

HW #2

we have

$$\begin{aligned} F(\omega) &= a \cos(\omega t_0) - a j \sin(\omega t_0) \\ &= a (\cos(\omega t_0) - j \sin(\omega t_0)) \\ &= a e^{j(-\omega t_0)} \\ [F(\omega) &= a e^{-j\omega t_0}] \end{aligned}$$

$$\begin{aligned} 1) |F(\omega)|^2 &= |a e^{-j\omega t_0}|^2 \\ &= a^2 |e^{-j\omega t_0}|^2 \\ &= a^2 \cdot 1 \\ |F(\omega)| &= a^2 \end{aligned}$$

2) we have, $F(\omega) = a e^{-j\omega t_0}$

Phase angle, $\boxed{\phi(\omega) = -\omega t_0}$

$$\begin{aligned} \text{Group delay, } -\frac{d\phi}{d\omega} &= -\left(\frac{d(-\omega t_0)}{d\omega} \right) \\ &= -(-1) t_0 \frac{d\omega}{d\omega} \\ &= \boxed{t_0} \end{aligned}$$