

Midterm 3

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Phys 180
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2 Chapter 11

- 1) a: into the page
b: left
c: out of the page

2a) $F_E = F_B$ so, $qE = qvB \sin \theta$

since $\theta = 90^\circ$, $qE = qvB$ (1)

$$v = \frac{qE}{qB} \Rightarrow \boxed{v = \frac{E}{B}}$$

2b) The E-field is constant.

$$E = \frac{\Delta V}{\Delta x} \Rightarrow \Delta V = E \Delta x$$

since $E = vB$, $\Delta V = vB \Delta x$

the drift velocity is $v_d = \frac{I}{nq_e A}$ so, $V = v_d$

$$\Delta V = \frac{B \Delta x I}{nq_e A}$$

$$B = 1.33$$

$$\Delta x = 2 \text{ cm} = .02 \text{ m}$$

$$I = 10 \text{ A}$$

$$n = 2 \times 10^{28} \text{ m}^{-3}$$

$$A = (1 \times 10^{-3})^2$$

$$\Delta V = \frac{1.33 (2 \times 10^{-2}) 10}{(2 \times 10^{28}) (1.6 \times 10^{-19}) (1 \times 10^{-3})^2}$$

$$\boxed{\Delta V = 8.3125 \times 10^{-5} \text{ V}}$$

$$3) \tau = NIAB \sin \theta \quad (2.5)$$

$$N = 1$$

$$I = 1.05 \times 10^4 \text{ A}$$

$$\tau = (1)(1.05 \times 10^4)(\pi(.65 \times 10^{-15})^2)(1)A = \pi(.65 \times 10^{-15})^2$$

$$= (1.05 \times 10^4)(1.33 \times 10^{-30})(2.5) \quad B = 2.5$$

$$\tau = 3.48 \times 10^{-26} \text{ N}\cdot\text{m}$$

$$\theta = 90^\circ$$

3 Chapter 12

$$1a) B = \mu_0 n I$$

$$n = 500$$

$$I = 0.3 \text{ A}$$

$$B = (4\pi \times 10^{-7})(500)(.3)$$

$$\mu_0 = 4\pi \times 10^{-7}$$

$$= 1.885 \times 10^{-4} \text{ T}$$

$$1b) \mu_0 = 5000(4\pi \times 10^{-7}) = .00628$$

$$B = .00628(500)(.3)$$

$$B = 0.9425 \text{ T}$$

$$2a) F_E = qE \quad F_B = q\vec{v} \times \vec{B}$$

$$F_{\text{net}} = F_E + F_B = 0$$

* $\vec{v} \times \vec{B}$ is down

$$\Rightarrow qE + q\vec{v} \times \vec{B} = 0$$

$$\Rightarrow F_{\text{net}} = q(E - vB) = 0$$

$$\text{since } v = \frac{E}{B}, \quad q\left(E - \frac{E}{B}B\right) = 0$$

$$\Rightarrow F_{\text{net}} = q(E - E) = q(0) = 0$$

$$2b) \quad \frac{mv^2}{r} = qvB$$

$$\Rightarrow r = \frac{mv^2}{qB} = \frac{mvr}{qB}$$

Since $v = \frac{E}{B}$, $r = \frac{mE}{qB^2}$

$$\begin{aligned} m &= 1.67 \times 10^{-27} \\ E &= 10 \\ q &= 1.602 \times 10^{-19} \\ B &= 0.01 \text{ T} \end{aligned}$$

$$r = \frac{(2.672 \times 10^{-26}) (10)}{(1.602 \times 10^{-19}) (0.01)^2}$$

$$= \frac{2.672 \times 10^{-25}}{1.602 \times 10^{-23}} = \boxed{0.0168 \text{ m}}$$

4 Chapter 13

i) $B(t) = B_0 \left(\frac{1}{2} + \frac{2}{\pi} \sin(2\pi ft) + \frac{2}{3\pi} \sin(6\pi ft) + \frac{2}{5\pi} \sin(10\pi ft) \right)$

a)

$$\frac{dB}{dt} = B_0 \left(\frac{2}{\pi} \cos(2\pi ft) 2\pi f + \frac{2}{3\pi} \cos(6\pi ft) 6\pi f + \frac{2}{5\pi} \cos(10\pi ft) 10\pi f \right)$$

Since $\mathcal{E} = -N \frac{d\Phi}{dt} \Rightarrow \mathcal{E} = -\frac{d\Phi}{dt}$

and $\Phi = BA$, $\mathcal{E} = -A \left(\frac{dB}{dt} \right)$ so, $A = \pi r^2$

$$\mathcal{E} = -4\pi r^2 f B_0 \left(\cos(2\pi ft) + \cos(6\pi ft) + \cos(10\pi ft) \right)$$

$$\begin{aligned}
 \text{b) } B_0 &= 0.1 \text{ T} \\
 r &= 0.1 \text{ m} \\
 f &= 10^3 \text{ Hz} \\
 t &= 0
 \end{aligned}$$

$$\mathcal{E} = 4\pi (0.1) (10^3) (0.1) (\cos(0) + \cos(0) + \cos(0))$$

$$= 4\pi 3$$

$$\boxed{\mathcal{E} = 12\pi \text{ V}}$$

$$\begin{aligned}
 \text{c) } \mathcal{E} &= 4\pi (\cos(2\pi) + \cos(6\pi) + \cos(10\pi)) \\
 \boxed{\mathcal{E} &= 12\pi \text{ V}}
 \end{aligned}$$

5 Chapter 14

$$\begin{aligned}
 \text{1) } L &= 0.50 \text{ H} \\
 \Delta \mathcal{E} &= 0.150 \text{ V}
 \end{aligned}$$

$$\Delta V = -L \left(\frac{dI}{dt} \right)$$

$$\Rightarrow \frac{dI}{dt} = -\frac{\Delta V}{L}$$

$$\frac{dI}{dt} = -\frac{0.150}{0.50} = \boxed{0.3 \text{ A}}$$

$$\text{2) } \Delta V = -L \left(\frac{dI}{dt} \right)$$

$$\Delta V = 500 \text{ V}$$

$$L = 2 \times 10^{-3} \text{ H}$$

$$I = -0.100 \text{ A}$$

$$500 = -(2 \times 10^{-3}) \left(\frac{-0.1}{dt} \right)$$

$$dt = \boxed{4 \times 10^{-7} \text{ s}}$$