

## Number Systems in pre-Columbian Context

### 2 Intro to Digits and Bases

1. D: All of the above

2. B: 10 digits

3. A: 8 digits

4.  $255 = 2 \times 10^2 + 5 \times 10^1 + 5 \times 10^0$

### 3 Base-2, or Binary

1.  $\begin{matrix} 2^3 & 2^2 & 2^1 & 2^0 \\ 1 & 0 & 0 & 0 \end{matrix}_2 = 1 \times 2^3 = \boxed{8_{10}}$

$1001_2 = 1 \times 2^3 + 1 = \boxed{9_{10}}$

$1101_2 = 1 \times 2^3 + 1 \times 2^2 + 1 = \boxed{13_{10}}$

$1111_2 = 2^3 + 2^2 + 2^1 + 1 = \boxed{15_{10}}$

2.  $32_{10} = 1 \times 2^5 \rightarrow \boxed{100000_2}$

$42_{10} = 1 \times 2^5 = 32$

$0 \times 2^4$

$1 \times 2^3 = 8$

$0 \times 2^2$

$1 \times 2^1$

$0 \times 2^0$

$\rightarrow \boxed{101010_2}$

$$11_{10} = \begin{array}{l} 1 \times 2^3 = 8 \\ 0 \times 2^2 \\ 1 \times 2^1 = 2 \\ 1 \times 2^0 = 1 \end{array} \rightarrow \boxed{1011_2}$$

$$17_{10} = \begin{array}{l} 1 \times 2^4 = 16 \\ 0 \times 2^3 \\ 0 \times 2^2 \\ 0 \times 2^1 \\ 1 \times 2^0 = 1 \end{array} \rightarrow \boxed{10001_2}$$

#### 4 Base-16, or Hexadecimals

1.  $B:C = 12_{10}$

2.  $255/16 = 15$ , remainder 15  $\xrightarrow{\text{LSB}}$   $\boxed{FF_{16}}$   
 $15/16 = 0$ , remainder 15  $\xrightarrow{\text{MSB}}$

$F = 15_{10}$  in hex

#### 5 Base-20 Systems

1. a)  $20^2 = 400_{10} \rightarrow \overset{b)}{100}_{20}$   
 $20^1 = 20_{10} \rightarrow 10_{20}$   
 $20^0 = 1_{10} \rightarrow 1_{20}$

c)  $401_{10} = 1 \times 20^2$   
 $0 \times 20^1$   
 $1 \times 20^0$   
 $= \boxed{101_{20}}$

$$2. \quad 25_{10} = \frac{1 \times 20^1}{5 \times 20^0} \rightarrow \boxed{15_{20}}$$

$$45 = \frac{2 \times 20^1}{5 \times 20^0} \rightarrow \boxed{25_{20}}$$

$$425 = \frac{1 \times 20^2}{1 \times 20^1}{5 \times 20^0} \rightarrow \boxed{115_{20}}$$

$$625 = \frac{1 \times 20^2 = 400}{11 \times 20^1 = 220}{5 \times 20^0 = 5} \rightarrow \boxed{1B5_{20}}$$

$$B = 11_{10}$$

$$3. \quad 25 = \begin{array}{|c|} \hline \text{—} \\ \hline \cdot \\ \hline \text{⊕} \\ \hline \end{array} \begin{array}{l} 20^0 \\ 20^1 \\ 20^2 \end{array}$$

$$45 = \begin{array}{|c|} \hline \text{—} \\ \hline \cdot \cdot \\ \hline \text{⊕} \\ \hline \end{array} \begin{array}{l} 20^0 \\ 20^1 \\ 20^2 \end{array}$$

$$425 = \begin{array}{|c|} \hline \text{—} \\ \hline \cdot \\ \hline \cdot \\ \hline \end{array} \begin{array}{l} 20^0 \\ 20^1 \\ 20^2 \end{array}$$

$$625 = \begin{array}{|c|} \hline \text{—} \\ \hline \cdot \\ \hline \cdot \\ \hline \end{array} \begin{array}{l} 20^0 \\ 20^1 \\ 20^2 \end{array}$$