

Electric Charge and Electric Fields

1. (a) $E_c = 2.00 \times 10^{-3} \text{ V/m}$ @ 1 mm
 $E_c = ?$ @ 5 mm

$$E = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$$

$$2.00 \times 10^{-3} = \frac{1}{4\pi\epsilon_0} \frac{q}{(1 \times 10^{-3})^2}$$

$$2.00 \times 10^{-3} \cdot 1 \times 10^{-6} = \frac{q}{4\pi\epsilon_0}$$

$$2.00 \times 10^{-3} \cdot 1 \times 10^{-6} \cdot \frac{1}{(5 \times 10^{-3})^2}$$

$$2.00 \times 10^{-3} \cdot 1 \times 10^{-6} \cdot \frac{1}{25 \times 10^{-6}}$$

$$= 8 \times 10^{-5} \text{ V/m}$$

(b) $1 \mu\text{C} \rightarrow E_c = 8.00 \times 10^{-3} \text{ V/m}$
 $3 \mu\text{C} \rightarrow E_c = ?$

$$(8.00 \times 10^{-3})(3)$$

$$= 0.024$$

$$= 2.4 \times 10^{-2} \text{ V/m}$$

2. (a) drop mass = $4 \times 10^{-16} \text{ kg}$
 $E\text{-field} = 6131.25 \text{ N/C}$

$$q = \frac{mg}{E} \Rightarrow \frac{(4 \times 10^{-16})(9.8)}{6131.25}$$

$$= \frac{6.39347604 \times 10^{-19}}{1.6 \times 10^{-19}}$$

$$= 3.99 \dots$$

$$\approx 4 \text{ electrons on the drops}$$

(b) $(4 \times 10^{-16})(9.8)$

$$= F_g = 3.92 \times 10^{-15} \text{ N}$$

$$(6.39 \times 10^{-19}) - (1.6 \times 10^{-19}) = 4.79 \times 10^{-19}$$

$$= F_e = (4.79 \times 10^{-19}) \cdot 6131.25 = 2.939 \times 10^{-15}$$

$$a = \frac{F_g - F_e}{m} \Rightarrow \frac{(3.92 \times 10^{-15}) - (2.939 \times 10^{-15})}{(4 \times 10^{-16})}$$

$$= 2.4525$$

$$a \approx 2.45 \text{ m/s}^2$$

(acceleration of droplet)

Potential Energy and Voltage, Capacitors

1. (a) $\Delta V = 4 \text{ kV}$

$$H = +1qe \quad He = +2qe$$

$$KE_H = (1.6 \times 10^{-19})(4.0 \times 10^3)$$

$$= 6.4 \times 10^{-16} \text{ J} \times \frac{6.242 \times 10^{18} \text{ eV}}{1 \text{ J}}$$

$$= 3994.88$$

$$KE_H \approx 3995 \text{ eV} \text{ (electron volts)}$$

$$KE_{He} = (2)(1.6 \times 10^{-19})(4.0 \times 10^3)$$

$$= 1.28 \times 10^{-15} \text{ J} \times \frac{6.242 \times 10^{18} \text{ eV}}{1 \text{ J}}$$

$$= 7989.76$$

$$KE_{He} \approx 7990 \text{ eV}$$

$$KE_{tot} = 3995 + 7990$$

$$KE_{total} = 11,985 \text{ eV}$$

(b) $\Delta x = 5 \text{ cm}$

$$\vec{E} = \frac{-\Delta V}{\Delta x}$$

$$= \frac{4 \text{ kV}}{5 \text{ cm}} = \frac{4 \times 10^3 \text{ V}}{5 \times 10^{-2} \text{ m}}$$

$$= -80,000 \text{ V/m}$$

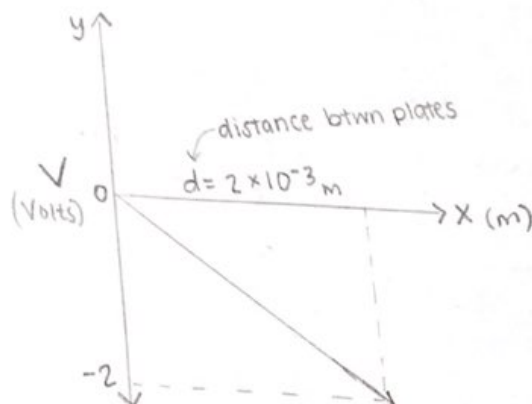
$$E = -8 \times 10^4 \text{ V/m}$$

2. $E\text{-field} = 1 \text{ kV/m} \rightarrow 1000 \text{ V/m} = \text{slope}$
 $\Delta x = 2 \text{ mm} \rightarrow 2 \times 10^{-3} \text{ m}$

$$y\text{-intercept} = ?$$

$$E = \frac{V}{x}$$

$$\text{slope} = -1000 \text{ V/m}$$



$$y\text{-intercept} = \text{zero}$$

3. (a) $\text{area} = 1 \text{ cm}^2 = 10^{-4} \text{ m}^2$

Capacitance_{sys} = ?

$\epsilon_0 = 8.85 \times 10^{-12} \text{ F/m}$

$$C = \frac{\epsilon_0 A}{d} \Rightarrow \frac{(8.85 \times 10^{-12})(10^{-4})}{2 \times 10^{-3}}$$

$= 4.425 \times 10^{-13}$

Capacitance_{sys} $\approx 4.43 \times 10^{-13} \text{ F}$

(b) if voltage = 5 V

Energy = $\frac{1}{2} CV^2$

$= 0.5(4.425 \times 10^{-13})(5)^2$

$= 5.531 \times 10^{-12}$

Energy $\approx 5.5 \times 10^{-12} \text{ J}$

4.

= If we want more capacitance, then we should connect an identical capacitor to the first in Parallel. The series would be $C/2$ whereas the parallel would be added so it would make sense for it to be in parallel if the goal is more capacitance.

Current, Resistance, and DC Circuits

1. (a) Serial Case

$-\epsilon_2 + Ir_2 + Ir_1 - \epsilon_1 + IR = 0$

$I = \frac{3V}{r_1 + r_2 + R} \Rightarrow \frac{3}{2+2+50} \Rightarrow \frac{3}{54} = 55.5$

$I = 55.6 \text{ mA}$

Parallel Case

$I = \frac{V}{R}$

$I = \frac{1.5}{50}$

$I = 30 \text{ mA}$

(b) Serial Case Power Consumption

$P_{\text{total}} = P_{r_1} + P_{r_2} + P_R$

$= I^2 r_1 + I^2 r_2 + I^2 R$

$= (55.56)^2(2) + (55.56)^2(2) + (55.56)^2(50)$

$= 6173.8 + 6173.8 + 154345.68$

$= 166693.33 \text{ W}$

$P_{\text{total}} = 166.7 \text{ mW}$ $*P_R = 154.3 \text{ mW}$

Parallel Case Power Consumption

$P_{\text{total}} = P_{r_1} + P_{r_2} + P_R$

$= I_1^2 R_1 + I_2^2 R_2 + I^2 R$

$= (15)^2(2) + (15)^2(2) + (30)^2(50)$

$= 450 + 450 + 45000$

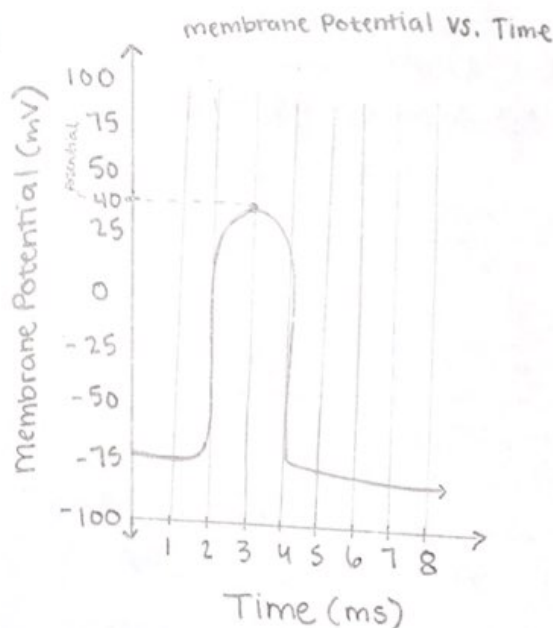
$= 45900 \text{ W}$

$P_{\text{total}} = 45.9 \text{ mW}$ $*P_R = 45 \text{ mW}$

(c) PHET CHECK

= correct

2.



(a) Pulse width = 2 ms

(b) Peak to Peak Voltage
 $= 40 - (-75)$
 $= 40 + 75$
 $= 115 \text{ mV}$