

# Algebra-Based Physics-2: Electricity, Magnetism, and Modern Physics (PHYS135B-01): Unit 2

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Jordan Hanson

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Whittier College Department of Physics and Astronomy

## Summary

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## Unit 2 Summary

### Reading: Chapters 21.1 - 21.4, 21.6

1. Resistors in series and parallel
2. Electromotive force (EMF) and terminal voltage
3. Kirchhoff's rules
4. Voltmeters and ammeters
5. RC circuits

# Resistors in Series and Parallel

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## Resistors in Series and Parallel, EMF

**Series and parallel** resistances change how current and power flow in a circuit.

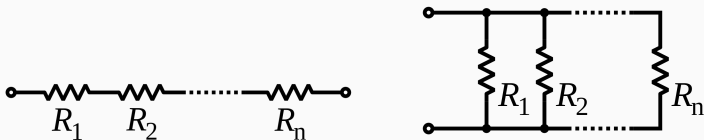


Figure 1: (Left) Resistors in series. (Right) Resistors in parallel.

# Resistors in Series and Parallel

**Series** resistances:

- Share one current
- Represent different voltage changes

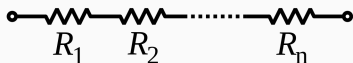


Figure 2: Resistors in series.

$$q\Delta V_{\text{tot}} = q\Delta V_1 + q\Delta V_2 + \dots + q\Delta V_n \quad (1)$$

$$\Delta V_{\text{tot}} = \Delta V_1 + \Delta V_2 + \dots + \Delta V_n \quad (2)$$

$$IR_{\text{tot}} = IR_1 + IR_2 + \dots + IR_n \quad (3)$$

$$R_{\text{tot}} = R_1 + R_2 + \dots + R_n \quad (4)$$

# Resistors in Series and Parallel

Parallel resistances:

- Share one voltage
- Represent different currents

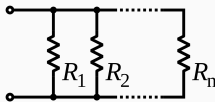


Figure 3: Resistors in parallel.

$$I_{\text{tot}} = I_1 + I_2 + \dots + I_n \quad (5)$$

$$\frac{\Delta V}{R_{\text{tot}}} = \frac{\Delta V}{R_1} + \frac{\Delta V}{R_2} + \dots + \frac{\Delta V}{R_n} \quad (6)$$

$$\frac{1}{R_{\text{tot}}} = \frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n} \quad (7)$$

# Resistors in Series and Parallel

Series resistances:

$$R_{\text{tot}} = R_1 + R_2 + \dots + R_n \quad (8)$$

Parallel resistances:

$$\frac{1}{R_{\text{tot}}} = \frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n} \quad (9)$$



## Resistors in Series and Parallel

Two  $50\Omega$  resistors are connected in *series*. What is the total resistance? Two  $50\Omega$  resistors are connected in *parallel*, What is the total resistance?

- A:  $25\Omega$
- B:  $50\Omega$
- C:  $100\Omega$
- D:  $150\Omega$

## Resistors in Series and Parallel

A  $1\text{ k}\Omega$  resistor and a  $0.1\text{ k}\Omega$  resistor are connected in *parallel*. What is the total resistance?

- A:  $1.1\text{ k}\Omega$
- B:  $0.091\text{ k}\Omega$
- C:  $1\text{ k}\Omega$
- D:  $0.1\text{ k}\Omega$

## Resistors in Series and Parallel

A  $1\text{ k}\Omega$  resistor and a  $0.1\text{ k}\Omega$  resistor are connected in *parallel*. Which resistor has the higher current? If the voltage is  $12\text{V}$ , what is the larger current?

- A: Smaller,  $120\text{ mA}$
- B: Larger,  $12\text{ mA}$
- C: Smaller,  $12\text{ mA}$
- D: Larger,  $120\text{ mA}$

Hint: draw the circuit if you are not sure.

# Resistors in Series and Parallel

**Parallel** resistances make sense in circuits with multiple devices requiring the same voltage:

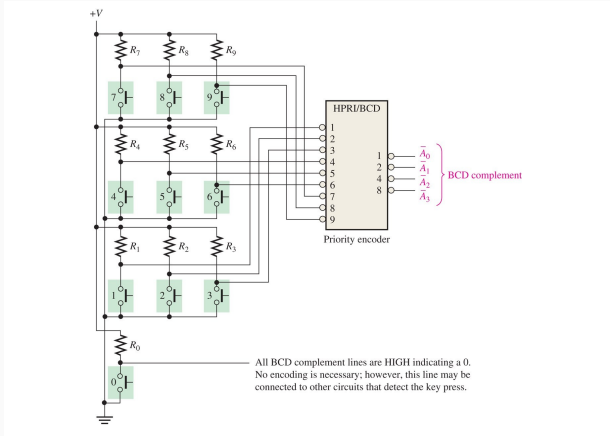


Figure 4: Resistors in parallel arranged in a keypad system.

## PhET Activity: Series and Parallel Resistors

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# PhET Activity: DC Circuits and Ohm's Law

## How do we deal with complex circuits?

1. Create a circuit that involves four identical resistors *in series*.
2. Use an ammeter to show that the current is the same in all resistors.
3. Calculate the *effective total resistance* by plotting an  $i - V$  curve of the system. Measure  $i$  and  $V$  by changing the voltage and using the voltmeter and ammeter. Does the slope of the  $i - V$  curve match your expectation?
4. Create a circuit that involves four identical resistors *in parallel*.
5. Use the voltmeter to show that the change in voltage is the same across all resistors.
6. Calculate the *effective total resistance* by plotting an  $i - V$  curve of the system. Measure  $i$  and  $V$  by changing the voltage and using the voltmeter and ammeter. Does the slope of the  $i - V$  curve match your expectation?

## Electromotive Force (EMF) and Terminal Voltage

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# Electromotive Force (EMF) and Terminal Voltage

The **electromotive force (EMF)** of a battery is the potential difference that induces current through the circuit. It is *almost* the same as the battery voltage.

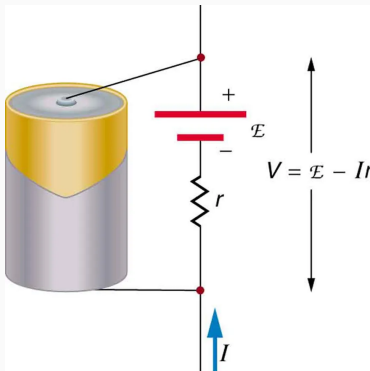
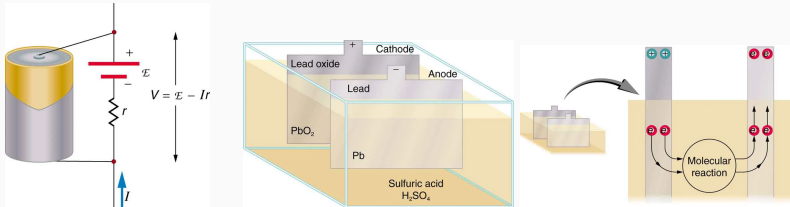


Figure 5: *Internal resistance* is one internal property of a battery.



# Electromotive Force (EMF) and Terminal Voltage

The **electromotive force (EMF)** of a battery is the potential difference that induces current through the circuit.



**Figure 6:** *Internal resistance* arises from battery chemistry, designed to pull electrons from the cathode to the anode before terminal connection.

$$V_{\text{out}} = \mathcal{E} - Ir \quad (10)$$

# Electromotive Force (EMF) and Terminal Voltage

The **electromotive force (EMF)** of a battery is the potential difference that induces current through the circuit.

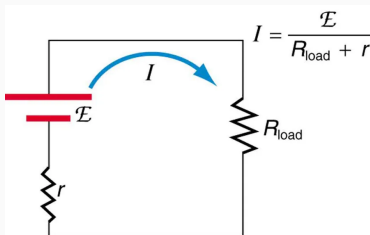


Figure 7: *Internal resistance* is one internal property of a battery.

$$I = \frac{\mathcal{E}}{R_{\text{load}} + r} \quad (11)$$

Reduces to Ohm's law if  $r$  is insignificant.

## Electromotive Force (EMF) and Terminal Voltage

If we treat the internal resistance of a 3.3 V battery as  $0\ \Omega$ , and we connect  $R_{\text{load}} = 100\ \Omega$  in a simple circuit, what will be the current?

- A: 3.3 A
- B: 3.3 mA
- C: 33 mA
- D: 33 A

Hint: draw the circuit if you are not sure.

# Electromotive Force (EMF) and Terminal Voltage

Internal resistance tends to rise if the battery is depleted of chemical energy. If we treat the internal resistance of a 3.3 V battery as  $10\ \Omega$ , and we connect  $R_{\text{load}} = 100\ \Omega$  in a simple circuit, what will be the current?

- A: 3.3 A
- B: 3.3 mA
- C: 30 mA
- D: 30 A

Hint: draw the circuit if you are not sure.

## Electromotive Force (EMF) and Terminal Voltage

Suppose we have a device that operates at 9V, and we have a 9V battery with  $r = 1\Omega$ . If we connect a  $9\Omega$  load resistance, what will be the terminal voltage? Will the device operate normally?

- A: 8.1V
- B: 8V
- C: 9.1V
- D: 9V

Will the device operate normally?

## Electromotive Force (EMF) and Terminal Voltage

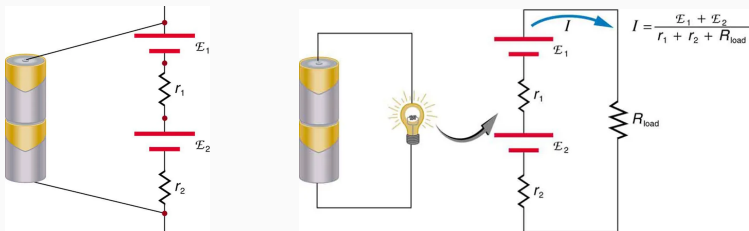
In the previous problem, what fraction of the power is dissipated in the internal resistor?

*Hint: think of dissipated power as  $P = I^2 R$  and  $P = I^2 r$  for the load and internal resistance, respectively.*

- A: 5%
- B: 10%
- C: 1%
- D: 11%

# Electromotive Force (EMF) and Terminal Voltage

Connecting real batteries in series raises the effective terminal voltage, but there are now two internal resistances.



**Figure 8:** (Left) Two batteries in series. (Right) Two batteries in series connected to a load resistance.

$$I = \frac{\mathcal{E}_1 + \mathcal{E}_2}{R_{\text{load}} + r_1 + r_2} \quad (12)$$

## Electromotive Force (EMF) and Terminal Voltage

Suppose we have a flashlight powered by four AA batteries *in series*. The EMF of each AA battery is 1.5V. The internal resistance is  $r = 0.5\Omega$  for each battery. The load resistance of the flashlight bulb is  $30\Omega$ . What is the current flow?

- A: 1.67 A
- B: 0.167 A
- C: 0.2 A
- D: 2.0 A

Remember to draw a picture of the whole circuit if you are stuck.



## Electromotive Force (EMF) and Terminal Voltage

Suppose we have a flashlight powered by four AA batteries *in series*. The EMF of each AA battery is 1.5V. The internal resistance is  $r = 0.5\Omega$  for each battery. The load resistance of the flashlight bulb is  $30\Omega$ . What is the terminal voltage?

- A: 6.0 V
- B: 1.5 V
- C: 3.33 V
- D: 5.67 V

Remember to draw a picture of the whole circuit if you are stuck.

# Kirchhoff's Rules

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# Kirchhoff's Rules

## Kirchhoff's Rules

The following two rules govern complex circuits:

- The sum of all currents entering a junction must equal the sum of all currents leaving the junction:

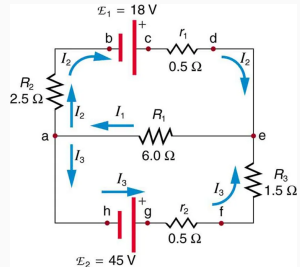
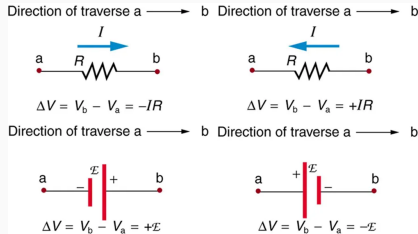
$$\sum_n I_{n,\text{in}} = \sum_n I_{n,\text{out}}.$$

- The algebraic sum of changes in potential around any closed loop must be zero:  $\sum_{n,\text{loop}} V_n = 0$ .

- The first rule follows from charge conservation, and is called the *junction rule*.
- The second rule follows from energy conservation, and is called the *loop rule*.

# Kirchhoff's Rules

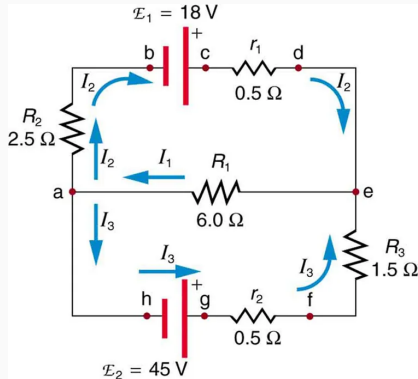
Kirchhoff's rules help organize calculations for complex circuits.



**Figure 9:** (Left) A change in voltage across a resistor is negative in the direction of current flow. The change is positive if aligned with the polarity of the battery. (Right) The complex circuit has two loops, three load resistors, two batteries, and two internal resistances.

# Kirchhoff's Rules

Kirchhoff's rules help organize calculations for complex circuits.



**Figure 10:** (a) Solve this one in small groups. (b) Model this in DC Circuit Constructor PhET.

# Voltmeters and Ammeters

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A **galvanometer** is a device that deflects a needle based on the strength of a current. This effect is caused by the force of a magnetic field on a current-carrying wire.

# Conclusion

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