

Unit 0

Midterm 1

$$1. \quad 2.0 \mu\text{C} \times \frac{1 \text{ C}}{10^6 \mu\text{C}} \times \frac{1 \text{ p}}{1.6 \times 10^{-19} \text{ C}} = 1.25 \times 10^{13} \text{ excess protons}$$

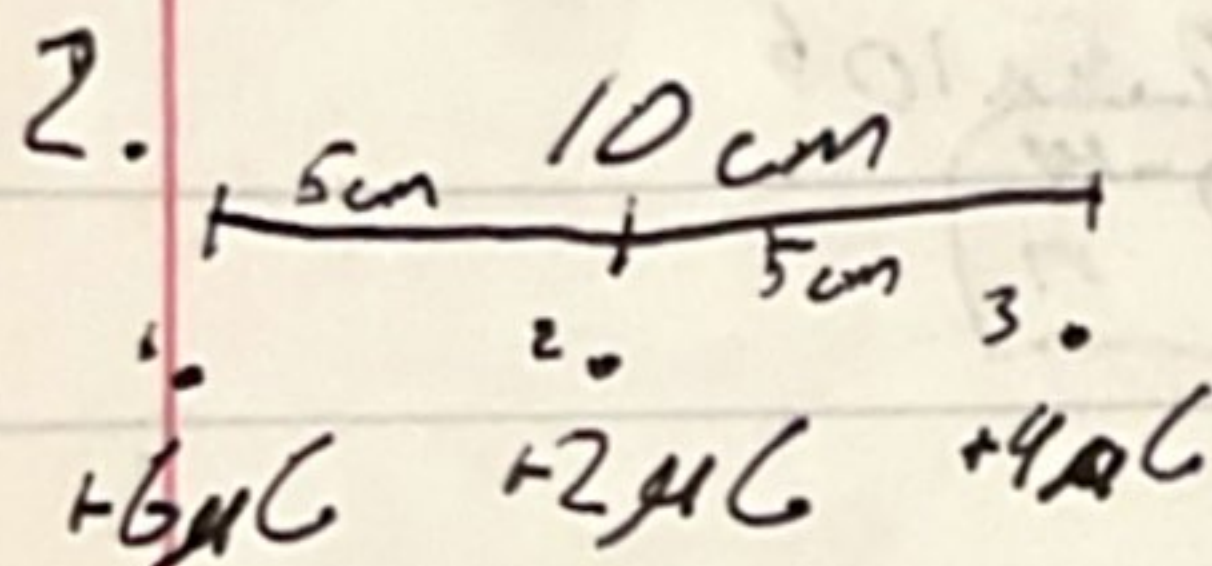
↑
removed electrons

e^- removed

total e^-

$$\frac{1.25 \times 10^{13}}{1.37 \times 10^{25}} = \frac{9.09 \times 10^{-13}}{1}$$

$$50 \text{ g} \times \frac{1 \text{ mol}}{63.5 \text{ g}} \times \frac{6.02 \times 10^{23} \text{ atoms}}{1 \text{ mol}} = 4.74 \times 10^{23} \text{ atoms Cu} \times \frac{29 e^-}{1 \text{ atom}} = 1.37 \times 10^{25}$$



$$a) \quad F_{1,2} = \frac{k |q_1 q_2|}{r^2}$$

$$F_{1,2} = \frac{8.99 \times 10^9 |6 \times 10^{-6} \cdot 2 \times 10^{-6}|}{(0.05)^2}$$

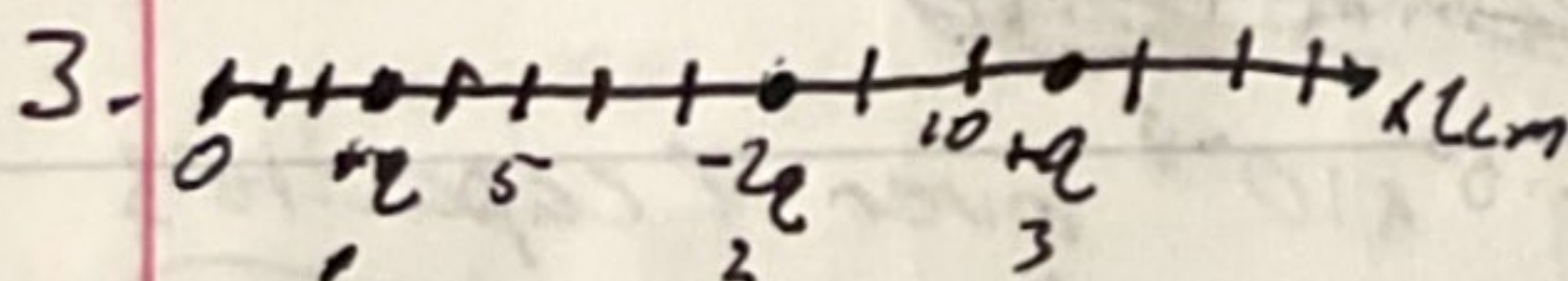
$$F_{1,2} = 43.152 \text{ N}$$

$$F_{3,2} = \frac{8.99 \times 10^9 |4 \times 10^{-6} \cdot 2 \times 10^{-6}|}{(0.05)^2}$$

$$F_{3,2} = 28.768 \text{ N}$$

$$F_{1,2} - F_{3,2} = 43.152 - 28.768 = \boxed{14.4 \text{ N}}$$

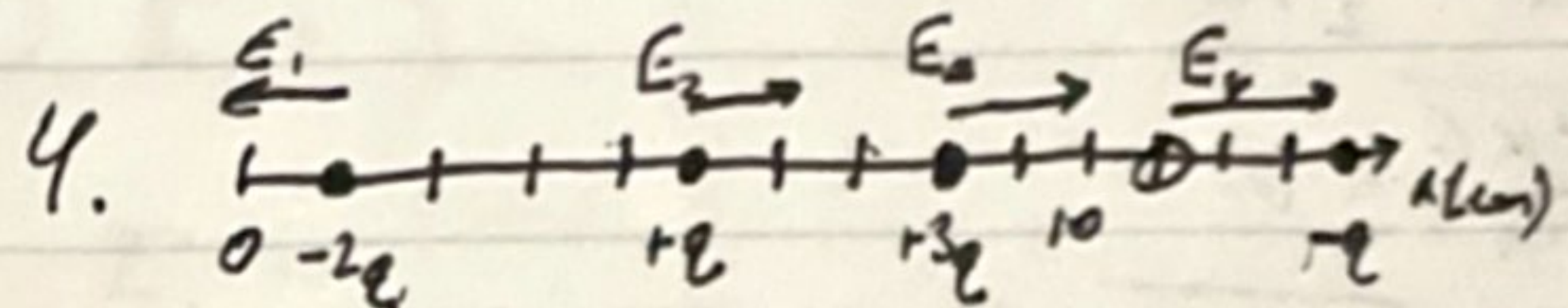
b) The direction is away from the +6 μC charge because it produces a larger force on the test charge.



$$F_{3,2} = \frac{8.99 \times 10^9 |1 \times 10^{-6} \cdot 2 \times 10^{-6}|}{(0.03)^2} = 19.978 \text{ N}$$

$$F_{1,2} = \frac{8.99 \times 10^9 |1 \times 10^{-6} \cdot 2 \times 10^{-6}|}{(0.05)^2} = 7.192 \text{ N}$$

$$F_{3,2} - F_{1,2} = \boxed{12.786 \text{ N}}$$

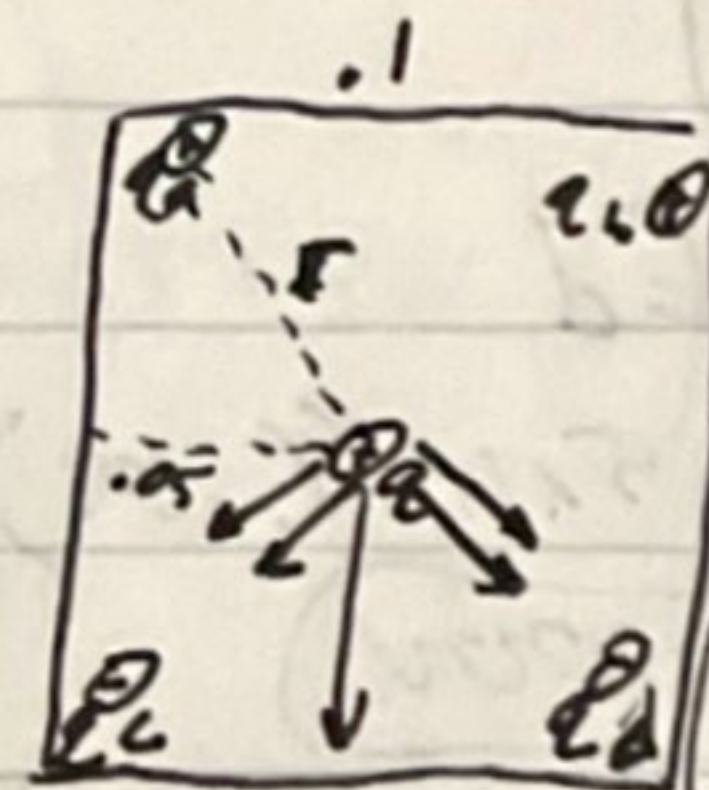


$$E_2 + E_3 + E_4 - E_1 = E_{\text{net}} \quad E = k \frac{|Q|}{r^2}$$

$$\frac{8.99 \times 10^9 |1 \times 10^{-6}|}{(0.06)^2} + \frac{8.99 \times 10^9 |3 \times 10^{-6}|}{(0.03)^2} + \frac{8.99 \times 10^9 |1 \times 10^{-6}|}{(0.03)^2} - \frac{8.99 \times 10^9 |2 \times 10^{-6}|}{(0.1)^2}$$

$$E_{\text{net}} = 4.0655 \times 10^7 \frac{\text{N}}{\text{C}}$$

5. a)



x components cancel

Direction of force is directly down

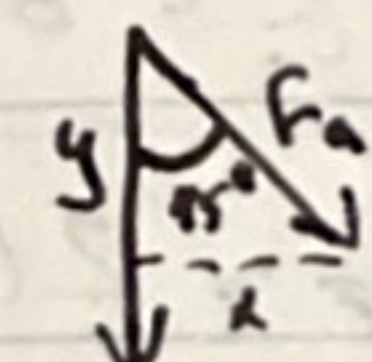
b)

$$\sqrt{0.05^2 + 0.05^2} = 0.0707 \text{ m} = r$$

$$F = \frac{k q_1 q_2}{r^2}$$

$$F = \frac{8.99 \times 10^9 (7.5 \times 10^{-6} \cdot 2 \times 10^{-6})}{(0.0707)^2}$$

$$F = 26.97$$



$$F_{\text{net}} = 26.97 \cos(45)$$

$$F_{\text{net}} = 19.09 \text{ N, all equal}$$

$$19.09 \cdot 4 = \boxed{76.3 \text{ N}}$$

$$6. a) \Delta V = \frac{\Delta PE}{q}$$

$$40000 = \frac{\Delta PE}{1.6 \times 10^{-19}}$$

$$\Delta PE = 6.4 \times 10^{-15} \text{ J}$$

$$KE = 6.4 \times 10^{-15} \text{ J}$$

$$KE = \frac{1}{2} mv^2$$

$$\sqrt{\frac{2KE}{m}} = v$$

$$v = \sqrt{\frac{2(6.4 \times 10^{-15})}{9.11 \times 10^{-31}}} = 1.16 \times 10^8 \text{ m/s}$$

$$b) \frac{V}{m} = \frac{N}{C} \quad V = \frac{E}{q} = \frac{J}{C}$$

$$\frac{W}{C \cdot m} = \frac{N}{C} \quad W = F \cdot d$$

$$\frac{N \cdot m}{C \cdot m} = \frac{N}{C} \quad J = N \cdot m$$

$$\frac{N \cdot m}{C \cdot m} = \frac{N}{C}$$

$$\left[\frac{N}{C} = \frac{N}{C} \right]$$

$$7. a) V = Ed$$

$$V = 7.5 \times 10^4 (1.04)$$

$$V = 7.8 \times 10^4 \text{ V}$$

$$b) \frac{1}{4}(3000) = 750 \text{ V}$$

$$c) V = Ed$$

$$E = \frac{V}{d}$$

$$E = \frac{7.8 \times 10^4}{8 \times 10^{-9}}$$

$$E = 8.89 \times 10^6 \frac{V}{m}$$

$$8. q = 2(1.6 \times 10^{-19} \text{ C}) = 3.2 \times 10^{-19} \text{ C}$$

$$E = 32 \text{ keV} \times \frac{1000 \text{ eV}}{1 \text{ keV}} \cdot \frac{1.6 \times 10^{-19} \text{ J}}{1 \text{ eV}} = 5.12 \times 10^{-15} \text{ J}$$

$$V = \frac{\Delta PE}{q} = \frac{5.12 \times 10^{-15} \text{ J}}{3.2 \times 10^{-19}} = 1.6 \times 10^4 \text{ V} \rightarrow E = \frac{V}{d} = \frac{1.6 \times 10^4}{.02} = 8.0 \times 10^5 \frac{V}{m}$$

$$9. 79 \cdot 1.6 \times 10^{-19} = 1.264 \times 10^{-17} \text{ C (gold)}$$

$$2 \cdot 1.6 \times 10^{-19} = 3.2 \times 10^{-19} \text{ C}$$

$$5 \text{ MeV} \cdot \frac{10^6 \text{ eV}}{1 \text{ MeV}} = 1.6 \times 10^{-19} \text{ J} = 8 \times 10^{-13} \text{ J}$$

$$\Delta V = \frac{\Delta PE}{q} = \frac{8 \times 10^{-13} \text{ J}}{3.2 \times 10^{-19}} = 2.5 \times 10^6 \text{ V}$$

$$V = \frac{kq}{r}$$

$$r = \frac{kq}{V} = \frac{9 \times 10^9 (1.264 \times 10^{-17})}{2.5 \times 10^6}$$

$$r = 4.55 \times 10^{-14} \text{ m}$$

Unit 1

$$1. C \sim \frac{q}{V}$$

$$C = \frac{3 \times 10^{-6}}{120} = 2.5 \times 10^{-8} \text{ F}$$

$$2. a) E = \frac{CV^2}{2} = \frac{10 \times 10^{-6} (4 \times 10^3)^2}{2} = 100 \text{ J}$$

$$b) q = CV = 10 \times 10^{-6} (9 \times 10^3) = 0.09 \text{ C}$$

$$c) V = \sqrt{\frac{2E}{C}}$$

$$V = \sqrt{\frac{2(40)}{(8 \times 10^{-6})}} = 3.16 \times 10^3 \text{ V}$$

$$d) q = CV = (8 \times 10^{-6}) (3.16 \times 10^3) = 0.0253 \text{ C}$$

3. ~~Capacitors in series~~

$C = 2.5 \times 10^{-8}$ over 4 capacitors

$$C_{\text{eq}} = \frac{2.5 \times 10^{-8}}{4} = 6.25 \times 10^{-9} \text{ F}$$

Capacitors in parallel result in additive values while in series results in diminished values, and could end up burning the skin.

$$4. A = \pi r^2$$

$$A = \pi (.5 \times 10^{-3})^2$$

$$A = 2.5 \times 10^{-7} \pi \text{ m}^2$$

$$\cancel{R = 1.72} \quad R = 2 \Omega$$

$$\rho = 1.72 \times 10^{-8} \Omega \cdot \text{m}$$

$$R = \frac{\rho \cdot L}{A}$$

$$L = \frac{RA}{\rho} = \frac{2(2.5 \times 10^{-7} \pi)}{1.72 \times 10^{-8}}$$

$$L = 45.663 \text{ m}$$

$$5. a) V = IR$$

$$I = \frac{V}{R}$$

$$I = \frac{3}{1000 + 3}$$

$$I = .00299 \text{ A}$$

$$b) P = IV$$

$$P = (.00299)(3)$$

$$P = .00897 \text{ W}$$

$$c) 1 \text{ A} = 1 \text{ C/s}$$

$$60 \text{ s} \cdot \frac{10 \text{ min}}{1 \text{ min}} = 600 \text{ s}$$

$$.00299 \text{ A for } 600 \text{ s}$$

$$.00299 \cdot 600 = 1.7946 \text{ C}$$

$$\text{Unit } \# 2$$

$$1. a) \frac{1}{R_s} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$$

$$\frac{1}{2000} = \frac{1}{10000} + \frac{1}{5000} + \frac{1}{R_3}$$

$$\frac{1}{2000} - \frac{1}{10000} - \frac{1}{5000} = \frac{1}{R_3}$$

$$\frac{1}{R_3} = \frac{1}{5000}$$

$$R_3 = 5000 \Omega$$

$$b) V = IR$$

$$I = \frac{R}{V}$$

$$I = \frac{2000}{12}$$

$$I = 166.67 \text{ A}$$

$$c) I_1 = \frac{R_1}{V}$$

$$I_1 = \frac{10000}{12}$$

$$I_1 = 833.33 \text{ A}$$

$$I_2 = \frac{R_2}{V}$$

$$I_2 = \frac{5000}{12}$$

$$I_2 = 416.67 \text{ A}$$

$$I_3 = \frac{R_3}{V}$$

$$I_3 = \frac{5000}{12}$$

$$I_3 = 416.67 \text{ A}$$

$$2. a) 1.5 + 1.5 = 3 \text{ V}$$

$$I = \frac{R}{V}$$

$$I = \frac{500}{3}$$

$$I = 166.67 \text{ A}$$

$$I = \frac{500}{3}$$

$$\cancel{I = 333.33 \text{ A}}$$

$$I = 166.67 \text{ A}$$

$$b) I = \frac{R}{V}$$

$$I = \frac{505}{3}$$

$$I = 168.33 \text{ A}$$

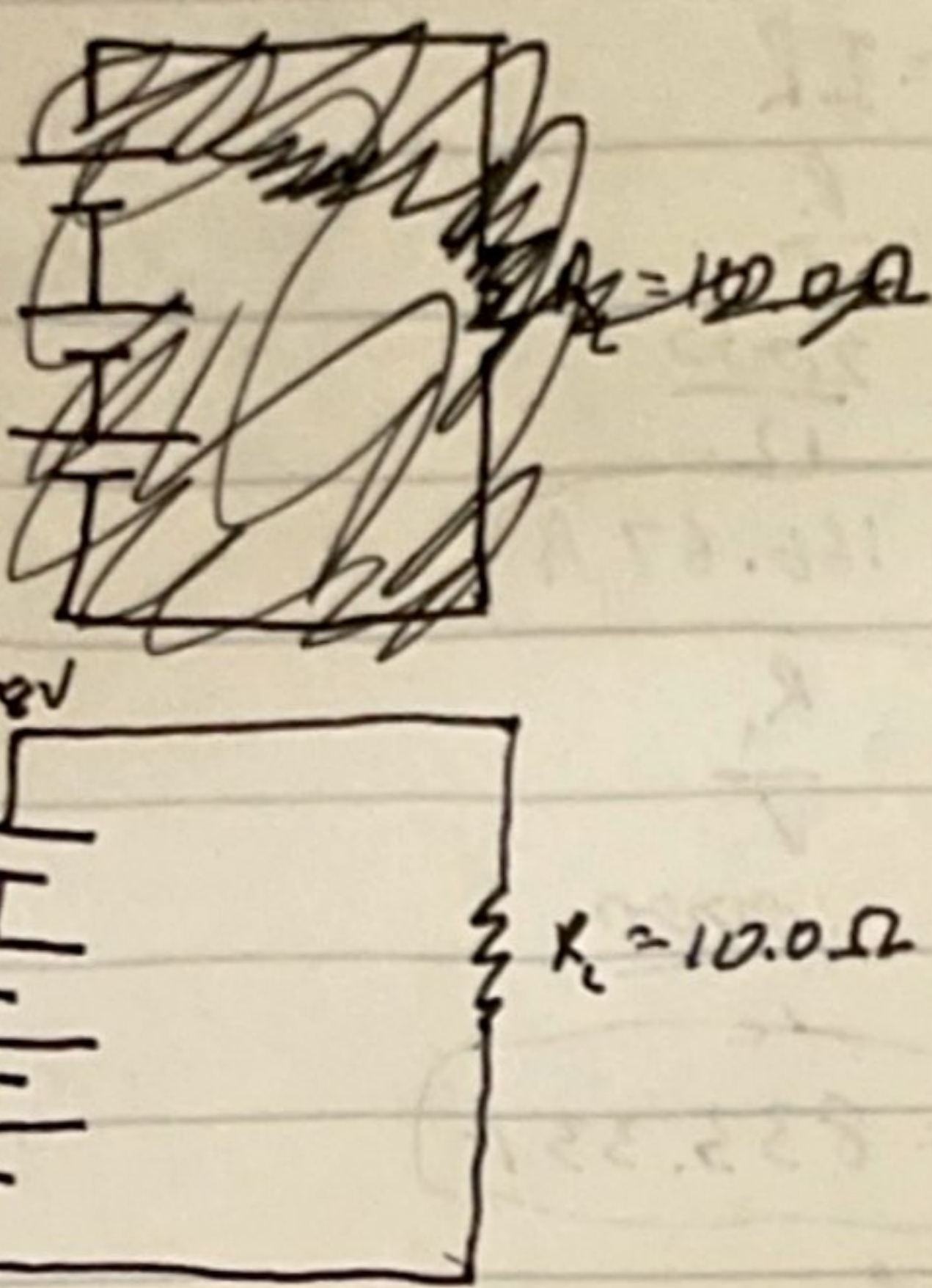
$$I = \frac{R}{V}$$

$$I = \frac{505}{3}$$

$$\cancel{I = 333.33 \text{ A}}$$

$$I = 168.33 \text{ A}$$

3. a)



EMF = 1.53V

$r = .01\Omega$

b) $I_T = \frac{V_T}{R_T}$

$I_T = \frac{3(1.58)(1.53)}{3(.02) + .1 + 10}$

$I_T = .617A$

c) $P_L = I_T^2 R_L$

$P = (.617)^2 (10)$

$P_L = 3.81W$

d) $P_L = I_L^2 R_L$

$.5 = I_L^2 (10)$

$I_L = .224A$

$I_T = \frac{V_T}{R_T}$

$I_T = \frac{3(1.58) + 1.53}{3(.02) + r + 10}$

$.224 = \frac{3(1.58) + 1.53}{3(.02) + r + 10}$

$.224 = \frac{6.27}{10.06 + r}$

$r = \frac{6.27}{.224} - 10.06$

$r = 18.0\Omega$

4. $\frac{72 \frac{\text{beats}}{\text{min}}}{1 \text{ min}} \cdot \frac{1 \text{ min}}{72 \text{ beats}} = .0139 \frac{\text{min}}{\text{beat}} \cdot \frac{60 \text{ s}}{1 \text{ min}} = .833 \frac{\text{s}}{\text{beat}}$

$\tau = R \cdot C$

$.833 = R(25 \times 10^{-9})$

$R = 3.33 \times 10^7 \Omega$

5. a) $\tau = 1 \times 10^{-4} s$

$R = 1 \times 10^3 \Omega$

$\frac{\tau}{R} = C$

$\frac{1 \times 10^{-4}}{1 \times 10^3} = C$

$C = 1 \times 10^{-7} F$

b) It would not be difficult

to limit the capacitance to less than the value in a) because the capacitance in practice must be less than that number.

Unit 3

| Case | V | B | F |
|------|------------|------------|------------|
| (a) | $-\hat{j}$ | \hat{k} | $-\hat{i}$ |
| (b) | \hat{j} | \hat{i} | $-\hat{k}$ |
| (c) | \hat{i} | $-\hat{k}$ | $-\hat{j}$ |
| (d) | — | — | — |

only 3? East ABC no D?

2. $F = qvB \sin \theta$

$\frac{F}{qvB} = \sin \theta$

$\frac{1.40 \times 10^{-16}}{(1.6 \times 10^{-19})(4 \times 10^3)(1.25)} = \sin \theta$

$.175 = \sin \theta$

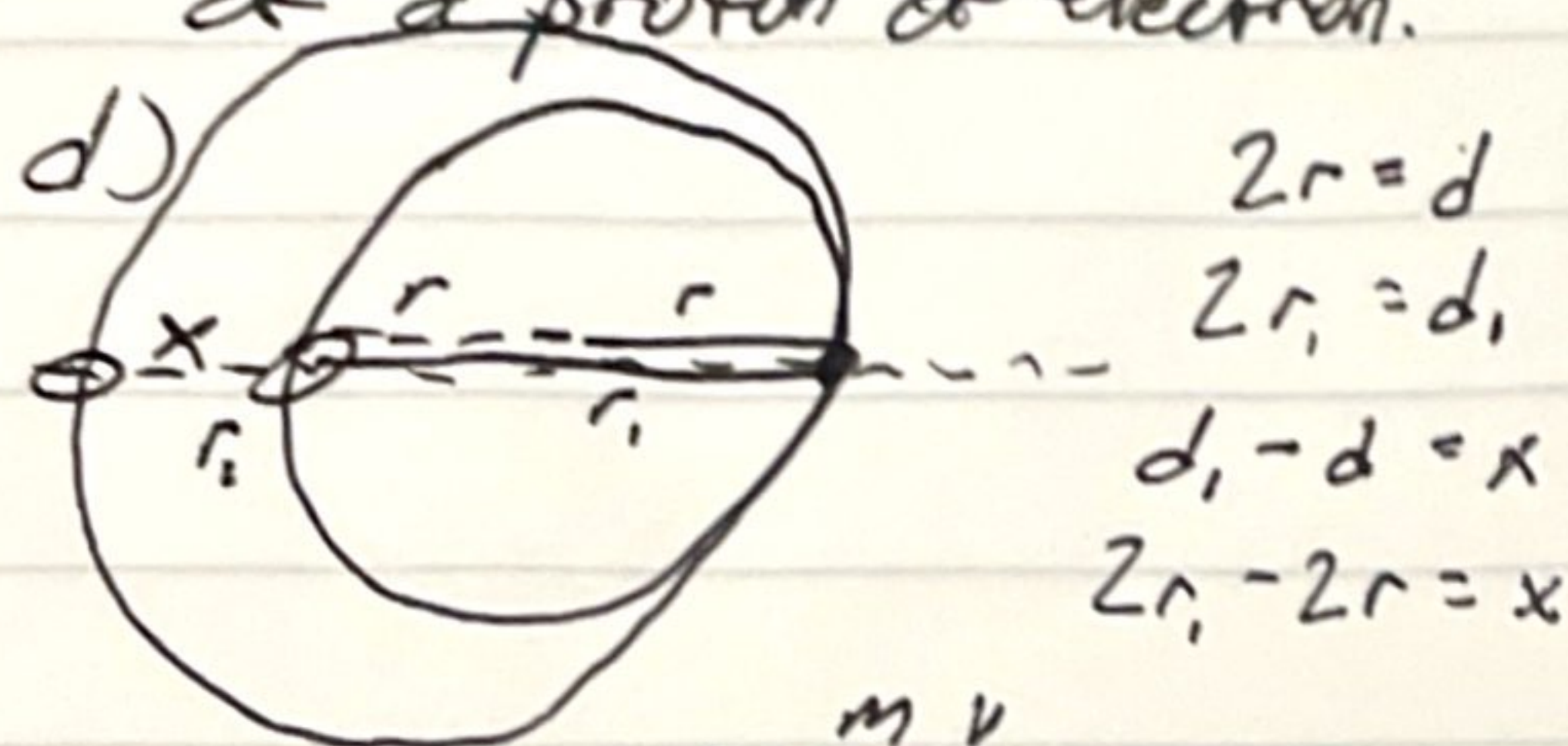
$\sin^{-1}(.175) = \theta$

$\theta = 10.1^\circ \approx 10^\circ$

3. a) $r = \frac{m v_T}{|q| B}$
 $q = \frac{m v_T}{r B}$
 $q = \frac{(2.66 \times 10^{-24})(5 \times 10^6)}{2.31(1.2)}$
 $q = 4.80 \times 10^{-19} C$

b) $\frac{4.8 \times 10^{-19}}{1.6 \times 10^{-19}} = 3$

c) It is not possible to have fractional amounts of a proton or electron.



$\frac{16}{18} = \frac{2.66 \times 10^{-26}}{m_1}$
 $m_1 = 2.99 \times 10^{-26}$
 $r = \frac{m v}{q B}$
 $r = \frac{2.66 \times 10^{-26}(5 \times 10^6)}{(1.6 \times 10^{-19})(1.2)}$
 $r = 0.693 m$
 $r_1 = \frac{m_1 v_1}{q_1 B_1} = \frac{(2.99 \times 10^{-26})(5 \times 10^6)}{(1.6 \times 10^{-19})(1.2)}$
 $r_1 = 0.779 m$
 $2(0.779 m) - 2(0.693) = 0.173 m$

4. $F = I l B \sin \theta$
 $F = 100(0.25)(2) \sin(90)$
 $F = 50 N$

5. $\tau = N I A B \sin \theta$

$\frac{\tau}{N I A \sin \theta} = B$

$B = \frac{300}{200(25) \times (2^2) (\sin 90)}$

$B = 1.5 T$

6.

| Case | B direction |
|------|-------------|
| (a) | $-\hat{j}$ |
| (b) | \hat{k} |
| (c) | $-\hat{k}$ |

7. $B = \frac{\mu_0 I}{2 \pi r}$ $P = I V$
 $I = \frac{P}{V}$

$B = \frac{4 \pi \times 10^{-7} (1500)}{2 \pi (20)}$ $I = \frac{450 \times 10^6}{3000000} = 1500$
 $B = 1.5 \times 10^{-5} T$

8. a) $B = \frac{\mu_0 N I}{2 \pi r}$
 $I = \frac{(4 \pi \times 10^{-7})(N I)}{2 \pi (5)}$

$\frac{10 \pi}{4 \pi \times 10^{-7}} = N I$

$2500000 = N I$

~~$I = 45455$~~ $I = 45455$

$N = 550$

$c = \text{speed of light}$

b) $v = c / 2 \pi R$

$v = \frac{3 \times 10^8}{2 \pi (5)}$

$v = 9.54 \times 10^6 m/s$