

19/20

Price

1) Scaling problem

a) $E_c = 2.00 \times 10^{-3} \text{ V/m}$, distance = 1 mm
value of E_c @ 5 mm?

$$E_c = \frac{1}{4\pi\epsilon_0} \times \frac{q_1}{r^2}$$

$$2 \times 10^{-3} = \frac{1}{4\pi\epsilon_0} \times \frac{q_1}{(1 \times 10^{-3})^2}$$

$$2 \times 10^{-3} = \frac{q_1}{(4\pi\epsilon_0)(1 \times 10^{-3})^2} \rightarrow (2 \times 10^{-3})(1 \times 10^{-6}) = \frac{q_1}{4\pi\epsilon_0}$$

$$E_c = \frac{q_1}{(4\pi\epsilon_0)(5 \times 10^{-3})^2} \quad \frac{q_1}{4\pi\epsilon_0} = 2 \times 10^{-3} \times 10^{-6}$$

$$E_c = \frac{q_1}{(4\pi\epsilon_0)(5 \times 10^{-3})^2}$$

$$E_c = \frac{2 \times 10^{-3} \times 10^{-6}}{25 \times 10^{-6}}$$

$$E_c = \frac{2}{25} \times 10^{-3}$$

$$= 0.08 \times 10^{-3} \frac{\text{V}}{\text{C}} \text{ or } 8 \times 10^{-5} \frac{\text{V}}{\text{C}}$$

b) $1 \mu\text{C}$, $E_c = 8.00 \times 10^{-3} \text{ V/m}$

value of E_c @ $3 \mu\text{C}$?

$$E_c = \frac{1}{4\pi\epsilon_0} \times \frac{q_1}{r^2} \quad q_1 = 1 \mu\text{C}, E_c = 8 \times 10^{-3} \text{ V/C}$$

$$8 \times 10^{-3} = \frac{1}{4\pi\epsilon_0} \times \frac{1 \times 10^{-6}}{r^2}$$

$$8 \times 10^{-3} = \frac{1 \times 10^{-6}}{4\pi\epsilon_0 r^2}$$

$$\frac{8 \times 10^{-3}}{1 \times 10^{-6}} = \frac{1}{4\pi\epsilon_0 r^2}$$

$$8 \times 10^3 = \frac{1}{4\pi\epsilon_0 r^2}$$

$$E_c = \frac{1}{4\pi\epsilon_0} \times \frac{3 \times 10^{-6}}{r^2}$$

$$= 8 \times 10^3 \times \frac{3 \times 10^{-6}}{r^2}$$

$$= 24 \times 10^{-3} \frac{\text{N}}{\text{C}}$$

2) mass = 4×10^{-16} kg, E-field = downward, value = 6131.25 N/C

a) how many electrons?

(-1)
$$= \frac{4 \times 10^{-16}}{9.0 \times 10^{-31}}$$
$$= 4.40 \times 10^{14}$$

b) acceleration?

$$q = NE$$
$$= (4.4 \times 10^{14})(1.6 \times 10^{-19})$$
$$= 7.03 \times 10^{-5} \text{ C}$$

$$qE = ma$$

$$\frac{qE}{m} = a$$

$$a = \frac{qE}{m}$$

$$= \frac{(7.03 \times 10^{-5} \text{ C})(6131.25 \text{ N/C})}{4.0 \times 10^{-16} \text{ kg}}$$

$$= 1.08 \times 10^{15} \text{ m/sec}^2$$

} neglects protons and neutrons, but I meant the excess e^- ...
 $4e^-$

(would have been right)

3) Potential Energy & Voltage, Capacitors

1a) $\Delta V = 4$ kV; hydrogen charge = $+1q_e$; helium charge = $+2q_e$

kinetic energy = qV

$$KE(\text{hydrogen}) = (1.6 \times 10^{-19})(4 \times 10^3)$$
$$= 6.4 \times 10^{-16} \text{ J}$$

$$KE(\text{helium}) = 2(1.6 \times 10^{-19})(4 \times 10^3)$$
$$= 2(6.4 \times 10^{-16})$$
$$= 12.8 \times 10^{-16} \text{ J}$$

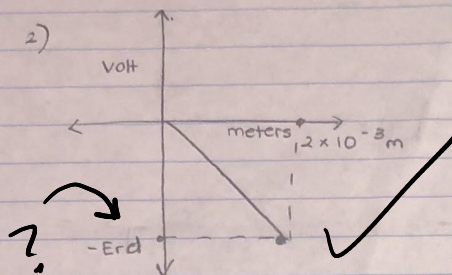
1b) $\Delta x = 5$ cm

electric field value?

$$E = \frac{\Delta V}{\Delta x}$$

$$= \frac{4 \times 10^3}{5 \times 10^{-2}}$$

$$= 8 \times 10^4 \text{ V/m or } 80,000 \text{ V/m}$$



Y-intercept = 0 b/c the line is at the origin point, (0, 0). ✓

3) $1 \text{ cm}^2 = \text{area}$

a) capacitance?

$$C = \frac{\epsilon_0 A}{d}$$

$$= \frac{(8.85 \times 10^{-12})(10^{-4})}{(2 \times 10^{-3})}$$

$$= \boxed{4.43 \times 10^{-13} \text{ F}}$$

b) energy if voltage is 5V?

$$\text{energy} = \frac{1}{2} CV^2$$

$$= \frac{1}{2} (4.43 \times 10^{-13})(25)$$

$$= \frac{1}{2} (11.075 \times 10^{-12})$$

$$= \boxed{5.538 \times 10^{-13} \text{ J}}$$

4) we should connect an identical capacitor to the 1st in parallel

b/c we can add up the capacitances.

$$C_{\text{net}} = C_1 + C_2$$

$$= 2C$$

↑ This is more capacitance in comparison to in series where $C_{\text{net}} = C/2$. capacitance is getting halved.

4) Current, Resistance, & DC Circuits

1) $r_1 = r_2 = 2\Omega$

$\mathcal{E}_1 = \mathcal{E}_2 = 1.5\text{ V}$

$R = 50\Omega$

4a) $-\mathcal{E}_2 + Ir_2 + Ir_1 - \mathcal{E}_1 + IR = 0$
 $-1.5 + I(r_2 + r_1 + R) - 1.5 = 0$

$I(r_2 + r_1 + R) - 3 = 0$

$I(r_2 + r_1 + R) = 3$

$I = \frac{3}{r_1 + r_2 + R}$

$= \frac{3}{2 + 2 + 50}$

$= \frac{3}{54}$

$= \frac{3}{54} = 0.0555 = 55.56\text{ mA}$

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$\frac{V_x - 1.5}{2} + \frac{V_x - 1.5}{2} + \frac{V_x}{50} = 0$

$\frac{25V_x - 37.5}{50} + \frac{25V_x - 37.5}{50} + \frac{V_x}{50} = 0$

$\frac{50V_x - 75 + V_x}{50} = 0$

$\frac{51V_x - 75}{50} = 0$

$51V_x - 75 = 0$

$51V_x = 75$

$V_x = \frac{75}{51} \text{ or } 1.47\text{ Volts}$

$I_1 = \frac{1.5 - 1.47}{2\Omega} = 15\text{ mA}$

$I_2 = \frac{1.5 - 1.47}{2} = 15\text{ mA}$

30 mA

parallel

4b) power consumption?

$$P_{\text{total}} = P_{r_1} + P_{r_2} + P_R \quad \text{--- series}$$

$$= I^2 r_1 + I^2 r_2 + I^2 R$$

$$= (55.56 \text{ mA})^2 \times 2 + (55.56 \text{ mA})^2 \times 2 + (55.56 \text{ mA})^2 \times 50$$

$$= 6.17 \text{ mW} + 6.17 \text{ mW} + 154.34 \text{ mW}$$

$$= \boxed{166.68 \text{ mW}}$$

$$P_R = 154.34 \text{ mW}$$

$$P_{\text{total}} = P_{r_1} + P_{r_2} + P_R \quad \text{--- parallel}$$

$$= I_1^2 r_1 + I_2^2 r_2 + I^2 R$$

$$= (15)^2 \times 2 + (15)^2 \times 2 + (30)^2 \times 50$$

$$= 450 + 450 + 45000$$

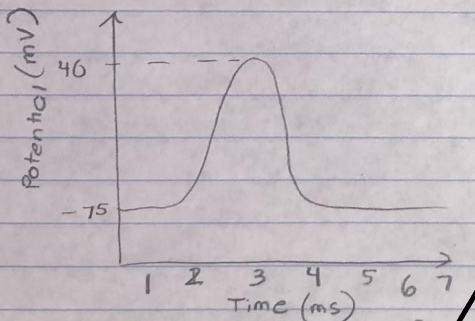
$$= 0.45 \text{ mW} + 0.45 \text{ mW} + 45 \text{ mW}$$

$$= \boxed{45.9 \text{ mW}}$$

$$P_R = 45 \text{ mW}$$

well done

2) Potential vs time



a) pulse width in milliseconds?

$$\boxed{2 \text{ ms}}$$

b) peak-to-peak voltage?

$$= 40 - (-75)$$

$$= 40 + 75$$

$$= \boxed{115 \text{ mV}}$$