

For A and B when I did the right hand rule the in and out of page results were flipped so I DK my right hand is broken

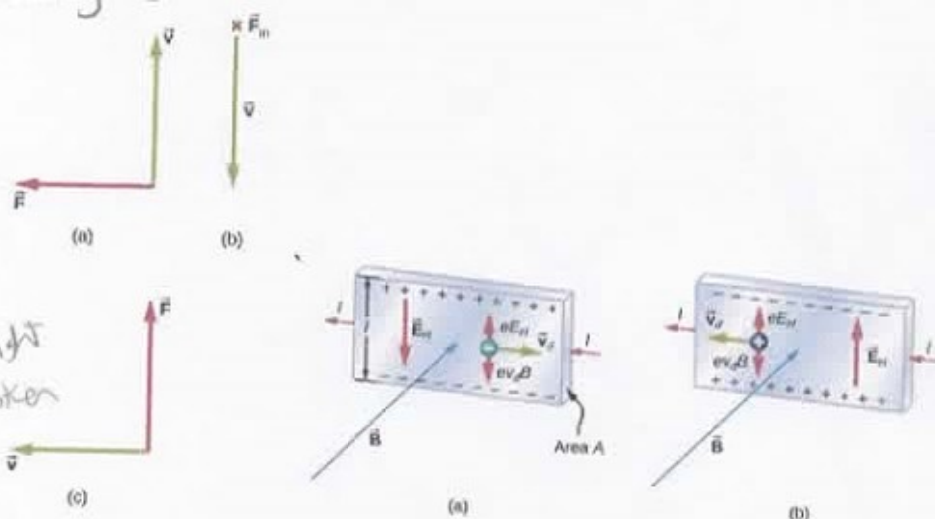


Figure 1: (Left) A current I experiences a force F in a B -field.

2 Chapter 11: Magnetic Forces and Fields

1. Consider Fig. 1 (left). In each of the three cases, determine the direction of the current given that F is the Lorentz force.

- a:
- b:
- c:

a.) $\hat{B} = \hat{F} \times \hat{V}$
 $\hat{B} = -\hat{i} \times \hat{j} = -\hat{k}$
 Into the Page

b.) $\hat{B} = -\hat{k} \times (-\hat{j}) = -\hat{i}$
 Left

B-field
 c.) $\hat{B} = \hat{j} \times (-\hat{j}) = \hat{k}$
 Out the Page

2. Consider Fig. 1 (right). **The Hall Effect.** An E -field exists in the vertical direction and a B -field is perpendicular to the direction of charge velocity. (a) Show that if the E -field force on a charge balances the Lorentz force on a charge, that $v = E/B$. (b) If the E -field is constant, $E = \Delta V / \Delta x$. Show that

$$\Delta V = \frac{B \Delta x I}{n q_e A} \quad (1)$$

where n is the charge carrier density, q_e is the electron charge, A is the cross-sectional area of the conductor, and I is the current. Plug in $B = 1.33 \text{ T}$, $\Delta x = 2 \text{ cm}$, $I = 10 \text{ A}$, $n = 2 \times 10^{28} \text{ m}^{-3}$, $A = 1 \text{ mm}^2$, and q_e is the charge of an electron.

$F_E = F_B$
 a.) $qVB \sin \theta$
 $\theta = 90^\circ \Rightarrow 1$

$qE = qVB \Rightarrow E = vB$
 $V = \frac{E}{B}$

b.) $\Delta V = E(\Delta x)$
 $\Delta V = vB(\Delta x)$
 $\Delta V = B(\Delta x)v$

Drift velocity, $v = \frac{I}{n q_e A}$
 $\Delta V = \frac{B(\Delta x)I}{n q_e A}$
 $\Delta V = 8.31 \times 10^{-5} \text{ V}$

3. A proton has a magnetic field due to its spin. The field is similar to that created by a circular current loop $0.65 \times 10^{-15} \text{ m}$ in radius with a current of $1.05 \times 10^4 \text{ A}$. Find the maximum torque on a proton in a 2.50-T field. (This is a significant torque on a small particle.)

Torque = $I A \times B$
 $A = \pi r^2 = 3.1415926 \times (0.65 \times 10^{-15})^2 = 1.33 \times 10^{-30} \text{ m}^2$
 $= (1.05 \times 10^4 \text{ A})(0.65 \times 10^{-15} \text{ m})(2.50 \text{ T}) = 3.49 \times 10^{-26} \text{ Nm}$

3 Chapter 12: Sources of Magnetic Fields

1. (a) What is the B -field inside a solenoid with 500 turns per meter, carrying a current of 0.3 A ? (b) Suppose we insert a piece of metal inside the solenoid, boosting μ_0 by a factor of 5000. What is the new B -field?

a.) $B = \mu_0 n I$

$B = (4\pi \times 10^{-7})(500)(0.3) = 1.88 \times 10^{-4} \text{ T}$

b.) $B = 5000(\mu_0)(500)(0.3)$
 $= 1.88 \times 10^{-4}(5000)$
 $= 0.94 \text{ T}$

$F_e + F_m = 0$
 $F_e = qE$
 $F_m = q(\vec{v} \times \vec{B})$
 $q|\vec{E} + \vec{v} \times \vec{B}| = 0$
 $q|\vec{E} - vB| = 0$
 $\vec{E} - vB = 0$
 $v = \frac{E}{B}$

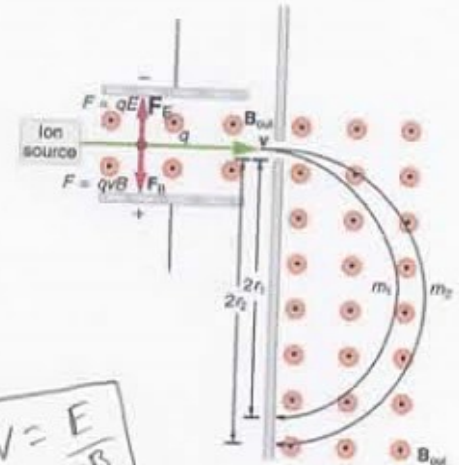


Figure 2: A basic diagram of a *toroid*, which is a solenoid wrapped into a circular tube.

2. Consider Fig. 2. **Mass spectrometer.** Suppose that the velocity of the charged particles moving to the right is $v = E/B$. (a) Show that if $v = E/B$, $F_{net} = 0$ in the region in the top left¹. (b) Recall that the centripetal force on a particle of mass m is mv^2/r . Set this equal to the magnitude of the Lorentz force to prove that

$$r = \frac{mE}{qB^2} \quad (2)$$

The mass of an oxygen nucleus is 16 times that of a proton (mass of proton: 1.67×10^{-27} kg). Suppose oxygen ions with the charge of 1 proton are sent through the mass-septometer. The E -field is 10 V/m, and the B -field is 0.01 T. What is the distance r ?

b.) $r = \frac{(16 \times 1.67 \times 10^{-27} \text{ kg})(10 \text{ V/m})}{(1.602 \times 10^{-19})(0.01)^2} = 0.017 \text{ m}$

4 Chapter 13: Electromagnetic Induction

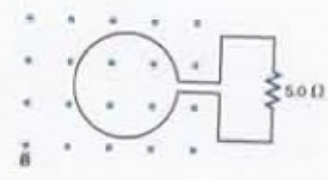


Figure 3: A voltage is induced on a loop by a changing B-field.

1. The magnetic field in Fig. 3 flows out of the page through a single ($N = 1$) loop, and is tuned to follow the form

$$B(t) = B_0 \left(\frac{1}{2} + \frac{2}{\pi} \sin(2\pi ft) + \frac{2}{3\pi} \sin(6\pi ft) + \frac{2}{5\pi} \sin(10\pi ft) \right) \quad (3)$$

The loop has a radius r . (a) In terms of the given variables, what is the induced voltage in the circuit? (b) If $B_0 = 0.1$ T, $r = 0.1$ m, and $f = 10^3$ Hz, what is the induced emf at $t = 0$? (c) What is the current through the resistor at $t = 1$ ms?

a.) $e = \frac{d\Phi}{dt}$
 $e = \frac{d}{dt} (B \cdot A)$
 $e = \pi r^2 \left(B_0 \left(\frac{2}{\pi} \sin(2\pi ft) + \frac{2}{3\pi} \sin(6\pi ft) + \frac{2}{5\pi} \sin(10\pi ft) \right) \right) \cdot \frac{1}{2}$
 b.) $t = 0$ all $\sin = 0$ so $e = 0.016 \text{ V}$
 c.) $I = \frac{e}{R}$
 $I = \frac{0.000338}{5.0 \Omega} = 6.8 \times 10^{-5} \text{ A}$

¹Molecules that do not have this velocity will hit the sides of this portion of the instrument.

5 Chapter 14: Inductance

1. What is (a) the rate at which the current through a 0.50-H coil is changing if an emf of 0.150 V is induced across the coil?

$$\frac{dI}{dt} = \frac{\text{emf}}{L} = \frac{0.150 \text{ V}}{0.50 \text{ H}} = \boxed{0.30 \frac{\text{A}}{\text{s}}}$$

2. When a camera uses a flash, a fully charged capacitor discharges through an inductor. In what time must the 0.100-A current through a 2.00-mH inductor be switched on or off to induce a 500-V emf?

$$\begin{aligned} \mathcal{E} &= L \frac{dI}{dt} \\ \downarrow \\ dt &= \frac{L}{\mathcal{E}} dI \end{aligned} \quad \begin{aligned} &\text{mH} \rightarrow \text{H} \\ &\uparrow \\ &(2.00 \text{ mH})(10^{-3}) \end{aligned} \quad \rightarrow \quad \frac{(2.00 \text{ mH})(10^{-3})}{500 \text{ V}} (0.100 \text{ A}) = \boxed{4.00 \times 10^{-7} \text{ s}}$$