

# RF Field Engineer Course: A Practical Introduction

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# Course Introduction

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4. Zoom Credentials: (ID) 796 092 0745 (Passcode) 667725
5. **Reading: Stimson's Introduction to Airborne Radar, 3rd Edition.** (Hughes Radar Handbook)
6. Box Folder: <https://app.box.com/s/qalsptcztyeq8hjvu3pmf4mlodmopop7>

## Summary

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## Reading: *Stimson3 ch. 1-6*

- **Week 1:** Units and estimation. **Key skills:** mental math, wave concepts
  - Electromagnetic units, estimation, and decibels
  - Waves and the wave equation
  - Reflections, refraction, and diffraction
  - Phase, amplitude, frequency, polarization
- **Week 2:** Basic Training in Mathematics. **Key skills:** estimate pulse bandwidth, pulse trains and uncertainty principle
  - **Complex numbers:** applications to phasors and radio waves, complex impedance of filters and antennas
  - **Fourier series and transforms,** filters and attenuation, properties of waveforms, power spectra, and spectrograms, cross-correlation and convolution
  - **Statistics and probability:** applications to noise, signal-to-noise ratio

## Reading: *Stimson3 ch. 7-11*

- **Week 3:** RF Antenna Properties. **Key skills:** characterize an antenna, diagnose a problem with an antenna system
  - Radiation pattern, directivity, and gain
  - Complex impedance and reflection coefficient,  $S_{11}$ ,  $S_{21}$
  - Bandwidth, narrow and wide
  - Antenna temperature
  - Angular resolution
  - Attenuation: applications to remote sensing
- **Week 4: Electronically Scanned Antenna Systems**
  - **Basics:** spacing, wavelength, and scan angle
  - **Design classes:** AESA and PESA
  - **Wideband considerations:** Scan losses, time-delays
  - **Bonus:** FDTD demonstrations of ESAs
- **Week 5:** Review of Weeks 1-4, pulsed radar concepts

## Reading: *Stimson3 ch. 12-13, part IV (18-22), 23*

- **Week 6:** Range Equations. **Key skills:** diagnose issues with distance target detection, estimate radar cross section (RCS)
  - Radar cross-section
  - Noise and noise figure, signal-to-noise ratio (SNR)
  - Thermal noise floor and detection probability
  - **Ranging techniques:** pulse compression, frequency modulation
- **Week 7: Overview of Pulse Doppler Radar (Cumulative Example)**
  - Connections with Telemetry
  - See *Stimson3* part IV
  - Connections to digital signal processing: sampling and digitization
- **Week 8:** Clutter and Attenuation
  - Clutter: sources and spectra
  - Attenuation: absorption and scattering, components

# Course Summary

- Week 9: Link Budgets (Cumulative Example)
  - Assembling the pieces
  - Example calculations
- Week 10: Course Review
  - Review Weeks 1-9
  - Skill Review
    1. Estimation and approximations
    2. Conceptual challenge questions
    3. Worked examples

## Estimation, Approximation, Units

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# Estimation, Approximation, Units

RF radiation travels at a constant speed.

$$\frac{c}{n} = \nu \lambda \quad (1)$$

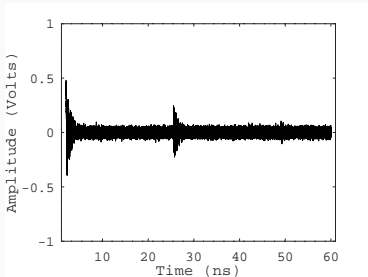
$$\Delta x = \left( \frac{c}{n} \right) \Delta t \quad (2)$$

$$T = \frac{1}{\nu} \quad (3)$$

- **c**: speed of light in vacuum, 0.299792458 m/ns,  $\approx 0.3$  m GHz
- $\nu$ : frequency of the radiation, Hz.
- $\lambda$ : wavelength of the radiation, meters.
- $\Delta x$ : displacement
- $\Delta t$ : time duration

# Estimation, Approximation, Units

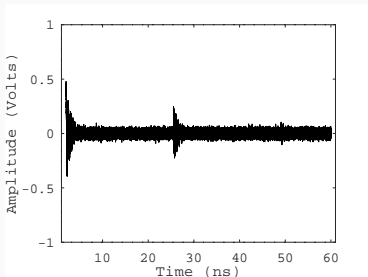
*A signal enters a cable that is 3 meters long and reflects at the end back towards the source. How many nanoseconds after the signal enters the cable will the signal return to the end?*



- How does it work conceptually? Distance equals speed multiplied by time duration.
- How do you correct for the speed in the cable?
- How could we apply this to radar? Remember, this is a *reflection*.

# Estimation, Approximation, Units

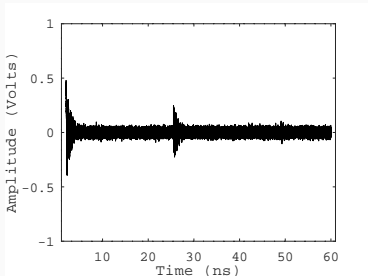
*A signal enters a cable that is 3 meters long and reflects at the end back towards the source. How many nanoseconds after the signal enters the cable will the signal return to the end?*



- $20 \text{ ns} \times 0.3 \text{ (m/ns)} \approx 6 \text{ m}$ .  
Why 6 meters?
- How do you correct for the speed in the cable?
- How could we apply this to radar? Remember, this is a *reflection*.

# Estimation, Approximation, Units

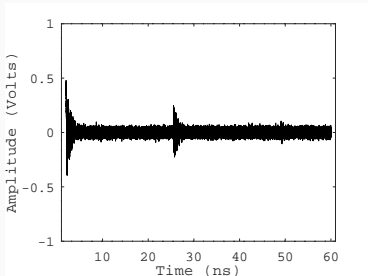
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- $20 \text{ ns} \times 0.3 \text{ (m/ns)} \approx 6 \text{ m}$ .  
Why 6 meters?
- Typical speed in RF cable:  
85% speed of light. What  
is  $\Delta t$  for 6 meters at  
reduced speed?
- How could we apply this to  
radar? Remember, this is a  
*reflection*.

# Estimation, Approximation, Units

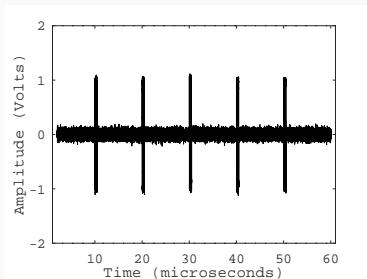
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Why 6 meters?
- Typical speed in RF cable:  
85% speed of light. What  
is  $\Delta t$  for 6 meters at  
reduced speed?
- If a radar echo returns 30  
microseconds later, how  
far away is the reflector?

# Estimation, Approximation, Units

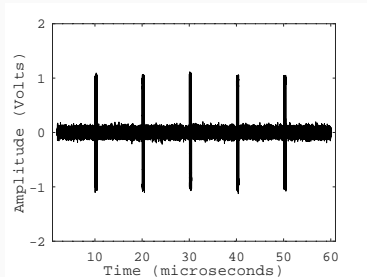
What does this mean? *A radar system creates a 20 MHz sine wave modulated by a 5 percent duty-cycle. The pulse repetition frequency is 0.1 MHz.*



- What's the period of a 20 MHz sine wave? Which part of the waveform at left represents this oscillation?
- If a signal is repeated regularly, it has a PRF, or pulse repetition frequency. Work out the PRF of the waveform at left.
- What does duty cycle mean?

# Estimation, Approximation, Units

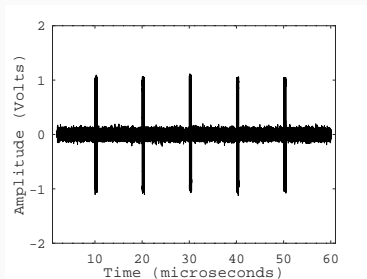
What does this mean? *A radar system creates a 20 MHz sine wave modulated by a 5 percent duty-cycle. The pulse repetition frequency is 0.1 MHz.*



- $1/20.0 \text{ MHz}^{-1} = 0.05 \mu\text{s} = 50 \text{ ns}$ . These oscillations are within the pulses.
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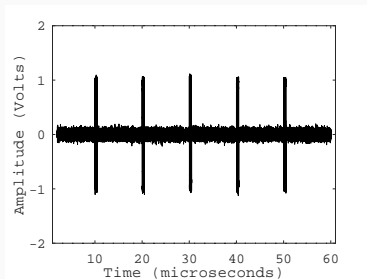


- $1/20.0 \text{ MHz}^{-1} = 0.05 \mu\text{s} = 50 \text{ ns}$ . These oscillations are within the pulses.
- It appears the pulses are separated by  $\approx 10 \mu\text{s}$ . Invert to find  $1/10 \text{ MHz}$ .
- What does duty cycle mean?



# Estimation, Approximation, Units

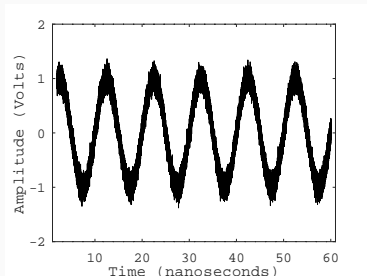
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- $1/20.0 \text{ MHz}^{-1} = 0.05 \mu\text{s} = 50 \text{ ns}$ . These oscillations are within the pulses.
- It appears the pulses are separated by  $\approx 10 \mu\text{s}$ . Invert to find  $1/10 \text{ MHz}$ .
- 100 percent corresponds a constant 20 MHz sine tone. Fifty percent is half-on, half-off ...  $D = PW/T \times 100$ .

# Estimation, Approximation, Units

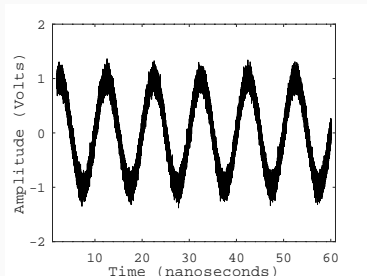
*What is the wavelength of the received radio wave in the figure? Recall  $c \approx 0.3 \text{ m/ns}$ .*



- What is the period? Pay attention to the units on the axes.
- What is the frequency? (How do you convert period to frequency?)
- What is the wavelength?
- What size antenna would receive this signal?

# Estimation, Approximation, Units

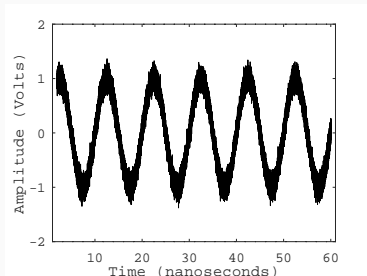
*What is the wavelength of the received radio wave in the figure? Recall  $c \approx 0.3 \text{ m/ns}$ .*



- The period appears to be about 10.0 ns.
- What is the frequency? (How do you convert period to frequency?)
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# Estimation, Approximation, Units

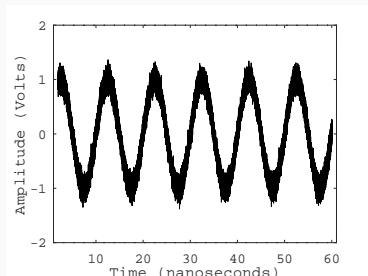
*What is the wavelength of the received radio wave in the figure? Recall  $c \approx 0.3 \text{ m/ns}$ .*



- The period appears to be about 10.0 ns.
- Invert the period:  
 $1/10 \text{ ns}^{-1} = 100 \text{ MHz}$ .
- What is the wavelength?
- What size antenna would receive this signal?

# Estimation, Approximation, Units

*What is the wavelength of the received radio wave in the figure? Recall  $c \approx 0.3 \text{ m/ns}$ .*



- The period appears to be about 10.0 ns.
- Invert the period:  
 $1/10 \text{ ns}^{-1} = 100 \text{ MHz}$ .
- What is the wavelength of a 100 MHz signal?

$$0.3 \text{ m GHz} = 100 \text{ MHz}(\lambda) \quad (4)$$

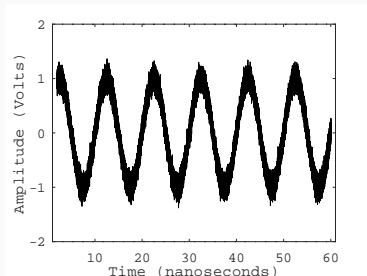
$$\frac{0.3 \text{ m GHz}}{100 \text{ MHz}} = \lambda \quad (5)$$

$$\lambda = 3 \text{ m} \quad (6)$$

- What size antenna?

# Estimation, Approximation, Units

*What is the wavelength of the received radio wave in the figure? Recall  $c \approx 0.3 \text{ m/ns}$ .*



- The period appears to be about 10.0 ns.
- Invert the period:  
 $1/10 \text{ ns}^{-1} = 100 \text{ MHz}$ .
- What is the wavelength of a 100 MHz signal?

$$0.3 \text{ m GHz} = 100 \text{ MHz}(\lambda) \quad (7)$$

$$\frac{0.3 \text{ m GHz}}{100 \text{ MHz}} = \lambda \quad (8)$$

$$\lambda = 3 \text{ m} \quad (9)$$

- About 1.5 meter dipole.

# Decibels

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# Decibels

RF parameters have a large dynamic range, and it becomes necessary to use logarithmic definitions.

$$P_{\text{dB}} = 10 \log_{10} \left( \frac{P_2}{P_1} \right) \quad (10)$$

$$\frac{P_2}{P_1} = 10^{P_{\text{dB}}/10} \quad (11)$$

- $P_{\text{dB}}$ : power ratio in decibels.
- $P_1$ : input power, transmitted power.
- $P_2$ : output power, received power.

Historical motivations for the decibel:

- $V(x) = V_i \exp(-x/\lambda)$ ,  $\lambda$  is attenuation factor, such that if  $x = \lambda$  for telephone cable,  $P_{\text{dB}} \approx -1$ .



# Decibels

RF parameters have a large dynamic range, and it becomes necessary to use logarithmic definitions.

$$P_{\text{dB}} = 10 \log_{10} \left( \frac{P_2}{P_1} \right) \quad (12)$$

$$\frac{P_2}{P_1} = 10^{P_{\text{dB}}/10} \quad (13)$$

- $P_{\text{dB}}$ : power ratio in decibels.
- $P_1$ : input power, transmitted power.
- $P_2$ : output power, received power.

## Historical motivations for the decibel:

- Let  $P_1$  and  $P_2$  be the initial and final acoustic power.  
 $P_{\text{dB}} \approx -1$  represents smallest change we can hear.

# Estimation, Approximation, Units

*If our transmit power is 1 W, and our return (echo) is only 2.5 mW, what is that in decibels?*

$$P_{\text{dB}} = 10 \log_{10} \left( \frac{P_2}{P_1} \right) \quad (14)$$

$$\frac{P_2}{P_1} = 10^{P_{\text{dB}}/10} \quad (15)$$

1. Which is  $P_2$  and which is  $P_1$ ?  
What's the ratio?
2. Perform logarithm on power of 10 and decimal separately.
3. Memorize the basics.

# Estimation, Approximation, Units

*If our transmit power is 1 W, and our return (echo) is only 2.5 mW, what is that in decibels?*

$$P_{\text{dB}} = 10 \log_{10} \left( \frac{P_2}{P_1} \right) \quad (16)$$

$$\frac{P_2}{P_1} = 10^{P_{\text{dB}}/10} \quad (17)$$

1. Transmit power ( $P_1$ ) is 1 W, and receive power ( $P_2$ ) is 2.5 mW, so  $P_2/P_1 = 2.5 \text{ mW W}^{-1} = 2.5 \times 10^{-3}$
2. Perform logarithm on power of 10 and decimal separately.
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# Estimation, Approximation, Units

*If our transmit power is 1 W, and our return (echo) is only 2.5 mW, what is that in decibels?*

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2. Take the  $\log_{10}$  of the number and multiply by 10:  
 $10 \log_{10}(2.5) + 10 \log_{10}(10^{-3}) = -30 + 10 \log_{10}(2.5).$
3. Memorize the basics.

# Estimation, Approximation, Units

*If our transmit power is 1 W, and our return (echo) is only 2.5 mW, what is that in decibels?*

$P_{\text{dB}}$	$P_2/P_1$
0	1
1	1.26
2	1.6
3	2
4	2.5
5	3.2
6	4
7	5
8	6.3
9	8

1. Transmit power ( $P_1$ ) is 1 W, and receive power ( $P_2$ ) is 2.5 mW, so  $P_2/P_1 = 2.5 \text{ mW W}^{-1} = 2.5 \times 10^{-3}$
2. Take the  $\log_{10}$  of the number and multiply by 10:  
 $10 \log_{10}(2.5) + 10 \log_{10}(10^{-3}) = -30 + 10 \log_{10}(2.5).$
3. So we know it's about  $-30$  dB. What is  $10 \log_{10}(2.5)$ ? About  $+4$ , so  $-30 + 4 = -26$  dB.

# Graphical Analysis and Radar Echoes

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# Graphical Analysis

*As an example, let's consider a radar echo, on a graph of signal frequency versus time.*

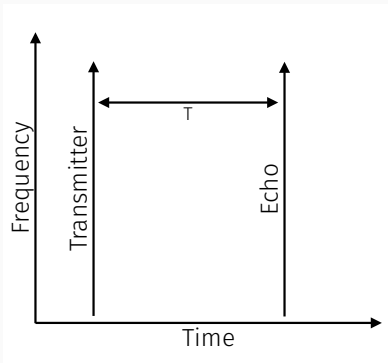


Figure 1

1. What does it mean to have a signal *at all frequencies* at a single time, for the transmitter?
2. What determines the echo time,  $T$ ?
3. How will the graph change if the radar target moves closer to the transmitter?

# Graphical Analysis

*As an example, let's consider a radar echo, on a graph of signal frequency versus time.*

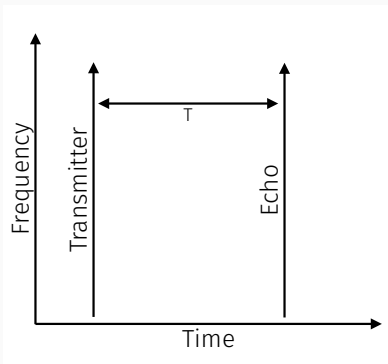


Figure 2

1. A *pulse* is a short time-duration signal. Pulses can be conceptualized as many signals of different frequencies added together with the right phases.
2. What determines the echo time,  $T$ ?
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# Graphical Analysis

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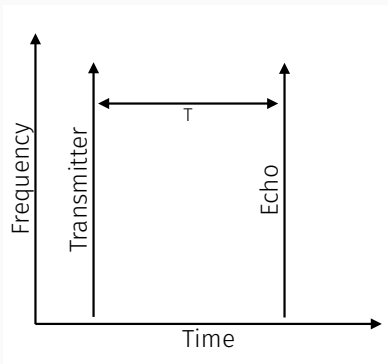


Figure 3

1. A *pulse* is a short time-duration signal. Pulses can be conceptualized as many signals of different frequencies added together with the right phases.
2.  $T = R/c$ , the range divided by the speed of light.
3. How will the graph change if the radar target moves closer to the transmitter?

# Graphical Analysis

*As an example, let's consider a radar echo, on a graph of signal frequency versus time.*

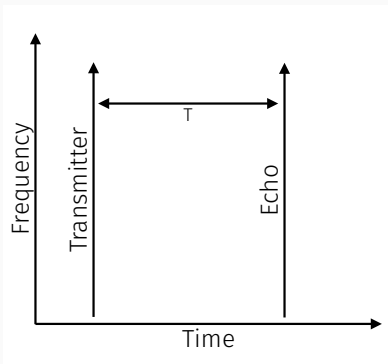


Figure 4

1. A *pulse* is a short time-duration signal. Pulses can be conceptualized as many signals of different frequencies added together with the right phases.
2.  $T = R/c$ , the range divided by the speed of light.
3.  $T = R/c$ , so if  $R$  decreases,  $T$  will decrease and thus the echo line will move left.

# Graphical Analysis

*Now a little more complex, we consider FM ranging. Imagine the transmitter chirps, and the echo returns.*

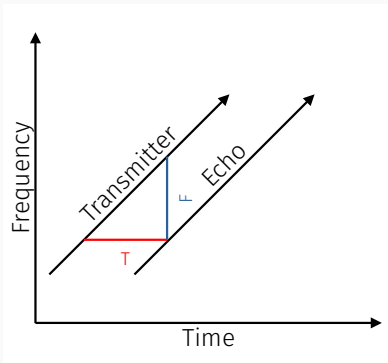


Figure 5

1. What does it mean to chirp? What is the chirp rate, and what are the units of chirp rate?
2. How are  $T$  and  $F$ , the time difference and frequency difference of the transmitter and echo, connected to range?
3. How can we derive the range without explicitly measuring  $T$ ?

# Graphical Analysis

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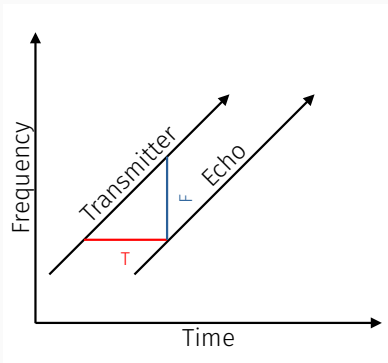


Figure 6

1. A chirp is a signal for which the frequency changes with time. The linear chirp rate is the slope of the transmitter signal, with units of  $1 \text{ Hz s}^{-1}$ .
2. How are  $T$  and  $F$ , the time difference and frequency difference of the transmitter and echo, connected to range?
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# Graphical Analysis

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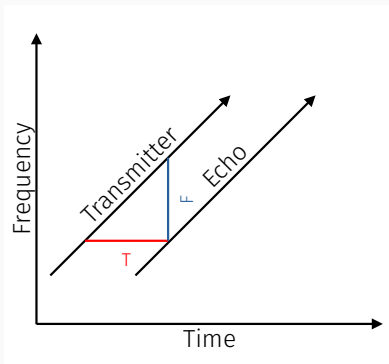


Figure 7

1. A chirp is a signal for which the frequency changes with time. The linear chirp rate is the slope of the transmitter signal, with units of  $1 \text{ Hz s}^{-1}$ .
2.  $R = (c/2)T$ . Show that  $F = kT$ .
3. How can we derive the range without explicitly measuring  $T$ ?

# Graphical Analysis

*Now a little more complex, we consider FM ranging. Imagine the transmitter chirps, and the echo returns.*

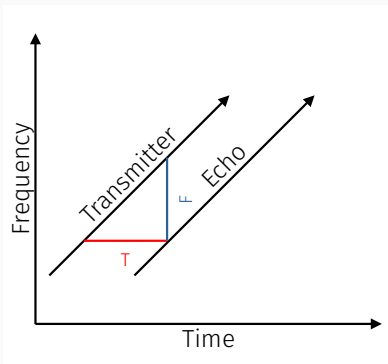


Figure 8

1. A chirp is a signal for which the frequency changes with time. The linear chirp rate is the slope of the transmitter signal, with units of  $1 \text{ Hz s}^{-1}$ .
2.  $R = (c/2)T$ . Show that  $F = kT$ .
3. This means:  $R = (c/2)(F/k)$ , so the range can be found *without* measuring  $T$ . Build a chirping system that measures  $F$ .

# Graphical Analysis

*Finally, the doppler shift of RF waves is a small effect introduced by relative target-source motion that changes the frequency.*

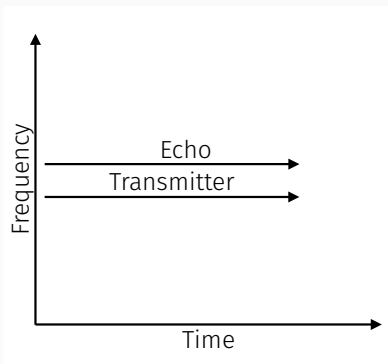


Figure 9

1. What is significance the ratio of frequencies?
2. What is the relationship between transmitter and echo frequencies?
3. What is a practical limitation of this technique?

# Graphical Analysis

*Finally, the doppler shift of RF waves is a small effect introduced by relative target-source motion that changes the frequency.*

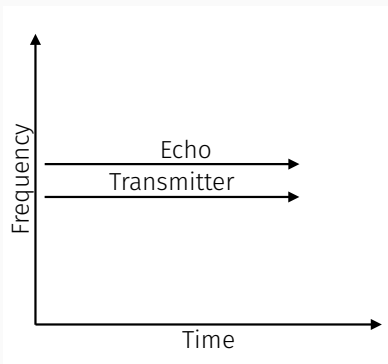


Figure 10

1. If  $f_e > f_t$ , the target is approaching the transmitter.  
If  $f_e < f_t$ , the target is moving away from the transmitter.
2. What is the relationship between transmitter and echo frequencies?
3. What is a practical limitation of this technique?



# Graphical Analysis

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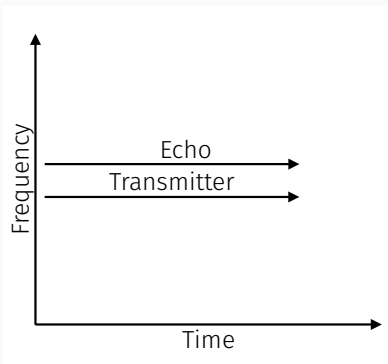


Figure 11

1. If  $f_e > f_t$ , the target is approaching the transmitter.  
If  $f_e < f_t$ , the target is moving away from the transmitter.
2.  $\Delta f \approx 2(\Delta v/c)f_t$ , with  $\Delta v$  equal to the relative velocity.
3. What is a practical limitation of this technique?

# Graphical Analysis

*Finally, the doppler shift of RF waves is a small effect introduced by relative target-source motion that changes the frequency.*

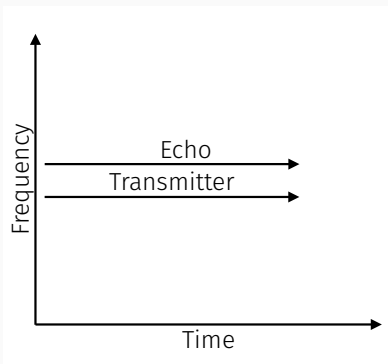


Figure 12

1. If  $f_e > f_t$ , the target is approaching the transmitter. If  $f_e < f_t$ , the target is moving away from the transmitter.
2.  $\Delta f \approx 2(\Delta v/c)f_t$ , with  $\Delta v$  equal to the relative velocity, and  $\Delta f = f_e - f_t$ .
3. For Earth-bound, anthropogenic targets,  $\Delta v/c \ll 1$ , so frequency shifts are very small.

*Finally, the doppler shift of RF waves is a small effect introduced by relative target-source motion that changes the frequency.*

$$\Delta f = 2(\Delta v/c)f_t \quad (20)$$

1. If the relative velocity, or range rate, of the target is  $400 \text{ km h}^{-1}$ , and  $f_t = 400 \text{ MHz}$ , what is  $f_e$ ?
2. How would we observe this shift? (Think about a *beat frequency*).

## Conclusion

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# Summary

Introductory concepts:

- Units, estimation, approximation
- Decibels
- Graphical analysis, range, and doppler shift

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5. **Reading: Stimson's Introduction to Airborne Radar, 3rd Edition.** (Hughes Radar Handbook)
6. **Box Folder:** <https://app.box.com/s/qalsptcztyeq8hjvu3pmf4mlodmopop7>