

midterm +1 for calligraphy

1) a) $E = \frac{1}{4\pi\epsilon_0} \frac{q_1}{r^2}$ @ $r = 1 \text{ mm}$
 $E = 2 \times 10^{-3}$

$$2 \times 10^{-3} = \frac{1}{4\pi\epsilon_0} = \frac{q}{(1 \times 10^{-3})^2}$$

$$r = 5 \text{ mm} \rightarrow E = \frac{1}{4\pi\epsilon_0} \frac{q}{(5 \times 10^{-3})^2}$$

$$E = 2 \times 10^{-3} \times 10^{-6} \cdot \frac{1}{25 \times 10^{-6}} \rightarrow \boxed{8 \times 10^{-5} \frac{\text{V}}{\text{C}}} \quad (\text{N/C})$$

b) $8 \times 10^{-3} = \frac{1}{4\pi\epsilon_0} \frac{1 \times 10^{-6}}{r^2}$

$$3 \mu\text{C} \rightarrow E = \frac{1}{4\pi\epsilon_0} \frac{3 \times 10^{-6}}{r^2}$$

$$= 8 \times 10^3 \times 3 \times 10^{-6} = \boxed{24 \times 10^{-3} \frac{\mu}{\text{C}}} \quad (\text{N/C})$$

2) a) $m = 4 \times 10^{-16} \text{ kg}$, $E = 6131.25 \text{ N/C}$

a) one electron = $9.1 \times 10^{-31} \text{ kg}$

$$\text{total \# of electrons} = \frac{4 \times 10^{-16}}{9.1 \times 10^{-31}}$$

neglects p^+ and
neutrons, but I
mean the excess
electrons
($4e^-$)

$$= \boxed{4.39 \times 10^{14}}$$

b) $q = 4.39 \times 10^{14} \times 1.6 \times 10^{-19} = 7.03 \times 10^{-5} \text{ C}$

$$qE = ma = \frac{7.03 \times 10^{-5} \times 6131.25}{4 \times 10^{-16}} = \boxed{1.078 \times 10^{15} \text{ m/sec}^2}$$

(would have been right)

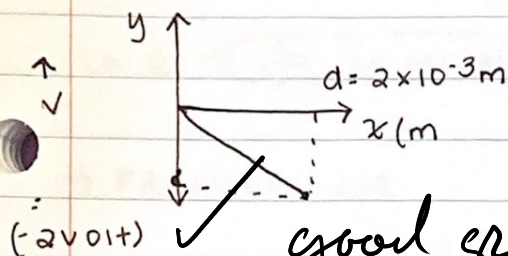
1) a) $K \cdot E = qV$

$$KE_{Hyd} = 1.6 \times 10^{-19} \times 4 \times 10^3 = 6.4 \times 10^{-16} \text{ J}$$

$$KE_{He} = 2 \times 1.6 \times 10^{-19} \times 4 \times 10^3 = 12.8 \times 10^{-16} \text{ J}$$

b) $E = \frac{\Delta V}{\Delta x} = \frac{4 \times 10^3}{5 \times 10^{-2}} = \boxed{8 \times 10^4 \text{ V/m}}$

2) $E = 1 \text{ kV/m}$ or 1000 V/m



the slope is $= m = -1000 \text{ V/m}$

the y-int of the fcn is 0 as the graph initiates at the origin.

3) a) $C = \frac{\epsilon_0 A}{d} = \frac{8.85 \times 10^{-12} \times 10^{-4}}{2 \times 10^{-3}} = \boxed{4.425 \times 10^{-13} \text{ F}}$

b) $E = \frac{1}{2} CV^2 = \frac{1}{2} \times 4.425 \times 10^{-13} \times 25 = \boxed{55.31 \times 10^{-13} \text{ J}}$

4) To get more capacitance, we should connect the identical capacitors in parallel. The total capacitance will increase.

$$I = ? \quad R = 50\Omega$$

$$50^2 \times 50 = 5^2 \times 100 \times 5 \times 10^3 = 125 \times 10^3$$

1) a) $r_1 = 2\Omega$

$$E_1 = 1.5V$$

$$\rightarrow -E_2 + I r_2 + I r_1 - E_1 + I R = 0$$

$$r_2 = 2\Omega$$

$$= -1.5 + I(r_1 + r_2 + R) - 1.5V = 0$$

$$E_2 = 1.5V$$

$$I = \frac{3V}{r_1 + r_2 + R} = \frac{3}{2 + 2 + 50} = \boxed{55.56 \text{ mA}}$$

$$(1 \text{ mA})^2 \times 25\Omega = 10^{-6} \text{ A}^2 \times 25\Omega = 10^{-3} \text{ mW}$$

b) $P_{\text{total}} = P_{r_1} + P_{r_2} + P_R$

$$= (55.56 \text{ mA})^2 \times 2 + (55.56 \text{ mA})^2 \times 2 + (55.56 \text{ mA})^2 \times 50$$

with $r_{\text{eq}} = \boxed{777.51 \text{ mWatts}}$

⊖ this works if the parallel is linear

in R $\rightarrow \boxed{154.34 \text{ mWatts}}$

→ Parallel case:

$$\frac{V_x - 1.5}{2} + \frac{V_x - 1.5}{2} + \frac{V_x}{50} = 0$$

$$25V_x - 37.5 + 25V_x - 37.5 + V_x = 0$$

$$= \boxed{1.47 \text{ V}}$$

$$I_1 = \frac{1.5 - 1.47}{2} = 15 \text{ mAmp}$$

$$I_2 = \frac{1.5 - 1.47}{2} = 15 \text{ mAmp}$$

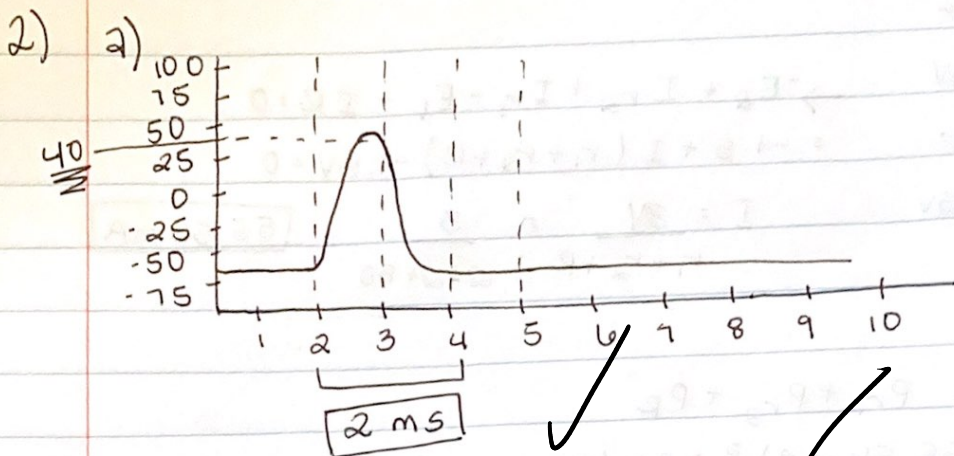
$$\left. \begin{array}{l} 15 \text{ mAmp} \\ 15 \text{ mAmp} \end{array} \right\} \underline{30 \text{ mAmp}}$$

Total PC: $P_{r_1} + P_{r_2} + P_R$

$$= (15 \text{ m})^2 \times 2 + (15 \text{ m})^2 \times 2 + (30 \text{ m})^2 \times 50$$

$$= \boxed{45.9 \text{ mW}}$$

R $\rightarrow \boxed{45 \text{ mW}}$



b) $40 - (-15) = 40 + 15 = 115 \text{ mV}$