

# Forces and Inclines *with Friction*

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## 1 Review of Friction Force

The friction force is  $f = \mu N$ . That is, the force is directly proportional to the *normal force*, and the constant of proportionality is  $\mu$ . If the object is not moving, then  $\mu$  is the static coefficient of friction. If the object is *sliding*, then  $\mu$  is the kinetic coefficient of friction. If  $N = mg$ , then  $f = \mu mg$  and the direction of  $f$  will be in the direction opposing motion.

## 2 Inclined Surfaces with Static Friction

Place a mass on the ruler and incline the ruler at some small angle. Draw a free body diagram below summarizing the weight, friction, and normal forces on the mass. Use the free body diagram to show that  $\mu = \tan(\theta)$ , if  $\mu$  is the static coefficient of friction.

## 3 Measurement of $\mu$

For several masses, measure  $\mu$  by measuring the largest possible  $\theta$  such that the mass does not slide down the ruler. Create a plot of  $\mu$  versus mass. Does  $\mu$  depend on mass?