

# Warm-Up for April 8th, 2022

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## 1 Memory Bank

1. Lorentz Force ...  $\mathbf{F} = I\mathbf{L} \times \mathbf{B}$
2. Torque ...  $\boldsymbol{\tau} = \mathbf{r} \times \mathbf{F}$
3. Continuity Equation ...  $\nabla \cdot \mathbf{J} = -\frac{\partial \rho}{\partial t}$

## 2 Torque on a Current Loop, Current Density

1. Suppose there is a square loop of current in the  $xy$ -plane, with side length  $a$ , centered on the origin. There is a constant, uniform magnetic field  $\mathbf{B} = B\hat{\mathbf{x}}$ . Let  $\boldsymbol{\mu} = I\mathbf{A}$ , where  $\mathbf{A}$  is an area vector for the loop. Show that there is a torque on the loop, equal to  $\boldsymbol{\tau} = \boldsymbol{\mu} \times \mathbf{B}$ .

2. Suppose the outflow of charged particles from some exploding astrophysical event has spherical symmetry and decays exponentially:

$$\mathbf{J} = I_0 \left( \frac{e^{-\lambda t}}{r^2} \right) \hat{\mathbf{r}} \quad (1)$$

Using the continuity equation, show that the charge lost by the exploding object is

$$Q(t) \frac{4\pi I_0}{\lambda} (e^{-1} - 1) \quad (2)$$