

Homework #4

Andy P.

Ch. 6 4, 7, 11, 15, 20, 21, 23, 29, 34, 45

①

$$\begin{aligned} 4. \Sigma_1 &= (A \oplus B) \oplus C \\ &= (1 \oplus 1) \oplus 0 \\ &= 0 \oplus 0 \\ &= 0 \end{aligned}$$

$$\begin{aligned} C_{out} &= AB + (A \oplus B)C_{in} \\ &= (1)(1) + (1 \oplus 1)(0) \\ &= 1 + 0 \\ &= 1 \end{aligned}$$

② $A=1 \quad B=0 \quad C_{in}=1$

$$\begin{aligned} \Sigma_2 &= (A \oplus B) \oplus C_{in} \\ &= (1 \oplus 0) \oplus 1 \\ &= 1 \oplus 1 \\ &= 0 \end{aligned}$$

$$\begin{aligned} C_{out} &= AB + (A \oplus B)C_{in} \\ &= 0 + (1)(1) \\ &= 1 \end{aligned}$$

③ $A=1 \quad B=1 \quad C_{in}=1$

$$\begin{aligned} \Sigma_3 &= (A \oplus B) \oplus C_{in} \\ &= (1 \oplus 1) \oplus 1 \\ &= 0 \oplus 1 \\ &= 1 \end{aligned}$$

$$\begin{aligned} C_{out} &= AB + (A \oplus B)C_{in} \\ &= 1 + 0 \\ &= 1 \end{aligned}$$

$$\Sigma_4 \Sigma_3 \Sigma_2 \Sigma_1 = \boxed{1100}$$

④

$$\begin{aligned} \Sigma_4 &= AB + (A \oplus B)C_{in} \\ &= 1 + (0)1 \\ &= 1 \end{aligned}$$

7. $A = 1001$ $B = 1100 \rightarrow 0011$
 Add/Subt. = 1

①

$A = 1$ $B = 1$ $C_{in} = 1$

$$\begin{aligned}\Sigma_1 &= (A \oplus B) \oplus C_{in} \\ &= (1 \oplus 1) \oplus 1 \\ &= 0 \oplus 1 \\ &= 1\end{aligned}$$

$$\begin{aligned}C_{out} &= AB + (A \oplus B) C_{in} \\ &= 1 + (0)(1) \\ &= 1\end{aligned}$$

② $A = 0$ $B = 1$ $C_{in} = 1$

$$\begin{aligned}\Sigma_2 &= (A \oplus B) \oplus C_{in} \\ &= (0 \oplus 1) \oplus 1 \\ &= 1 \oplus 1 \\ &= 0\end{aligned}$$

$$\begin{aligned}C_{out} &= AB + (A \oplus B) C_{in} \\ &= 0 + (1)(1) \\ &= 1\end{aligned}$$

③ $A = 0$ $B = 0$ $C_{in} = 1$

$$\begin{aligned}\Sigma_3 &= (A \oplus B) \oplus C_{in} \\ &= (0 \oplus 0) \oplus 1 \\ &= 0 \oplus 1 \\ &= 1\end{aligned}$$

$$\begin{aligned}C_{out} &= AB + (A \oplus B) C_{in} \\ &= 0 + (0)(1) \\ &= 0\end{aligned}$$

④ $A = 1$ $B = 0$ $C_{in} = 0$

$$\begin{aligned}\Sigma_4 &= (A \oplus B) \oplus C_{in} \\ &= (1 \oplus 0) \oplus 0 \\ &= 1 \oplus 0 \\ &= 1\end{aligned}$$

$$\begin{aligned}C_{out} &= AB + (A \oplus B) C_{in} \\ &= 0 + (1)0 \\ &= 0 + 0 \\ &= 0\end{aligned}$$

$$\Sigma_4 \Sigma_3 \Sigma_2 \Sigma_1 = \boxed{1101}$$

11. ① A to Σ and $C_{out} = 40\text{ns}$
 ② B to " " = 40ns
 ③ C_{in} to $\Sigma = 35\text{ns}$
 ④ " " to $C_{out} = 25\text{ns}$

$$t_p = (1) + 6(4) + (3) \\ = 40 + 6(25) + 35 \\ = \boxed{225\text{ns}}$$

15.

a)

$A > B$	1
$A = B$	0
$A < B$	0

b)

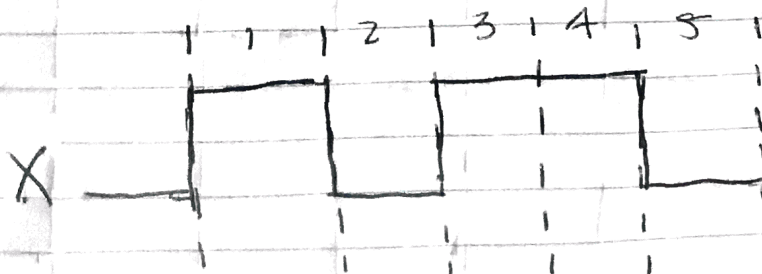
$A > B$	0
$A = B$	0
$A < B$	1

c)

$A > B$	0
$A = B$	1
$A < B$	1

20)

$$Y = A_2 A_1 \bar{A}_0 + A_2 \bar{A}_1 A_0 + \bar{A}_2 A_1 \bar{A}_0$$

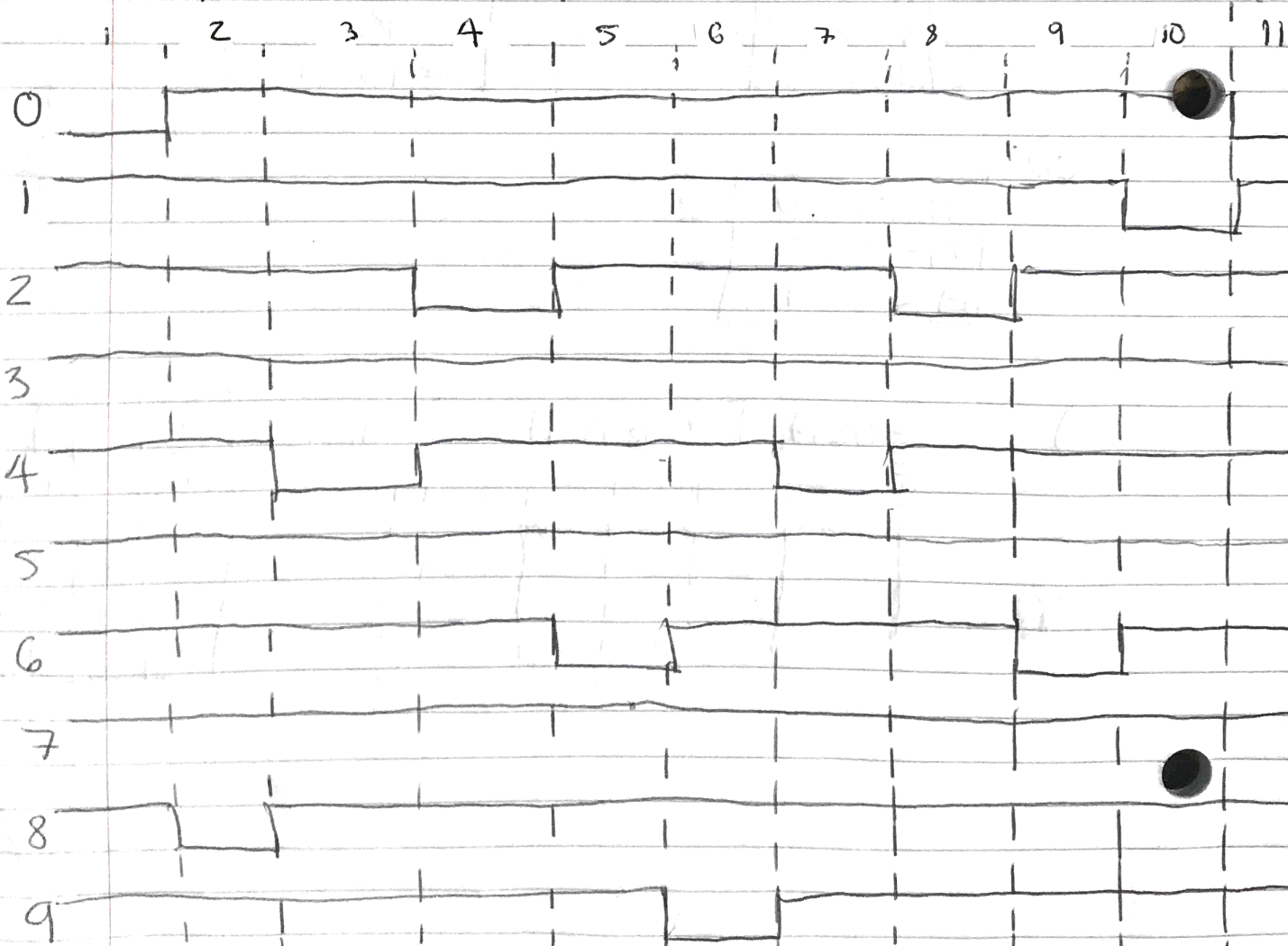


A_2	A_1	A_0	X
1	0	1	1
1	0	0	0
1	1	0	1
0	1	0	1
0	0	1	0

21. $A_3 \ A_2 \ A_1 \ A_0$

O/U in active low

1	0	0	0	0	0
2	1	0	0	0	8
3	0	1	0	0	4
4	0	0	1	0	2
5	0	1	1	0	6
6	1	0	0	1	9
7	0	1	0	0	4
8	0	0	1	0	2
9	0	1	1	0	6
10	0	0	0	1	1
11	0	0	0	0	0



23. 9=High = A_0 & A_3 are 1
 3=High = A_1 is 1

Output Code: 1011

This is not a valid BCD code
 since $1011 = 12$ and its not 0-9.

29. S_1 S_0 D_x
 0 0 $D_0 = 0$
 1 0 $D_2 = 1$
 0 1 $D_1 = 1$
 1 1 $D_3 = 0$
 1 1 $D_3 = 0$
 0 1 $D_1 = 1$
 1 0 $D_2 = 1$
 0 0 $D_0 = 0$
 0 1 $D_1 = 1$
 1 0 $D_2 = 1$
 1 1 $D_3 = 0$
 0 0 $D_0 = 0$

X	D_0	D_2	D_1	D_3	D_3	D_1	D_2	D_0	D_1	D_2	D_3	D_0
---	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------	-------

34.	A	B	Cin	Σ	Cout
1	0	0	0	0	0
2	0	0	1	1	0
3	0	1	0	1	0
4	0	1	1	0	1
5	1	0	0	1	0
6	1	0	1	0	1
7	1	1	0	0	1
8	1	1	1	1	1

On 1 $A=0, B=0, Cin=0$ yet $\Sigma=1$!

On 2 $A=0, B=0, Cin=1$ yet $Cout=0$

It is not operating properly.

Cin is at fault here since it is oscillating yet it is always considering logic 1 to all intervals.

$$45. \bar{A}\bar{B}C_{in} + \bar{A}B\bar{C}_{in} + A\bar{B}\bar{C}_{in} + ABC_{in} = \Sigma$$

$$\bar{A}BC_{in} + A\bar{B}C_{in} + A\bar{B}\bar{C}_{in} + ABC_{in} = C_{out}$$

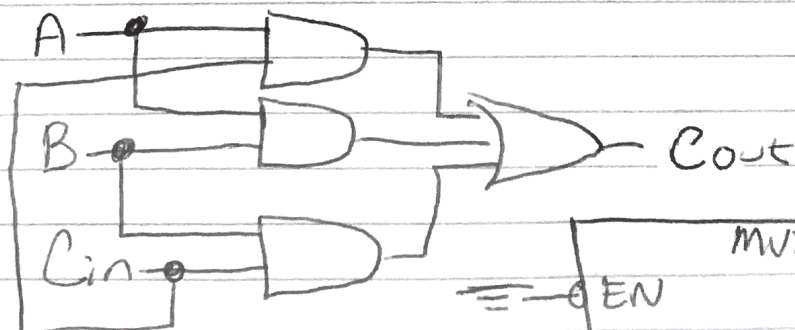
A \ BC	00	01	11	10
0	0	1	0	1
1	1	0	1	0

= Σ

A \ BC	00	01	11	10
0	0	0	1	0
1	0	1	1	1

= C_{out}

$$C_{out} = AC_{in} + BC_{in} + AB$$



101 = 5
111 = 7
011 = 3
110 = 6

010 = 2
100 = 4
001 = 1
111 = 7

