

# Study Guide for Midterm 1

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September 21, 2017

## 1 Types of Problems on the Midterm

- There are three problems on estimation, approximation, and unit analysis. One of these involves kinematics, and another is multiple choice.
- There are two problems on kinematics with constant acceleration.
- There is one four-part problem on vectors.

## 2 Estimation, Approximation, and Unit Analysis

Remember our three techniques for establishing estimates:

- Choose the right *scale*. For example, don't work in meters if the distances are between planets. Work in *AU* or light-minutes.
- Obtain complex quantities from simpler ones. For example, estimate lengths first, and then multiply them to estimate volumes and areas.
- Constrain the unknown with upper and lower limits. For example, the height of a child should not be 10 meters, or 0.1 meters.

## 3 Displacement, Velocity, and Constant Acceleration Vectors

The definition of average velocity is

$$\bar{v} = \frac{x_f - x_i}{t_f - t_i} = \frac{\Delta x}{\Delta t} \quad (1)$$

If the velocity is constant, the average velocity and the instantaneous velocity are the same. The numerator of Eq. 1 is in general a vector called *the displacement*:  $\Delta \vec{x}$ , describing the change in position of something. If the velocity is constant, then

$$\Delta \vec{x} = \vec{v} \Delta t \quad (2)$$

If the velocity is not constant, but the acceleration is constant, we have a system of equations relating displacement, time, velocity, and acceleration:

$$x(t) = x_0 + v_0 t + \frac{1}{2} a t^2 \quad (3)$$

$$v(t) = v_0 + a t \quad (4)$$

$$a(t) = a \quad (5)$$

$$v^2 = v_0^2 + 2a\Delta x \quad (6)$$

## 4 Vectors

- Practice adding and subtracting vectors.
  1. Graphically
  2. As lists of numbers
- Practice breaking vectors into components:  $\hat{x} \cdot \vec{v} = v \cos \theta$ ,  $\hat{y} \cdot \vec{v} = v \sin \theta$  (if  $\theta$  goes from x-axis to vector).
- Practice taking the magnitude of a vector:  $\sqrt{\vec{v} \cdot \vec{v}}$ , or Pythagorean theorem.