# Warm Up: Centripetal Acceleration, Circular Motion, and Applied Forces

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### 1 Memory Bank

- $s = r\theta$  ... Let s be the arc length around a curve, with r being the radius of curvature, and  $\theta$  being angle between the initial and final position vectors.
- $a_{\rm C}=v^2/r$  ... The centripetal acceleration given the speed v around a circular path r.

#### 2 Uniform Circular Motion: Curved Coordinates

- 1. Suppose a circular path as a radius of 10 m. If we travel 10 degrees around the circle, how far have we walked?
- 2. If we walk 200 meters along a circular path, and later determine that our direction changed by 90 degrees (say, from North to West), what was the radius of curvature?
- 3. In Fig. 1 (left), a system moves in a circle with speed v. The velocity changes direction by an angle  $\Delta\theta$ , as does the position. It may be shown that this leads to *centripetal acceleration*,  $a_{\rm C}$ . (a) If a system is moving at 4 m/s around a curve with radius 0.25 m, what is  $a_{\rm C}$ ? (b) What is  $a_{\rm C}$  if r=1 m?

## 3 Applied Forces, II

1. Assuming there is no friction on  $m_1$  in Fig. 1 (right), derive an expression for the acceleration of  $m_2$ . Start with the free-body diagram of each block, and assume both blocks are accelerating.

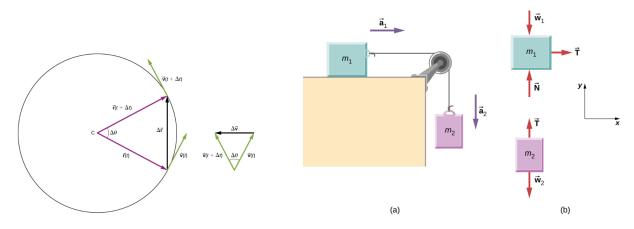


Figure 1: (Left) The origin of centripetal acceleration. (Right) A pulley system with two masses.