

Algebra-Based Physics: Electricity, Magnetism, and Modern Physics (PHYS135B): Unit 4

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November 9, 2023

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Summary

Summary

1. Magnetic induction - **Chapters 23.1 - 23.5, 23.7, 23.9**

- Induced EMF and magnetic flux
- Faraday's Law
- Motional EMF, generators, and transformers

2. AC circuits - **Chapters 23.9 - 23.12**

- Inductors
- RL circuits
- RLC circuits

Magnetic induction

Magnetic induction

First set of observations: a *moving* magnet can induce an emf in a coil of wire. The induced current polarity depends on (a) magnet polarity and (b) direction of magnet velocity. The induced current magnitude

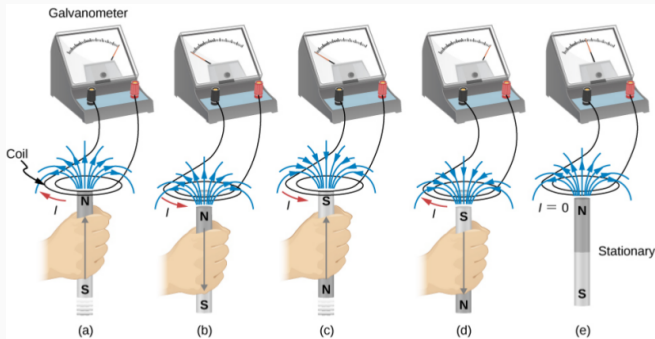


Figure 1: Observations of magnetic induction.

Magnetic induction

Second set of observations: a *changing* current in a loop can induce an emf in another loop. The induced current polarity depends on (a) inducing current polarity and (b) whether the inducing current is increasing or decreasing.

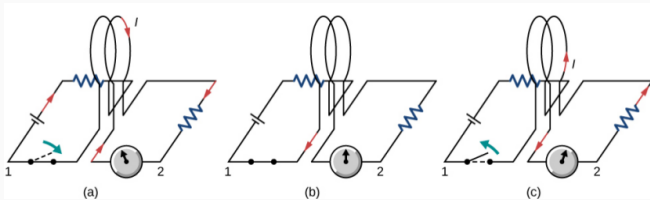


Figure 2: Observations of magnetic induction.

Magnetic induction

Third observation: a *changing* loop area in a magnetic field induces an emf, and current. The induced current polarity depends on whether the loop area is (a) increasing or (b) decreasing. The current magnitude depends on how quickly the area is changing.

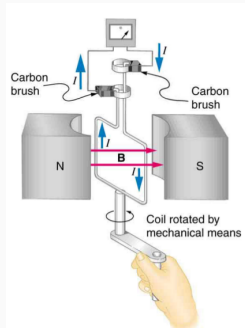


Figure 3: Observations of magnetic induction.

Magnetic induction

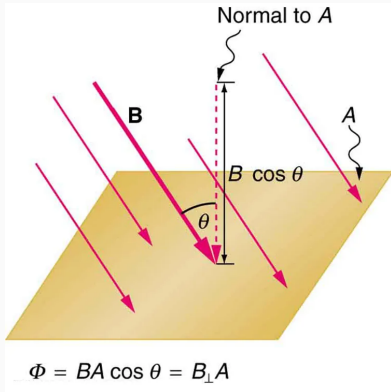
Video summary of magnetic induction:

https://youtu.be/pQp6bmJPU_0

- Magnet inducing current in loop of wire
- Solenoids inducing current in adjacent solenoids
- Magnetic flux
- Faraday's Law
- Lenz's Law

Magnetic induction

Magnetic flux is the dot-product of the area vector and the magnetic field through loops of wire with area A .



The **area vector** has a magnitude A , the area of the loop. The direction of the area vector is *normal* to the area of the loop.

$$\vec{A} = A\hat{n} \quad (1)$$

The magnetic flux, Φ , is therefore

$$\Phi = \vec{B} \cdot \vec{A} \quad (2)$$

Figure 4: The area vector is *normal* to the loop area.

Faraday's Law

Faraday's Law

Faraday's Law

Let the product of the magnetic field and the vector area be the magnetic flux: $\Phi = \vec{B} \cdot \vec{A}$. The induced emf ϵ in N turns of a conductor will be

$$\epsilon = -\frac{\Delta\Phi}{\Delta t} \quad (3)$$

The induced current from ϵ will create a new B-field that opposes changes in Φ .

The unit of magnetic flux is the Weber, or $1 \text{ Wb} = 1 \text{ T m}^2$.

Faraday's Law

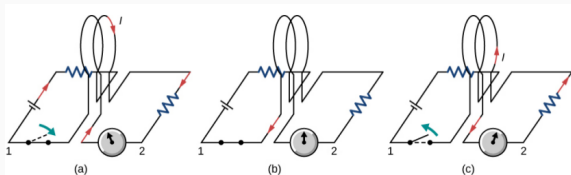


Figure 5: A pickup coil system.

Suppose the switch in Fig. 5 (a) is closed, inducing a current I in the right-hand loop. The B-field directions at the centers of the left and right loops are

- A: Right and left, respectively
- B: Left and right, respectively
- C: Both to the right
- D: Both to the left

Faraday's Law

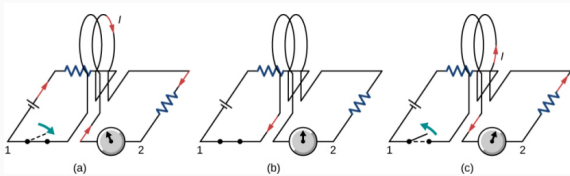


Figure 6: A pickup coil system.

Suppose the switch in Fig. 5 (b) remains closed, and no induced current is observed. This is because

- A: The magnetic flux is zero
- B: The inducing current is zero
- C: The magnetic flux is not changing
- D: The loop area is zero

Faraday's Law

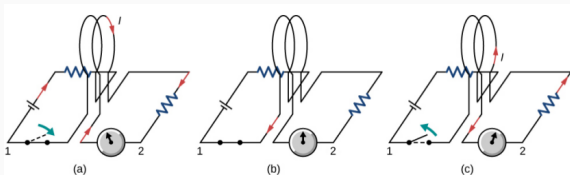


Figure 7: A pickup coil system.

Suppose the switch in Fig. 5 (b) remains closed, and no induced current is observed. This is because

- A: The magnetic flux is zero
- B: The inducing current is zero
- C: The magnetic flux is not changing
- D: The loop area is zero

Faraday's Law

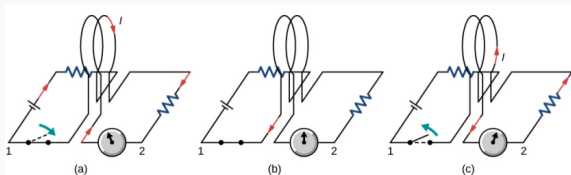


Figure 8: A pickup coil system.

Suppose the switch in Fig. 5 (c) is opened. The induced current in Fig. 5 is in the opposite direction of Fig. 5 (c) because

- A: The magnetic field from the right loop decreased
- B: The magnetic field from the left loop increased
- C: The magnetic field from the left loop is constant
- D: The magnetic field from the left loop decreased

Faraday's Law

Group board problem:

A magnetic field B passes orthogonally through a circular coil of radius $r = 0.05$ m and $N = 100$ turns. The field magnitude decreases linearly according to

$$B(t) = B_0 - at \quad (4)$$

with $B_0 = 0.015$ T and $a = 0.01$ T s⁻¹. (a) Calculate the magnitude of the emf induced in the coil at the times $t_0 = 0$, and $t_2 = 1.0$ second. (b) Determine the current in the coil if the resistance is 1Ω .

Sketch this system, and indicate both the direction of the instantaneous B-field, and the direction of current.

Faraday's Law - PhET Activity

Brief simulation of Faraday's Law, and Lenz's Law:

<https://phet.colorado.edu/en/simulations/faradays-law>

1. Learn to control the position and orientation of the bar magnet.
2. Activate the voltmeter in parallel with the light bulb.
3. Use the coil with four loops of wire.
4. Produce the following results:
 - A positive voltage from a moving bar magnet
 - A negative voltage from a moving bar magnet
 - A positive voltage from switching the bar magnet polarity
 - A negative voltage from switching the bar magnet polarity
5. Is your voltage positive or negative when you are increasing Φ ?
How do you *decrease* Φ ?

Motional EMF, Generators, and Transformers

Motional EMF, Generators, and Transformers

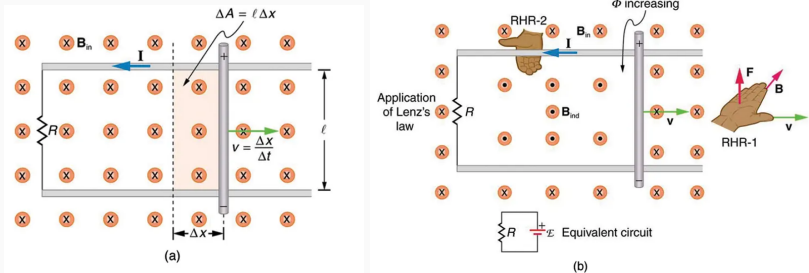


Figure 9: Motional emf in a loop with changing area.

Group board problems:

1. Show that power is $P = \vec{F} \cdot \vec{v}$ when acceleration is constant.
2. Show that the emf is $\epsilon = Blv$, where l is the length of the rod.
3. Show that power generated, $P = I^2 R = \epsilon/R$, is equal to power injected.

Motional EMF, Generators, and Transformers

How do we use Faraday's Law to induce power in a generator?

Start with Faraday's Law:

$$\epsilon = -N \frac{\Delta \Phi}{\Delta t} \quad (5)$$

The flux Φ depends on time:

$$\Phi = \vec{B} \cdot \vec{A}(t) = BA \cos(\theta(t)) \quad (6)$$

Let the *angular velocity* be constant: $\theta = \omega t$. Then we have

$$\Phi = BA \cos(\omega t) \quad (7)$$

Thus the emf (with N loops) is (...calculus...)

$$\epsilon = N\omega BA \sin(\omega t) = \epsilon_0 \sin(\omega t) \quad (8)$$

Motional EMF, Generators, and Transformers

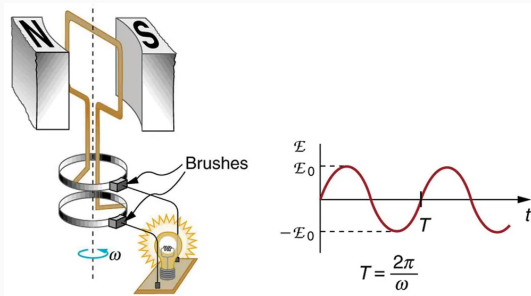


Figure 10: (Left) The AC generator with brushes generates an AC voltage. (Right) This is a diagram of the AC voltage.

- Amplitude: ϵ_0 , the maximum value of the AC signal. Units: Volts.
- Period: $T = 2\pi/\omega$, the time to complete one AC cycle. Units: seconds.
- Frequency: $f = 1/T$, the number of cycles per second. Units: Hertz.

Motional EMF, Generators, and Transformers

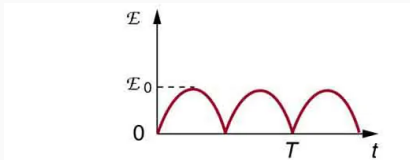
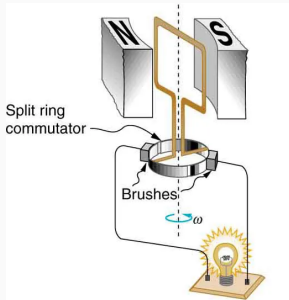


Figure 11: (Left) The AC generator with brushes and *commutator* generates pulsed DC. (Right) This is a diagram of the signal.

- Amplitude: E_0 , the maximum value of the AC signal. Units: Volts.
- Period: $T = 2\pi/\omega$, the time to complete one AC cycle. Units: seconds.
- Frequency: $f = 1/T$, the number of cycles per second. Units: Hertz.

Motional EMF, Generators, and Transformers

Equation 9 is a basic model for the emf from a generator.

$$\epsilon = N\omega BA \sin(\omega t) = \epsilon_0 \sin(\omega t) \quad (9)$$

Which of the following would increase the *amplitude* of the emf?

- A: Turning the shaft more slowly
- B: Turning the shaft more quickly
- C: Decreasing the B-field
- D: Increasing N

Motional EMF, Generators, and Transformers

Equation 10 is a basic model for the emf from a generator.

$$\epsilon = N\omega BA \sin(\omega t) = \epsilon_0 \sin(\omega t) \quad (10)$$

Which of the following would increase the *frequency* of the emf?

- A: Turning the shaft more slowly
- B: Turning the shaft more quickly
- C: Decreasing the B-field
- D: Increasing N

Motional EMF, Generators, and Transformers

Equation 11 is a basic model for the emf from a generator.

$$\epsilon = N\omega BA \sin(\omega t) = \epsilon_0 \sin(\omega t) \quad (11)$$

Group exercise: Suppose an AC generator rotates at 200 rpm, in a B-field with 0.1 T, and has 100 loops with radius 5 cm. (a) What is the peak voltage this generator will produce? (b) If the generator powers a system with resistance of $1\text{k}\Omega$, what will be the peak current?

PhET: Motional EMF, Generators, and Transformers

PhET: AC Power generator

Link to the (CheerpJ) simulation:

<https://phet.colorado.edu/en/simulation/generator>

1. Set the water rate such that the meter reads 10 rotations per minute (rpm).
2. Choose the voltage meter under the pickup coil menu.
3. Under loops, choose 1 loop, and under area, leave it at 50%.
4. Choose show field meter in the upper right, and place the tool in the loop center.
5. On the same graph, plot the average B-field and voltage versus time. What is the period and amplitude of your signal? Use the left y-axis for B-field units, and the right y-axis for voltage units.
6. Create the same graph for $N = 3$ loops.
7. Create the same graph for $N = 1$ loop, but for 20 rpm.

Hint: you know the rpm of the magnet, so you know how much time corresponds to one rotation.

Motional EMF, Generators, and Transformers

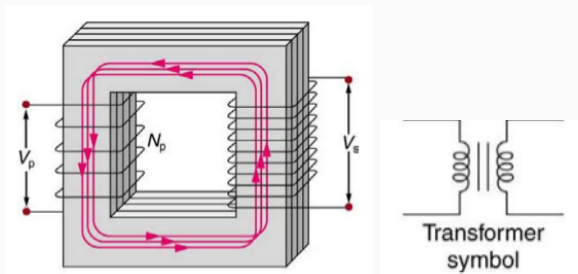


Figure 12: A transformer uses Faraday's law to change voltages in AC-generated systems.

The magnetizable core (gray) creates a loop in the B-field that passes through the left and right coils. Use Faraday's law to show that

$$\frac{V_L}{V_R} = \frac{N_L}{N_R} \quad (12)$$

Motional EMF, Generators, and Transformers

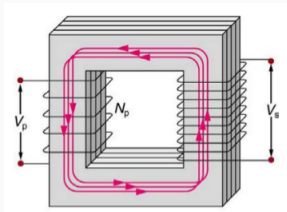


Figure 13: The *transformer* changes AC voltage levels.

Suppose the transformer in Fig. 13 has $N_L = 5$, $N_R = 100$, $V_L = 1$ kV (peak). What is V_R (peak), in kV?

- A: 20 kV
- B: 5 kV
- C: 0.05 kV
- D: 0.05 V

Motional EMF, Generators, and Transformers

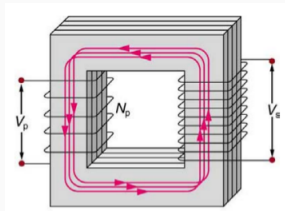


Figure 14: The *transformer* changes AC voltage levels.

Suppose we need the transformer in Fig. 14 to produce $V_R = 120$ V, and $V_L = 12$ kV. Which combination of coils will satisfy the requirement?

- A: $N_L = 3$, $N_R = 10$
- B: $N_L = 10$, $N_R = 1000$
- C: $N_L = 10$, $N_R = 100$
- D: $N_L = 1000$, $N_R = 10$

Motional EMF, Generators, and Transformers

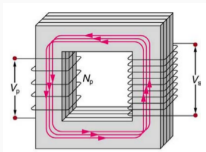


Figure 15: The *transformer* changes AC voltage levels.

If the $V_L \neq V_R$, how are energy and power conserved?

- A: The induced current is larger on the right.
- B: The induced current is smaller on the right.
- C: The induced current is conserved from left to right.
- D: The induced emf is conserved from left to right.

Demonstrate on board how power is conserved by (a) deriving the currents I_L and I_R , then forming the powers P_L and P_R .

Inductors

Inductors

It turns out you can *reverse* transformers, through symmetry. Between the coils in the transformer in Fig. 15, there is *mutual inductance*, M :

$$\epsilon_R = -M \frac{\Delta I_L}{\Delta t} \quad (13)$$

$$\epsilon_L = -M \frac{\Delta I_R}{\Delta t} \quad (14)$$

The **inductance** accounts for everything except the current: the geometry, number of turns, and field strength. Inductance is useful for systems with fixed geometry, where we often do not need to know Φ .

Derive an expression that relates M to Φ , given the original version of Faraday's Law.

Inductors

Consider the case of **self-inductance**, L , which accounts for the magnetic field created inside (for example) a solenoid when current is introduced. New current creates a change in Φ within the solenoid, so Faraday's Law predicts a backwards emf opposing the change:

$$\boxed{\epsilon = -L \frac{\Delta I}{\Delta t}} \quad (15)$$

The inductance unit is the *Henry* (after Joseph Henry), $\text{V A}^{-1} \text{ s}$, or $\Omega \text{ s}$.

Inductors

Self-inductance applies to increasing and decreasing current:

$$\epsilon = -L \frac{\Delta I}{\Delta t} \quad (16)$$

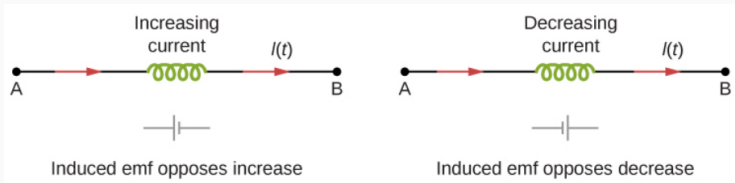


Figure 16: (a) Increasing current yields a negative voltage. (b) Decreasing current yields a positive voltage.

Inductors

Suppose we have an inductor with $L = 0.1 \text{ mH}$, carrying a current of 100 mA . If we switch off the current in 1 ms , what is the induced emf?

- A: 0.1 mV
- B: 1 mV
- C: 10 mV
- D: 100 mV

(Ahh, units ... Got heem! Also, why are the answers *positive*?)

Inductors

Suppose we have a current that switches from 100 mA to -100 mA in 1 ms. We observe a 100 mV emf across the inductor. What is the inductance?

- A: -0.5 mH
- B: -0.5 H
- C: 0.5 H
- D: 0.5 mH

Inductors

What is the **inductance** of a solenoid, given solenoid properties? Recall how the inductance relates to flux, current, and turn number:

$$L = N \frac{\Delta \Phi}{\Delta I} \quad (17)$$

$$L = N \frac{A \Delta B}{\Delta I} \quad (18)$$

$$\Delta B = \mu_0 \left(\frac{N}{l} \right) \Delta I \quad (19)$$

$$L = N \frac{A \mu_0 (N/l) \Delta I}{\Delta I} \quad (20)$$

$$\boxed{L = \frac{\mu_0 N^2 A}{l}} \quad (21)$$

Inductors

Recall the solenoid used in the Ampère's Law lab activity.

Suppose we count $N = 80$ turns, and measure $A = 8 \times 10^{-3} \text{ m}^2$, and $l = 0.1 \text{ m}$. What is the inductance?

- A: 0.6 H
- B: 0.06 H
- C: 6 mH
- D: 0.6 mH

Recall that $\mu_0 = 4\pi \times 10^{-7} \text{ T A}^{-1} \text{ m}$.

What is the inductance of the same solenoid, but with twice the turns?

- A: 2.4 mH
- B: 1.2 mH
- C: 24 mH
- D: 12 mH

This is a scaling problem. How does L depend on N ?

Inductors

How much **energy** is stored in an inductor? Suppose potential energy is considered at a *constant voltage*, given some charging circuit that pushes current through an inductor (with some resistance).

$$\Delta U = \Delta q \epsilon \rightarrow \epsilon = \Delta U / \Delta q \quad (22)$$

$$|\epsilon| = \frac{\Delta U}{\Delta q} = L \frac{\Delta I}{\Delta t} \quad (23)$$

$$\Delta U = L \Delta I \left(\frac{\Delta q}{\Delta t} \right) \quad (24)$$

$$\Delta U = LI \Delta I \quad (25)$$

$$\boxed{U = \frac{1}{2} LI^2} \quad (26)$$

If you do not know how to integrate in the last step, consider the analogy of the area of a triangle.

Inductors

How much energy is stored in an inductor with inductance 50 mH that was charged with a current that reaches 1 A?

- A: 25 J
- B: 2.5 J
- C: 25 mJ
- D: 2.5 mJ

Nom nom nom, more units.

A Massive Clue about Electricity and Magnetism

A Massive Clue

The energy stored in a **capacitor**:

$$\Delta U = \Delta q \epsilon \rightarrow \epsilon = \Delta U / \Delta q \quad (27)$$

$$q = C \epsilon \quad (28)$$

$$q = C \frac{\Delta U}{\Delta q} \quad (29)$$

$$C^{-1} q \Delta q = \Delta U \quad (30)$$

$$\boxed{U = \frac{1}{2} \frac{q^2}{C}} \quad (31)$$

The energy stored in an **inductor**:

$$\Delta U = \Delta q \epsilon \rightarrow \epsilon = \Delta U / \Delta q \quad (32)$$

$$|\epsilon| = \frac{\Delta U}{\Delta q} = L \frac{\Delta I}{\Delta t} \quad (33)$$

$$\Delta U = L \Delta I \left(\frac{\Delta q}{\Delta t} \right) \quad (34)$$

$$\Delta U = L I \Delta I \quad (35)$$

$$\boxed{U = \frac{1}{2} L I^2} \quad (36)$$

It seems the energy stored in a capacitor is *in the E-field*, and the energy stored in the inductor is *in the B-field*. Suppose we charge a parallel plate capacitor and solenoid ($N = 1$) charged with the same current, I , that have the same cross-sectional area A , and the same length d , such that they have equal energies?

A Massive Clue

Assume the proper formulas for capacitance and inductance, and equate energies.

$$C = \frac{\epsilon_0 A}{d} \quad (37)$$

$$L = \frac{\mu_0 N^2 A}{d} \quad (38)$$

$$U_C = U_L \quad (39)$$

$$\frac{1}{2} \frac{Q^2}{C} = \frac{1}{2} L I^2 \quad (40)$$

$$\frac{Q^2 d}{\epsilon_0 A} = \frac{\mu_0 N^2 A I^2}{d} \quad (41)$$

$$N = 1 \quad (42)$$

$$\frac{1}{\epsilon_0 \mu_0} \frac{Q^2}{I^2} = \frac{A^2}{d^2} \quad (43)$$

Recall that the currents used to charge the capacitor and inductor are the same.

$$\frac{Q^2}{I^2} = t^2 \quad (44)$$

Note that the volumes of the capacitor and inductor are both $V = Ad$. Let the lateral dimension of the capacitors (parallel to A) be x , and

$$A = \pi x^2 \quad (45)$$

Combining formulas,

$$\frac{1}{\epsilon_0 \mu_0} = \frac{\pi x^2}{t^2} = v^2 \quad (46)$$

A Massive Clue

The result is a constant **velocity!** Solving for v ,

$$v = \frac{1}{\sqrt{\epsilon_0 \mu_0}} \quad (47)$$

Insert known values for ϵ_0 and μ_0 . What speed do you obtain?

- A: 3×10^6 m/s
- B: 3×10^7 m/s
- C: 3×10^8 m/s
- D: 3×10^9 m/s

The speed of light appears in electromagnetic energy



RL Circuits

RL Circuits

An **RL circuit** is a circuit with some resistance R and some inductance L .

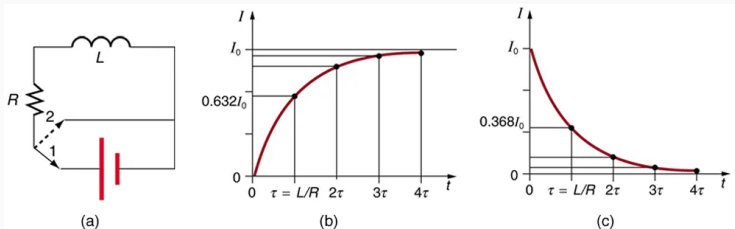


Figure 17: (a) Put switch in lower position to charge inductor, and put switch in upper position to discharge it. (b) The charging current takes a characteristic time to reach the steady state. (d) The discharging current takes a characteristic time to reach zero.

Applying Kirchhoff's loop rule to Fig. 17 (a), we have

$$\mathcal{E} - iR - L \frac{\Delta i}{\Delta t} = 0 \quad (48)$$

- \mathcal{E} is a positive emf in the loop direction.
- The second term is negative because the resistor *decreases the voltage* by consuming energy. The side with the larger voltage is towards the emf.
- The third term is negative because the inductor *produces an emf* counteracting the positive emf. The side with the larger voltage is towards the emf.
- There is an exact solution to this equation. Let $\tau = L/R$:

$$i(t) = \frac{\mathcal{E}}{R} \left(1 - e^{-tR/L}\right) \quad (49)$$

Letting $i_0 = \mathcal{E}/R$, and $\tau = L/R$,

$$i(t) = i_0 \left(1 - e^{-t/\tau}\right) \quad (50)$$

Suppose an RL circuit has an inductance of 1 mH and a resistance of 1 k Ω . What is the time constant?

- A: 1 millisecond
- B: 1 microsecond
- C: 1 nanosecond
- D: 1 second

Letting $i_0 = \mathcal{E}/R$, and $\tau = L/R$,

$$i(t) = i_0 \left(1 - e^{-t/\tau}\right) \quad (51)$$

If $\tau = 1\mu\text{s}$, and $R = 1\text{ k}\Omega$, with $\mathcal{E} = 5\text{V}$, what will the current be after $100\mu\text{s}$?

- A: 1 mA
- B: 5 A
- C: 5 mA
- D: 1 A

Letting $i_0 = \mathcal{E}/R$, and $\tau = L/R$,

$$i(t) = i_0 \left(1 - e^{-t/\tau}\right) \quad (52)$$

If $\tau = 1\mu\text{s}$, and $R = 1\text{ k}\Omega$, with $\mathcal{E} = 5\text{V}$, what will the current be at $1\mu\text{s}$?

- A: 1.20 mA
- B: 3.16 mA
- C: 4.12 mA
- D: 10.1 mA

RL Circuits

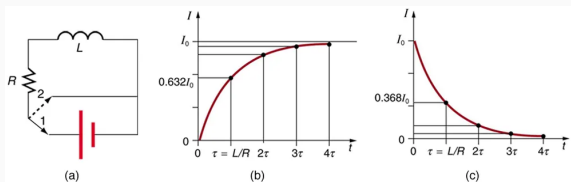


Figure 18: Current discharge is not instantaneous (c).

Inductor discharge in RL circuit:

$$i(t) = i_0 e^{-t/\tau} \quad (53)$$

What is the current as $t \rightarrow \infty$? What is the current at $t = 0$?

- A: 0, R/\mathcal{E}
- B: 0, \mathcal{E}/R
- C: \mathcal{E}/R
- D: R/\mathcal{E} , 0

RL Circuits Application: Signal Filters and PhET

PhET: RL and RC Circuits as Filters

RC and RL circuits can act as *high-pass* and *low-pass* **signal filters**.

- In the **RC circuit**, with $\tau = RC$, the capacitor *voltage* charges and discharges like

$$V_{charge}(t) = V_0 \left(1 - e^{-t/\tau}\right) \quad (54)$$

$$V_{discharge}(t) = V_0 e^{-t/\tau} \quad (55)$$

- In the **RL circuit**, with $\tau = L/R$, the inductor *current* charges and discharges like

$$i_{charge}(t) = i_0 \left(1 - e^{-t/\tau}\right) \quad (56)$$

$$i_{discharge}(t) = i_0 e^{-t/\tau} \quad (57)$$

PhET: RL and RC Circuits as Filters

Go to <https://phet.colorado.edu/en/simulations/circuit-construction-kit-ac>.

- In the AC Circuits PhET simulator, create an **RC circuit**, with $R = 8\Omega$, and $C = 0.05 \text{ F}$ (50 mF), and a AC voltage source set to 120V amplitude.
 1. Click and drag a voltage chart from the right side to measure the AC source voltage.
 2. Click and drag a voltage chart from the right side to measure the capacitor voltage.
 3. Create a spreadsheet with three columns: (1) frequency of the AC voltage source, (2) peak AC voltage source amplitude, and (3) peak capacitor voltage amplitude.

PhET: RL and RC Circuits as Filters

Go to <https://phet.colorado.edu/en/simulations/circuit-construction-kit-ac>.

- In the AC Circuits PhET simulator, create an **RL circuit**, with $R = 10\Omega$, and $L = 1.0\text{ H}$, and a AC voltage source set to 120V amplitude.
 1. Click and drag a voltage chart from the right side to measure the AC source voltage.
 2. Click and drag a voltage chart from the right side to measure the inductor voltage.
 3. Create a spreadsheet with three columns: (1) frequency of the AC voltage source, (2) peak AC voltage source amplitude, and (3) peak capacitor voltage amplitude.

PhET: RL and RC Circuits as Filters

1. Create a graph with a range $[0.0,1.0]$ for the y-axis, for a unitless ratio, and a domain of $[0.0,2.0]$ Hz for the x-axis.
2. Plot the ratio of V_C/V_{source} versus frequency on your graph.
3. Plot the ratio of V_L/V_{source} versus frequency on your graph.
4. For a **bonus point**, convert your ratio to decibels (dB, $20 \log_{10}(\text{ratio})$).
5. Which AC circuit is the *low-pass* filter, and which AC circuit is the *high-pass* filter? How is energy conserved if the voltage changes?

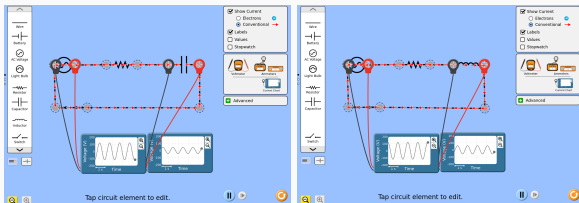


Figure 19: (Left) Example of the RC circuit. (Right) Example of the RL circuit.

Reactance, Inductive and Capacitive

Reactance, Inductive and Capacitive

Reactance is resistance that is associated with a change in the signal *phase*. What is the phase?

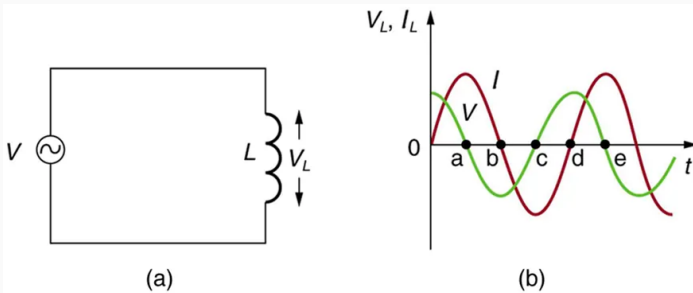


Figure 20: (a) An AC source connected to an inductor. (b) Voltage and current at the inductor are no longer *in-phase*. Voltage leads the current by a 90 degree phase shift.

Phase Shift of a Sinusoid

Let a time-dependent signal have an amplitude A , frequency f , and phase ϕ :

$$s(t) = A \cos(2\pi ft + \phi) \quad (58)$$

Two signals with phases ϕ_1 and ϕ_2 have a relative *phase shift* $\Delta\phi = \phi_2 - \phi_1$, measured in degrees or radians.

Reactance, Inductive and Capacitive

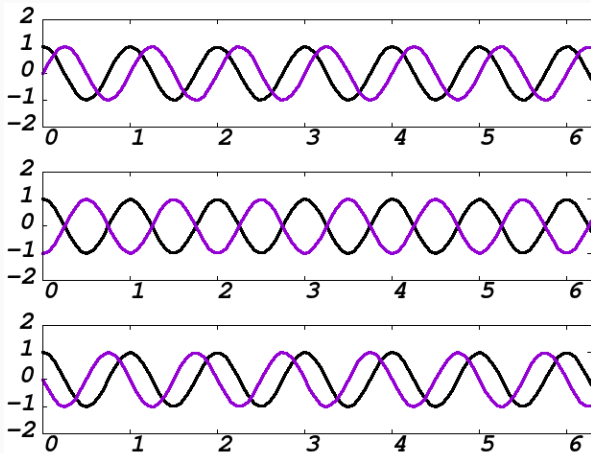


Figure 21: (Top) $\Delta\phi = 90$ deg. (Middle) $\Delta\phi = 180$ deg. (Bottom) $\Delta\phi = 270$ deg.

Reactance, Inductive and Capacitive

Reactance and Inductors

Let ϕ_V be the phase of the voltage, and ϕ_I be the phase of the current. When a sinusoidal voltage is applied to an inductor:

$$\phi_V - \phi_I = \pi/2 \quad (59)$$

The voltage leads the current by a 90 degree phase shift. The reactance from the inductor is X_L , and fits into Ohm's law like $V = IX_L$. Finally,

$$X_L = 2\pi fL \quad (60)$$

Units: 1 H is $1\Omega \text{ s}$, and frequency is 1 Hz, or 1 s^{-1} .

Reactance, Inductive and Capacitive

Suppose the reactance of an inductor is $1\text{ k}\Omega$ at a frequency of 1 kHz . What is the inductance?

- A: 2π Henries
- B: 2π Ohms
- C: $1/(2\pi)$ Henries
- D: $1/(2\pi)$ Ohms

Reactance, Inductive and Capacitive

What is the reactance at half the frequency, 0.5 kHz?

- A: π Henries
- B: π Ohms
- C: $1/(4\pi)$ Henries
- D: $1/(4\pi)$ Ohms

Hint, treat this like a scaling problem.

Reactance, Inductive and Capacitive

Suppose we are dealing with a *series* RL circuit. The resistor has $R = 1 \text{ k}\Omega$, and the frequency is $1/(2\pi) \text{ MHz}$. If the inductance is 1 mH , what is the total resistance, in $\text{k}\Omega$?

- A: $2 \text{ k}\Omega$
- B: $4 \text{ k}\Omega$
- C: $1/(2\pi) \text{ k}\Omega$
- D: $1/(4\pi) \text{ k}\Omega$

Hint, deal with the units via powers of ten.

Reactance, Inductive and Capacitive

Suppose we are dealing with the same resistance and inductance, but they are connected *in parallel*. What is the total resistance?

- A: $0.25 \text{ k}\Omega$
- B: $1 \text{ k}\Omega$
- C: $0.1 \text{ k}\Omega$
- D: $0.5 \text{ k}\Omega$

Recall that series resistances (and reactances) sum differently when they are connected in parallel.

RLC Circuits

Conclusion

1. Magnetic induction - **Chapters 23.1 - 23.5, 23.7, 23.9**
 - Induced EMF and magnetic flux
 - Faraday's Law
 - Motional EMF, generators, and transformers
2. AC circuits - **Chapters 23.9 - 23.12**
 - Inductors
 - RL circuits
 - RLC circuits