

2023/03/23

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### Mountain Sort

Let recorder = dict # to store and search found index in O(1)

Let counter = 0 # to record if all elements are found

Let result = []

While counter < array.length

    Let left = queue, l=0

    Let right = heap, r=0

    Let result = []

    For i = 0 to array.length # scan array → ←

        If dict[i] ≠ l and array[i] > l

            left.append(array[i])

            l = array[i], counter += 1, dict[i] = l

        If dict[array.length-i-1] ≠ r and array[array.length-i-1] > r

            right.push(array[array.length-i-1])

            r = array[array.length-i-1], counter += 1, dict[i] = r

    result = merge(result, left, right)

return result

Time complexity: Best O(n), AVG O(n<sup>2</sup>), Worst O(n<sup>2</sup>)

Space complexity: O(n)

First we scan the array from left to right, and from right to left (O(n)) to get two strictly increasing lists, then we use O(n) time to merge three list (result, left, and right), repeat these steps until all element are sorted.

array = [5, 1, 7, 3, 2, 6, 8, 4]

strictly increasing

(from right to left)

Step 1:  $\text{left} = [5, 7, 8]$ ,  $\text{right} = [4, 6]$

→ result = [ 4, 5, 6, 7, 8 ]

Step 2:  $\text{left} = [1, 3]$  ,  $\text{right} = [2]$

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→ result = [1, 2, 3, 4, 5, 6, 7, 8]
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# The worst case

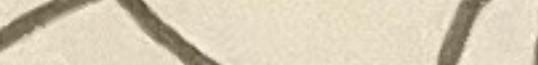
if the input array is like M, then we can find

$$T(n) = T(n-2) + n$$

$$= T(n-4) + n + n = T(n-6) + n + n + n = \dots$$

$$= \frac{1}{2}n \cdot n = O(n^2)$$

# The best case

If the input array is like  ,  , or  (like a mountain), then we can find all elements at 1 scan

$$T(n) = n + n = 2n = O(n)$$

