

Electric charge & electric field

2. 1. a) $E_0 = 200 \cdot 10^{-3} \text{ V/m}$
 $\frac{2.00 \cdot 10^{-3}}{25} = 8 \cdot 10^{-5} \text{ V/m}$

$q = 1 \mu\text{C}$ b) $E = \frac{1}{4\pi\epsilon_0} \cdot \frac{q}{r^2}$
 $1 \mu\text{C} = 1 \cdot 10^{-6} \text{ C}$ $8 \cdot 10^{-3} = \frac{1}{4\pi\epsilon_0} \cdot \frac{1 \cdot 10^{-6}}{r^2}$
 $(1 \cdot 10^{-5}) (8 \cdot 10^{-3}) = \frac{1 \cdot 10^{-6}}{4\pi\epsilon_0 r^2} \cdot (1 \cdot 10^{-6})$
 $8 \cdot 10^{-3} = \frac{1}{4\pi\epsilon_0 r^2}$

$q = 3 \mu\text{C} = 3 \cdot 10^{-6} \text{ C}$
 $E = \frac{1}{4\pi\epsilon_0} \cdot \frac{q}{r^2}$
 $E = \frac{1}{4\pi\epsilon_0} \cdot \frac{3 \cdot 10^{-6}}{r^2}$

$$B = \frac{3 \cdot 10^{-6}}{4\pi\epsilon_0 r^2}$$

$$E = \frac{1}{4\pi\epsilon_0 r^2} \cdot \frac{3 \cdot 10^{-6}}{1} \quad \star \text{Substitution for } \frac{1}{4\pi\epsilon_0 r^2}$$

$$F = (8 \cdot 10^9) (3 \cdot 10^{-6})$$

$$F = 2.4 \cdot 10^{-2}$$

Electric Charge & Electric Fields

$$2.2 \text{ a) } q = \frac{q}{E} \\ = \frac{(4 \times 10^{-16})(9.8)}{6131.25}$$

$$q = 6.39 \times 10^{-19}$$

$$\text{b) } q' = q - e \\ (6.39 \times 10^{-19}) - (1.6 \times 10^{-19}) \\ q' = 4.79 \times 10^{-19}$$

solve for F_E

$$F_E = q' \cdot E \\ = (4.79 \times 10^{-19})(6131.25) \\ F_E = 2.94 \times 10^{-15} \text{ N}$$

solve for oil drop mass

$$m' = m - me \quad (\text{mass of oil}) - (\text{mass of } e^-) \\ m' = (4 \times 10^{-16}) - (9.1 \times 10^{-31}) \\ m' \approx 4 \times 10^{-16}$$

solve for F_g

$$F_g = m'g \\ = (4 \times 10^{-16})(9.8) \\ F_g = 3.92 \times 10^{-15} \text{ N}$$

Finally, solve for a

$$a = \frac{F_g - F_E}{m} = \frac{(3.92 \times 10^{-15}) - (2.94 \times 10^{-15})}{(4 \times 10^{-16})}$$

$$a = 2.45 \text{ m/s}^2$$

POTENTIAL ENERGY & VOLTAGE, CAPACITORS

3. 1. a) $KE = qV$
 $= (1.6 \cdot 10^{-19})(4 \text{ kV})$
 $= 6.4 \cdot 10^{-19} \text{ eV}$ Hydrogen

$$\text{Hydrogen: } 2qV = 1(1.6 \cdot 10^{-19}) = 1.6 \cdot 10^{-19}$$

$$\text{Helium: } 2qV = 2(1.6 \cdot 10^{-19}) = 3.2 \cdot 10^{-19}$$

$$\cancel{1.6 \cdot 10^{-19} \text{ eV}} = \cancel{4 \text{ kV}}$$

$$1 \text{ eV} = 10^3 \text{ V}$$

$$2(1.6 \cdot 10^{-19})(4)$$

$$= 1.28 \cdot 10^{-18} \text{ eV}$$

b) $E = \frac{dV}{dx}$ $\Delta x = 5 \text{ cm}$ $5 \text{ cm} = 5 \times 10^{-2} \text{ m}$

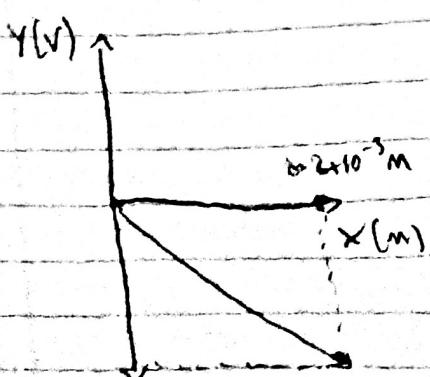
$$E = \frac{4 \times 10^3}{5 \times 10^{-2}}$$

$$E = 8 \times 10^4 \text{ V/m}$$

2. $E = 1 \text{ kV/m} = 1000 \text{ V/m}$

- B/C question deals w/ parallel plate capacitor, E-field is constant
- E-field is also slope of voltage function
- This makes the function linear due to the constant slope
- Function will also point downward since E-field relative to potential

$$1000 \text{ V/m} \quad 2 \text{ mm} = 2 \times 10^{-3} \text{ m}$$



$$E = -\frac{dV}{dx}$$

$$y = mx + b$$

$$y = 1000x + y_0$$

• Y-intercept is 0 due to function beginning at (0,0)

Potential Energy & Voltage, Capacitors

3. a) $C = \frac{E_p}{V}$ $V = (1 \cdot 10^{-2} \text{ m})^2$ $d = 2 \text{ mm} = 2 \cdot 10^{-3} \text{ m}$

$$C = \frac{(8.85 \cdot 10^{-12})(1 \cdot 10^{-2})^2}{(2 \cdot 10^{-3})}$$

$$C = 4.45 \cdot 10^{-13} \text{ F}$$

b) $W = \frac{1}{2}CV^2$ $V = 5$

$$W = \frac{1}{2}(4.45 \cdot 10^{-13})(5^2)$$

$$W = 5.56 \cdot 10^{-12} \text{ J}$$

4. The identical capacitors should be connected in parallel in order to achieve more energy

A parallel combination allows for the sum of all capacitance

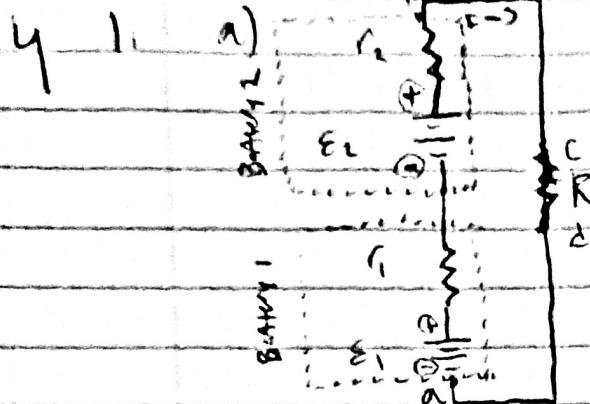
$$C_{\text{tot}} = C_1 + C_2 + \dots \quad \uparrow C$$

A series combination adds the reciprocals of all capacitors, which results in the equivalent capacitor being smaller than the smaller individual capacitance. Results in less energy

$$C_{\text{tot}}^{-1} = C_1^{-1} + C_2^{-1} \quad \downarrow C$$

Current, Resistance, & DC Circuits

series



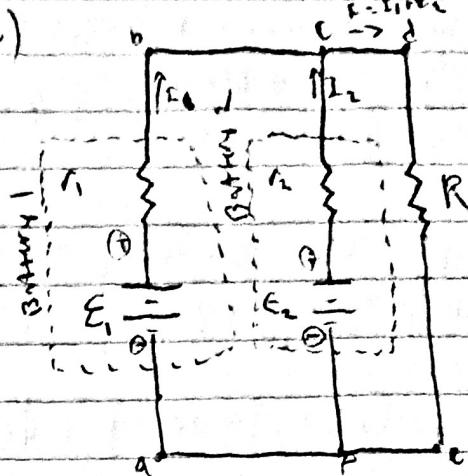
$$E_1 - Ir_1 + E_2 - Ir_2 = 0$$

$$I = \frac{E_1 + E_2}{r_1 + r_2 + R}$$

$$I = \frac{1.5 + 1.5}{2 + 2 + 50} \approx 55.6 \text{ mA}$$

$$\begin{aligned} b) P_{\text{total}} &= P_{r_1} + P_{r_2} + P_R \\ &= I^2 r_1 + I^2 r_2 + I^2 R \\ &= (55.6)^2 2 + (55.6)^2 2 + (55.6)^2 50 \\ &\approx 166 \text{ mW} \end{aligned}$$

parallel



$$\frac{1}{R_{\text{total}}} = \frac{1}{R_1} + \frac{1}{r_2} + \frac{1}{R}$$

$$0 = \frac{1}{r_1} + \frac{1}{r_2} + \frac{1}{R}$$

$$0 = \frac{V_x - 1.5}{2} + \frac{V_x - 1.5}{2} + \frac{V_x}{50}$$

Now common denominator

$$0 = \left(\frac{25}{25}\right) \cdot \left(\frac{V_x - 1.5}{2}\right) + \left(\frac{25}{25}\right) \cdot \left(\frac{V_x - 1.5}{2}\right) + \frac{V_x}{50}$$

$$0 = 25V_x - 37.5 + 25V_x - 37.5 + V_x$$

$$0 = 75 + 51V_x$$

$$V_x = 1.47 \text{ V}$$

$$V = IR \rightarrow I = \frac{V}{R}$$

$$\begin{aligned} I_1 &= \frac{1.5 - 1.47}{2} = 15 \text{ mA} \\ I_2 &= \frac{1.5 - 1.47}{2} = 15 \text{ mA} \end{aligned}$$

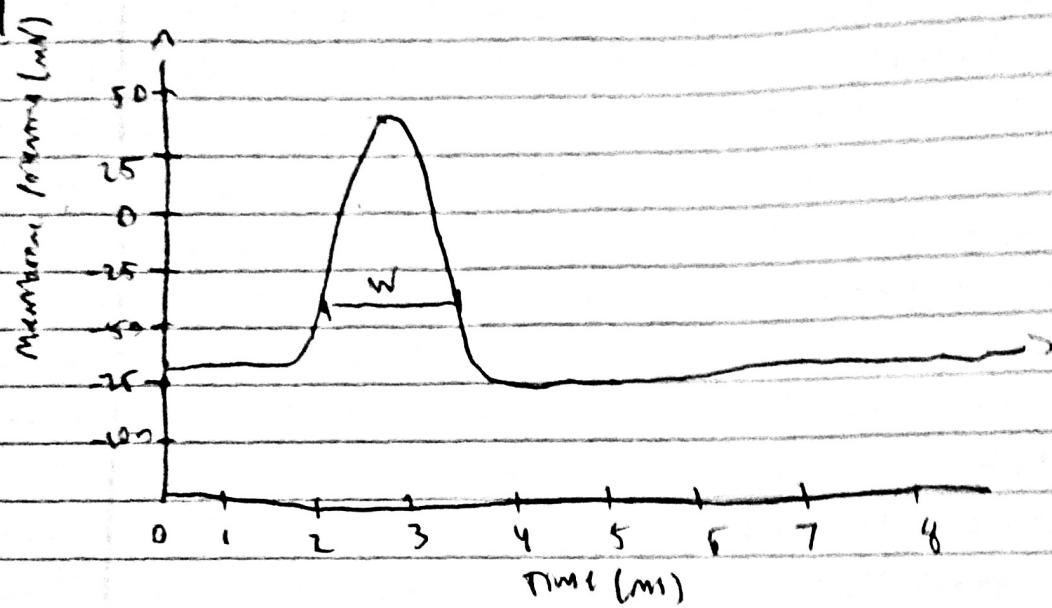
$$I = 30 \text{ mA}$$

$$b) P_{\text{total}} = P_{r_1} + P_{r_2} + P_R$$

$$\begin{aligned} &= I^2 r_1 + I^2 r_2 + I^2 R \\ &= (15)^2 2 + (15)^2 2 + (30)^2 50 \\ &\approx 45.9 \text{ mW} \end{aligned}$$

Current, Resistance, & DC Circuits

4.2 a) After stimulating nerve, I find graph of membrane potential vs time



4-2

$$= 2 \text{ ms}$$

b) greater voltage = 1 volt

$$40 - (-75)$$

$$= 115 \text{ V}$$