

# Roy Kailu DSP HW 2

$$\frac{j\omega}{1+j\omega}$$

2. The digital signal frequency would be 50 kHz.

(b) The digital signal frequency would be 100 kHz

$$(c) 750 - 500 = 250 \text{ kHz}$$

$$(d) 1000 - 500 = 500 \text{ kHz}$$

$$3. \text{ Gain} = \frac{0.33}{3.3} = 0.1$$

$$0.1 = \frac{1}{\sqrt{1 + (25 \cdot 10^6 / f_c)^2}}$$

$$1 + (25 \cdot 10^6 / f_c)^2 = 100$$

$$\frac{25 \cdot 10^6}{f_c} = \approx 9.95$$

$$f_c = \frac{25 \cdot 10^6}{9.95}$$

$$f_c = 2.51 \text{ MHz.}$$

$$f_c = \frac{1}{2\pi RC}, C = \frac{1}{2\pi f_c R}$$

$$C = \frac{1}{2\pi(10,000)(2.51 \cdot 10^6)}$$

$$= \frac{1}{1.57 \cdot 10^{11}}$$

$$C = 6.37 \cdot 10^{-12} \text{ F}$$

### 3. ADC and DAC

(a)  $\Delta V = \text{voltage}$

$$= \frac{2.55}{256} \quad \boxed{\Delta V \approx 0.01V}$$

(b)  $\Delta V = \frac{4.095}{4096}$

$$\boxed{\Delta V \approx 0.001V}$$

(c)  $\frac{12V}{0.001} = 12,000$

$$\log_2(12,000) \approx 13.55 \rightarrow 14 \text{ if rounded up.}$$

14 bits of precision

(d)  $5V = \text{voltage range}$

num of levels = 2048

$$\frac{5V}{2048} \approx 0.00244V$$

$$\frac{2.52V}{0.00244V} \approx 1032.79$$

Digital amplitude = 1033 counts.

Dac

$$(a) \text{ Sig Amp} = 0.0098V \cdot 256 = 2.5088V$$

[Signal Amplitude = 2.51 V]

$$(b) \text{ Signal Amp} = 0.505V \\ = 2.5V$$

[The signal Amplitude = 2.5V]

$$(c) \text{ max voltage} = \frac{0.250511}{128} \\ = \underline{127.75} \\ \underline{128} \\ \approx 0.997V$$

[The maximum voltage is 0.997V]

$$4. G = \frac{0.33}{3.3} = 0.1$$

$$c = \frac{1}{6.28 \cdot 10^{12}}$$

$$f_c = \sqrt{\left(\frac{f}{0.1}\right)^2 - f^2}$$

$$c = 159 \mu F$$

$$f_c = \sqrt{\left(\frac{10^7}{0.1}\right)^2 - (10^7)^2}$$

$$= \sqrt{10^{16} - 10^{14}}$$

$$\approx 10^8 \text{ Hz}$$

$$C = \frac{1}{2\pi \cdot 10^4 \cdot 10^8}$$