

Midterm #2

Cross Simpson

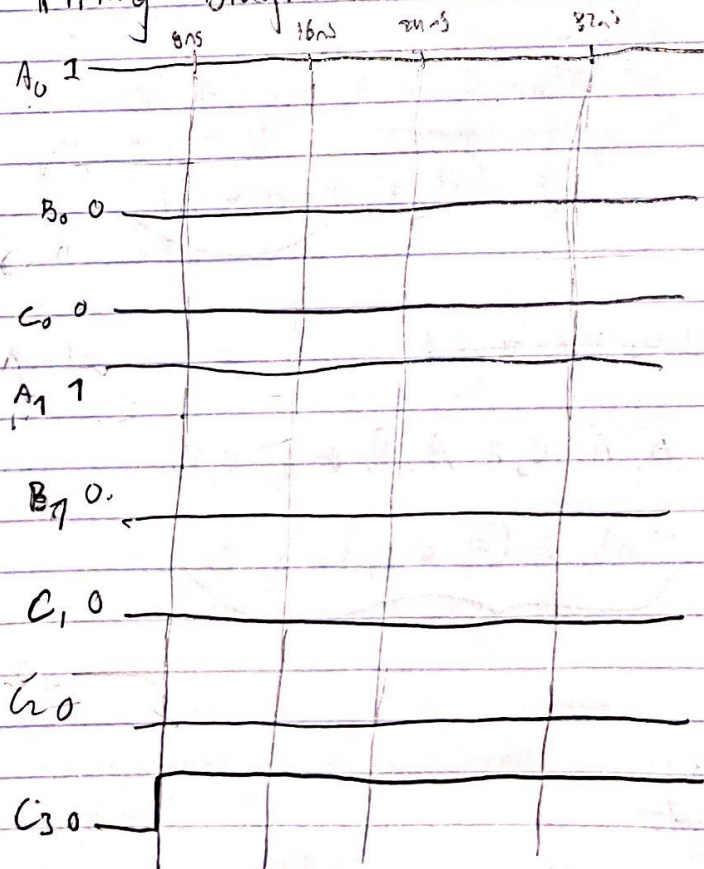
① Total delay 32 ns

a) $\frac{1}{32} = f_{max} \Rightarrow 31.25 \text{ MHz}$

b) 8-bits, worst delay = 64 ns

$f_{max} = 15.625 \text{ MHz}$

c) Timing Diagram



C = Cout

$S_3 S_2 S_1 S_0 = 0111$

②

a) $A > B$

$$f(A, B) = (4, 5, 6, 12, 13, 14)$$

A	B	00	01	11	10
00	0	0	0	0	0
01	1	0	1	0	0
11	1	1	1	1	1
10	1	1	1	1	0

$$\begin{aligned} & \rightarrow A_0 B_1 \bar{B}_0 + A_1 \bar{B}_1 + A_1 A_0 \bar{B}_0 \\ & = A_0 B_0 (A_1 \vee A_1) + A_1 B_1 \end{aligned}$$

b) $A = B$

$$f(A, B) = (0, 5, 10, 15)$$

A	B	00	01	11	10
00	1	1	0	0	0
01	0	0	1	0	0
11	0	0	0	1	0
10	0	0	0	0	1

$$\begin{aligned} & \bar{A}_1 \bar{A}_0 \bar{B}_1 \bar{B}_0 + A_1 \bar{A}_0 B_1 \bar{B}_0 + A_1 A_0 B_1 B_0 + A_1 \bar{A}_0 B_1 B_0 \\ & = (\bar{A}_1 \bar{A}_0 + A_1 \bar{A}_0) (\bar{B}_1 \bar{B}_0 + B_1 B_0) \\ & = (A_0 \oplus B_0) (A_1 \oplus B_1) \end{aligned}$$

c) $A < B$

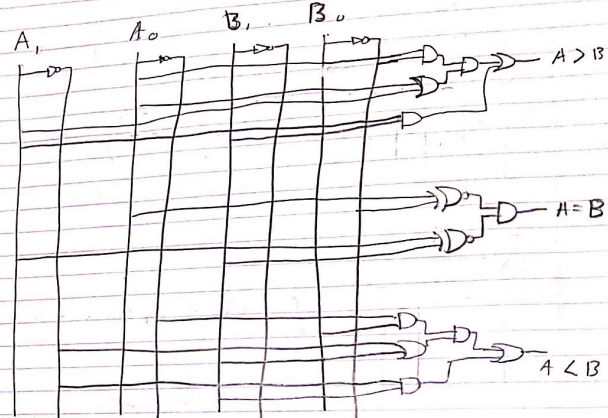
$$f(A, B) = (1, 2, 3, 6, 7, 11)$$

A	B	00	01	11	10
00	0	0	0	0	0
01	1	0	1	0	0
11	1	1	1	1	1
10	0	0	0	0	1

$$\begin{aligned} & \bar{A}_1 \bar{A}_0 B_0 + A_1 B_1 + \bar{A}_0 B_1 B_0 \\ & = \bar{A}_0 B_0 (\bar{A}_1 + B_1) + A_1 B_1 \end{aligned}$$

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a)



③ Binary = 13
Gray = 6

B_0 k-map

π				
σ_0				
σ_1	1		1	
π		1		1
σ_2	1		1	

$$\begin{aligned} & \overline{\sigma_0} \overline{\sigma_1} \overline{\sigma_2} \overline{\sigma_3} + \overline{\sigma_0} \overline{\sigma_1} \sigma_2 \overline{\sigma_3} + \overline{\sigma_0} \sigma_1 \overline{\sigma_2} \overline{\sigma_3} + \overline{\sigma_0} \sigma_1 \sigma_2 \overline{\sigma_3} \\ & + \sigma_0 \overline{\sigma_1} \overline{\sigma_2} \overline{\sigma_3} + \sigma_0 \overline{\sigma_1} \sigma_2 \overline{\sigma_3} + \sigma_0 \sigma_1 \overline{\sigma_2} \overline{\sigma_3} + \sigma_0 \sigma_1 \sigma_2 \overline{\sigma_3} \\ & \Rightarrow \sigma_0 \oplus \sigma_1 \oplus \sigma_2 \oplus \sigma_3 \end{aligned}$$

B_1 k-map

π				
σ_0				
σ_1	1		1	
π		1		1
σ_2	1		1	

$$\begin{aligned} & \overline{\sigma_1} \overline{\sigma_2} \overline{\sigma_3} + \overline{\sigma_1} \overline{\sigma_2} \sigma_3 + \overline{\sigma_1} \sigma_2 \overline{\sigma_3} + \overline{\sigma_1} \sigma_2 \sigma_3 \\ & + \sigma_1 \overline{\sigma_2} \overline{\sigma_3} + \sigma_1 \overline{\sigma_2} \sigma_3 + \sigma_1 \sigma_2 \overline{\sigma_3} + \sigma_1 \sigma_2 \sigma_3 \\ & = \sigma_1 \oplus \sigma_2 \oplus \sigma_3 \end{aligned}$$

B_2 k-map

π				
σ_0				
σ_1	1		1	
π		1		1
σ_2	1		1	

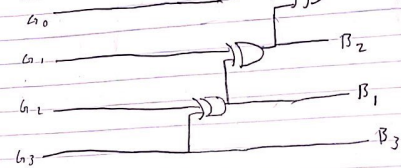
$$\begin{aligned} & \overline{\sigma_1} \overline{\sigma_2} + \overline{\sigma_1} \sigma_2 \\ & = \sigma_1 \oplus \sigma_2 \end{aligned}$$

B_3 k-map

π				
σ_0				
σ_1				
π				
σ_2				

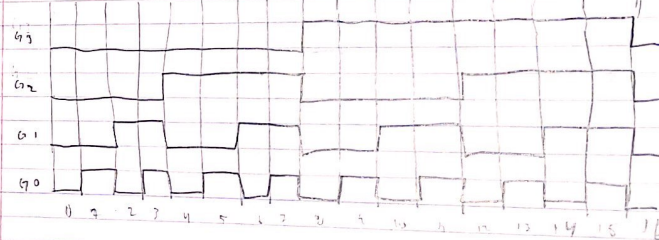
$$\begin{aligned} & B_3 = \sigma_1 \\ & \sigma_1 \wedge B_3 \end{aligned}$$

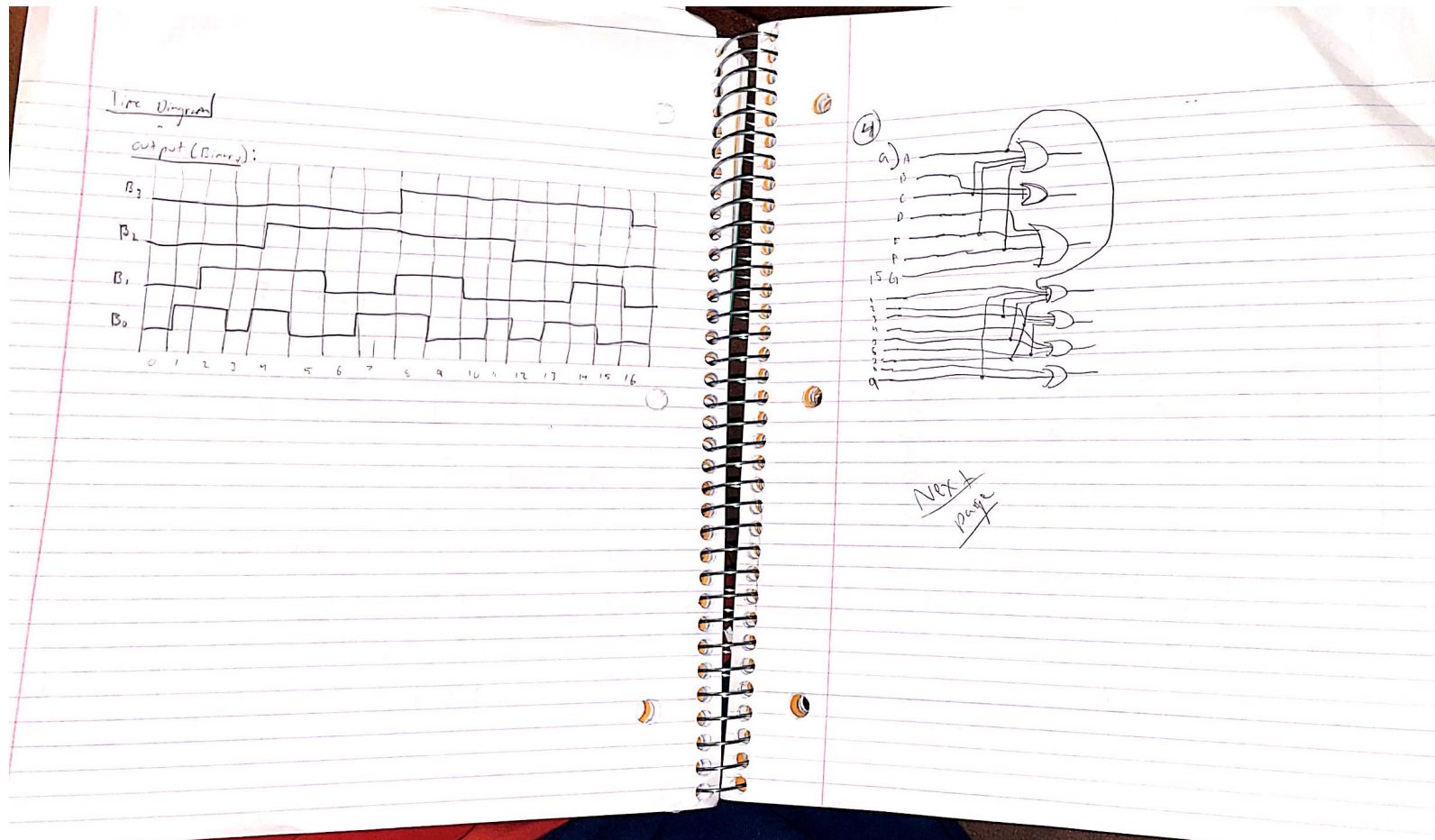
Circuit



Time Diagram

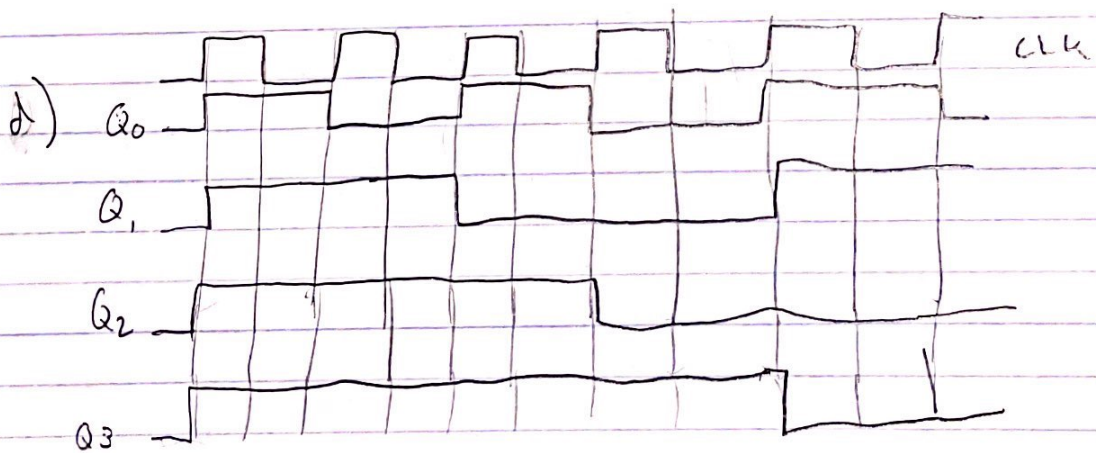
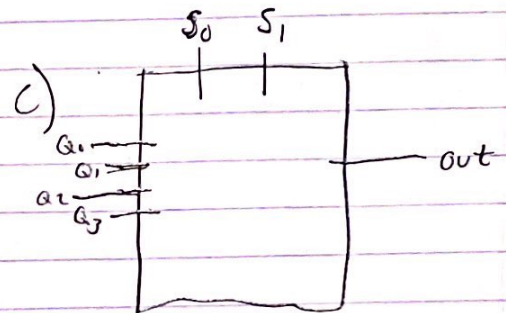
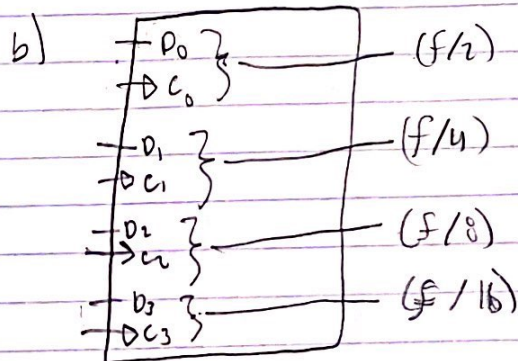
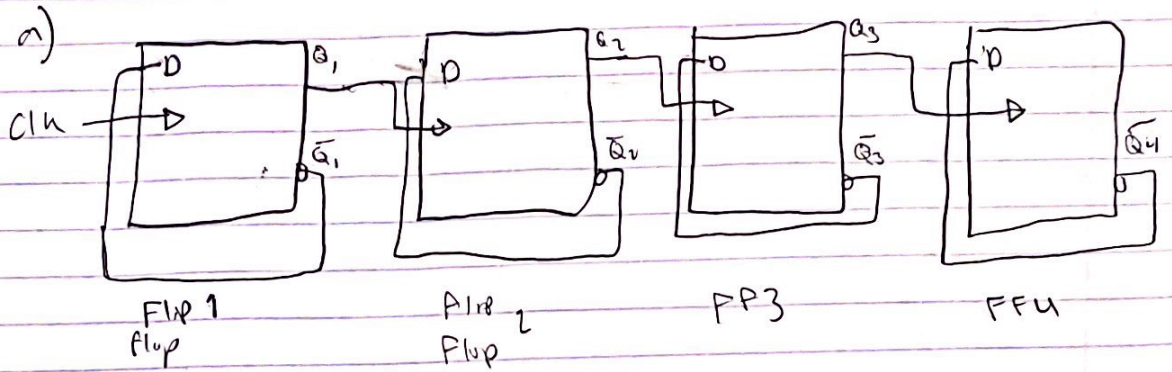
Input (Gray):





Ch. 7

(1)



Ch 8-9

(1)

clk	Q ₀	Truth table							Shift	
		7	2	3	4	5	6	Q ₇	right	left
0									1	0
1							1	0	1	0
2							0	0	1	0
3							0	0	1	0
4							0	0	1	0
5							0	0	1	0
6	1	1					0	0	1	0
7	1						0	0	1	0
8	1						0	0	0	1
9		1					0	0	0	1
10			1				0	0	0	1
11				1			0	0	0	1
12					1		0	0	0	1
13						1	0	0	0	1
14							1	0	0	1
15							1	0	0	1

Circuit

S=Shift

