

Physics Midterm

10-8-22

2. Estimations + Unit Analysis

$$1.) a. 0.5 \text{ km} \cdot \frac{1000 \text{ m}}{1 \text{ km}} = 500 \text{ m} \rightarrow \bar{v} = \frac{x}{t} = \frac{500 \text{ m}}{1.5 \text{ s}} = \boxed{333.3 \text{ m/s}}$$

$$b. 333.3 \text{ m/s to km/hr} \rightarrow \frac{333.3 \text{ m}}{1 \text{ s}} \cdot \frac{1 \text{ km}}{1000 \text{ m}} \cdot \frac{3600 \text{ s}}{1 \text{ hr}} = \boxed{1,199.9 \text{ km/hr}}$$

$$2.) a. 0.25 \text{ m}^3 \text{ in cm}^3 \rightarrow 0.25 \text{ m}^3 \cdot \frac{(100)^3 \text{ cm}^3}{1 \text{ m}^3} = \boxed{250000 \text{ cm}^3}$$

$$b. 100 \text{ km/hr in m/s} \rightarrow \frac{100 \text{ km}}{1 \text{ hr}} \cdot \frac{1000 \text{ m}}{1 \text{ km}} \cdot \frac{1 \text{ hr}}{60 \text{ min}} \cdot \frac{1 \text{ min}}{60 \text{ sec}} = \frac{100,000 \text{ m}}{3600 \text{ s}} = \boxed{27.8 \text{ m/s}}$$

$$c. 2 \text{ kg m s}^{-2} \text{ in gm cm ms}^{-2} \rightarrow \frac{2 \text{ kg}}{1 \text{ s}^2} \cdot \frac{1000 \text{ g}}{1 \text{ kg}} \cdot \frac{100 \text{ cm}}{1 \text{ m}} \cdot \frac{1 \text{ s}^2}{1,000,000 \text{ ms}^2} = \boxed{0.2 \text{ gm cm ms}^{-2}}$$

3. Vectors ($\vec{x} = a\hat{i} + b\hat{j}$)

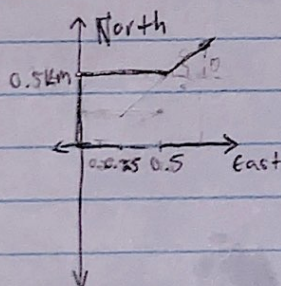
$$1.) a. \vec{a} = 10 \cos(15^\circ), \quad b = 10 \sin(15^\circ) \quad \vec{x}_1 = -8\hat{i} + 7\hat{j}$$

$$a = -8 \quad b = 7$$

$$b. a = 20 \cos(135.0^\circ) \quad b = 20 \sin(135.0^\circ) \quad \vec{x}_2 = -20\hat{i} + 2\hat{j}$$

$$a = -20.0 \quad b = 2.0$$

2.) a.



$$b. x = 0.5 \text{ km} + (0.25 \cos(45^\circ)) = 0.63 \text{ km}$$

$$y = 0.5 \text{ km} + (0.25 \sin(45^\circ)) = 0.71 \text{ km}$$

$$\text{final location} = \boxed{(0.63 \text{ km}, 0.71 \text{ km})}$$

$$c. a^2 + b^2 = c^2 \rightarrow 0.5^2 + 0.5^2 = c^2 \rightarrow 0.71$$

$$0.71 \text{ km} + 0.25 \text{ km} \approx \boxed{1 \text{ km}}$$

4. Motion Along a Straight Line

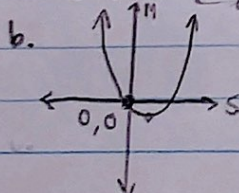
$$1.) a. x(t) = -1.0 - 4.0t \text{ m} \rightarrow x(-2.0) = -1.0 - (4.0 \times -2.0) = -1.0 + 8.0 = 7.0 \text{ m}$$

$$x(2.0) = -1.0 - (4.0 \times 2.0) = -1.0 - 8.0 = -9.0 \text{ m} \quad (-9.0 - (7.0)) = \boxed{-16 \text{ m}}$$

$$b. \frac{-16 \text{ m}}{4 \text{ s}} = \boxed{-4 \text{ m/s}}$$

$$2.) a. x(t) = -2t + 7t^2 \rightarrow x(0) = -2(0) + 7(0)^2 \quad x(2) = -2(2) + 7(2)^2$$

$$(24 - 0) = \frac{24 \text{ m}}{2 \text{ s}} = \boxed{12 \text{ m/s}} = 0$$



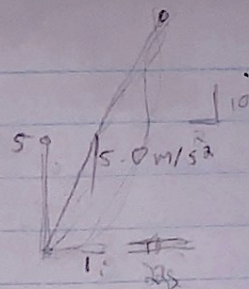
$$c. x(1) = -2(1) + 7(1)^2$$

$$= -2 + 7$$

$$= \boxed{5 \text{ m/s}}$$

$$d. \frac{24 - 0 \text{ m/s}}{2} = \boxed{12 \text{ m/s}^2}$$

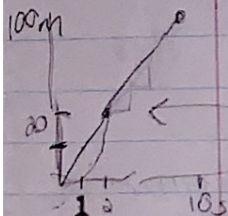
$$a = 5.0 \text{ m/s}^2 \quad v_i = 0 \text{ m/s} \quad v_f = 10.0 \text{ m/s}$$



$$3.) a. t = \frac{v_f - v_i}{a} = \frac{10.0 - 0 \text{ m/s}}{5.0 \text{ m/s}^2} = \boxed{2.0 \text{ s}}$$

$$b. \boxed{20 \text{ m}}$$

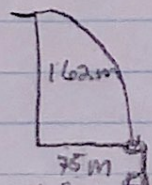
$$c. \boxed{10 \text{ s}}$$



$$10 \text{ m/s} \cdot 2 \text{ s} = 20 \text{ m}$$

5. Motion in Two and Three Dimensions

1.) a.



$$b. v^2 = v_i^2 + 2a\Delta y$$

$$16 \text{ m}^2 = (0)^2 + 2(9.81 \text{ m/s}^2)(75 \text{ m})$$

$$\sqrt{v^2} = \sqrt{1471.5 \text{ m}^2/\text{s}^2}$$

$$\boxed{v = 38.36 \text{ m/s}}$$

$$2.) a. R = \frac{v_0^2 \sin(2\theta_0)}{g}$$

$$R = \frac{40^2 \sin(2(45))}{9.81}$$

$$\boxed{R = 163.10 \text{ m}}$$

$$b. \text{ For } b. t_{\text{up}} = \frac{2(v_0 \sin(\theta_0))}{g} \rightarrow t_{\text{up}} = \frac{2(40 \text{ m/s}) \sin(45)}{9.81 \text{ m/s}^2}$$

$$\boxed{t_{\text{up}} = 5.77 \text{ s}}$$

6. Forces

$$1.) F_x = 10 \cos(45^\circ) + 8 \cos(30^\circ)$$

$$= 14.0 \text{ N}$$

$$F_y = 10 \sin(45^\circ) - 8 \sin(30^\circ)$$

$$= 3.1 \text{ N}$$

$$F_f = -7.5 \text{ N}$$

$$F_{\text{net}} = (14 \text{ N} - 7.5 \text{ N}) + 3.1 \text{ N} = 6.5 \text{ N} + 3.1 \text{ N}$$

$$a = \frac{F}{m} \rightarrow \frac{6.5 \text{ N} + 3.1 \text{ N}}{49 \text{ kg}} = (0.13 + 0.06) \text{ m/s}^2$$

$$= 0.73 \text{ m/s}^2$$