

# Thursday Reading Assessment: Chapter 2-8, 2-10 through 2-12

Prof. Jordan C. Hanson

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## 1 Binary, Hexadecimal, BCD, and Gray Codes

1. Let  $x_1 = 10110$ . Show that taking the 2's complement of  $x_1$  *twice* returns  $x_1$ .
2. Show that the range of 4-bit signed binary numbers in 2's complement form is  $[-8, 7]$ , assuming one sign bit.
3. Let  $x_1 = F7_{16}$ , and  $x_2 = 9D_{16}$ .
  - (a) What is  $x_1$  in binary?
  - (b) What is  $x_2$  in decimal?
4. Imagine a stream of binary digits coming through a serial line. They are: 1001...0001...0001. If we know the bitstream is in binary coded decimal (BCD), what is the code being sent?
5. What property of the four-bit gray code in Fig. 1 distinguishes it from straight binary counting?

| TABLE 2-6           |        |           |         |        |           |
|---------------------|--------|-----------|---------|--------|-----------|
| Four-bit Gray code. |        |           |         |        |           |
| Decimal             | Binary | Gray Code | Decimal | Binary | Gray Code |
| 0                   | 0000   | 0000      | 8       | 1000   | 1100      |
| 1                   | 0001   | 0001      | 9       | 1001   | 1101      |
| 2                   | 0010   | 0011      | 10      | 1010   | 1111      |
| 3                   | 0011   | 0010      | 11      | 1011   | 1110      |
| 4                   | 0100   | 0110      | 12      | 1100   | 1010      |
| 5                   | 0101   | 0111      | 13      | 1101   | 1011      |
| 6                   | 0110   | 0101      | 14      | 1110   | 1001      |
| 7                   | 0111   | 0100      | 15      | 1111   | 1000      |

Figure 1: A four-bit binary gray code.

6. Convert 1010 (gray code) to binary, showing how the process works.
7. Circle all the following 4-bit BCD code word sequences below that have a *single-bit* error, assuming *even* parity:
  - 1 0011 0010
  - 0 1110 1010
  - 1 0111 1110 1000 1010