

1. 1)

$$\vec{r} = r \hat{r}$$

$$\vec{r} = \vec{r} \times \vec{F} = \vec{r} \sin \theta \vec{F}$$

$$\vec{E} = \frac{\vec{F}}{q}$$

$$\vec{E} = \vec{r} \cdot E_0 \sin \theta$$

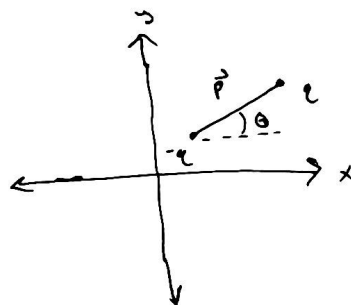
$$\vec{r} = \vec{r} \times \vec{E}$$

$$F_{+z} = E_0 \cdot r$$

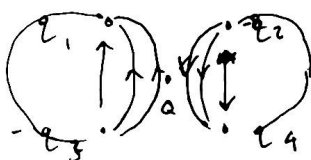
$$\vec{E} = \frac{\vec{F}}{q}$$

$$F_{-z} = E_0 \cdot r$$

$$\vec{F} = \vec{E} q$$



2. 1)



$$E = \frac{1}{4\pi\epsilon_0}$$

$$\begin{aligned} 2.1) a) \quad E_z &= \frac{1}{4\pi\epsilon_0} \int_0^L \frac{\lambda dx}{r^2} \cos \theta \\ &= \frac{1}{4\pi\epsilon_0} \lambda \int_0^L \frac{1}{(z^2 + x^2)^{3/2}} dx \\ &= \frac{1}{4\pi\epsilon_0} \frac{\lambda}{z} \frac{L}{\sqrt{z^2 + L^2}} \end{aligned}$$

$$\begin{aligned} E_x &= -\frac{1}{4\pi\epsilon_0} \int_0^L \frac{\lambda dx}{r^2} \sin \theta \\ &= -\frac{1}{4\pi\epsilon_0} \lambda \int_0^L \frac{x dx}{(x^2 + z^2)^{3/2}} \\ &= -\frac{1}{4\pi\epsilon_0} \lambda \left[\frac{1}{z} - \sqrt{z^2 + L^2} \right] \end{aligned}$$

$$E = \frac{1}{4\pi\epsilon_0} \frac{\lambda}{z} \left[\left(-1 + \frac{z}{\sqrt{z^2 + L^2}} \right) \hat{x} + \left(\frac{L}{\sqrt{z^2 + L^2}} \right) \hat{z} \right]$$

$$b) \quad \oint \vec{E} \cdot d\vec{A} = \frac{Q}{\epsilon_0}$$

$$E \oint dA = \frac{Q}{\epsilon_0}$$

$$E 4\pi r^2 = \frac{Q}{\epsilon_0}$$

$$E = \frac{Q}{\epsilon_0 4\pi r^2}$$

$$Q = \lambda dx$$

$$E_r = \int_0^L \frac{\lambda dx}{4\pi\epsilon_0 r^2}$$

leads to answer from

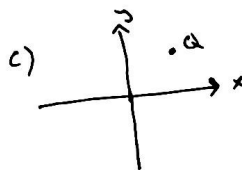
$$E = \frac{1}{4\pi\epsilon_0} \frac{\lambda}{z} \left[\left(-1 + \frac{z}{\sqrt{z^2 + L^2}} \right) \hat{x} + \left(\frac{L}{\sqrt{z^2 + L^2}} \right) \hat{z} \right]$$

2. 2

$$E = \frac{\sigma}{2\epsilon_0}$$

$$a) \quad E = \frac{\sigma_1 - \sigma_2}{\epsilon_0}$$

$$b) \quad E = \frac{\sigma_1 + \sigma_2}{2\epsilon_0}$$



$$E = \frac{\sigma_1 + \sigma_2}{2\epsilon_0} \hat{x} + \frac{\sigma_2 - \sigma_1}{2\epsilon_0} \hat{y}$$

$$3.1 \quad \oint \vec{E} \cdot d\vec{l} = 0 \quad E = -\nabla V \quad -\oint_A \vec{E} \cdot d\vec{l} = V(b) - V(a)$$

$$-\int_a^b -\nabla V \cdot d\vec{l} = \int_a^b V' dl = V(b) - V(a)$$

$$V(r) = -\int_{\infty}^r E(r') dr' \quad E = k \frac{q}{r^2} \hat{r}$$

$$V(r) = -\int_{\infty}^r \left(\frac{1}{4\pi\epsilon_0} \frac{q}{r'^2} \right) dr' = \frac{1}{4\pi\epsilon_0} \frac{q}{r} \Big|_{\infty}^r = k \frac{q}{r}$$