

1.

```
>> function y = square(frequency, duration, sampling_rate)
    t = 0:1/sampling_rate:duration-1/sampling_rate;
    y = sign(sin(2 * pi * frequency * t));
end
function y = triangle(frequency, duration, sampling_rate)
    t = 0:1/sampling_rate:duration-1/sampling_rate;
    y = 2 * abs(2 * (t * frequency - floor(t * frequency + 0.5))) - 1;
end
function y = gaussian_noise(mean_val, std_dev, num_samples)
    y = mean_val + std_dev * randn(1, num_samples);
end
>> |
```

```
>> ds = 1; % Duration
fs = 1000; % Sampling frequency
freq = 5; % Frequency
sq_wave = square(freq, ds, fs);
tri_wave = triangle(freq, ds, fs);
gauss_noise = gaussian_noise(ds, fs);

figure;
subplot(3,1,1);
histogram(sq_wave);
title(' Square Wave Histogram');

subplot(3,1,2);
histogram(tri_wave);
title(' Triangle Wave Histogram ');

subplot(3,1,3);
histogram(gauss_noise);
title(' Gaussian Noise Histogram');

>> N = length(sq_wave);

figure;
subplot(3,1,1);
histogram(sq_wave, 'Normalization', 'probability');
title('Normalized Histogram of Square Wave');
xlabel('Value'); ylabel('Frequency / N');

subplot(3,1,2);
histogram(tri_wave, 'Normalization', 'probability');
title('Normalized Histogram of Triangle Wave');
xlabel('Value'); ylabel('Frequency / N');

subplot(3,1,3);
histogram(gauss_noise, 'Normalization', 'probability');
title('Normalized Histogram of Gaussian Noise');
xlabel('Value'); ylabel('Frequency / N');
```

### Square

Mean = 0      Standard Deviation = 1

### Triangle

Mean = 0      Standard Deviation = 0.578

### Gauss Noise

Mean = 0      Standard Deviation = 1

Loren  
Grey

## Problem Set # 2

### 11. ADC

a)  $\Delta V = \frac{V_{max} - V_{min}}{N} = \frac{2.55 - 0}{255+1} \cdot 2.55 = 0.00996$  b)  $\Delta V = \frac{4.095 - 0}{4095+1} \cdot 4.095 = 0.0009998$

$\Delta V \approx 0.01 \text{ V}$  or  $10 \text{ mV}$   $\Delta V \approx 0.001 \text{ V}$  or  $1 \text{ mV}$

c)  $\Delta V < 1 \text{ mV}$   $[0, 12] \text{ V}$  d)  $2.52 \text{ V}$   $[0, 5] \text{ V}$  2048 levels

$\frac{\Delta V}{2^N} < 1 \text{ mV} \rightarrow 0.001 \text{ V} \cdot 2^N > \frac{12}{0.001} = 12000 < 2^N$   $\Delta V = \frac{5 \text{ V}}{2048} = 0.0024414$

$\frac{12 \text{ V}}{0.001 \text{ V}} < 0.001 \text{ V} \cdot 2^N$   $\log_2 12000 < N$  Count =  $\frac{2.52}{.0024414} = 1032.1946$

$12000 < 0.001 \text{ V} \cdot 2^N$   $= 13.56$   $.0024414$   $= [1032 \text{ counts}]$

$2^{14} = [16,384 \text{ levels}]$   $N \approx 14$

### DAC

a) 256 counts  $[0, 5] \text{ V}$   $\Delta V = 9.8 \text{ mV}$  b) 2048 counts  $[0, 5] \text{ V}$  max count = 4095

signal amp = count  $\cdot \Delta V$  signal amp =  $\frac{2048}{4095} \times 5 \text{ V}$

$= 256 \cdot 0.0098 \text{ V}$   $= 0.5 \times 5$

$= 2.5088 \text{ V}$   $\text{Sig Amp} = 2.5 \text{ V}$   $0 < 2.5 < 5$

Signal Amp  $\approx 2.51 \text{ V}$   $0 < 2.5 < 5$

c) 128 counts max count = 511  $0.25 \text{ V}$

$V_{max} = \frac{\text{analog} \times \text{max counts}}{\text{counts}} = \frac{0.25 \text{ V} \cdot 511}{128} = 0.997 \text{ V} \approx V_{max} \approx 1.0 \text{ V}$

2.

a)  $s_r = 500 \text{ kHz}$   $s_f = 50 \text{ kHz}$

Analog sig freq = Digital sig freq

digital sf =  $50 \text{ kHz}$

b)  $f_{Nyquist} = \frac{f_s}{2}$

$= \frac{500}{2} = 250 \text{ kHz} = f_{Nyquist}$

digital signal frequency =  $[0 \text{ Hz}]$

c)  $f_{dig} = f_a - f_s = 750 - 500$   
 $= [250 \text{ kHz}]$

d)  $f_a = f_{analog} - f_s N$   $N = \frac{f_{analog}}{f_s} = \frac{1000}{50} = 20$

$= 1000 - 2(500) = 1000 - 1000$   $= [0 \text{ Hz}]$

$$3. V_{in} = 3.3V \quad f = 25 \text{ MHz} \quad \omega = 2\pi \cdot 25 \times 10^6$$

$$\frac{(V_{out})^2}{(V_{in})^2} = \frac{1}{1 + (\omega RC)^2}$$

$$\frac{(3.3)^2}{(3.3)^2} = \frac{1}{1 + (\omega RC)^2} = \left(\frac{1}{10}\right)^2 = 0.01$$

$$(\omega RC)^2 = \frac{1}{0.01} - 1 = \sqrt{99}$$

$$C = \frac{\sqrt{99}}{2\pi \cdot 25 \times 10^6}$$

$$C = 6.334 \times 10^{-8}$$

$$\omega RC = \sqrt{99} \rightarrow \frac{RC}{R} = \frac{\sqrt{99}}{\omega} \cdot \frac{1}{R} \rightarrow C = \frac{\sqrt{99}}{\omega R}$$

$$4. V_{in} = 3.3V \quad f = 10 \text{ MHz} \quad R = 10k\Omega$$

$$\frac{V_{out}}{V_{in}} = \frac{0.33}{0.3} = 0.1 = \frac{(\omega RC)^2}{1 + (\omega RC)^2} \quad C = \frac{0.1}{\omega R} = \frac{0.1}{(2\pi \cdot 10 \times 10^6)(10,000)}$$

$$(\omega RC)^2 = 0.01(1 + (\omega RC))$$

$$(1 - 0.01)(\omega RC)^2 = 0.01$$

$$C = 1.59 \times 10^{-3} \text{ F}$$

$$\frac{0.99(\omega RC)^2}{0.99} = \frac{0.01}{0.99}$$

$$\sqrt{(\omega RC)^2} = \sqrt{0.0101}$$

$$\omega RC = 0.1$$

### 5. Bonus

$$a) \tan \theta = 1/(\omega RC)$$

$$\theta = \tan^{-1}(\omega RC)$$

$$\omega RC = 2\pi \cdot 25 \times 10^6$$

$$= \tan^{-1}(2\pi \cdot 25 \times 10^6)$$

$$\theta = -84.3^\circ \text{ or } -1.47 \text{ rad}$$

$$b) \theta = \tan^{-1}(\omega RC)$$

$$= \tan^{-1}(2\pi \cdot 10 \cdot 10^6)$$

$$\theta = 89.9^\circ \text{ or } 1.57 \text{ rad}$$