are positively or negatively charged.”

MAGNETS AND MAGNETIC FIELDS

What is a cross-product and how does it work?

Computing the cross product [\[edit \]](#)

Coordinate notation [\[edit \]](#)

The [standard basis](#) vectors \mathbf{i} , \mathbf{j} , and \mathbf{k} satisfy the following equalities in a right hand coordinate system:

$$\mathbf{i} \times \mathbf{j} = \mathbf{k}$$

$$\mathbf{j} \times \mathbf{k} = \mathbf{i}$$

$$\mathbf{k} \times \mathbf{i} = \mathbf{j}$$

which imply, by the [anticommutativity](#) of the cross product, that

$$\mathbf{j} \times \mathbf{i} = -\mathbf{k}$$

$$\mathbf{k} \times \mathbf{j} = -\mathbf{i}$$

$$\mathbf{i} \times \mathbf{k} = -\mathbf{j}$$

The definition of the cross product also implies that

$$\mathbf{i} \times \mathbf{i} = \mathbf{j} \times \mathbf{j} = \mathbf{k} \times \mathbf{k} = \mathbf{0} \text{ (the [zero vector](#))}.$$

Figure 1: The cross-product is a way of multiplying unit vectors.

Let $\vec{v} = 2\hat{i}$ and $\vec{w} = -2\hat{j}$. What is $\vec{v} \times \vec{w}$?

- A: $-4\hat{k}$
- B: $4\hat{k}$
- C: $-2\hat{i}$
- D: $2\hat{j}$

Let $\vec{v} = 3\hat{j}$ and $w = 5\hat{k}$. What is $\vec{v} \times \vec{w}$?

- A: $15\hat{i}$
- B: $5\hat{j}$
- C: $3\hat{i}$
- D: $15\hat{k}$

Let $\vec{v} = 3\hat{i} \times 3\hat{j}$ and $w = 2\hat{k}$. What is $\vec{v} \times \vec{w}$?

- A: $-6\hat{j} + 6\hat{k}$
- B: $-6\hat{j} + 6\hat{i}$
- C: $6\hat{j} + 6\hat{i}$
- D: $6\hat{k} + 6\hat{i}$

Group board exercise: Compute the following cross product:

$$\vec{v} = 2\hat{i} - 2\hat{j} \quad (1)$$

$$\vec{w} = 4\hat{j} - 4\hat{i} \quad (2)$$

$$\vec{v} \times \vec{w} = ?? \quad (3)$$

Group board exercise: Compute the following cross product:

$$\vec{v} = 2\hat{i} - 2\hat{j} + \hat{k} \quad (4)$$

$$\vec{w} = 4\hat{j} - 4\hat{i} - \hat{k} \quad (5)$$

$$\vec{v} \times \vec{w} = ?? \quad (6)$$

The Lorentz Force

Let a particle with charge q and velocity \vec{v} move through a *magnetic field* \vec{B} . The **Lorentz force** on the charged particle is

$$\vec{F}_L = q\vec{v} \times \vec{B} \quad (7)$$

As a helpful memory tool, we have the right-hand rule to remember the direction of the cross-product. The units of the magnetic field are the Telsa, after Nikola Tesla. We also have the Gauss which is 10^{-4} Tesla.

MAGNETS AND MAGNETIC FIELDS

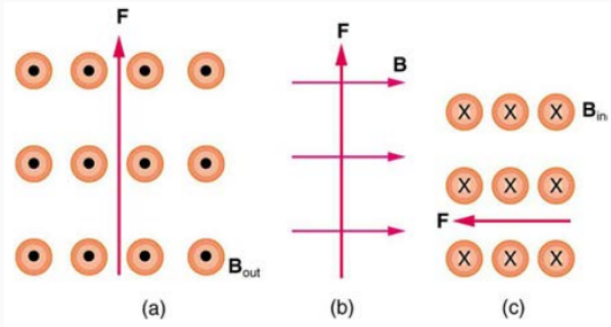


Figure 2: Three different magnetic field and charge scenarios. The vector \vec{F} is the direction of the Lorentz force, and the magnetic field is uniform. A dot indicates that the magnetic field is coming out of the page, and an x indicates that the field is going into the page.

MAGNETS AND MAGNETIC FIELDS

In which of the diagrams is a positively charged particle moving to the left?

- A: A
- B: B
- C: C
- D: WAT WAT
WAT

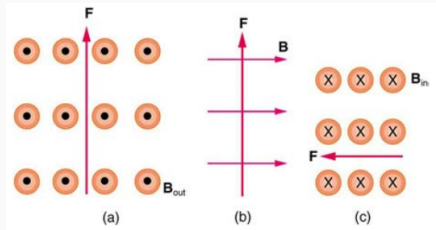


Figure 3: Three different magnetic field and charge scenarios.

MAGNETS AND MAGNETIC FIELDS

In which of the diagrams is a positively charged particle moving upwards?

- A: A
- B: B
- C: C
- D: WAT WAT
WAT

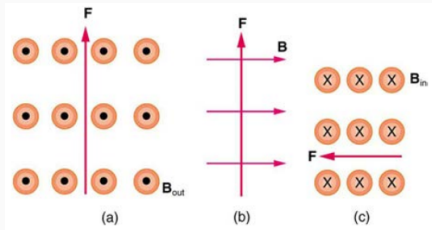


Figure 4: Three different magnetic field and charge scenarios.

MAGNETS AND MAGNETIC FIELDS

In which of the diagrams is a negatively charged particle into the page?

- A: A
- B: B
- C: C
- D: WAT WAT
WAT

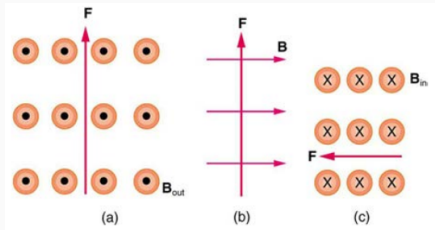


Figure 5: Three different magnetic field and charge scenarios.

MAGNETS AND MAGNETIC FIELDS

In which of the diagrams is a negatively charged particle to the right?

- A: A
- B: B
- C: C
- D: WAT WAT
WAT

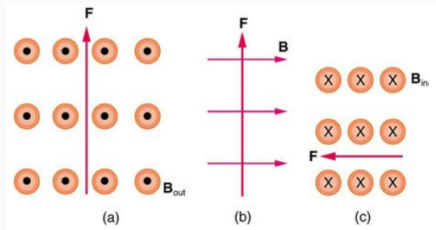


Figure 6: Three different magnetic field and charge scenarios.

A theorem for the magnitude of the cross-product: Let \vec{a} and \vec{b} be vectors and θ be the angle between them. The magnitude of the cross-product is

$$|\vec{a} \times \vec{b}| = ab \sin \theta \quad (8)$$

Thus, the magnitude of the Lorentz force is

$$F_L = qvB \sin \theta \quad (9)$$

The angle θ is between the velocity and the magnetic field.

A cosmic ray proton moving toward the Earth at 3×10^6 m/s experiences a magnetic force of 2×10^{-17} N. What is the strength of the magnetic field if there is a 45 degree angle between it and the proton's velocity? (Remember that q for a proton is 1.6×10^{-19} C).

- A: 0.1 Gauss
- B: 0.6 Gauss
- C: 1 Gauss
- D: 6 Gauss

22 MAGNETISM

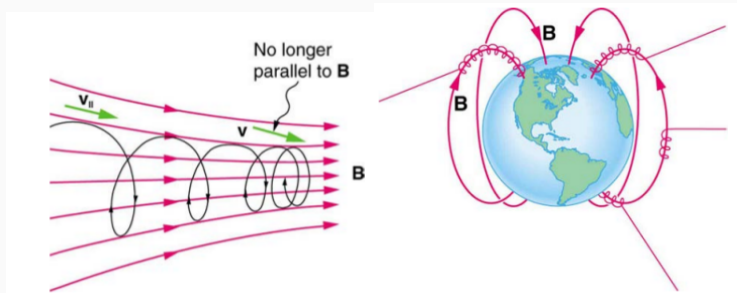


Figure 7: The aurora borealis, or northern lights.

MAGNETS AND MAGNETIC FIELDS

A cool talk on the aurora borealis:

<https://youtu.be/czMh3BnHFHQ>



One un-explained piece: what does it mean for the electrons and protons to *high-five* the neutral oxygen and nitrogen atoms?

THE HALL EFFECT

THE HALL EFFECT

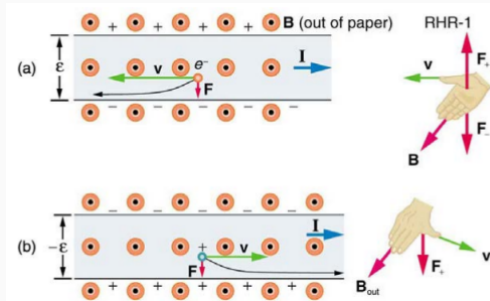


Figure 8: Diagram of the Hall effect. The Hall emf reveals the sign of the moving charges.

The Hall emf is

$$\epsilon = Blv \quad (10)$$

The B is the magnetic field, l is the length across the region where charge is flowing, and v is the velocity of the charges.

Group board exercise: Let n be the charge number density in a conductor. Let q be the charge of an electron. Let A be the cross-sectional area, and I be the current. Recall that the *drift velocity of charges in a wire* is given by the equation

$$v_d = \frac{I}{nqA} \quad (11)$$

The Hall emf is $\epsilon = Blv$. Let $v = v_d$, and substitute the first equation into the second equation, and solve for n . Choose reasonable numbers for the current, diameter of a metal wire, and assume a uniform 0.001 T magnetic field is being created around the wire. Assume a drift velocity of about 1 mm/sec, and solve for n .

MOTORS

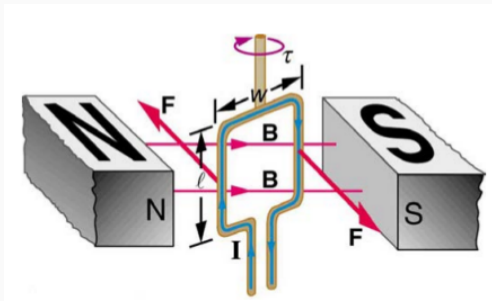


Figure 9: In a loop of current in a uniform magnetic field, we find forces going the opposite directions.

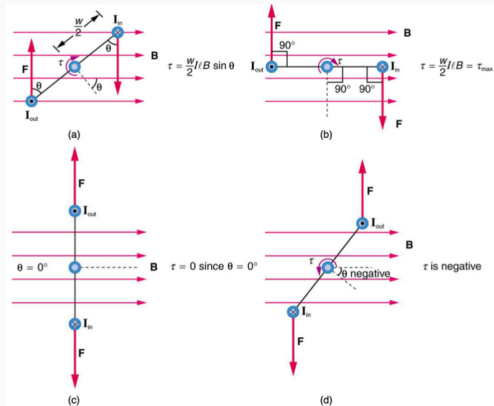


Figure 10: This leads to torque.

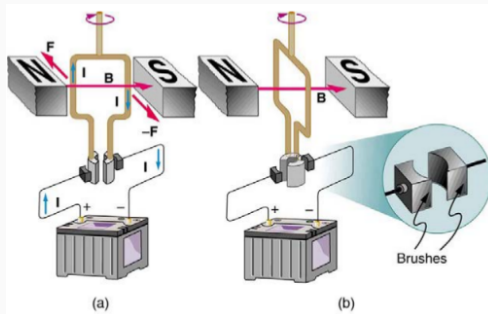


Figure 11: Torque can be used to drive a motor.

Let the number of loops in the coil be N , the current be I , the area of the loops be A , and the magnetic field be B . The angle between the force and loops is θ . The magnitude of the torque τ is

$$\tau = NIAB \sin \theta \quad (12)$$

At what angle between the loops and the B field is the torque maximized?

- A: 0 degrees
- B: 45 degrees
- C: 90 degrees
- D: 135 degrees

Which of the following would boost the torque of a motor?

- A: Increasing the B-field magnitude
- B: Decreasing the number of loops
- C: Increasing the number of loops
- D: A and C

Suppose $I = 10$ amps, $B = 0.01$ T, $N = 200$, and the loops have a common radius of 5 cm. **Group exercise:** what is the maximum torque?

AMPÈRE'S LAW

AMPÈRE'S LAW

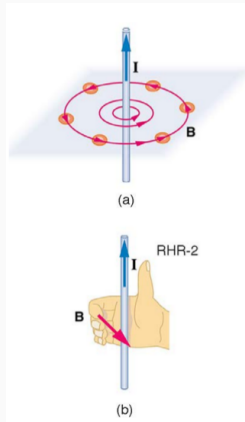


Figure 12: Magnetic fields create currents! To remember the direction, use your right hand.

JITT 1.6

1. Imagine you are observing the magnetic field, B , created by a current, I , in a wire (Ampere's law) a distance r from the wire. What happens to the B -field if a) you move farther from the wire, b) increase the current, and c) Add another wire near the first with current of opposite sign?
2. Suppose we are measuring the current on a coil of wire, and we drop a bar magnet through the coil. What happens if a) the magnet goes through the coil North to South? b) South to North? c) If we just hold the magnet still inside the coil?
3. If we move a coil of wire in a B -field, we get an emf. Emf is a voltage, and voltages can make charged things move. If something can be made to move, work is being done on it. Can magnetic fields therefore do work?

“a.) If you move farther from the wire, the magnetic field will get smaller. b.) If you increase the current then the field gets larger c.) If a parallel wire is placed next to the field with an opposite charge then they would be attracted to each other and have similar magnetic fields”

“A. the field will decrease. B. the field will increase C. the field will stay the same.”

Ampère's Law states that the current produced by a long straight wire is

$$B = \frac{\mu_0 I}{2\pi r} \quad (13)$$

The current is I , the distance from the wire is r , and $\mu_0 = 4\pi \times 10^{-7} \text{ T m/A}$.

Group exercise: Suppose we have a wire carrying 10 A, and we are 1 cm away from it. What is the magnetic field? What is the magnetic field if another wire is located 2 cm away from us, but carries -10 A?

<https://youtu.be/1JZLKvW00ks>

MAGNETIC FIELDS AND WORK.

CONCLUSION

Reading: Chapter 22

1. Magnets and magnetic fields
2. Force on a moving charge in a magnetic field
3. **The Hall effect**
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ANSWERS

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- $a = \frac{q_p}{m} E, v_f = v_i + \frac{q_p}{m} Et$
- $\frac{2k\lambda}{r} \hat{r}$
- 12 mA, 144 mW
- $-4\hat{k}$
- $15\hat{i}$
- $-6\hat{j} + 6\hat{i}$
- A
- C
- B
- A
- 0.6 Gauss
- 90 degrees
- A and C