

Physics Midterm

1. a) at $r = 1 \text{ mm}$

$$E = 2 \times 10^{-3}$$

$$E = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$$

$$2 \times 10^{-3} = \frac{1}{4\pi\epsilon_0} \frac{q}{(1 \times 10^{-3})^2}$$

Value at $r = 5 \text{ mm}$

$$E = \frac{1}{4\pi\epsilon_0} \frac{q}{(5 \times 10^{-3})^2}$$

$$E = 2 \times 10^{-3} \times 10^{-6} \cdot \frac{1}{25 \times 10^{-6}}$$

$$E = 0.08 \times 10^{-3} \Rightarrow 8 \times 10^{-5} \text{ V/m}$$

b) $1 \mu\text{C}$ charge $E = 8.00 \times 10^{-3} \text{ V/m}$ In this the electric field is 3X bigger so we need to multiply $(8 \times 10^{-3} \text{ V/m})$ 3 times 3 because it is a scaling problem

$$L = 24 \times 10^{-3} \text{ V/m}$$

2. a) mass = $4 \times 10^{-16} \text{ kg}$ Electric field = 6131.25 N/C let Charge = q

$$qE = mg$$

$$q = \frac{mg}{E} \rightarrow q = \frac{4 \times 10^{-16} \times 9.8}{6131.25} \Rightarrow q = 6.39 \times 10^{-19}$$

We know $q = ne$

$$\frac{q}{e} = n \rightarrow n = \frac{6.39 \times 10^{-19}}{1.6 \times 10^{-19}} \approx 3.99 \Rightarrow n = 4 \text{ electrons}$$

b) IF one electron removed...

$$q' = q - e = 4.793 \times 10^{-19}$$

Electrostatic Force: $q'E$ (F_e)

$$F_e = q'E \rightarrow F_e = (4.793 \times 10^{-19})(6131.25) = 2.9 \times 10^{-15}$$

Mass of drop is

$$m' = m - me \approx 4.0 \times 10^{-16} \text{ kg}$$

Gravitational Force

$$F_g = m'g$$

$$= 4.0 \times 10^{-16} \times 9.8 \Rightarrow F_g = 3.92 \times 10^{-15} \text{ N}$$

Acceleration

$$a = \frac{F_g - F_e}{m} \rightarrow \frac{3.92 \times 10^{-15} - 2.939 \times 10^{-15}}{4 \times 10^{-16}}$$

$$a = 2.45 \text{ m/s}^2$$

Potential Energy : Voltage, Capacitors

1. a) $KE = 9V$

$$KE_{\text{hydrogens}} = (1.6 \times 10^{-19})(4 \times 10^3) = 6.4 \times 10^{-16} \text{ J} \Rightarrow 3995 \text{ electron-volts}$$

$$1J = 6.242 \times 10^8 (6.4 \times 10^{-16})(6.242 \times 10^8) = 3994.88$$

$$\text{Total: } 11985 \text{ electron-volts}$$

$$KE_{\text{Helium}} = (2 \times 10^{-19})(4 \times 10^3) = 12.8 \times 10^{-16} \text{ J} \Rightarrow 7990 \text{ electron-volts}$$

$$1J = 6.242 \times 10^8 (12.8 \times 10^{-16})(6.242 \times 10^8) = 7989.76$$

b) $E = -\frac{\Delta V}{\Delta x} \rightarrow \frac{4 \times 10^3}{5 \times 10^{-2}} = -8 \times 10^4 \text{ V/m}$

$$(5 \text{ cm} \rightarrow 5 \times 10^{-2} \text{ m})$$

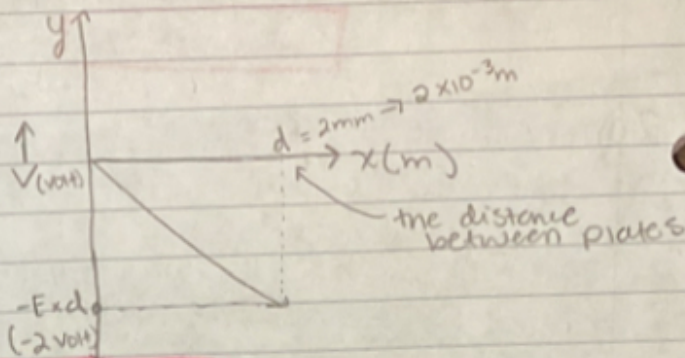
2 $E = 1000 \text{ V/m}$

$$\rightarrow E = -\frac{dV}{dx} \text{ or } V = -E \times x$$

$$\text{Slope} = -1000 \text{ V/m}$$

$$-y \text{ intercept is zero}$$

* Graph is between V & x is straight line w/ -ve slope



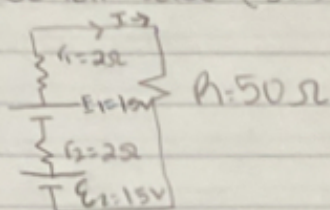
3. a) $C = \frac{\epsilon_0 A}{d} = \frac{8.85 \times 10^{-12} \times 10^{-4}}{2 \times 10^{-3}} = 4.425 \times 10^{-13} \text{ F}$

b) Energy = $\frac{1}{2} CV^2$
 $= \frac{1}{2} (4.425 \times 10^{-13}) (5)^2$
 $= 5.5 \times 10^{-12} \text{ J}$

4. To get a system with more capacitance, we should connect the identical capacitors in parallel because in parallel combination capacitance gets added up in parallel combination
 $C_{\text{net}} = C_1 + C_2 = 2C$
 but in series C_{net} becomes $C/2$ so the inverse

Current, Resistance, and DC circuits

1. a) Serial case (3V)



Kirchoff's rule

$$-E_2 + I r_2 + I r_1 - E_1 + I R = 0$$

$$I = \frac{3V}{r_1 + r_2 + R} = \frac{3}{2 + 2 + 50} = \frac{3}{54}$$

$$I = 0.0555 A \Rightarrow \boxed{55.6 mA}$$

b) Power consumption series

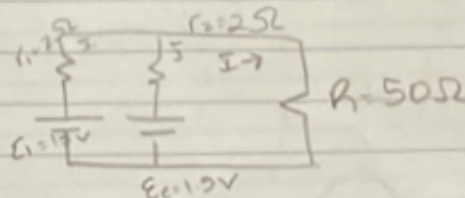
$$P = IV$$

$$V_{tot} = V_1 + V_2$$

$$P = (55.6 \times 10^{-3})(3) = 0.1668 W$$

$$= \boxed{166.8 mW}$$

Parallel case



$$I = I_1 + I_2$$

$E = 1.5V$ the system is in Parallel

$$I = \frac{V}{R}$$

$$I = \frac{1.5}{50} \rightarrow 0.03 \Rightarrow \boxed{30 mA}$$

Power consumption Parallel

$$P = IV$$

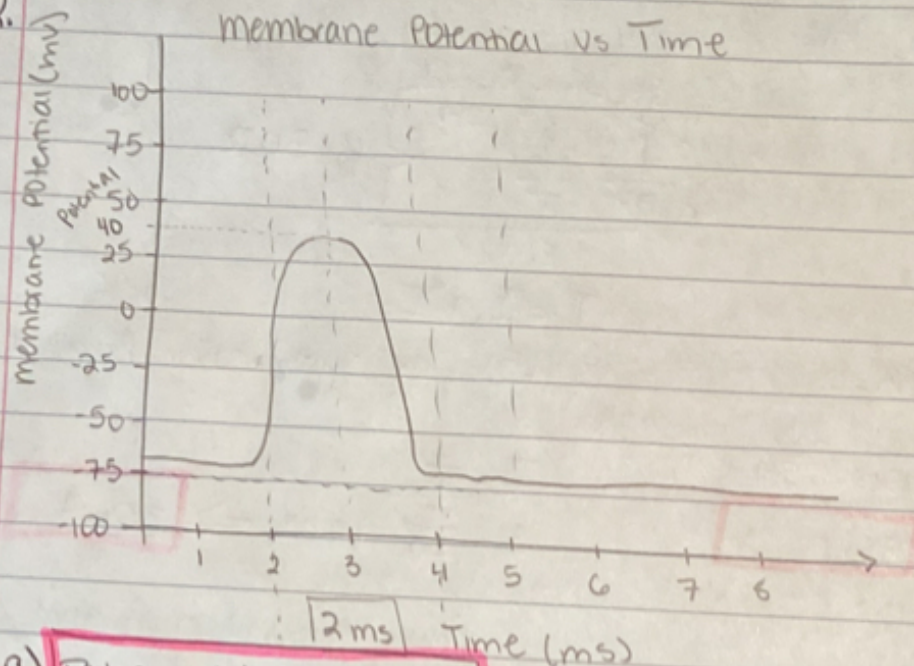
$$V_{tot} = 1.5V$$

$$P = (30 \times 10^{-3})(1.5) = 0.045$$

$$= \boxed{45 mW}$$

c) Checked on PhET ✓ correct

2.



a) Pulse width is 2 ms

b) Peak to Peak voltage
 $= 40 - (-75)$
 $= 40 + 75$

$$V_{\text{peak peak}} = 115 \text{ mV}$$