

SUBJECT: physics midterm

2. Estimations and Unit Analysis

1. a) what is the speed of sound in meters per second?

$$t = 1.5 \text{ sec} \quad x = 0.5 \text{ km}$$

$$\frac{0.5 \text{ km}}{1 \text{ km}} \times \frac{1000 \text{ m}}{1 \text{ km}} = 500 \text{ m} = d/t$$

$$500 \text{ m} / 1.5 = 333.3 \text{ m/s}$$

b) what is it in kilometers per hour

$$\frac{0.5 \text{ km}}{1.5 \text{ sec}} \times \frac{60 \text{ sec}}{1 \text{ min}} \times \frac{60 \text{ min}}{1 \text{ hour}} = 1200 \text{ km/hr}$$

2. a) what is 0.25 m^3 in cm^3 ?

$$0.25 \text{ m}^3 \left(\frac{100 \text{ cm}}{1 \text{ m}} \right)^3 = 250,000 \text{ cm}^3$$

b) what is 100 km/hour in m/s ?

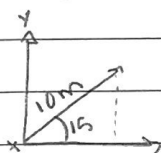
$$\frac{100 \text{ km}}{1 \text{ hr}} \times \frac{1000 \text{ m}}{1 \text{ km}} \times \frac{1 \text{ hour}}{60 \text{ min}} \times \frac{1 \text{ min}}{60 \text{ sec}} = 27.78 \text{ m/s}$$

c) what is 2 kg m s^{-2} in gm cm ms^{-2} ?

$$\frac{2 \text{ kg m}}{\text{s}^2} \left(\frac{1000 \text{ g}}{1 \text{ kg}} \right) \left(\frac{100 \text{ cm}}{1 \text{ m}} \right) = 2 \times 10^5 \text{ g cm/s}^2$$

3. Vectors

1 a) \vec{x}_1 is a vector w/ a magnitude of 10 meters and makes an angle of 15 degrees w/ respect to y-axis.



$$10 \sin(15) = 2.59 \text{ m} \quad 10 \cos(15) = 9.66 \text{ m}$$

$$\vec{x}_1 = 9.66 \hat{i} + 2.58 \hat{j}$$

b) \vec{x}_2 is a vector w/ a magnitude 20 meters that makes an angle 135 degrees w/ respect to x-axis

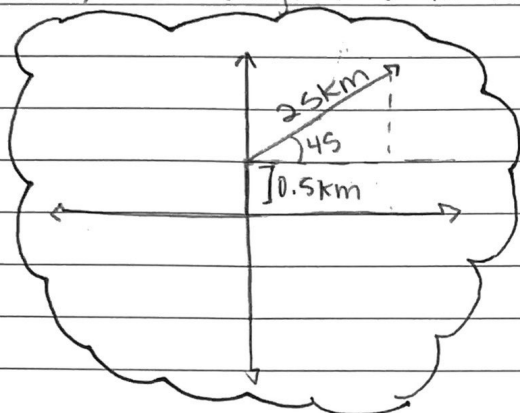
$$20 \cos(135) = -14.14 \text{ m}$$

$$20 \sin(135) = 14.14 \text{ m}$$

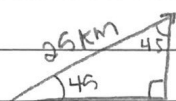
$$\vec{x}_2 = -14.14 \hat{i} + 14.14 \hat{j}$$

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2. a) Draw diagram of their trajectory (E is x-axis, N is y-axis)



b) what is the final location in x-y coordinates?



$$(0.25)\cos(45) = 0.176\hat{j}$$

$$(0.25)\sin(45) = 0.176\hat{i}$$

$$0.5 + 0.176 = 0.67$$

$$x_f = 0.67\text{ km}\hat{i} + 0.67\text{ km}\hat{j}$$

c) what is the distance from the origin?

$$\sqrt{0.67^2 + 0.67^2} = \sqrt{C^2}$$

$$C = 0.95\text{ km}$$

4. Motion Along a straight line

1 a) what is the displacement of the particle btwn

$$t = -2.0\text{ sec} \text{ to } t = 2.0\text{ sec?}$$

$$\Delta x = x_f - x_i$$

$$x(t) = -1.0 - 4.0t\text{ m}$$

$$x_f = -1.0 - 4.0(2)\text{ m} = -9.0\text{ m}$$

$$\Delta x = -9.0 - 7.0 = -16\text{ m}$$

$$x_i = -1.0 - 4.0(-2\text{ m}) = 7.0\text{ m}$$

b) what is the velocity?

$$v = x/t$$

$$v = -16.0\text{ m} / 4\text{ sec} = -4\text{ m/s}$$

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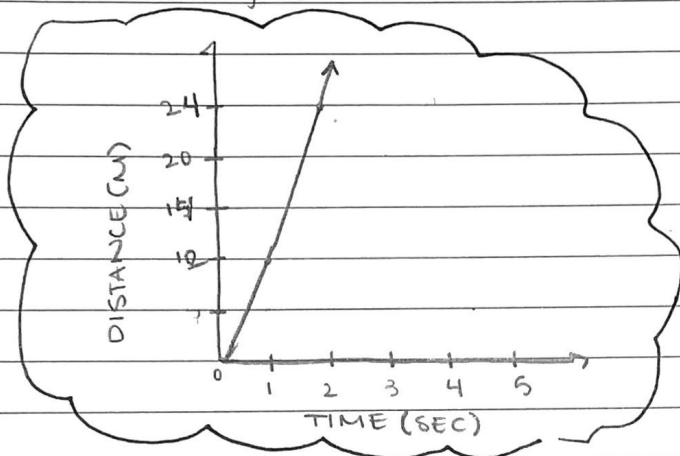
2. $x(t) = -2(t) + 7(t)^2$

a) what is the average velocity btwn $t=0$ + $t=2$ sec?

$x(0) = -2(0) + 7(0)^2$ $x = 0$ $v = \frac{\Delta x}{\Delta t}$ $\frac{24-0}{2-0} = 12 \text{ m/s}$

$x(2) = -2(2) + 7(2)^2$ $x = 24$ Δt $2-0$
 $-4 + 7(4)$
 $-4 + 28$
 $= 12 \text{ m/s}$

b) Draw a graph of the velocity.



c) what is the instantaneous velocity at $t=1$ second?

$x(1) = -2(1) + 7(1)^2$
 $-2 + 7 = x = 5 \text{ m/s}$

d) what is the acceleration?

$a = \frac{\Delta v}{\Delta t} = \frac{12 \text{ m/s}}{2 \text{ m/s}} = 6 \text{ m/s}^2$

3. a) How long does it take her to reach her top speed of 10.0 m/s ?

constant acceleration $(a) = 5.0 \text{ m/s}^2$

$a = \frac{\Delta v}{\Delta t}$ $(t) \frac{5.0 \text{ m/s}^2}{5.0} = \frac{10 \text{ m/s}}{5.0 \text{ m/s}^2} (t)$

$t = 2 \text{ seconds}$

b) what is her displacement at that time?

$x(t) = \frac{1}{2} (5.0 \text{ m/s}^2) (2 \text{ s})^2 + (0) + 0$
 $\frac{1}{2} (20)$
 $x(t) = 10 \text{ m}$

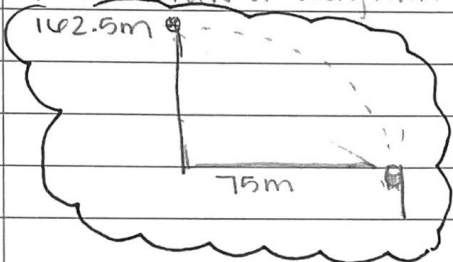
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c) suppose she is running the 100 m sprint. If she continues at 10.0 m/s for the remainder of the race, what will be her total time?

$$100\text{m} - 20\text{m} = 80\text{m} / 10\text{m/s} = 8\text{s} + 2\text{s} = 10\text{seconds}$$

5 motion in two + Three Dimensions

1. a) draw a diagram of the situation.



b) what is the horizontal velocity required to make the shot?

$$a = 9.81\text{m/s}^2$$

$$\Delta x = 75\text{m}$$

$$\Delta y = -162.5\text{m}$$

$$V_{0x} = ?$$

$$a_y = -9.81\text{m/s}^2$$

$$75\text{m} = V_{0x}(5.76\text{s})$$

$$162.5\text{m}^2 = 0 + \frac{1}{2}(9.81\text{m/s}^2)t^2$$

$$V_{0x} = 13.02\text{m/s}$$

$$t = 5.76\text{s}$$

2. a) How far away does it land?

$$R = \frac{V_0^2 \sin(2\theta)}{g} = \frac{(40)^2 \sin 2(45)}{9.81} = 63\text{m}$$

b) How long is it in the air?

$$T = \frac{2V_0 \sin(\theta)}{g} = \frac{2(40) \sin 45}{9.81} = 6\text{seconds}$$

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6 Forces

1. Two children pull a third child on a snow saucer sled exerting forces \vec{F}_1 & \vec{F}_2 as shown from above in Fig. 1. Find the acceleration of the system if the mass of the child and sled together is 49.0 kg. Note that the direction of the frictional force is unspecified; it will be in the opposite direction of the sum of \vec{F}_1 and \vec{F}_2 .

$$\begin{aligned}\vec{F}_1 \quad x &= 10 \cos 45 & y &= 10 \sin 45 \\ &= 7.07 \text{ N} & &= 7.07 \text{ N}\end{aligned}$$

$$\begin{aligned}\vec{F}_2 \quad x &= 8 \cos 30 & y &= 8 \sin 30 \\ &= 6.92 \text{ N} & &= -4 \text{ N}\end{aligned}$$

$$\begin{aligned}R \quad x &= 13.99 \text{ N} & y &= 3.07 \text{ N} \\ R &= \sqrt{13.99^2 + 3.07^2} = 14.32 \text{ N}\end{aligned}$$

$$\tan \theta = 3.07 / 13.99 \quad \theta = 12.37^\circ$$

$$F_{\text{net}} = ma_x = 14.32 - 7.5 = 49(a)$$

$$\frac{6.82}{49} = \frac{49(a)}{49}$$

$$a = 14 \text{ m/s}^2$$