

Score: 20/25. Well done!

Midterm 1

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1.  $\Delta t = 1.5s$   $\Delta \text{distance} = .5km$

a) speed in m/s?  $.5km = 500$   $500/1.5 = 333.\bar{3} m/s$

b) speed in km/hr?  $1.5s = .0004hr$   $.5/.0004 = 1250 km/hr$

2. a)  $.25 m^3$  in  $cm^3$ ?  $.25 m^3 \times 1000 \times 1000 = 250,000 cm^3$

b)  $100 km/hr$  in  $m/s$ ?  $100km = 100,000m$   $hr = 3600s$

$$\frac{100000m}{hr} \div \frac{3600s}{hr} = 27.78 m/s$$

c)  $2 kg/m/s^2$  in  $gm/cm s^2$

(-1)  $0.2 gm cm s^{(-2)}$

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1. Write in component form

a)  $\vec{x}_1$ , vector with magnitude of  $10m$ ,  $\angle 15^\circ$  with respect to x-axis



$$\sin(15^\circ) = .2588 = \frac{y}{10} \Rightarrow .255 \times 10 = y$$

$$= 2.59$$

$$(2.59)^2 + (x)^2 = 100$$

$$\vec{x}_1 = 9.66\hat{i} + 2.59\hat{j}$$

$$x^2 = 93.3$$

$$x = 9.66$$

b)  $\vec{x}_2$ , magnitude  $20m$ ,  $\angle 135^\circ$  respect to x-axis



$$\sin(135^\circ) = .707 = \frac{y}{20} \Rightarrow .707 \times 20 = y$$

$$= 14.14$$

$$\vec{x}_2 = 14.14\hat{i} + 2.59\hat{j}$$

$$(14.14)^2 + (x^2) = 400$$

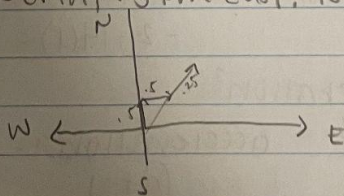
$$x^2 = 200.016$$

$$x = 14.14$$

(-1) The x-component is negative, but the x and y components have the same magnitude

2. Person goes .5km North, .5km East, NE  $\angle 45^\circ$  for .25km

a) draw diagram



b) final location in coordinates  $45-45-90 \Delta$   $.25 = x\sqrt{2}$

North  $.5 + .18 km$

$$= (.68, .68)$$

$$x = .18$$

East  $.5 + .18 km$

$$c) (.5)^2 + (.5)^2 = h^2 \quad h = .71$$

$$.71 + .25 = .96 km$$

$$-1 + 8 = 7$$

$$x(2) = -1 - 4(2)$$

$$-1 - 8$$

$$= -9$$

displacement is -16.

b) velocity?

$$\frac{\Delta x}{\Delta t} = \frac{-16}{4} = -4 \text{ m/s}$$

2.  $x(t) = -2t + 7t^2$

a) average velocity between  $t=2$  and  $t=0$

$$-2(0) + 7(0)^2 = 0 \quad \frac{24}{2} = 12 \text{ m/s}$$

$$-2(2) + 7(2)^2 = 24$$

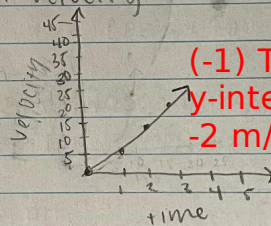
b) draw graph of velocity

$$-2(1) + 7(1)^2 = 5$$

$$\frac{5}{1} = 5 \text{ m/s}$$

$$-2(2) + 7(2)^2 = 24$$

$$\frac{24}{2} = 12 \text{ m/s}$$



c) instantaneous velocity at  $t=1$

$$\frac{d}{dx} = \frac{d}{dx} (-2t + 7t^2) = -2 + 14t$$

$$t=1$$

$$-2 + 14(1) = 12 \text{ m/s at } t=1$$

d) acceleration?

$$a = \frac{dv}{dt}$$

acceleration  $14 \text{ m/s}^2$  slope of velocity

$$\text{at } t=1$$

$$1 \text{ m/s}^2$$



3. acceleration =  $5 \text{ m/s}^2$  constant

a)  $v(t) = v_i + at$

$10 = 0 + 5.00(t) \quad t = 2$

b)  $x(t) = \frac{1}{2}(5)(2)^2 + 0(2) + 0$

$\frac{1}{2}(5)(4)$

$x(2) = 10$

c)  $x(2) = 10 \quad \Delta x = 90$

$x(t) = x_i + vt$

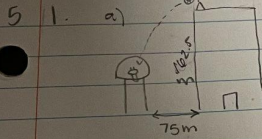
$100 = 10 + 10(t)$

$90 = 10(t)$

$t = 9$

$t = 2$

$t = 11 \text{ s}$



time  
 $dy = \frac{1}{2}gt^2$

$\Delta y = 102.5$

$g = 9.81 \text{ m/s}^2$

$\sqrt{\frac{2\Delta y}{g}} = t$

$\sqrt{\frac{2(102.5)}{9.81}}$

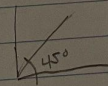
$\sqrt{33.13} = 5.76 = t \text{ sec}$

b)  $v_x = \frac{\Delta x}{\Delta t}$

$\frac{75}{5.76} = 13.02 \text{ m/s}$

2.  $45^\circ$  with respect to horizontal at  $40 \text{ m/s}$

a) how far away does it land



$40 \text{ m/s}$

$R = \frac{v^2 \sin(2\theta)}{g}$

$\frac{(40)^2 \sin 90}{9.81}$

$\frac{1600}{9.81} = 163.1 \text{ m}$

lands  $163.1 \text{ m}$  away

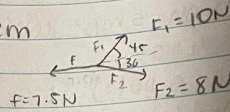
b) how long in air?

$T = \frac{2v_0 \sin(\theta)}{g}$

$\frac{2(40) \sin 45}{9.81}$

$\frac{56.57}{9.81} = 5.77 \text{ s}$

6. 1. acceleration of system  
mass = 49 kg



$$a = \frac{F}{m} \quad a = \frac{18}{49}$$

$$a = \frac{F_{app} - \mu_s m g}{m}$$

$$\frac{18 - 0.06(49)(9.81)}{(49)} = \frac{10.31}{49} = .21 \text{ m/s}^2$$

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$$49 \times 9.81 = 480.69$$

$$\frac{7.5}{f} = \frac{480.69}{F_N} \times .016$$

$$a = (F - F_f) / m$$

$$18 - 7.5 / 49 = .21 \text{ m/s}^2$$

(-1) Almost! This is close, except remember that we add F1 and F2 like vectors, not numbers