Computer Logic and Digital Circuit Design (PHYS306/COSC330): Unit 1

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SUMMARY

UNIT 1 SUMMARY - THEORETICAL LOGIC GATES, AND OPERATIONS

1. Logic Gates
    - Circuit diagram
    - Truth table
    - Timing diagram
    - Boolean logic
2. Boolean algebra I
3. IC Circuits, **data sheets**
4. Boolean algebra II

LOGIC GATES

LOGIC GATES

A **logic gate** is a digital circuit component made of transistors, that performs a basic logic function with n inputs and m outputs.

We will cover this basic set:

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

Each gate has n inputs, and m outputs. We represent the inputs (HIGH/LOW) with A, B, ..., and the output usually with X.

- Circuit diagram
- Truth table
- Timing diagram
- Boolean logic

The NOT gate: flips the input from LOW/HIGH to HIGH/LOW.

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

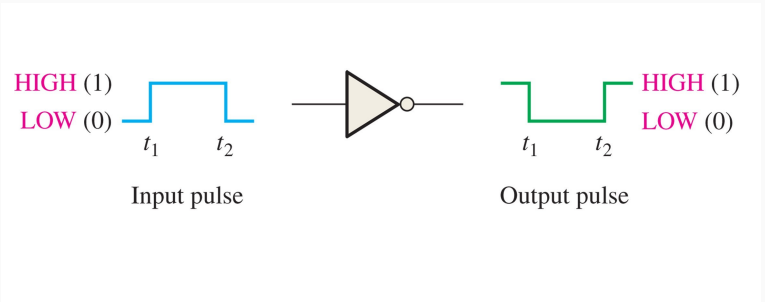

Figure 1: The NOT gate is represented with a triangle and a circle. It has one input and one output.

The NOT gate: flips the input from LOW/HIGH to HIGH/LOW.

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

IN	OUT
1	0
0	1

Table 1: Truth table for NOT.

The NOT gate: flips the input from LOW/HIGH to HIGH/LOW.

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

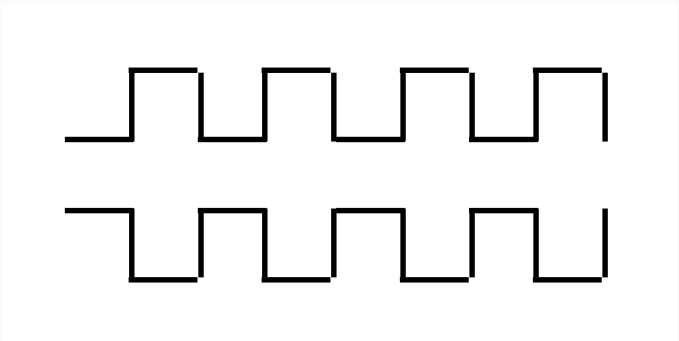

Figure 2: Example timing diagram for the NOT gate. (Top) example signal, s. (Bottom) NOT s, or $\bar{s}$.

The NOT gate: flips the input from LOW/HIGH to HIGH/LOW.

- NOT, $n = 1, m = 1$
- AND, $n, m = 1$
- OR, $n, m = 1$
- NAND, $n, m = 1$
- NOR, $n = 2, m = 1$
- XOR, $n = 2, m = 1$
- XNOR, $n = 2, m = 1$

$$NOT(A) = \bar{A} \tag{1}$$

The NOT gate: flips the input from LOW/HIGH to HIGH/LOW.

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

In class exercises:

- Using NOT gates, create a circuit that forms the 2's compliment of an 8 bit binary number.
- Once you have this, draw a timing diagram representing the conversion of 13 to the proper 1's compliment.

The AND gate: requires both inputs to be HIGH, for HIGH output.

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

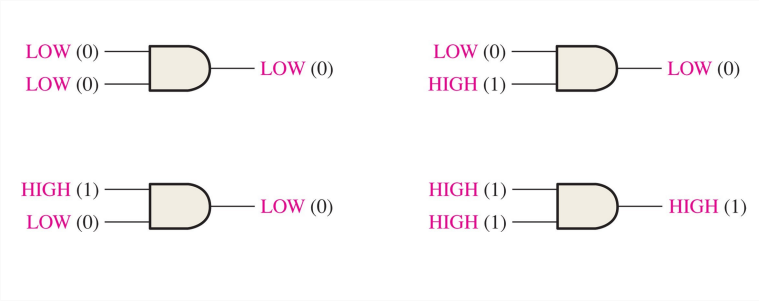

Figure 3: The circuit representation of an AND gate. Two inputs, one output.

The AND gate: requires both inputs to be HIGH, for HIGH output.

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

A	B	X
1	1	1
1	0	0
0	1	0
0	0	0

Table 2: Truth table for AND.

How many input combinations are there for n? Specifically, how many for two-input gates? Three-input?

The AND gate: requires both inputs to be HIGH, for HIGH output.

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

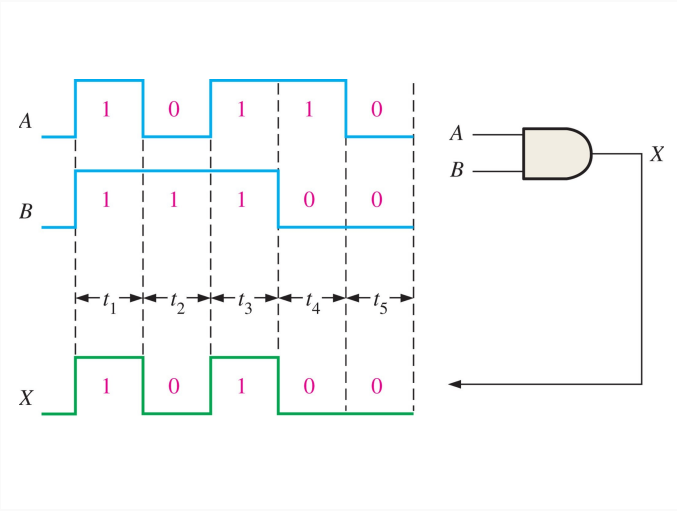

Figure 4: Example timing diagram for AND gate. (Top) Input *A*. (Middle) Input *B*. (Bottom) *AB* (A AND B).

The AND gate: requires both inputs to be HIGH, for HIGH output.

- NOT, $n = 1, m = 1$
- AND, $n, m = 1$
- OR, $n, m = 1$
- NAND, $n, m = 1$
- NOR, $n = 2, m = 1$
- XOR, $n = 2, m = 1$
- XNOR, $n = 2, m = 1$

$$A\ AND\ B = AB \tag{2}$$

The AND gate: requires both inputs to be HIGH, for HIGH output.

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

In-class exercises:

- Using AND as "enable:" Develop a circuit that activates an LED circuit every time the clock signal is HIGH, but only if an enable signal is also raised to HIGH.
- Derive the truth table for a 3-input AND gate. How many input combinations should there be?

The AND gate: requires both inputs to be HIGH, for HIGH output.

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

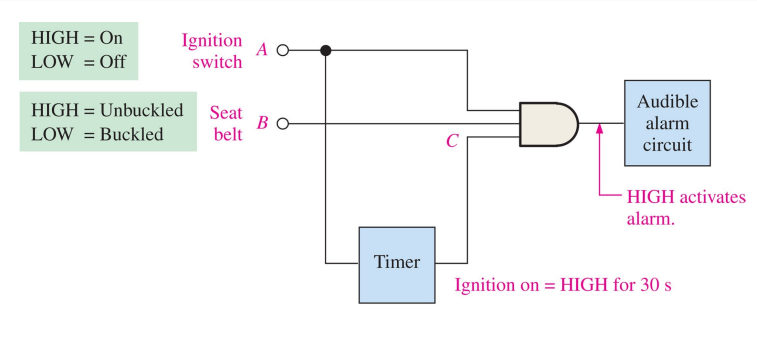

Figure 5: Example of AND enable plus timing: seatbelt sensor.

The OR gate: requires either input to be HIGH, for HIGH output.

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

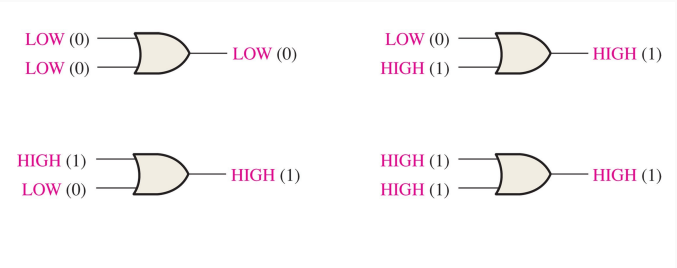

Figure 6: The circuit representation of an OR gate. Two inputs, one output.

The OR gate: requires either input to be HIGH, for HIGH output.

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

A	B	X
1	1	1
1	0	1
0	1	1
0	0	0

Table 3: Truth table for OR.

The OR gate: requires either input to be HIGH, for HIGH output.

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

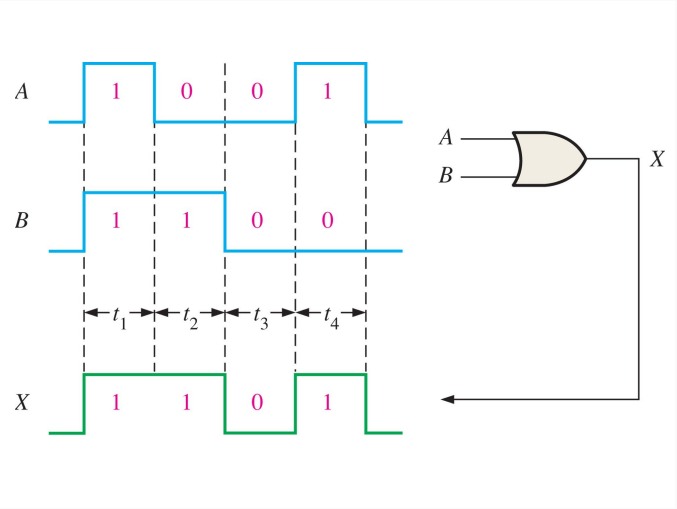

Figure 7: Example timing diagram for OR gate. (Top) Input A. (Middle) Input B. (Bottom) $A + B$ (A OR B).

The OR gate: requires either input to be HIGH, for HIGH output.

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

$$A\ OR\ B = A + B \tag{3}$$

The OR gate: requires either input to be HIGH, for HIGH output.

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

In-class exercises:

- In physics experiments, sometimes we establish a *combinatorial trigger*, sometimes called a coincidence trigger. Suppose the task of three digital channels is to observe a high-energy particle pass through a detector. If there is an observation in a channel, it raises HIGH for a time called a *gate time*.
- Using OR gates, draw a circuit that triggers if **two of the three** channels observes the particle. Draw an example of a timing diagram corresponding to a trigger. (The gate time is up to you, it just means that if a channel is HIGH it stays high for at least one gate).

The NAND gate: requires **neither** input to be HIGH for the output to be HIGH

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

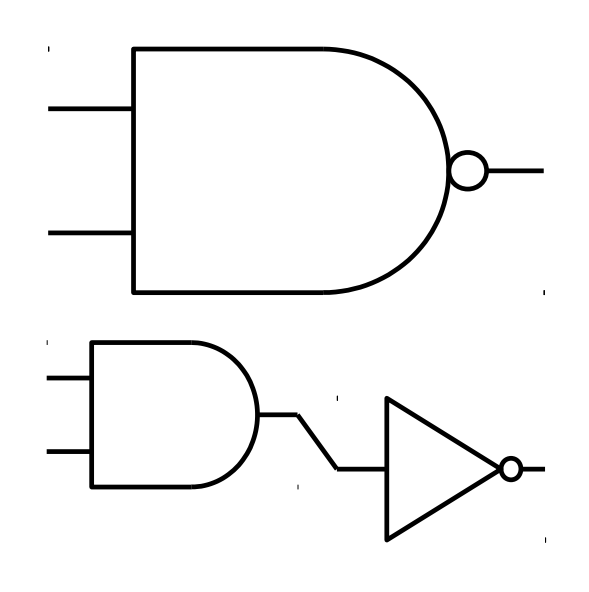

Figure 8: The circuit representation of an NAND gate. Two inputs, one output.

The NAND gate: requires **neither** input to be HIGH for the output to be HIGH

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

A	B	X
1	1	0
1	0	1
0	1	1
0	0	1

Table 4: Truth table for NAND.

The NAND gate: requires **neither** input to be HIGH for the output to be HIGH

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

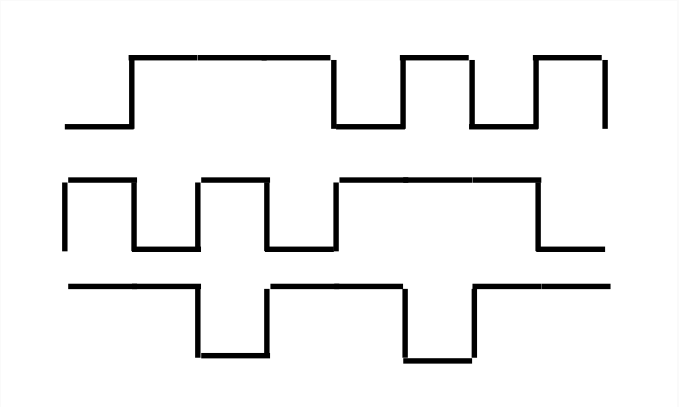

Figure 9: Example timing diagram for NAND gate. (Top) Input A. (Middle) Input B. (Bottom) $\overline{AB}$ (A NAND B or NAND AB).

The NAND gate: requires **neither** input to be HIGH for the output to be HIGH

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

$$A \; NAND \; B = \overline{AB} \tag{4}$$

Note: have you started to pick up the notation here? The bar is like complex conjugation, or the ***compliment*** of the signal.

The NAND gate: requires **neither** input to be HIGH for the output to be HIGH

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

In-class exercises:

- A certain fluid pump has a display that shows sensor information from two pairs of pipes, pair A and pair B. The sensors are raised HIGH if no fluid is flowing through a pipe, and there is one sensor per pipe.

The NAND gate: requires **neither** input to be HIGH for the output to be HIGH

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

In-class exercises:

- Design a system using NAND gates that produces three output signals: one LOW if neither pipe in pair A has fluid flowing, one LOW if neither pipe in pair B has fluid flowing, and one LOW if neither pair has fluid flowing. Create a timing diagram that shows pair A turning off, then pair B.

The NAND gate: requires **neither** input to be HIGH for the output to be HIGH

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

In-class exercises:

- Create an OR gate with NAND and NOT gates. a) 2-input version 3) 3-input version.
- Create an AND gate with NAND and NOT gates. a) 2-input version 3) 3-input version.

The NOR gate: requires **both** inputs to be LOW for the output to be HIGH

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

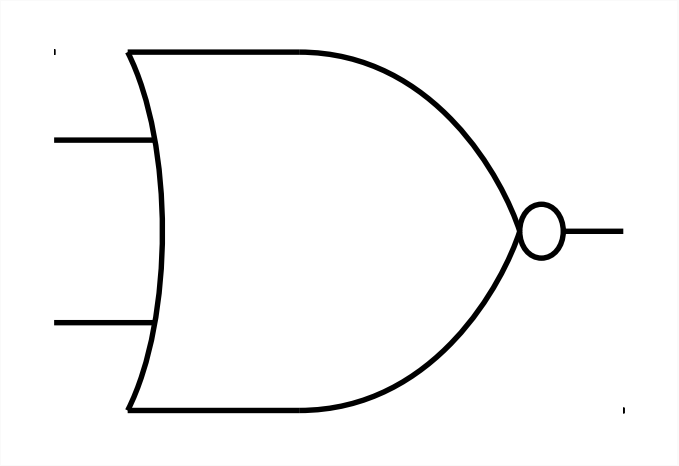

Figure 10: The circuit representation of an NOR gate. Two inputs, one output.

The NOR gate: requires **both** inputs to be LOW for the output to be HIGH

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

A	B	X
1	1	0
1	0	0
0	1	0
0	0	1

Table 5: Truth table for NOR.

The NOR gate: requires **both** inputs to be LOW for the output to be HIGH

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

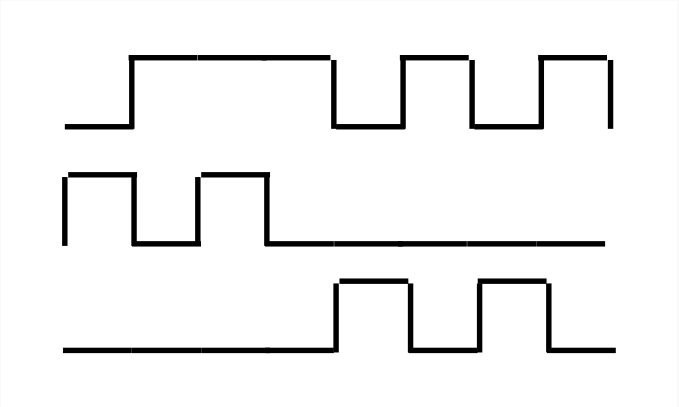

Figure 11: Example timing diagram for NOR gate. (Top) Input A. (Middle) Input B. (Bottom) $\overline{A + B}$ (A NOR B or NOR AB).

The NOR gate: requires **both** inputs to be LOW for the output to be HIGH

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

$$A \; NOR \; B = \overline{A + B} \tag{5}$$

The NOR gate: requires **both** inputs to be LOW for the output to be HIGH

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

In-class exercises:

- Create a NOR gate from a NAND gate and inverters. a) 2-input version b) 3-input version. Verify with either a timing diagram or truth table.

The NOR gate: requires **both** inputs to be LOW for the output to be HIGH

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

In-class exercise (from the text, this one is cool)

- As part of an aircraft's functional monitoring system, a circuit is required to indicate the status of the landing gears prior to landing. A green LED display turns on if all three gears are properly extended when the gear-down switch has been activated in preparation for landing. A red LED display turns on if any of the gears fail to extend properly prior to landing. When a landing gear is extended, its sensor produces a LOW voltage. When a landing gear is retracted, its sensor produces a HIGH voltage. Implement a circuit to meet this requirement.

To solve this problem, let's have a quick aside as to how LED's (light emitting diodes) work...

LED - light emitting diode. What's a diode? What is a transistor? One kind of transistor is a p-n-p junction, or a n-p-n junction:

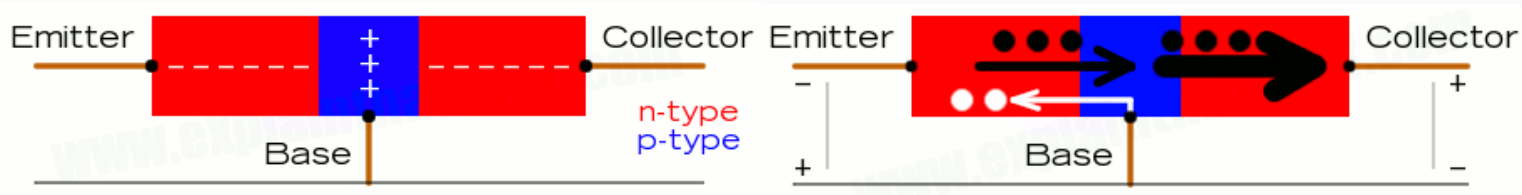

Figure 12: One kind of transistor is the sandwich of semiconductors.

LED - light emitting diode. What's a diode? Like a transistor, minus one layer. Diodes will only conduct in one direction.

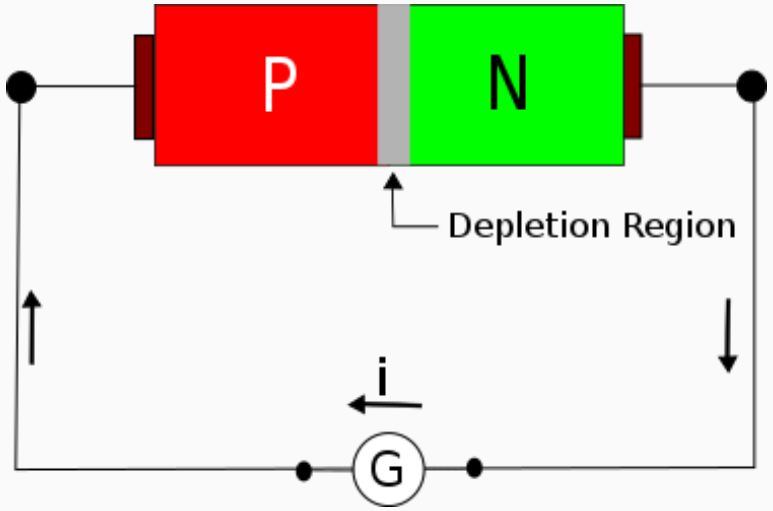

Figure 13: A diode is a sandwich of only two layers of semiconductor rather than three.

LED - light emitting diode. What's a diode? Like a transistor, minus one layer. Diodes will only conduct in one direction.

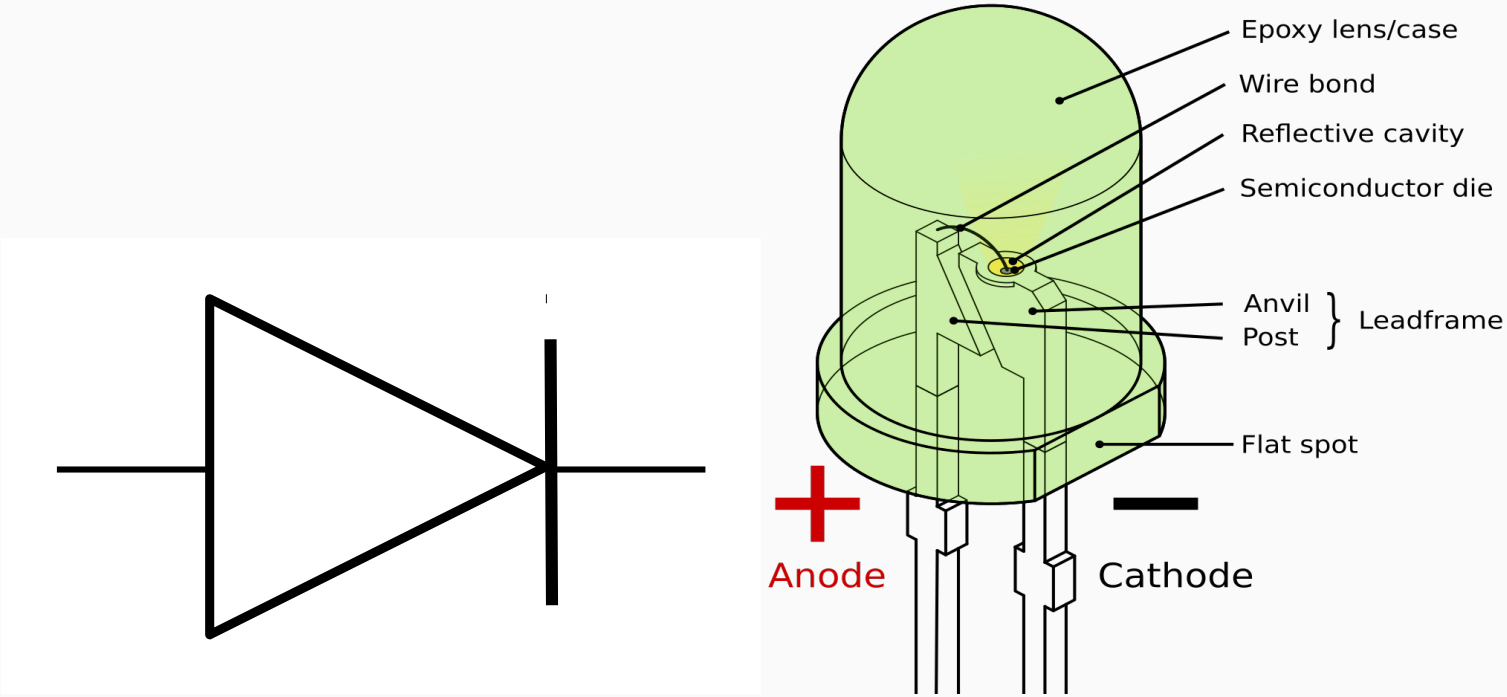

Figure 14: (Left) The symbol for a diode. Current flows towards the flat line. (Right) Some diodes emit visible photons when conducting electricity.

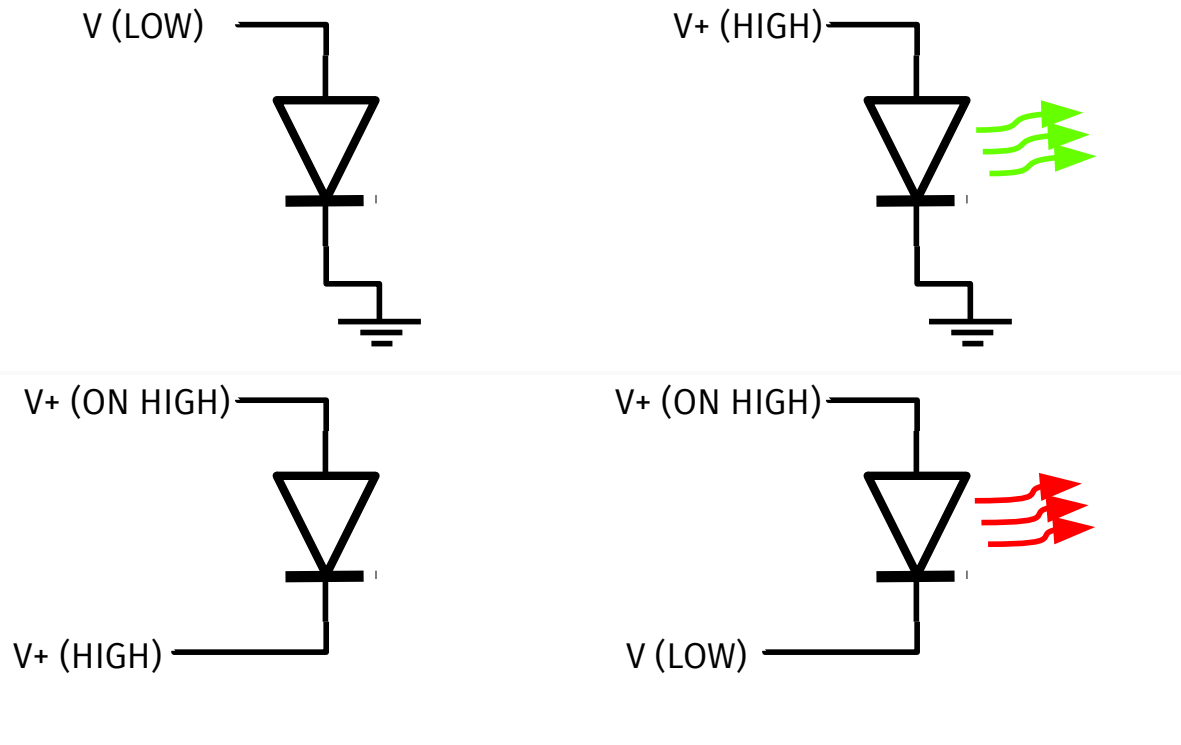

Figure 15: (Upper left): The green LED is held off by a LOW signal, no voltage gradient. (Upper right) The green LED is activated by a HIGH signal, a voltage gradient. (Lower left): The red LED is held off by a HIGH signal, no voltage gradient. (Lower right): The red LED is activated by a LOW signal, a voltage gradient.

The NOR gate: requires **both** inputs to be LOW for the output to be HIGH

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

So now we can solve this problem:

- As part of an aircraft's functional monitoring system, a circuit is required to indicate the status of the landing gears prior to landing. A green LED display turns on if all three gears are properly extended when the gear-down switch has been activated in preparation for landing. A red LED display turns on if any of the gears fail to extend properly prior to landing. When a landing gear is extended, its sensor produces a LOW voltage. When a landing gear is retracted, its sensor produces a HIGH voltage. Implement a circuit to meet this requirement.

The XOR gate: requires **exactly one** input to be HIGH for the output to be HIGH

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

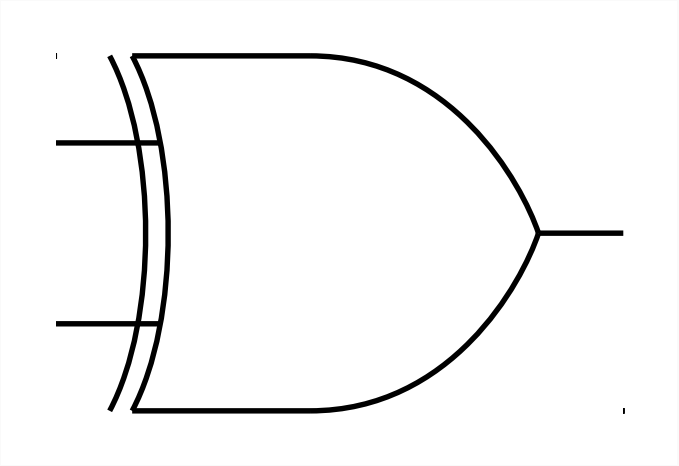

Figure 16: The circuit representation of an XOR gate. Two inputs, one output.

The XOR gate: requires **exactly one** input to be HIGH for the output to be HIGH

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

A	B	X
1	1	0
1	0	1
0	1	1
0	0	0

Table 6: Truth table for XOR.

The XOR gate: requires **exactly one** input to be HIGH for the output to be HIGH

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

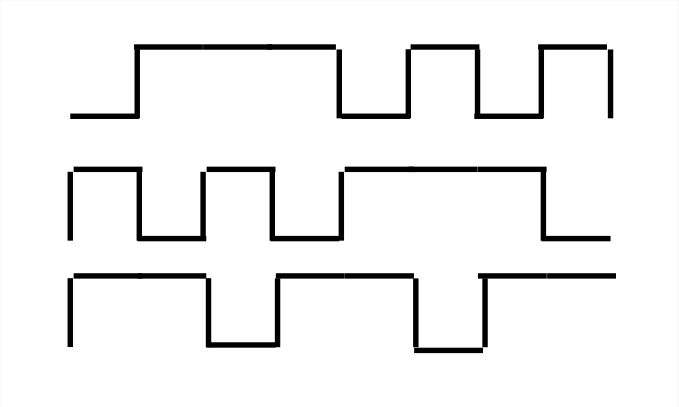

Figure 17: Example timing diagram for XOR gate. (Top) Input *A*. (Middle) Input *B*. (Bottom) Output

The XNOR gate: requires **both** inputs to be HIGH or LOW for the output to be HIGH

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

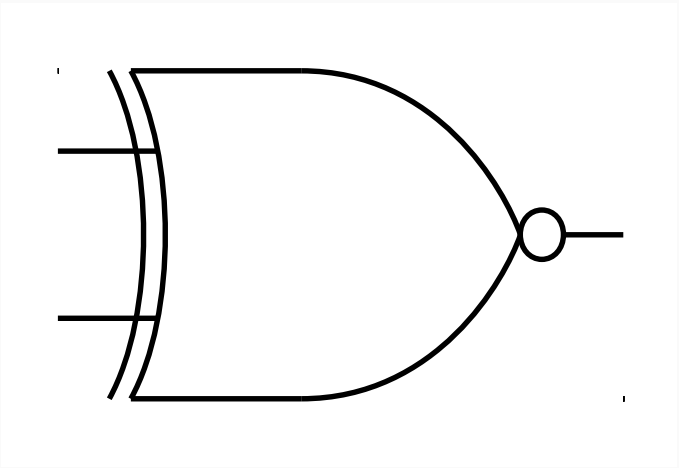

Figure 18: The circuit representation of an XNOR gate. Two inputs, one output.

The XNOR gate: requires **both** inputs to be HIGH or LOW for the output to be HIGH

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

A	B	X
1	1	1
1	0	0
0	1	0
0	0	1

Table 7: Truth table for XNOR.

The XNOR gate: requires **both** inputs to be HIGH or LOW for the output to be HIGH

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

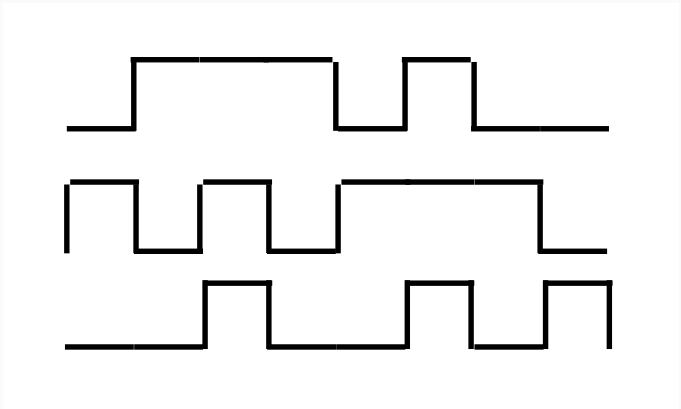

Figure 19: Example timing diagram for XNOR gate. (Top) Input *A*. (Middle) Input *B*. (Bottom) Output

The NOR gate: requires **both** inputs to be LOW for the output to be HIGH

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

In-class exercises:

- Show that an XOR gate is a two-bit adder, neglecting the carry bit.
- Create an 2-bit adder from XOR and AND gates.

The NOR gate: requires **both** inputs to be LOW for the output to be HIGH

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

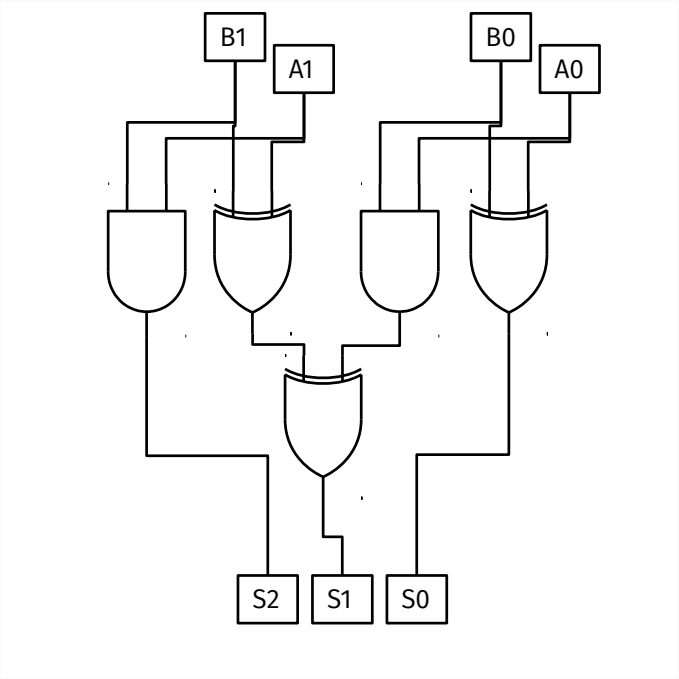

Figure 20: Example of a circuit that adds two-bit digital numbers.

The NOR gate: requires **both** inputs to be LOW for the output to be HIGH

- NOT, $n = 1$, $m = 1$
- AND, n, $m = 1$
- OR, n, $m = 1$
- NAND, n, $m = 1$
- NOR, $n = 2$, $m = 1$
- XOR, $n = 2$, $m = 1$
- XNOR, $n = 2$, $m = 1$

In-class exercises:

- Create an 8-bit adder from XOR and AND gates.
- Account for all-possible carry bits...

CONCLUSION

Unit 2.1 Summary - Theoretical Logic Gates, and Operations

Reading: DF Chapter 3-4 (Moodle)

1. Logic Gates
    - Circuit diagram
    - Truth table
    - Timing diagram
    - Boolean logic
2. Boolean algebra I
3. IC Circuits, **data sheets**
4. Boolean algebra II