CALCULUS-BASED PHYSICS-2: ELECTRICITY, MAGNETISM, AND THERMODYNAMICS (PHYS180-02): UNIT 1

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Physics - $\phi v \sigma \iota \kappa \acute{\eta}$ - "phusiké": knowledge of nature from $\phi \acute{v} \sigma \iota \varsigma$ - "phúsis": nature

Reading: Chapters 1 and 2 (for Unit 1)

- 1. Estimation/Approximation
 - Estimating the correct order of magnitude
 - Building complex quantities
 - Unit analysis
- 2. Review of concepts from Newtonian mechanics
 - Kinematics and Newton's Laws
 - · Work-energy theorem, energy conservation
 - · Momentum, conservation of momentum

Two molucules collide elastically. Which of the following is true?

- A: Both potential energy and momentum are conserved for each molecule
- B: Only the momentum is conserved for each molecule
- C: Momentum and kinetic energy are conserved for each molecule
- D: Neither momentum nor energy is conserved for each molecule

Suppose a molecule is headed towards the wall of a container with speed v and mass m. If it collides elastically with the wall and returns in the exact same direction from which it came, what is the change in momentum of the molecule?

- A: mv
- B: $\frac{1}{2}mv^2$
- C: mv^2
- D: 2mv

Do you remember how to take the derivative of an exponential function? Let $f(t) = \exp(\alpha t)$. What is f'(t)?

- A: $\exp(\alpha t)$
- B: $\alpha \exp(\alpha t)$
- C: $\exp(\alpha t)/\alpha$
- D: $\exp(2\alpha t)$

What about multiplying exponentials? What is f(t)g(t), if $f(t) = \exp(\alpha t)$ and $g(t) = \exp(\beta t)$?

- A: $\exp(\alpha\beta t)$
- B: $\exp(\frac{\alpha}{\beta}t)$
- C: $\exp(\frac{\beta}{\alpha}t)$
- D: $\exp((\alpha + \beta)t)$

UNIT 1 SUMMARY

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Reading: Chapters 1 and 2

- 1. Temperature, Heat, and the 0th Law of Thermodynamics
- 2. Heat flow and transfer mechanisms
- 3. Kinetic Theory of Gases

JITT - READING QUIZ RESULTS

TEMPERATURE, HEAT, AND THE OTH LAW

OF THERMODYNAMICS



Figure 1: The zeroeth law of thermodynamics. We need this idea to have a firm understanding of temperature readings, because a **thermometer** is itself a thermal system.

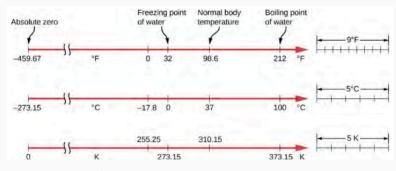


Figure 2: Three temperature scales.

To convert from	Use this equation	
Celsius to Fahrenheit	$T_{\rm F} = \frac{9}{5}T_{\rm C} + 32$	
Fahrenheit to Celsius	$T_{\rm C} = \frac{5}{9}(T_{\rm F} - 32)$	
Celsius to Kelvin	$T_{\rm K} = T_{\rm C} + 273.15$	
Kelvin to Celsius	$T_{\rm C} = T_{\rm K} - 273.15$	
Fahrenheit to Kelvin	$T_{\rm K} = \frac{5}{9}(T_{\rm F} - 32) + 273.15$	
Kelvin to Fahrenheit	$T_{\rm F} = \frac{9}{5}(T_{\rm K} - 273.15) + 32$	

Figure 3: Three temperature scales. The Fahrenheit scale places 0 for a solution of brine and ice, with 180 degrees between freezing and boiling of water. Celsius scale has 0 for freezing and 100 for boiling. Absolute zero of Kelvin scale will be discussed below.

Suppose the temperature of a system is raised by 10° F. Which of the following is true?

- A: The increase is more than 10 degrees in °C.
- B: The increase is smaller than 10 degrees in °C.
- · C: The increase is the same in °C.
- D: Depends on the initial temperature in °F.

Suppose the temperature of a system is raised by 10°C. Which of the following is true?

- A: The increase is more than 10 degrees in °K.
- B: The increase is smaller than 10 degrees in °K.
- C: The increase is the same in °K.
- D: Depends on the initial temperature in °C.

The formula for conversion from Celcius temperature to Fahrenheit temperatures is $T_{\rm F}=\frac{9}{5}T_{\rm C}+32$. Which of the following is true?

- A: $0^{\circ} 10^{\circ}$ C is comparable to room temperature
- B: 35° 40°C is comparable to human body temperature
- \cdot C: 30° 35°C is comparable to human body temperature
- $\cdot\,$ D: 15° 20°C outdoors would correspond to hot weather

How do thermometers work? What is temperature, really? Temperature is a macroscopic indication of microscopic kinetic energy. We need the idea of thermal expansion:

$$\frac{dL}{dT} = \alpha L \tag{1}$$

In Eq. 1, T is the temperature, L is the length of an object, and α is the coefficient of linear thermal expansion, in units of inverse degrees.

Material	Coefficient of Linear Expansion $\alpha(1)^{\circ}$ C)	
Solids		
Aluminum	25×10^{-6}	
Brass	19×10^{-6}	
Copper	17×10^{-6}	
Gold	14×10^{-6}	
Iron or steel	12×10^{-6}	
Invar (nickel-iron alloy)	0.9×10^{-6}	
Lead	29×10^{-6}	
Silver	18×10^{-6}	
Glass (ordinary)	9×10^{-6}	
Glass (Pyrex®)	3×10^{-6}	
Quartz	0.4×10^{-6}	
Concrete, brick	$\sim\!12\times10^{-6}$	
Marble (average)	2.5×10^{-6}	

Figure 4: Linear thermal expansion coefficients.

$$\frac{dL}{dT} = \alpha L \tag{2}$$

Equation 2 is a differential equation with a particular solution:

$$L(T) = L_0 \exp(\alpha T) \tag{3}$$

We've seen that in practice, α values are small. In this case we may approximate:

$$L(T)/L_0 \approx 1 + \alpha T \tag{4}$$

$$\Delta L \approx \alpha L_0 \Delta T \tag{5}$$

Equation 5 is the equation found in Chapter 1 of the reading.





Figure 1.5 (a) Thermal expansion joints like these in the (b) Auckland Harbour Bridge in New Zealand allow bridges to change length without buckling. (credit: "\$Jū"/Wikimedia Commons)

Figure 5: Bridge expansion joints.

Chapter 1 also contains these formulae for two and three-dimensional expansion:

$$\Delta A \approx 2\alpha A_0 \Delta T \tag{6}$$

$$\Delta V \approx 3\alpha V_0 \Delta T \tag{7}$$

Why? Properties of exponentials. **Group board exercise**: prove Eq. 7 using Eq. 3.

Pipe Transport: Some oil and gasoline pipelines are above ground, exposed to the elements. The coefficient of thermal volumetric expansion for gasoline is much larger than that of steel. Why would it be a bad idea to completely fill a pipeline with gasoline, knowing there will be large temperature variations?

- A: For large increases in temperature, the pipeline expands more rapidly than gasoline, leaving gaps for leaks.
- B: For large increases in temperature, the gasoline expands more rapidly than the pipeline, building pressure and causing pipeline bursts.
- C: For large decreases in temperature, the gasoline shrinks more rapidly than the pipeline, building pressure and causing pipeline bursts.
- · D: None of these.

If an object has a length of 10 cm, and a linear thermal expansion coefficient of 100×10^{-6} 1/°C, what is the change in length of the object if the temperature is increased from 0 °C to 100 °C?

- · A: 0.1 mm
- B: 1 mm
- C: 1 cm
- D: 10 cm

Recall from last semester that we studied stress and strain:

$$\frac{F}{A} = Y \frac{\Delta L}{L} \tag{8}$$

$$stress = Y \times strain$$
 (9)

Now we can predict strain from temperature changes, and make statements about the implied *thermal stresses*. This is important for mechanical engineering designs.

$$\frac{F}{A} = Y\alpha\Delta T \tag{10}$$

$$\frac{F}{A} = Y\alpha\Delta T \tag{11}$$

Steel pipeline design: Suppose a steel pipeline ($\alpha = 12 \times 10^{-6}$ 1/°C, Y = 30 × 10⁹ N/m) is designed and built at temperatures of 30 °C, but experiences temperatures of 0 °C. What stress does the pipeline experience at the attachment point?

- · A: 0.1 MPa
- B: 1 MPa
- C: 10 MPa
- D: 100 MPa

Is the pipeline pulling or pushing on the attachment point?

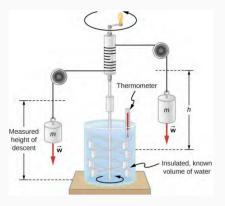


Figure 6: Demonstrating that work and heat are equivalent (paper topic from last semester).

Which of the following is true, regarding Fig. 6?

- A: The temperature increase is proportional to the decrease in height of the masses.
- B: The temperature increase is proportional to *g*.
- · C: A and B
- · D: None of these

Regarding Fig. 6, if total mass is 1.0 kg (two 0.5 kg masses), $g = 10 \text{ m/s}^2$, and h = 1 m, what is the temperature increase in the water?

- A: 10 J
- B: 10 °K
- C: 10 °C
- · D: Cannot determine

The heat required to obtain a change in temperature is proportional to the mass of the substance to be heated (obvious if you understand heat to be caused by motions of molecules). The coefficient is called the *specific heat capacity*:

$$Q = mc\Delta T \tag{12}$$

More generally,

$$c = \frac{1}{m} \frac{dQ}{dT} \tag{13}$$

Units: Joules per unit temperature per unit mass (J/(kg C)). 1 calorie is the energy required to heat 1 gram of water 1 degree C. For food, 1 kcal = 1 Calorie → endless debates about food science...

Substances	Specific Heat (c)	
Solids	J/kg⋅°C	kcal/kg · °C [2]
Aluminum	900	0.215
Asbestos	800	0.19
Concrete, granite (average)	840	0.20
Copper	387	0.0924
Glass	840	0.20
Gold	129	0.0308
Human body (average at 37 °C)	3500	0.83
Ice (average, $-50^{\circ}\mathrm{C}$ to $0^{\circ}\mathrm{C}$)	2090	0.50
Iron, steel	452	0.108
Lead	128	0.0305
Silver	235	0.0562
Wood	1700	0.40
Liquids		
Benzene	1740	0.415
Ethanol	2450	0.586
Glycerin	2410	0.576
Mercury	139	0.0333
Water (15.0 °C)	4186	1.000

Figure 7: Notice how water is on a different scale than most other substances.

A 0.500 kg aluminum pan on a stove and 0.250 L of water in it are heated from 20.0 °C to 80.0 °C. a) How much heat is required? What percentage of the heat is used to raise the temperature of b) the pan and c) the water?

Group board exercise: $c_{\rm W}=4186~{\rm J/kg/C}$ and $c_{\rm Al}=900~{\rm J/kg/C}$.

For a thermodynamically isolated system, we have

$$Q_{\text{cold}} + Q_{\text{hot}} = 0 \tag{14}$$

That is, if heat is conserved, the heat lost by a hot system is equal and opposite to the heat gained by the cold object. This sort of balancing is known as *calorimetry*.

Es como la palabra "calor" en español: hace calor hoy.

Suppose two systems in contact have the same mass, and are otherwise isolated from other systems. System 1 has a much larger heat capacity than system 2, and they are at different temperatures. Which temperature change is the largest?

- The temperature change corresponding to system 1.
- The temperature change corresponding to system 2.
- The changes corresponding to system 1 and 2 are equal.
- The changes are zero because the total heat is conserved.

Suppose two systems in contact have the same mass, and are otherwise isolated from other systems. System 1 has the same heat capacity than system 2, and they are at different temperatures. Which temperature change is the largest?

- The temperature change corresponding to system 1.
- The temperature change corresponding to system 2.
- The changes corresponding to system 1 and 2 are equal.
- The changes are zero because the total heat is conserved.

The brakes in a car increase in temperature by T when bringing the car to rest from a speed v. How much greater would T be if the car initially had twice the speed? You may assume the car stops fast enough that no heat transfers out of the brakes.

- Higher by a factor of 2
- · Higher by a factor of 4
- Same temperature difference (no potential energy change).
- Higher by a factor of 8

The survival situation: Suppose two people (60 kg each) are cuddling to stay warm in a tent because it is cold outside. One person is at 37 Celsius, and the other is at 30 Celsius. What is their final temperature, assuming they are calorimetrically isolated?

Group board exercise: $c_{\text{Human}} = 3500 \text{ J/kg/C}$.

Hint: We need Eq. 14, but ΔT is a variable and we need to use the heat capacity. Moral of the story: The temperature of one person has to go down so the temperature of the other person can go up.

Bonus problem: Temperature-dependent heat capacities. Repeat Example 1.8 in the text, except substitute NaI (sodium iodide) for NaCl (sodium chloride) and look up the relevant heat capacity functions. Turn this in for +2 bonus points on this week's homework (homeworks are usually out of 10 points).

Materials have four phases, and three are relevant for the classical physics in this course.

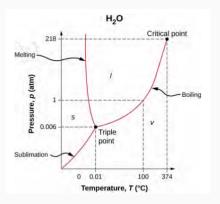


Figure 8: Phase transitions occur when crossing the lines. Boiling, melting, and sublimation are the three possible processes.

A pressure cooker contains water and steam in equilibrium at a pressure greater than atmospheric pressure. How does this greater pressure increase cooking speed?

- · A: Raises the boiling point
- B: Raises the vapor pressure
- · C: Both A and B
- D: Changes the heat capacity of water and steam

Triple point explained:

https://www.youtube.com/watch?v=MP6MVLWuNZQ

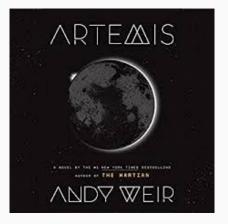


Figure 9: Idea for bonus paper or group project: read *Artemis* by Andy Weir and pick a chapter. Explain each of the statements about surviving on the moon with lower artifical **vapor pressure**, artificial **boiling point**, no atmosphere, and a different *g* value, etc.

During a phase transition, the temperature of a substance does not change. The heat energy required to drive the phase transition is just proportional to the mass, for liquids and solids:

$$Q = mL_{\rm f} \tag{15}$$

$$Q = mL_{v} \tag{16}$$

These coefficients are known as the laten heats of *fusion* and *vaporization*. These numbers have a molecular interpretation.

		$L_{\mathbf{f}}$			$L_{\rm v}$	
Substance	Melting Point (°C)	kJ/ kg	kcal/ kg	Boiling Point (°C)	kJ/kg	kcal/ kg
Helium ^[2]	-272.2 (0.95 K)	5.23	1.25	-268.9(4.2 K)	20.9	4.99
Hydrogen	-259.3(13.9 K)	58.6	14.0	-252.9(20.2 K)	452	108
Nitrogen	-210.0(63.2 K)	25.5	6.09	-195.8(77.4 K)	201	48.0
Oxygen	-218.8(54.4 K)	13.8	3.30	-183.0(90.2 K)	213	50.9
Ethanol	-114	104	24.9	78.3	854	204
Ammonia	-75	332	79.3	-33.4	1370	327
Mercury	-38.9	11.8	2.82	357	272	65.0
Water	0.00	334	79.8	100.0	2256 ^[3]	539 ^[4]
Sulfur	119	38.1	9.10	444.6	326	77.9
Lead	327	24.5	5.85	1750	871	208
Antimony	631	165	39.4	1440	561	134
Aluminum	660	380	90	2450	11400	2720
Silver	961	88.3	21.1	2193	2336	558

Figure 10: As usual, look at water! (and aluminum).

Three ice cubes are used to chill a soda at 20 °C with mass 0.25 kg. The ice is at 0 °C and each ice cube has a mass of 6.0 g. Assume that the soda is kept in a foam container so that heat loss can be ignored and that the soda has the same specific heat as water. Find the final temperature when all ice has melted. **Group board exercise**: Latent heat of fusion of the ice: 334 kJ/kg, and heat capacity of water: 4186 J/kg/C.

Heat transfer mechanisms:

- Conduction
- Convection
- Radiation

Conduction - Heat transfer through stationary matter by physical contact.

Which of the following do you think is not an example of heat conduction?

- · A: Accidentally touching a hot stove and feeling the burn
- B: The sun shining on your face, making your face feel warm
- · C: Laying on hot sand on the beach, making you feel warm
- D: A wire getting hot because it is carrying too much current

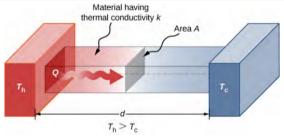


Figure 1.22 Heat conduction occurs through any material, represented here by a rectangular bar, whether window glass or walrus blubber.

Figure 11: Our model for heat transfer follows a differential equation.

$$P = \frac{dQ}{dt} = \frac{kA(T_{\rm h} - T_{\rm c})}{d} \to -kA\frac{dT}{dx}$$
 (17)

Rate of conductive heat transfer:

$$P = \frac{dQ}{dt} = \frac{kA(T_{\rm h} - T_{\rm c})}{d} \to -kA\frac{dT}{dx}$$
 (18)

- k: Thermal conductivity, W/m °C
- A: Surface area in contact, m²
- · d: Thickness of contact area, m
- \cdot $T_{\rm h}$, $T_{\rm c}$: Hot and cold initial temperatures

The x-coordinate is the direction of heat flow and the minus sign reflects the corresponding decrease in temperature. In American construction, sometimes R = d/k, known as the R-factor.

An aluminum can with thermal conductivity k has a total area of A, and walls that are x thick. The soda in the can is much colder than the air outside, and a density ρ . How much time passes before the soda is at the same temperature as the air?

- A: $t = \frac{\rho Vcx}{kA}$
- B: $t = \frac{cx}{kA}$
- C: $t = \frac{kAT}{x}$
- D: $t = \frac{kAT}{x}$

Why does the temperature difference not matter in the prior answer?

- · A: Heat is not a rate, it's a substance
- · B: The aluminum does the heat conduction, not the soda
- C: Energy conservation: the heat transferred does not depend on the initial and final temperature
- D: The capacity of the air to absorb heat is much larger than the small can, so it happens as fast as possible

Heat convection: we will not cover this quantitatively because it involves fluid dynamics. However, a good example is fur insulation against wind:

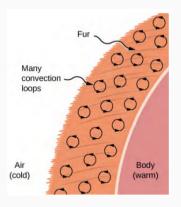


Figure 12: Fur helps to insulate against wind chill.

Heat radiation: We can make one quantitative statement about radiative heat transfer.

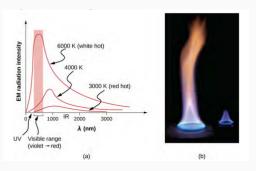


Figure 13: Black-body radiation, where color depends on temperature.

$$P_{\text{net}} = \sigma A e (T_2^4 - T_1^4)$$
 (19)

The Stephan-Boltzmann law of radiation

$$P_{\text{net}} = \sigma A e (T_2^4 - T_1^4) \tag{20}$$

- σ : Stefan-Boltsmann constant, 5.67 \times 10⁻⁸ W/(m² K⁴)
- A is the surface area
- T_1 , T_2 : temperatures of the object and environment
- e: emissivity of the object (can depend on the wavelength)

This may sound like an odd question, but why do people need clothing? Even if we are standing around in a room at room temperature, why do we get cold and get sick?

- · A: The air conducts heat away from us if it is slightly colder
- · B: If there is a breeze, convection takes heat away from us
- · C: We naturally radiate heat in the infrared
- · D: All of these

Group board exercise: Let's estimate the heat radiated by a person. Use Stefan-Boltzmann law of radiation, with emissitivity of 1 for infrared light. Compare this to what you think is the natural amount of heat generated by a normal person's body (could start with 2000 Calories per day, for example).

Greenhouse effect as heat transfer problem: https://phet.colorado.edu/en/simulation/greenhouse

- What is the CO₂ concentration in the previous ice age, and what temperature does this allow on the Earth's surface? With clouds?
- Repeat, but with the numbers of today. Add clouds, and repeat.
 Write down all the temperatures you think are the equilibrium temperatures.
- Open the photon absorption tab. Create three different atmospheres: all methane, all carbon dioxide, and all nitrogen. What happens to the infrared photons in each?

When we say the word "molecule," we take it for granted. How do you actually know substances are made of molecules? Can we know this by observing gases?

Chapter 2 leads us into the subject of the kinetic theory of gases, acting on the hypothesis of the existence of molecules and drawing conclusions about the behavior of gases.

After observations in the 16th-19th centuries (Boyle's Law, Charles's Law, Guy-Lussac Law), we arrived here:

$$\frac{p_1 V_1}{T_1} = \frac{p_2 V_2}{T_2} \tag{21}$$

- · p: pressure
- · V: volume
- T: temperature

Suppose we guess that gases are made of smaller pieces, and that temperature is the experience of the flow of heat, and that heat is proportional to the kinetic energy of the smaller pieces.

Let us name that last idea *equipartition of energy*, that each degree of freedom gets one piece of kinetic energy proportional to temperature:

$$e_{\rm dof} = \frac{1}{2}kT \tag{22}$$

- T is the temperature of the gas of molecules
- · k, for now, is some constant
- · e is the energy per degree of freedom

Suppose a molecule bounces off of a flat container. What if pressure is just the collective force per unit area of molecules all bouncing around at the same time? How do we describe this process with concepts from last semester?

- · Elastic collisions, momentum conservation
- Force in terms of momentum

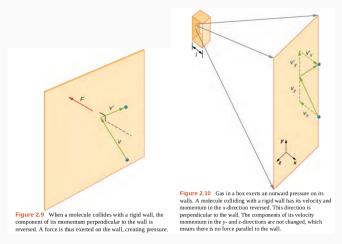


Figure 14: The force imparted on the wall by a molecule with velocity *v*, then *v'*, causes pressure. The box is a length *l* and the molecule is assumed to travel all the way across.

Assumptions:

- Large number N of molecules with mass m.
- Molecules are classical (Newton's laws)
- Molecules are much smaller than the container and distance between each other
- · All collisions are elastic

Momentum transfer of one molecule colliding with the wall:

$$F_i = (mv_x - m(-v_x'))/\Delta t = \frac{2mv_x}{\Delta t}$$
 (23)

The box has a length *l*:

$$F_i = \frac{2mv_x}{2l/v_x} = \frac{mv_x^2}{l} \tag{24}$$

Now let's account for all molecules:

$$F = \frac{m}{l} \Sigma_i^N v_X^2 = \frac{Nm}{l} \bar{v_X^2}$$
 (25)

(That's the *average* of the squared velocity). The x-direction is not special, so we may assume $\bar{v_x^2} = \frac{1}{3}\bar{v^2}$

$$F = \frac{Nm\bar{v}^2}{3l} \tag{26}$$

And pressure is just force per surface area:

$$pA = \frac{Nmv^2}{3l} \tag{27}$$

Now we realize that Al = V...

Now we realize that Al = V...

$$pV = \frac{Nm\bar{v^2}}{3} = \frac{2}{3}N\left(\frac{1}{2}\right)m\bar{v^2} \tag{28}$$

Now, use the *equipartition theorem*, assuming three degrees of freedom per molecule (three dimensions of velocity):

$$\bar{K} = \frac{3}{2}kT \tag{29}$$

Substituting the kinetic energy into Eq. 28, we find

$$pV = NkT \tag{30}$$

The Ideal Gas Law.

We need a new unit, a new *scale*, since the number of molecules is so large. How about the number of carbon atoms in 12 grams of carbon-12 (the most common isotope)?

Let's call the number of molecules $N_{\rm A}$ in 12 grams of carbon a mole, and let $n=N/N_{\rm A}$. If the Gas constant $R=kN_{\rm A}$, then the Ideal Gas Law says

$$pV = nRT (31)$$

where *n* is the number of moles and $R = kN_A = 8.31$ J/mole/Kelvin ≈ 2 cal/mole/Kelvin.

Guess what's about to happen? A ton of problems with the Idea Gas Law? You're right!

If we have a 1 liter (10^{-3} m³) vessel of argon at a temperature of 300 K, what should the pressure be, if there are only 0.3 moles in the vessel?

- A: 0.2 atm
- B: 2 atm
- · C: 20 atm
- D: 200 atm

How many air molecules are in a liter of air? (p = 1 atm = 100 kPa, $V = 10^{-3}$ m³, R = 8.31 J/mole/Kelvin, T = 300 K).

- A: 3×10^{21}
- B: 3×10^{22}
- C: 6×10^{21}
- D: 6×10^{22}

Precise measurement of Avogadro's Number $N_A = 6.02 \times 10^{23}$ molecules.

PhET Simulation: https://phet.colorado.edu/en/simulation/gas-properties

I would like you to measure Boltzmann's Constant, $k_{\rm B}$, using the idea gas law and the PhET simulation.

- $pV = Nk_{\rm B}T$
- N is calibrated on right side
- p and T are measurements
- Assume V = Al. The ruler can measure l, and assume A is $(35 \text{ nm})^2$.
- You can independently adjust the temperature by adding heat at the bottom.

Separately, confirm Boyle's Law and Charles's Law.

Boltzmann's Constant, $k_{\rm B}$ is related to the gas constant R by $R=N_{\rm A}k_{\rm B}$. Electrochemical measurements and Brownian motion measurements (*paper idea*) tell us that $N_{\rm A}=6.02\times10^{23}$. So R involves cancellation of many orders of magnitude to have the value of 8.31 in SI units...

Modification to Idea Gas Law: known as van der Waals equation of state.

$$\left(p + a\left(\frac{n}{V}\right)^2\right)(V - nb) = nRT \tag{32}$$

- · a and b are empirical constants
- Same temperature for a lower pressure → molecular attractions
- Corrects for high density gases in which the molecule volume matters

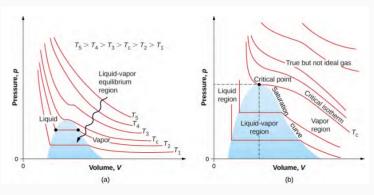


Figure 15: The van der Waals equation of state leads to more realistic isotherms, and probes the liquid-vaper region near the critical point.

Heat capacities of gases: As we saw from the PhET simulation activity, we cannot just change the temperature of a gas without either the pressure or the volume changing. To understand heat flow into gases, we need to hold these constant (theoretically). Recall that the average energy for a molecule in a gas is

$$E_{\rm int} = \frac{3}{2} nRT \tag{33}$$

Let the *molar heat capacity at constant volume* be defined in a similar way to solids:

$$C_{\rm V} = \frac{1}{n} \frac{Q}{\Delta T} \tag{34}$$

Combining these two equations, we find

$$C_{\rm V} = \frac{3}{2}R\tag{35}$$

 $C_{\rm V}$ is independent of temperature, merely a constant of nature for idea gases. However, note that we only find the number $\frac{3}{2}$ because of the equipartition theorem while assuming only three degrees of freedom. If we had identified more degrees of freedom, we would have drawn a different conclusion.

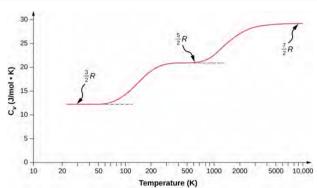


Figure 2.13 The molar heat capacity of hydrogen as a function of temperature (on a logarithmic scale). The three "steps" or "plateaus" show different numbers of degrees of freedom that the typical energies of molecules must achieve to activate. Translational kinetic energy corresponds to three degrees of freedom, rotational to another two, and vibrational to yet another two.

Figure 16: $C_{\rm V}$ for H-gas reveals molecular (atomic) nature of the gas. The right-most temperatures correspond to a few percent of 1 Rydberg energy.

CONCLUSION

UNIT 1 SUMMARY

Reading: Chapters 1 and 2

- 1. Temperature, Heat, and the 0th Law of Thermodynamics
- 2. Heat flow and transfer mechanisms
- 3. Kinetic Theory of Gases

ANSWERS

ANSWERS

- Momentum and kinetic energy are conserved for each molecule
- · 2mv
- $\alpha \exp(\alpha t)$
- $\exp((\alpha + \beta)t)$
- The increase is smaller than 10 degrees in °C
- The increase is the same in ${}^{\circ}K$
- 35° 40°C is comparable to human body temperature
- Answer B

- 1 mm
- · 1 MPa
- · A and B
- Cannot determine (would have needed the heat capacity of water)
- The temperature change corresponding to system 2
- The changes corresponding to system 1 and 2 are equal
- Higher by a factor of 4
- · Both A and B

ANSWERS

- The sun shining on your face, making your face feel warm
- $t = \frac{\rho VcX}{kA}$
- Energy conservation: the heat transferred does not depend on the initial and final temperature
- · 20 atm
- 3×10^{22}