

Score: 19/25

Physics Midterm

10-8-22

2. Estimations + Unit Analysis

Technically, there is a factor of 2 for sounding going "there and back"

$$1.) a. 0.5 \text{ km} \cdot \frac{1000 \text{ m}}{1 \text{ km}} = 500 \text{ m} \rightarrow v = \frac{x}{t} = \frac{500 \text{ m}}{1.5 \text{ s}} = \boxed{333.3 \text{ m/s}}$$

$$b. 333.3 \text{ m/s to km/hr} \rightarrow \frac{333.3 \text{ m}}{1 \text{ s}} \cdot \frac{1 \text{ km}}{1000 \text{ m}} \cdot \frac{3600 \text{ s}}{1 \text{ hr}} = \boxed{1,199.9 \text{ km/hr}}$$

$$2.) a. 0.25 \text{ m}^3 \text{ in cm}^3 \rightarrow 0.25 \text{ m}^3 \cdot \frac{(100)^3 \text{ cm}^3}{1 \text{ m}^3} = \boxed{250000 \text{ cm}^3}$$

$$b. 100 \text{ km/hr in m/s} \rightarrow \frac{100 \text{ km}}{1 \text{ hr}} \cdot \frac{1000 \text{ m}}{1 \text{ km}} \cdot \frac{1 \text{ hr}}{60 \text{ min}} \cdot \frac{1 \text{ min}}{60 \text{ sec}} = \frac{100,000 \text{ m}}{3600 \text{ s}} = \boxed{27.8 \text{ m/s}}$$

$$c. 2 \text{ kg m s}^{-2} \text{ in gm cm ms}^{-2} \rightarrow \frac{2 \text{ kg}}{1 \text{ s}^2} \cdot \frac{1000 \text{ g}}{1 \text{ kg}} \cdot \frac{100 \text{ cm}}{1 \text{ m}} \cdot \frac{1 \text{ s}^2}{1,000,000 \text{ ms}^2} = \boxed{0.2 \text{ gm cm ms}^{-2}}$$

3. Vectors ($\vec{x} = a\hat{i} + b\hat{j}$)

$$1.) a. \vec{a} = 10 \cos(15^\circ), \quad b = 10 \sin(15^\circ) \quad \vec{x}_1 = -8\hat{i} + 7\hat{j}$$

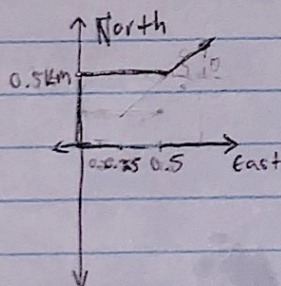
$$a = -8 \quad b = 7$$

(-1) The formulas are correct, but I think you may have confused degrees and radians

$$b. a = 20 \cos(135.0) \quad b = 20 \sin(135.0) \quad \vec{x}_2 = -20\hat{i} + 2\hat{j}$$

$$a = -20.0 \quad b = 2.0$$

2.) a.



$$b. x = 0.5 \text{ km} + (0.25 \cos(45^\circ)) = 0.63 \text{ km}$$

$$y = 0.5 \text{ km} + (0.25 \sin(45^\circ)) = 0.71 \text{ km}$$

$$\text{final location} = \boxed{(0.63 \text{ km}, 0.71 \text{ km})}$$

$$c. a^2 + b^2 = c^2 \rightarrow 0.5^2 + 0.5^2 = c^2 \rightarrow 0.71$$

$$0.71 \text{ km} + 0.25 \text{ km} \approx \boxed{1 \text{ km}}$$

4. Motion Along a Straight Line

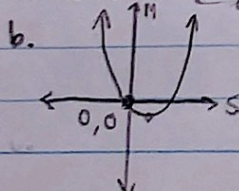
$$1.) a. x(t) = -1.0 - 4.0t \text{ m} \rightarrow x(-2.0) = -1.0 - (4.0 \times -2.0) = -1.0 + 8.0 = 7.0 \text{ m}$$

$$x(2.0) = -1.0 - (4.0 \times 2.0) = -1.0 - 8.0 = -9.0 \text{ m} \quad (-9.0 - (7.0)) = \boxed{-16 \text{ m}}$$

$$b. \frac{-16 \text{ m}}{4 \text{ s}} = \boxed{-4 \text{ m/s}}$$

$$2.) a. x(t) = -2t + 7t^2 \rightarrow x(0) = -2(0) + 7(0)^2 \quad x(2) = -2(2) + 7(2)^2$$

$$(24 - 0) = \frac{24 \text{ m}}{2 \text{ s}} = \boxed{12 \text{ m/s}} = 0$$



$$c. x(1) = -2(1) + 7(1)^2$$

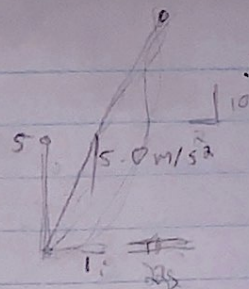
$$= -2 + 7$$

$$= \boxed{5 \text{ m/s}}$$

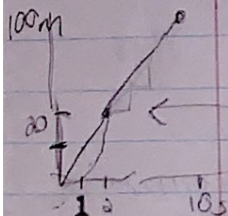
(-2) The graph is of the position but we wanted the $v(t)$. (c) is 12 m/s, and (d) is 14 m/s²

$$d. \frac{24 - 0 \text{ m/s}}{2} = \boxed{12 \text{ m/s}^2}$$

$$a = 5.0 \text{ m/s}^2 \quad v_i = 0 \text{ m/s} \quad v_f = 10.0 \text{ m/s}$$



$$3.) a. \quad t = \frac{v_f - v_i}{a} = \frac{10.0 - 0 \text{ m/s}}{5.0 \text{ m/s}^2} = \boxed{2.0 \text{ s}}$$



$$b. \quad \boxed{20 \text{ m}}$$

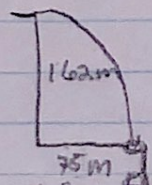
$$c. \quad \boxed{10 \text{ s}}$$

(-1) Part (b) is 10 meters, from equations of constant acceleration vs. time with no initial velocity. This would have given you the correct part (c), or 11 s.

5. Motion in Two and Three Dimensions

(-1) This equation is either applied to x-velocity or y-velocity and associated displacement

1.) a.



$$b. \quad v^2 = v_i^2 + 2a\Delta y$$

$$16 \text{ m}^2 = (0)^2 + 2(9.81 \text{ m/s}^2)(75 \text{ m})$$

$$\sqrt{v^2} = \sqrt{1471.5 \text{ m}^2/\text{s}^2}$$

$$\boxed{v = 38.36 \text{ m/s}}$$

$$2.) a. \quad R = \frac{v_0^2 \sin(2\theta_0)}{g}$$

$$R = \frac{40^2 \sin(2(45))}{9.81}$$

$$\boxed{R = 163.10 \text{ m}}$$

$$b. \quad t_{\text{tot}} = \frac{2(v_0 \sin(\theta_0))}{g} \rightarrow t_{\text{tot}} = \frac{2(40 \text{ m/s}) \sin(45)}{9.81 \text{ m/s}^2}$$

$$\boxed{t_{\text{tot}} = 5.77 \text{ s}}$$

6. Forces

$$1.) \quad F_x = 10 \cos(45^\circ) + 8 \cos(30^\circ)$$

$$= 14.0 \text{ N}$$

$$F_y = 10 \sin(45^\circ) - 8 \sin(30^\circ)$$

$$= 3.1 \text{ N}$$

$$F_f = -7.5 \text{ N}$$

$$F_{\text{net}} = (14 \text{ N} - 7.5 \text{ N}) + 3.1 \text{ N} = 6.5 \text{ N} + 3.1 \text{ N}$$

$$a = \frac{F}{m} \rightarrow \frac{6.5 \text{ N} + 3.1 \text{ N}}{49 \text{ kg}} = (0.13 + 0.06) \text{ m/s}^2$$

$$= 0.73 \text{ m/s}^2$$

(-1) Almost! The 7.5 N should be subtracted from the magnitude of the total pulling force (because they are in opposite directions).