

Figure 1: (Left) A current I experiences a force F in a B -field.

2 Chapter 11: Magnetic Forces and Fields

1. Consider Fig. 1 (left). In each of the three cases, determine the direction of the B -field given that F is the Lorentz force.

- a: Down, into page
- b: Left
- c: Up, away from page

2. Consider Fig. 1 (right). **The Hall Effect.** An E -field exists in the vertical direction and a B -field is perpendicular to the direction of charge velocity. (a) Show that if the E -field force on a charge balances the Lorentz force on a charge, that $v = E/B$. (b) If the E -field is constant, $E = \Delta V / \Delta x$. Show that

$$\Delta V = \frac{B \Delta x I}{n q_e A} \quad (1)$$

where n is the charge carrier density, q_e is the electron charge, A is the cross-sectional area of the conductor, and I is the current. Plug in $B = 1.33 \text{ T}$, $\Delta x = 2 \text{ cm}$, $I = 10 \text{ A}$, $n = 2 \times 10^{28} \text{ m}^{-3}$, $A = 1 \text{ mm}^2$, and q_e is the charge of an electron.

a) $F_E = F_B \Rightarrow qE = qvB \sin \theta$, $\theta = 90^\circ$

$$E = vB \Rightarrow v = \frac{E}{B}$$

b) $I = n q_e A v$

$$\Delta V = \frac{B \Delta x I}{n q_e A}$$

$$\Delta V = \frac{B \Delta x I}{n q_e A} = \frac{1.33 (2 \times 10^{-2}) 10}{2 \times 10^{28} (1.6 \times 10^{-19}) (1 \times 10^{-6})} = 8.312 \times 10^{-5} \text{ V}$$

3. A proton has a magnetic field due to its spin. The field is similar to that created by a circular current loop $0.65 \times 10^{-15} \text{ m}$ in radius with a current of $1.05 \times 10^4 \text{ A}$. Find the maximum torque on a proton in a 2.50-T field. (This is a significant torque on a small particle.)

$$\tau_{\text{max}} = N I \pi r^2 B$$

$$= 1 (1.05 \times 10^4 \text{ A}) \pi (0.65 \times 10^{-15} \text{ m})^2 (2.50 \text{ T}) = 3.48 \times 10^{-26} \text{ N}\cdot\text{m}$$

3 Chapter 12: Sources of Magnetic Fields

1. (a) What is the B -field inside a solenoid with 500 turns per meter, carrying a current of 0.3 A ? (b) Suppose we insert a piece of metal inside the solenoid, boosting μ_0 by a factor of 5000. What is the new B -field?

a) $B = \mu_0 n I$
 $= 4\pi \times 10^{-7} \times 500 \times 0.3$
 $= 1.885 \times 10^{-4} \text{ T}$

b) $B = 5000 \times 1.885 \times 10^{-4} \times 0.3$
 $B = 0.28275 \text{ T}$
 $= 2.8275 \times 10^{-1} \text{ T}$

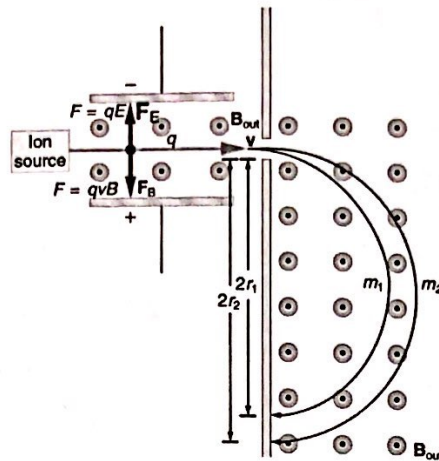


Figure 2: A basic diagram of a *toroid*, which is a solenoid wrapped into a circular tube.

2. Consider Fig. 2. **Mass spectrometer.** Suppose that the velocity of the charged particles moving to the right is $v = E/B$. (a) Show that if $v = E/B$, $F_{net} = 0$ in the region in the top left¹. (b) Recall that the centripetal force on a particle of mass m is mv^2/r . Set this equal to the magnitude of the Lorentz force to prove that

$$r = \frac{mE}{qB^2} \quad (2)$$

The mass of an oxygen nucleus is 16 times that of a proton (mass of proton: 1.67×10^{-27} kg). Suppose oxygen ions with the charge of 1 proton are sent through the mass-septometer. The E-field is 10 V/m, and the B-field is 0.01 T. What is the distance r ?

a)

4 Chapter 13: Electromagnetic Induction

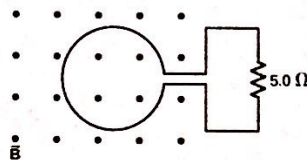


Figure 3: A voltage is induced on a loop by a changing B-field.

1. The magnetic field in Fig. 3 flows out of the page through a single ($N = 1$) loop, and is tuned to follow the form

$$B(t) = B_0 \left(\frac{1}{2} + \frac{2}{\pi} \sin(2\pi ft) + \frac{2}{3\pi} \sin(6\pi ft) + \frac{2}{5\pi} \sin(10\pi ft) \right) \quad (3)$$

The loop has a radius r . (a) In terms of the given variables, what is the induced voltage in the circuit? (b) If $B_0 = 0.1$ T, $r = 0.1$ m, and $f = 10^3$ Hz, what is the induced emf at $t = 0$? (c) What is the current through the resistor at $t = 1$ ms?

a) $\mathcal{E} = \frac{d\Phi}{dt} = \frac{d}{dt}(B\pi r^2)$

b) $\sin 0 = 0$
 $B_0 \left(\frac{1}{2} \right) = B(t)$
 $B(t) = .05$

$\mathcal{E} = \pi r^2 \times \frac{dB_0}{dt} \left(\frac{1}{2} + \frac{2}{\pi} \sin(2\pi ft) + \frac{2}{3\pi} \sin(6\pi ft) + \frac{2}{5\pi} \sin(10\pi ft) \right)$

¹Molecules that do not have this velocity will hit the sides of this portion of the instrument.

5 Chapter 14: Inductance

1. What is (a) the rate at which the current through a 0.50-H coil is changing if an emf of 0.150 V is induced across the coil?

$$\mathcal{E} = -L \frac{dI}{dt} \Rightarrow \frac{dI}{dt} = \left| -\frac{\mathcal{E}}{L} \right| = \frac{0.15 \text{ V}}{0.50 \text{ H}} = \boxed{0.3 \text{ A/s}}$$

2. When a camera uses a flash, a fully charged capacitor discharges through an inductor. In what time must the 0.100-A current through a 2.00-mH inductor be switched on or off to induce a 500-V emf?

$$\mathcal{E} = L \frac{dI}{dt} \Rightarrow dt = \frac{L}{\mathcal{E}} dI$$

$$dt = \frac{2 \text{ mH}}{500 \text{ V}} (0.100 \text{ A})$$

$$= \frac{2 \text{ mH} \cdot \frac{0.100 \text{ A}}{1 \text{ A}}}{500 \text{ V}} (0.100 \text{ A})$$

$$= \boxed{4.00 \times 10^{-7} \text{ s}}$$