

Sum of two signals

$$V(t) = a_1 e^{jX_1} + a_2 e^{jX_2}, \quad X_i = 2\pi f_i t + \phi_i$$

Let

$$V_1(t) = a_1 e^{jX_1} \quad \& \quad V_2(t) = a_2 e^{jX_2} \quad \begin{matrix} \phi_2 - \phi_1 = 0 \\ \phi_2 - \phi_1 = \pi \end{matrix}$$

$$V_1(t) = a_1 \cos X_1 \quad \& \quad V_2 = a_2 \cos X_2$$

$$\Rightarrow a_1 \cos(2\pi f_1 t) \quad \Rightarrow a_2 \cos(2\pi f_2 t) \quad \uparrow$$

Real
 $V_1(t) + V_2(t) =$

$$V_{re} = a_1 e^{j(2\pi f_1 t)} + a_2 e^{j(2\pi f_2 t)}$$

Positive &
negative

Imaginary
 $V_1(t) + V_2(t) =$

$$V^* = a_1 e^{-j(2\pi f_1 t)} + a_2 e^{-j(2\pi f_2 t)}$$

$$VV^* = a_1^2 + a_1 a_2 + a_2^2 + a_2 a_1 = (a_1 + a_2)^2$$

Which shows constructive interference as in the amplitudes will be added and not destroy each other.