

Name: Almas Waseem

H.w#2

3.1 ADC and DAC

(a) ΔV for 8-bit ADC (0-2.55V, 255 levels): $\Delta V = 2.55 / 255 = 0.0100 \text{ V/level}$

(b) ΔV for 12-bit ADC (0-4.095V, 4095 levels): $\Delta V = 4.095 / 4095 = 0.001000 \text{ V/level}$

(c) Bits required for $\Delta V < 1\text{mV}$ in 0-12V: $12 / 0.001 = 12000 \text{ levels} \Rightarrow \text{ceil}(\log_2(12000)) = 14 \text{ bits}$

(d) Digital amplitude of 2.52V in 2048 levels over 0-5V: $\text{Value} = (2.52 / 5) * 2047 \approx 1032 \text{ counts}$

(e) DAC amplitude for 256 counts at 9.8mV/level: $256 * 0.0098 = 2.5088 \text{ V}$

(f) DAC amplitude for 2048 counts, 0-5V, 4095 max: $(2048 / 4095) * 5 = 2.5024 \text{ V}$

(g) Max voltage when output = 0.25V, 128 counts out of 511: $V_{\text{max}} = 0.25 * (511 / 128) = 1.00 \text{ V}$

3.2 Digital Signal Frequency

(a) $f_{\text{analog}} = 50\text{kHz}$: $f_{\text{digital}} = |50\text{k} - 0 * 500\text{k}| = 50,000 \text{ Hz}$

(b) $f_{\text{analog}} = 250\text{kHz}$: $f_{\text{digital}} = |250\text{k} - 1 * 500\text{k}| = 250,000 \text{ Hz}$

(c) $f_{\text{analog}} = 750\text{kHz}$: $f_{\text{digital}} = |750\text{k} - 2 * 500\text{k}| = 250,000 \text{ Hz}$

(d) $f_{\text{analog}} = 1000\text{kHz}$: $f_{\text{digital}} = |1000\text{k} - 2 * 500\text{k}| = 0 \text{ Hz}$

3.3 Low-Pass RC Filter

Given: $A_{\text{in}} = 3.3\text{V}$, $A_{\text{out}} = 0.33\text{V}$, $f = 25 \text{ MHz}$, $R = 10\text{k}\Omega$

Gain = $0.33 / 3.3 = 0.1$

$C = \sqrt{1/G^2 - 1} / (2\pi f R) \approx 6.33 \text{ pF}$

3.4 High-Pass RC Filter

Given: $A_{\text{in}} = 3.3\text{V}$, $A_{\text{out}} = 0.33\text{V}$, $f = 10 \text{ MHz}$, $R = 10\text{k}\Omega$

Gain = 0.1

$$C = (G / \sqrt{1 - G^2}) / (2\pi fR) \approx 0.16 \text{ pF}$$

3.5 Bonus: Phase Shift Introduced

Low-pass filter phase shift = -84.26°

High-pass filter phase shift = $+84.26^\circ$