

Physics Midterm

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2- Electric Charge + Fields

1. a) $E = 2.0 \times 10^{-3} \text{ V/m}$; $r = 1 \text{ mm}$
 $E = ?$; $r = 5 \text{ mm}$

$$\left\{ \begin{array}{l} E = k \frac{q}{r^2} \\ E = k_2 \left(\frac{1}{25} \right) \Rightarrow \frac{2.0 \times 10^{-3}}{25} \approx \boxed{8.0 \times 10^{-5} \text{ V/m}} \end{array} \right.$$

b) $q = 1 \mu\text{C}$ or $1 \times 10^{-6} \text{ C}$
 $E_c = 8.0 \times 10^{-3} \text{ V/m}$
 value of E @ $q = 3 \mu\text{C}$ or 3×10^{-6}

$$\left\{ \begin{array}{l} E = k \frac{q}{r^2} \\ E = \frac{k}{r^2} (3) \Rightarrow 8.0 \times 10^{-3} (3) \approx \boxed{2.4 \times 10^{-2} \text{ V/m}} \end{array} \right.$$

2. a) $m = 4 \times 10^{-16} \text{ kg}$
 $F = 6131.25 \text{ N/C down}$
 $e^- ?$

$$\left\{ \begin{array}{l} F = \frac{\text{weight}}{\text{charge}} \Rightarrow 6131.25 = \frac{3.92 \times 10^{-15}}{\text{charge}} \Rightarrow \text{charge} = 6.393 \times 10^{-19} \text{ C} \\ W = m \cdot g \\ W = (4 \times 10^{-16}) (9.8) = 3.92 \times 10^{-15} \text{ kg} \end{array} \right.$$

$$\# \text{ of } e^- = \frac{6.393 \times 10^{-19} \text{ C}}{1.6 \times 10^{-19} \text{ C}} = 3.996 \approx \boxed{4 \text{ electrons}}$$

b) removal of $1e^-$

$$\hookrightarrow \text{charge} = (6.393 \times 10^{-19}) - (1.6 \times 10^{-19}) \approx 4.79 \times 10^{-19} \text{ C}$$

Acceleration: $a = \frac{F \cdot e}{m} \quad a = \frac{(6131.25 \text{ N/C})(4.79 \times 10^{-19} \text{ C})}{4 \times 10^{-16} \text{ kg}} \Rightarrow \boxed{a = 7.34 \text{ m/s}^2}$

3. Potential Energy, Voltage + Capacitors

1. a) $\Delta V = 4 \text{ kV}$
 $H = +1qe$
 $H_e = +2qe$

$$\left\{ \begin{array}{l} \Delta U = q \Delta V \\ \Delta U = (3qe)(4000 \text{ V}) = 12,000 \text{ eV} \approx \boxed{12 \text{ eV}} \end{array} \right.$$

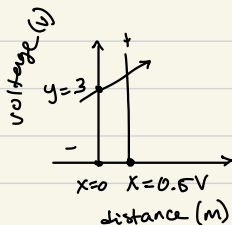
b) $\Delta x = 5 \text{ cm}$

$$\left\{ \begin{array}{l} E = \frac{\Delta V}{\Delta x} \Rightarrow E = \frac{4000 \text{ V}}{0.05 \text{ m}} = 80,000 \text{ V/m} \approx \boxed{8.0 \times 10^4 \text{ V/m}} \end{array} \right.$$

2. $E = 1 \text{ kV/m}$

$\Delta x = 2 \text{ mm}$

$\Delta V = \frac{1 \times 10^3 \text{ V/m}}{2 \times 10^{-3} \text{ m}} = 0.5 \text{ V}$



$F(x) = mx + b$

$V(x) = Ex + b \Rightarrow 5.0 = (1 \times 10^3)(2 \times 10^{-3}) + b$
 $= 5 - 2 = b \Rightarrow \boxed{b = 3}$

3. a) $C = \frac{\epsilon_0 A}{d}$

$A = 1 \text{ cm}^2 \approx 1 \times 10^{-4} \text{ m}^2$

$d = 2 \text{ mm} \approx 2 \times 10^{-3} \text{ m}$

$$\left\{ \begin{array}{l} C = \frac{(8.85 \times 10^{-12})(1 \times 10^{-4} \text{ m}^2)}{(2 \times 10^{-3} \text{ m})} = \frac{8.85 \times 10^{-13}}{2} = \boxed{4.42 \times 10^{-13} \text{ C}} \end{array} \right.$$

3. cont.

$$\begin{aligned} \text{b) } V &= 5V \\ U &= \frac{1}{2} CV^2 \end{aligned} \quad \left\{ \begin{aligned} U &= \frac{1}{2} (4.42 \times 10^{-13} \text{C}) (5V) \\ &= \boxed{1.105 \times 10^{-12} \text{J}} \end{aligned} \right.$$

4. To store more energy for the same voltage (capacitance), an identical capacitor should be placed in parallel.

$$\begin{aligned} \hookrightarrow C_{\text{tot}} (\text{in parallel}) &= C_1 + C_2 + C_n \dots \\ C_{\text{tot}} (\text{in series}) &= \left(\frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_n} \dots \right)^{-1} \end{aligned}$$

4 - Current, Resistance, & DC Circuits

1. a) Current through R?

$$\text{In series: } I_{\text{total}} = I_1 = I_2 = I_3$$

$$I = \frac{V}{R_{\text{total}}} = \frac{3V}{54\Omega} = \underline{0.06A}$$

I is same across all resistors, so
current through R is $\boxed{0.06A}$

In parallel: $V = \text{same across all resistors.}$

$$I_R = \frac{V}{R} \Rightarrow \frac{1.5V}{50\Omega} = 0.03A$$

Since V is the same across all resistors,
then $V = 1.5V$ (Volts are not additive in parallel),
then I_R is $\boxed{0.03A}$

b) Power consumption?

$$\text{In series: } P = I^2 R$$

$$P = (0.06)^2 (54)$$

$$\boxed{P = 0.194W}$$

$$\text{In Parallel: } P = I^2 R \rightarrow \frac{1}{R} = \frac{1}{2} + \frac{1}{2} + \frac{1}{50} = 0.98$$

$$P = (0.03)^2 (0.98\Omega)$$

$$\boxed{P = 8.8 \times 10^{-4} W}$$

c) Checked & found to be correct.

2. a) Pulse width:

$$3ms \rightarrow 5ms \approx \boxed{3ms}$$

b) Peak to peak voltage:

$$35mV - (-75mV) = \boxed{110mV}$$