

2.1

a.  $-\hat{j} = \hat{j} \times (-\hat{k})$  Into the plane of the paper

b.  $-\hat{k} = -\hat{j} \times (-\hat{i})$  Along the left side, negative x-axis

c.  $\hat{j} = -\hat{i} \times \hat{k}$  Out of the page

2.2

a. Electric Force on charge balances the Lorentz force.

Therefore  $qE = qVB \sin \theta \rightarrow \theta = 90^\circ$

Therefore  $\cancel{q}E = \cancel{q}VB$

$E = VB$

$$\boxed{V = \frac{E}{B}}$$

Electric Field is constant

b.

$\Delta V = (VB) \Delta x$

$\Delta V = B(\Delta x) V$

$V = V_d = \frac{I}{nq_e A}$  Therefore  $\rightarrow \Delta V = \frac{B(\Delta x) I}{nq_e A}$

$\Delta V = \frac{1.33 \times (2 \times 10^{-2}) \times 10}{2 \times 10^{28} \times 1.6 \times 10^{-19} \times (1 \times 10^{-3})^2}$

$\Delta V = 8.3125 \times 10^{-5} \text{ V}$

$\boxed{\Delta V = 8.3125 \times 10^{-5} \text{ V}}$

2.3

$$\begin{aligned}
 \tau &= IAB \\
 &= 1.05 \times 10^{-4} \times \pi \times (0.65 \times 10^{-15})^2 \times 2.50 \\
 &= \boxed{3.48 \times 10^{-26} \text{ N}\cdot\text{m}}
 \end{aligned}$$

3.1

a.  $B = \mu_0 n I$

$$B = (4\pi \times 10^{-7} \text{ T}\cdot\text{m/A}) \times (500 \text{ m}^{-1}) \times (0.3 \text{ A}) = \boxed{1.88 \times 10^{-4} \text{ T}}$$

b. Increase by 5000,  $B \times 5000 = \boxed{0.942 \text{ T}}$

3.2

a. Top Left: Electric Field upwards  
Magnetic Field out of the page  
Velocity: Right

$$F_{\text{tot}} = F_E + F_M = 0$$

$$q\vec{E} + \vec{v} \times \vec{B} = 0$$

↓

$$F_{\text{tot}} = q[E - vB] = 0$$

$$E = vB \rightarrow v = \frac{E}{B} \text{ for } F_{\text{tot}} = 0$$

b. Centripetal Force  $mv^2/r$

$$qvB = \frac{mv^2}{r} \rightarrow r = \frac{mv}{qB} \quad \left(v = \frac{E}{B}\right) \text{ so } r = \frac{m \frac{E}{B}}{qB} = \frac{mE}{qB^2}$$

Mass oxygen =  $16 \times 1.67 \times 10^{-27} = 1.602 \times 10^{-19} \text{ C} = q$

$$r = \frac{16 \times (1.67 \times 10^{-27}) \times 10}{1.602 \times 10^{-19} \times (0.01)^2} = \boxed{0.0167 \text{ m}}$$

4.1

a. Induced Voltage

$$e = \frac{d\phi}{dt} = \frac{d}{dt} (BA)$$

$$e = A \frac{dB}{dt}$$

$$e = \pi r^2 \times \frac{B_0}{T_0} \sin(2\pi f t)$$

b. Induced emf at  $t=0$

$$\sin(2\pi f t) \quad t=0 \text{ so } \sin(0) = 0$$

therefore induced emf at  $t=0$  is 0.

$$c. \quad e = \pi \times (0.1)^2 \times \frac{0.1}{1\text{ms}} \sin(2\pi \times 10^3 \times 0.16 \times 10^{-3})$$

$$= 3.14 \times \frac{(0.1)^3}{1\text{ms}} (\sin(0.32\pi))$$

$$e = 0.055 \text{ V}$$

$$d. \quad \text{Current at } t_1 \quad I = \frac{e}{R} = \frac{0.055 \text{ V}}{5 \Omega}$$

$$I = 0.011 \text{ A}$$

5.1

$$L (\text{inductance}) = 0.50 \text{ H}$$

$$\mathcal{E}_{\text{ind}} = 0.150 \text{ V}$$

$$\mathcal{E} = -L \frac{dI}{dt}$$

$$\frac{dI}{dt} = \frac{-\mathcal{E}}{L} = \frac{-0.150 \text{ V}}{0.50 \text{ H}} = -0.3 \text{ A/s}$$

Rate of change is  $-0.3 \text{ A/s}$

$$\text{Magnitude } \left| \frac{dI}{dt} \right| = 0.3 \text{ A/s}$$

5.2

$$\mathcal{E} = -L \frac{dI}{dt}$$

$$\text{Magnitude } \mathcal{E} = L \frac{dI}{dt}$$

$$500 = 2 \times 10^{-3} \frac{dI}{dt}$$

$$2.5 \times 10^5 = \frac{dI}{dt}$$

$$dI = 2.5 \times 10^5 dt$$

$$\int dI = \int 2.5 \times 10^5 dt$$

$$I = 2.5 \times 10^5 t$$

$$t = \frac{0.100}{2.5 \times 10^5}$$

$$t = 4 \times 10^{-7} \text{ sec}$$