

Score: 23/25. Well done!

Midterm

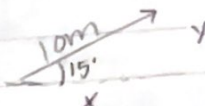
2. a. $s = \frac{d}{t} = \frac{0.5 \text{ km}}{1.5 \text{ sec}} \cdot \frac{1000 \text{ m}}{1 \text{ km}} = 333.33 \text{ m/s}$

b. $\frac{0.5 \text{ km}}{5 \text{ sec}} \cdot \frac{60 \text{ sec}}{1 \text{ min}} \cdot \frac{60 \text{ min}}{1 \text{ hr}} = 1200 \text{ km/hr}$

2a. $0.25 \text{ m}^3 \cdot \frac{100 \text{ cm}}{1 \text{ m}} \cdot \frac{100 \text{ cm}}{1 \text{ m}} \cdot \frac{100 \text{ cm}}{1 \text{ m}} = 250,000 \text{ cm}^3$

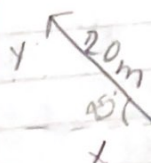
b. $\frac{100 \text{ km}}{\text{hr}} \cdot \frac{1000 \text{ m}}{1 \text{ km}} \cdot \frac{1 \text{ hr}}{60 \text{ min}} \cdot \frac{1 \text{ min}}{60 \text{ sec}} = 27.78 \text{ m/s}$

c. $\frac{2 \text{ kg m}}{\text{s}^2} \cdot \frac{1000 \text{ g}}{1 \text{ kg}} \cdot \frac{100 \text{ cm}}{1 \text{ m}} \cdot \frac{1 \text{ s}}{1000 \text{ ms}} \cdot \frac{1 \text{ s}}{1000 \text{ ms}} = 0.2 \text{ g cm/ms}^2$

3. a.  $\sin(15^\circ) = \frac{y}{10} = 2.59 \text{ m}$

$9.66\hat{i} + 2.59\hat{j}$

$\cos(15^\circ) = \frac{x}{10} = 9.66 \text{ m}$

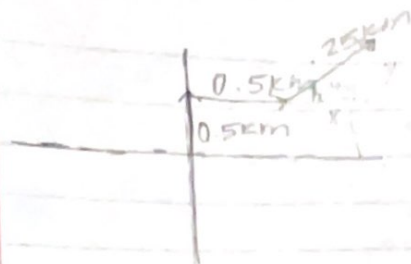


$\sin(45^\circ) = \frac{y}{20} = 14.14 \text{ m}$

$\cos(45^\circ) = \frac{x}{20} = -14.14 \text{ m}$

$-14.14\hat{i} + 14.14\hat{j}$

2.



x 0.5 km y 0.5 km

$$\frac{y}{0.25} = \sin(45^\circ) = 0.18 \text{ km}$$

$$\frac{x}{0.25} = \cos(45^\circ) = 0.18 \text{ km}$$

$x \hat{i}$	$y \hat{j}$
0.18 km	0.18 km
0.5 km	0.5 km
0.68	0.68

$$0.68 \hat{i} + 0.68 \hat{j}$$

$$\text{Distance} = 0.5 + 0.5 + 0.25 = 1.25 \text{ km}$$

For this one, I meant the magnitude of $0.68 \hat{i} + 0.68 \hat{j}$, but the total distance is 1.25 km if you follow the path

$$4.1 \quad x(t) = -1.0 - 4.0t \text{ m}$$

$$a) \quad \Delta x = x_f - x_i$$

$$x_f = x(2) = -1.0 - 4.0(2) \text{ m} = -9.0 \text{ m}$$

$$x_i = x(-2) = -1.0 - 4.0(-2) \text{ m} = 7.0 \text{ m}$$

$$\Delta x = -9.0 - 7.0 \text{ m} = -16.0 \text{ m}$$

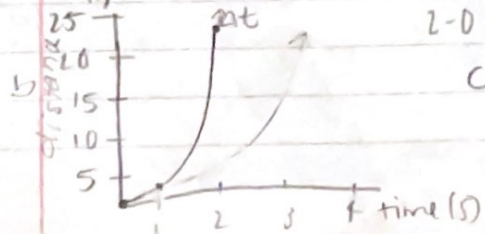
$$b) \quad v = \frac{\Delta x}{\Delta t} = \frac{-16.0 \text{ m}}{4 \text{ s}} = -4.0 \text{ m/s}$$

$$2 - (-2) = 4$$

(-1) The velocity is a linear graph

$$2. \quad x(t) = -2t + 7t^2$$

$$a) \quad v = \frac{\Delta x}{\Delta t} = \frac{x(2) - x(0) \text{ m}}{2.0 \text{ s} - 0 \text{ s}} = \frac{24 \text{ m} - 0 \text{ m}}{2 \text{ s}} = 12 \text{ m/s}$$



$$c) \quad \frac{-2(1) + 7(1)^2 \text{ m}}{1 \text{ s}} = 5 \text{ m/s}$$

$$a) a = \frac{\Delta v}{\Delta t} = \frac{12 \text{ m/s}}{2.0 \text{ s}} = \boxed{6 \text{ m/s}^2}$$

$$3.) a = 5.0 \text{ m/s}^2 \quad v_i = 0 \text{ m/s}$$

$$a) a = \frac{\Delta x}{\Delta t} \quad 5.0 \text{ m/s}^2 = \frac{10 \text{ m/s}}{\Delta t} \quad \Delta t = \frac{10 \text{ m/s}}{5.0 \text{ m/s}^2} = \boxed{2 \text{ s}}$$

$$b) x(t) = \frac{1}{2} (5.0 \text{ m/s}^2) (2 \text{ s})^2 + (0 \text{ m/s}) (2 \text{ s}) + 0$$

$$\boxed{x(t) = 10 \text{ m}}$$

$$c. 100 \text{ m} - 10 \text{ m} = 90 \text{ m}$$

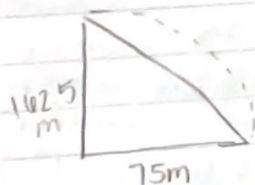
$$10 \text{ m/s} = 90 \text{ m/t}$$

$$10x = 90$$

$$x = 9$$

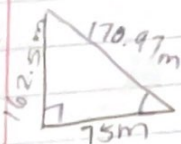
$$9 \text{ s} + 2 \text{ s} = \boxed{11 \text{ s}}$$

5.) 1.



This solution is technically not right, but it is clever and comes very close to the right result! The trajectory is not straight, but quadratic.

b.



$$162.5^2 + 75^2 = x^2$$

$$x = 170.97$$

$$\theta \tan(\theta) = \frac{162.5 \text{ m}}{75 \text{ m}} = 65.22^\circ$$

$$R = \frac{v_0^2 \sin(2\theta_0)}{g}$$

$$75 \text{ m} = \frac{v_0^2 \sin(2 \cdot 65.22^\circ)}{9.8 \text{ s}}$$

$$v_0 = 31.08 \text{ m/s}$$

$$v_{x,i} = v_0 \cos(\theta)$$

$$v_{x,i} = 31.08 \text{ m/s} \cdot \cos(65.22^\circ)$$

$$\boxed{v_{x,i} = 13.08 \text{ m/s}}$$

2.



$$R = \frac{V_0^2 \sin(2\theta)}{g} = \frac{(40 \text{ m/s})^2 \sin(2 \cdot 20^\circ)}{9.8} = \boxed{103.20 \text{ m}}$$

b)

$$x(t) = (x_i + v_{xi}t) \uparrow$$

$$103.20 \text{ m} = 0 \text{ m} + 40 \text{ m/s} \cdot t$$

$$\boxed{2.580 \text{ s} = t}$$

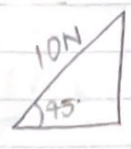
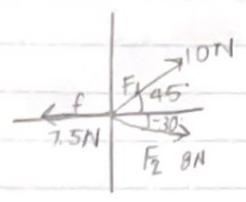
(-1) Use the time of flight formula

c)

$$m = 49.0 \text{ kg}$$

$$\vec{F}_{\text{net}} = m\vec{a}$$

$$\vec{W} = mg$$

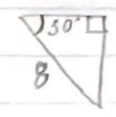


$$x = 7.1 \text{ N} + 0.9 \text{ N} = 8.0 \text{ N}$$

$$y = 7.1 \text{ N} + (-4.0 \text{ N}) = 3.1 \text{ N}$$

$$\cos(45^\circ) \cdot 10 = 7.1 \text{ N}$$

$$\sin(45^\circ) \cdot 10 = 7.1 \text{ N}$$



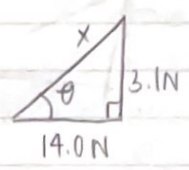
$$\cos(30^\circ) \cdot 8 = 0.9 \text{ N}$$

$$\sin(30^\circ) \cdot 8 = -4.0 \text{ N}$$

$$x^2 = 8.0^2 + 3.1^2$$

$$x = 8.6 \text{ N}$$

$$\tan^{-1} \frac{3.1 \text{ N}}{8.0 \text{ N}}$$



$$\theta = 12^\circ$$

$$\frac{8.6 - 7.5}{49.0} = \frac{49.0 \cdot a}{49.0}$$

$$a = \frac{1.1}{49.0} = \boxed{0.022 \text{ m/s}^2}$$

Nicely done!