Warm-Up 14

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August 3, 2020

1 Formula Area

- 1. Normal distribution PDF: $p(x) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{1}{2}(x-\mu)^2/\sigma^2\right)$
- 2. The z-score of a particular event x drawn from a normal distribution is $z = (x \mu)/\sigma$.
- 3. Probabilities for a normal distribution: $p(-1\sigma < x < 1\sigma) = 0.68$, $p(-2\sigma < x < 2\sigma) = 0.95$, and $p(-3\sigma < x < 3\sigma) = 0.997$.
- 4. Notation for normal distribution: $X = N(\mu_x, \sigma_x)$, where μ_x and σ_x are the population mean and standard deviation, respectively.
- 5. Central Limit Theorem: Suppose you have a continous random variable X, with mean μ_x and standard deviation σ_x . Suppose you draw n values from its distribution (whatever that distribution is), and calculate the average, \bar{x} . If you repeat this process, the distribution of the averages \bar{x} will be $N(\mu_x, \sigma_x/\sqrt{n})$. That is, the mean of the distribution of averages will be the mean of X, and the standard deviation of the distribution of averages will be the standard deviation of X divided by \sqrt{n} .

2 Normal Distribution, Central Limit Theorem

- 1. The GPA of freshmen admitted to Whittier College is normally distributed, with $\mu = 3.0$ and $\sigma = 0.2$. If we encounter a student with a 4.0 GPA, how many standard deviations above the mean is their GPA?
 - A: 2
 - B: 3
 - C: 4
 - D: 5
- 2. The GPA of freshmen admitted to Rio Hondo Community College is normally distributed, like N(2.7, 0.5). What GPA is two standard deviations above the mean?
 - A: 3.1
 - B: 3.5
 - C: 3.7
 - D: 4.0
- 3. Suppose we draw 100 randomly selected Whittier College students, and calculate their average GPA. We repeat this process 10 times, to get a distribution of averages. We do not assume that the GPA distribution for *all students* is normal. However, we do know the mean is 3.0 and the standard deviation is 0.2. So we have 10 averages, measured from 100 students each. What is the mean of these 10 averages, and what is the standard deviation of these 10 averages? (Consult the central limit theorem above).