

IMPERIAL COLLEGE LONDON

DEPARTMENT OF COMPUTING

Symbolic Reinforcement Learning using Inductive Logic Programming

Author:
Kiyohito Kunii

Supervisor:
Prof. Alessandra Russo
Mark Law
Ruben Vereecken

Submitted in partial fulfillment of the requirements for the MSc degree in MSc in
Computing Science of Imperial College London

September 2018

Abstract

Reinforcement Learning (RL) has been applied and proven to be successful in many domains. However, most of current RL methods face limitations, namely, low learning efficiency, lack of abstract reasoning, and inability of transfer learning to a similar environment. In order to tackle these shortcomings, we introduce a new approach called ILP(RL), which applies Answer Set Programming (ASP), a declarative logic programming suitable for complex search problems, and Inductive Learning of Answer Set Programs (ILASP), a learning framework of non-monotonic Inductive Logic Programming (ILP). ILP is another field of machine learning that is based on logic programming, and recent advance on ILP research have shown promising potentials in many applications. ILP(RL) learns a general concept of a valid move in an environment, called a hypothesis, using ILASP, and generates a plan for a sequence of actions to the destination using ASP. The learnt hypotheses is highly expressive and transferrable to a similar environment. While there are a number of past papers that attempt to incorporate symbolic representation to RL problems in order to achieve efficient learning, there has not been any attempt of applying ILP into a RL problem. We examined ILP(RL) in various simple maze environments, and show that ILP(RL) learns faster than existing RL methods. We also show that transfer learning of the learnt hypothesis successfully improves learning on a new but similar environment. This proof of concept approach shows potentials for this new way of learning using ILP. Although the experiments were conducted in a simple environment, the results of the experiments show promising, and there is an avenue for potential improvement.

Acknowledgments

I would like to thank Prof. Alessandra Russo for accepting to supervise my project, her enthusiasm for my work and invaluable guidance throughout.

I would also like to thank Mark Law for his expertise on inductive logic programming and answer set programming, and fruitful discussions, and Ruben Verreken for his expertise on reinforcement learning and for providing me with advice and assistance for technical implementation.

Contents

List of Figures and Tables

Chapter 1

Introduction

1.1 Motivation

Reinforcement learning (RL) is a subfield of machine learning concerned with scenarios where an agent learns how to behave in an environment by interacting with the environment in order to maximise the total rewards it receives. The strength of RL is that it can be applied to many different domains where it is unknown to an agent how to perform a task. RL has been proven to work well in a number of complex environments, such as dynamic, real environments given sufficient learning time. Especially together with deep learning (DL), there have been many successful applications of RL in a number of domains, such as video games [?], the game of Go [?] and robotics [?].

Despite of these successful applications of RL, however, there are still a number of issues to overcome. First, most of RL algorithms requires large number of trial-and-error interactions with long time of training, which is also computationally expensive. Second, most of RL algorithms have no thought process to the decision making, and do not make use of high-level abstract reasoning, such as understanding symbolic representations or causal reasoning. Third, the transfer learning (TL), where the experience that an agent gained to perform one task can be applied in a different task, is limited and the agent performs poorly even on a new but similar task.

In order to overcome these limitations of existing RL methods, we introduce a new RL approach by applying Inductive Logic Programming (ILP). ILP is another subfield of machine learning based on logic programming and derives a hypothesis in the form of logic program that, together with background knowledge, entails all of positive examples and none of the negative examples. ILP has several advantages compared to RL. First, unlike most of statistical machine learning methods, ILP requires a small number of training data due to the presence of language bias which defines what the logic program can learn. Second, the learnt hypothesis by ILP is expressed with a symbolic representation and therefore is easy to interpret for human users. Third, since the learnt hypothesis is a abstract and general concept, it can be easily applied to a different learning task. Transfer learning is therefore possible. The disadvantages of ILP system are that the examples, or training data, have to be clearly defined and, unlike statistical machine learning, ambiguous dataset, such as images,

cannot be used for learning. Another disadvantage is that ILP suffers from learning scalability. The search space for a hypothesis defined by the language bias increases with respect to the complexity for learning tasks and slows down learning process. Despite these shortcomings, however, there has been a number of advance in ILP, especially ILP frameworks based on Answer Set Programming (ASP), a declarative logic programming which defines semantics based on Herbrand models (Gelfond and Lifschitz 1988). Due to the progress on both RL and ILP, we developed an new RL approach by incorporating a new ASP-based ILP framework called Learning from Answer Set (ILASP), which learns a valid move of an environment, and uses the learnt hypothesis and background knowledge to generate a sequence of actions in the environment.

In recent RL research, there is a number of research of introducing symbolic representation into RL in order to achieve more data-efficient learning as well as transparent learning. One of the methods is to incorporate symbolic representations into the system [?]. This approach is promising and shows a potential. However, none of the papers attempt to apply inductive learnig in RL senarios. but the combining of ILP and RL has not been explored. In addition, most of the ILP frameworks are also tested in senarios where the environment is known to the agent in advance.

Since the recent ILP frameworks enable us to learn a complex hypothesis in a more realistic environments, Finally, the recent advance of Inductive Logic Programming (ILP) research has enabled us to apply ILP in more complex situations and there are a number of new algorithms based on Answer Set Programmings (ASPs) that work well in non-monotonic scenarios. Because of the recent advancement of ILP and RL, it is natural to consider that a combination of both approaches would be the next field to explore. Therefore my motivation is to combine these two different subfields of machine learnig and devise a new way of RL algorithm in order to overcome some of the RL problems.

Particularly since [?], there have been several researches that further explored the incorporation of symbolic reasoning into RL, but the combining of ILP and RL has not been explored.

1.2 Objectives

The main objective of this project is to provide a proof-of-concept of a new RL framework using ILP called ILP(RL) and to investigate the potentials of ILP(RL) for improving the learning efficiency and transfer learning capability that current RL methods suffer.

The objective of this paper is devided into the following high-level objectives:

1. Translation of state transitions into ASP syntax.

In RL, an agent interacts with an environment by taking an action and observes a state and rewards (MDP). Since ASP-based ILP algorithms require their inputs to be specified in ASP syntax, the conversion between MDP and ASP is required.

2. Development of learning tasks.

ILP frameworks are based on a search space specified by language bias for a learning task, and is needed to be specified by the user. Various hyper-parameters for the learning task are also considered.

3. Using the learnt concept to execute actions.

Having learnt a hypothesis using a ILP algorithm, the agent needs to choose an action based on the learnt hypothesis. We investigate how the agent can effectively plan a sequence of actions using the hypothesis.

4. Evaluation of the new framework in various environments.

In order to investigate the applicabilities of ILP-based approach, evaluation of the new framework on various scenarios is conducted in order to gain insights of the potentials, especially how it improves the learning process and capability of transfer learning.

This paper is a proof of concept for the new way of RL using ILP and therefore there is a limit to which the current framework can be applied to. More complex environments such as continuous states or stochastic environment are not considered in this paper. Possibilities of applying these more complex environment are discussed in Section ??.

1.3 Contributions

The main contribution of this paper is the development of a novel ILP based approach to reinforcement learning and contributes to an incorporation of ASP-based ILP learning frameworks and Reinforcement Learning by applying a latest ILP framework called Learning from Answer Sets. To my knowledge, this is the first attempt that a ASP-based ILP learning framework is incorporated into a RL scenario.

In simple environments, we show that an agent learns rules of the game and reaches an optimal policy faster than existing RL algorithms. We also show that the learnt hypothesis is easy to understand for human users, and can be applied to other environment to optimise its learning process.

The full hypotheses were learnt in the early phase of learning and exploration phase. Thus with sufficient exploration, the model of the environment is correct and therefore it is able to find the optimal policy, or the shortest path.

We show that ILP(RL) is able to solve a reduced MDP where the rewards are assumed to be associated with a sequence of actions planned as answer sets. Although this is a limited solution, there is a potential to expand it to solve full MDP as discussed in Further Research.

TODO more details on the strength of the algorithm. Validity

1.4 Report Outline

Chapter 2. The necessary background of Answer Set Programming, Inductive Logic Programming and Reinforcement Learning for this paper are described.

Chapter 3. The descriptions of the new framework, called ILP(RL), is explained in details, and we highlight each aspect of learning steps with examples.

Chapter 4. The performance of ILP(RL) is measured in various maze game environments and compared it against two existing RL algorithms, in terms of learning efficiency and the capability of the transfer learning. We evaluate the outcomes and discuss some of the issues we currently face with the current framework.

Chapter 5. We review previous research on the related fields. Since there is no research that attempts to apply ASP-based ILP to RL, we review applications of ASP in RL and the symbolic representations in RL.

Chapter 6. We summarise the framework and experiments of ILP(RL) and discuss the avenues of further research.

Chapter 2

Background

This chapter introduces necessary background of Answer Set Programming (ASP), Inductive Logic Programming (ILP) and Reinforcement Learning (RL), which provide the foundations of our research.

2.1 Answer Set Programming (ASP)

Answer Set Programming (ASP) is a form of declarative programming aimed at knowledge-intensive applications such as difficult search problems [?]. We first introduce a stable model which is foundation of ASP, and describe ASP syntax.

2.1.1 Stable Model Semantics

The semantics of the logic is based on the notion of interpretation, which is defined under a *domain*. A domain contains all the objects that exist. In logic, it is convention to use a special interpretation called a *Herbrand interpretation*.

Definition 2.1. *Herbrand Domain*, or *Herbrand Universe*, of a normal logic program P , denoted $HD(P)$, is the set of all ground terms that are constants and function symbols appeared in P .

Definition 2.2. *Herbrand Base* of a normal logic program P , denoted $HB(P)$, is the set of all ground predicates that are formed by predicate symbols in P and terms in $HD(P)$.

Definition 2.3. *Herbrand Interpretation* of a set of a program P , denoted $HI(P)$, is a subset of the HB_p , and is a set of ground atoms that are true in terms of interpretation.

In order to define a stable model, we need to define a minimal Herbrand model of a normal logic program P .

Definition 2.4. *Herbrand Model* of a normal logic program P is a $HI(P)$ if and only if a set P of clauses is satisfiable. In other words, the set of clauses P is unsatisfiable if no Herbrand model was found.

Definition 2.5. *Minimal Herbrand Model* of a normal logic program P is an Herbrand model M if none of the subset of M is an Herbrand model of P .

Example 2.1.1. (Herbrand Interpretation, Herbrand Model and $M(P)$)

$$P = \begin{cases} p(X) \leftarrow q(X). \\ q(a). \end{cases} \quad \text{HD}(P) = \{ a \}, \text{HB}(P) = \{ q(a), p(a) \}$$

Given above, there are four Herbrand Interpretations $\text{HI}(P) = \langle \{q(a)\}, \{p(a)\}, \{q(a), p(a)\}, \{\} \rangle$, and one Herbrand Model (as well as $M(P) = \{q(a), p(a)\}$)

Definite Logic Program is a set of definite rules, and a *definite rule* is of the form $h \leftarrow a_1, \dots, a_n$. h and a_1, \dots, a_n are all atoms. h is the *head* of the rule and a_1, \dots, a_n are the *body* of the rule. *Normal Logic Program* is a set of normal rules, and a *normal rule* is of the form $h \leftarrow a_1, \dots, a_n, \text{not } b_1, \dots, \text{not } b_n$ where h is the head of the rule, and $a_1, \dots, a_n, b_1, \dots, b_n$ are the body of the rule (both the head and body are all atoms).

To solve a normal logic program P , the program P needs to be grounded. The *grounding* of P is the set of all clauses that are $c \in P$ and variables are replaced by terms in the Herbrand Domain.

Definition 2.6. The algorithm of grounding starts with an empty program $Q = \{\}$ and the relevant grounding is constructed by adding to each rule R to Q such that:

- R is a ground instance of a rule in P .
- Their positive body literals already occurs in the in the of rules in Q .

The algorithm terminates when no more rules can be added to Q .

Example 2.1.2. (Grounding)

$$P = \begin{cases} q(X) \leftarrow p(X). \\ p(a). \end{cases}$$

$\text{ground}(P)$ in this example is $\{p(a), q(a)\}$, as $p(a)$ is already grounded and added to Q , and it is also a positive body literal for the first rule, resulting in $q(a)$.

Not only the entire program needs to be grounded in order for an ASP solver to work, but also each rule must be *safe*. A rule R is *safe* if every variable that occurs in the head of the rule occurs at least once in $\text{body}^+(R)$. Since there is no unique least Herbrand Model for a normal logic program, Stable Model of a normal logic program was defined in [?]. In order to obtain the Stable Model of a program P , P needs to be converted using *Reduct* with respect to an interpretation X .

Definition 2.7. The *reduct* of P with respect to X can be constructed such that:

- If the body of any rule in P contains an atom which is not in X , those rules need to be removed.
- All default negation atoms in the remaining rules in P need to be removed.

Example 2.1.3. (Reduct)

$$P = \begin{cases} p(X) \leftarrow \text{not } q(X). \\ q(X) \leftarrow \text{not } p(X). \end{cases} \quad X = \{p(a), q(b)\}$$

Where X is a set of atoms. $\text{ground}(P)$ is

$p(a) \leftarrow \text{not } q(a).$

$p(b) \leftarrow \text{not } q(b).$

$q(a) \leftarrow \text{not } p(a).$

$q(b) \leftarrow \text{not } p(b).$

The first step removes $p(b) \leftarrow \text{not } q(b).$ and $q(a) \leftarrow \text{not } p(a).$

$p(a) \leftarrow \text{not } q(a).$

$q(b) \leftarrow \text{not } p(b).$

The second step removes negation atoms from the body.

Thus reduct P^x is $(\text{ground}(P))^x = \{p(a), q(b).\}$

Definition 2.8. A *Stable Model* of P , denoted $\text{SM}(P)$, is an interpretation X if and only if X is the unique least Herbrand Model of $\text{ground}(P)^x$ in the logic program.

2.1.2 Answer Set Programming (ASP) Syntax

Definition 2.9. Answer set of normal logic program P is a Stable Model defined by a set of rules, where each rule consists of literals, which is made up with an atom p or its default negation $\text{not } p$ (*negation as failure*). Answer Set Programming (ASP) is a normal logic program with extensions: constraints, choice rules and optimisation statements.

A *definite rule* is:

$$\underbrace{h}_{\text{head}} \leftarrow \underbrace{a_1, a_2, \dots, a_n}_{\text{body}} \quad (2.1)$$

A *normal rule* is:

$$\underbrace{h}_{\text{head}} \leftarrow \underbrace{a_1, a_2, \dots, a_n, \text{not } b_{n+1}, \dots, \text{not } b_{n+k}}_{\text{body}} \quad (2.2)$$

where h, a_1, \dots, b_{n+k} are all atoms. A rule with empty body is a *fact*, and a rule with empty head is a *constraint*. The constraint filters any irrelevant answer sets. When computing $\text{ground}(P)_x$, the empty head becomes \perp , which cannot be in the answer sets.

A *choice rule* can express possible outcomes given an action choice, which is of the form:

$$\underbrace{l\{h_1, \dots, h_m\}u}_{\text{head}} \leftarrow \underbrace{a_1, \dots, a_n, \text{not } b_1, \dots, \text{not } b_n}_{\text{body}} \quad (2.3)$$

where l and u are integers and h_i for $1 \leq i \leq m$ are atoms. The head in the choice rule is called *aggregates*.

Optimisation statement is useful to sort the answer sets in terms of preference, which is of the form:

$$\begin{aligned} &\#minimize[a_1=w_1, \dots, a_n=w_n] \text{ or} \\ &\#maximize[a_1=w_1, \dots, a_n=w_n] \end{aligned} \quad (2.4)$$

where w_1, \dots, w_n is integer weights and a_1, \dots, a_n is ground atoms. ASP solvers compute the scores of the weighted sum of the sets of ground atoms based on the true answer sets, and find optimal answer sets which either maximise or minimise the score.

Clingo is one of the modern ASP solvers that executes the ASP program and returns answer sets of the program [?]. We will use *Clingo* 5 for the implementation of our new framework.

2.2 Inductive Logic Programming (ILP)

Inductive Logic Programming (ILP) is a subfield of machine learning research area aimed at supervised inductive concept learning, and is the intersection between machine learning and logic programming [?]. The purpose of ILP is to inductively derive a hypothesis H that is a solution of a learning task, which covers all positive examples and none of negative examples, given a hypothesis language for search space and cover relation [?]. ILP is based on learning from entailment, as shown in Equation ??.

$$B \wedge H \models E \quad (2.5)$$

where E contains all of the positive examples, denoted E^+ , and none of the negative examples, denoted E^- .

An advantage of ILP over statistical machine learning is that the hypothesis that an agent learn can be easily understood by a human, as it is expressed in first-order logic, making the learning process explainable. By contrast, a limitation of ILP is learning scalability. There are usually thousands or more examples in many real-world examples. Scaling ILP task to cope with large examples is a challenging task [?].

2.2.1 ILP under Answer Set Semantics

There are several ILP non-monotonic learning frameworks under the answer set semantics . We first introduce two of them: *Cautious Induction* and *Brave Induction* ([?]), which are foundations of *Learning from Answer Sets* discussed in Section ??, a state-of-art ILP framework that we will use for our new framework. (for other non-monotonic ILP frameworks, see [?], [?], [?] and [?]).

Cautious Induction

Definition 2.10. *Cautious Induction* task¹ is of the form $\langle B, E^+, E^- \rangle$, where B is the background knowledge, E^+ is a set of positive examples and E^- is a set of negative examples. $H \in \text{ILP}_{\text{cautious}} \langle B, E^+, E^- \rangle$ if and only if there is at least one answer set A of $B \cup H$ ($B \cup H$ is satisfiable) such that for every answer set A of $B \cup H$:

- $\forall e \in E^+ : e \in A$
- $\forall e \in E^- : e \notin A$

Example 2.2.1. (Cautious Induction)

$$B = \begin{cases} \text{exercises} \leftarrow \text{not eat_out.} \\ \text{eat_out} \leftarrow \text{exercises.} \end{cases} \quad E^+ = \{\text{tennis}\}, E^- = \{\text{eat_out}\}$$

One possible $H \in \text{ILP}_{\text{cautious}}$ is $\{\text{tennis} \leftarrow \text{exercises}, \leftarrow \text{not tennis}\}$.

The limitation of Cautious Induction is that positive examples must be true for all answer sets and negative examples must not be included in any of the answer sets. These conditions may be too strict in some cases, and Cautious Induction is not able to accept a case where positive examples are true in some of the answer sets but not all answer sets of the program.

Example 2.2.2. (Limitation of Cautious Induction)

$$B = \begin{cases} 1\{\text{situation}(P, \text{awake}), \text{situation}(P, \text{sleep})\} 1 \leftarrow \text{person}(P). \\ \text{person}(\text{john}). \end{cases}$$

Neither of $\text{situation}(\text{john}, \text{awake})$ nor $\text{situation}(\text{john}, \text{sleep})$ is false in all answer sets. In this example, the hypothesis only contains $\text{person}(\text{john})$. Thus no examples could be given to learn the choice rule.

Brave Induction

Definition 2.11. *Brave Induction* task is of the form $\langle B, E^+, E^- \rangle$ where, B is the background knowledge, E^+ is a set of positive examples and E^- is a set of negative examples. $H \in \text{ILP}_{\text{brave}} \langle B, E^+, E^- \rangle$ if and only if there is at least one answer set A of $B \cup H$ such that:

- $\forall e \in E^+ : e \in A$
- $\forall e \in E^- : e \notin A$

¹This is more general definition of Cautious Induction than the one defined in [?], as the concept of negative examples was not included in the original definition.

Example 2.2.3. (Brave Induction)

$$B = \begin{cases} \text{exercises} \leftarrow \text{not eat_out.} \\ \text{tennis} \leftarrow \text{holiday} \end{cases} \quad E^+ = \{\text{tennis}\}, E^- = \{\text{eat_out}\}$$

One possible $H \in \text{ILP}_{\text{brave}}$ is $\{\text{tennis}\}$, which returns $\{\text{tennis, holiday, exercises}\}$ as answer sets.

The limitation of Brave Induction is that it is not possible to learn constraints, since the conditions of the Definition ?? only apply to at least one answer set A, whereas constraints must rule out all answer sets that meet the conditions of the Brave Induction.

Example 2.2.4. (Limitation of Brave Induction)

$$B = \begin{cases} 1\{\text{situation}(P, \text{awake}), \text{situation}(P, \text{sleep})\}1 \leftarrow \text{person}(P). \\ \text{person}(C) \leftarrow \text{super_person}(C). \\ \text{super_person}(\text{john}). \end{cases}$$

In order to learn the constraint hypothesis $H = \{ \leftarrow \text{not situation}(P, \text{awake}), \text{super_person}(P) \}$, it is not possible to find an optimal solution.

2.2.2 Inductive Learning of Answer Set Programs (ILASP)

Learning from Answer Sets (LAS)

Learning from Answer Sets (LAS) was developed in [?] to facilitate more complex learning tasks that neither Cautious Induction nor Brave Induction could learn. Examples used in LAS are a tuple of pair of atoms called *Partial Interpretations*, which is of the form:

$$E = \langle e^{\text{inc}}, e^{\text{exc}} \rangle. \quad (2.6)$$

(called *inclusions* and *exclusions* of E respectively). A Herbrand Interpretation extends a partial interpretation if it includes all of E^{inc} and none of E^{exc} .

A *Learning from Answer Sets* task is of the form:

$$T = \langle B, S_M, E^+, E^- \rangle \quad (2.7)$$

where B is background knowledge, S_M is hypothesis space, and E^+ and E^- are examples of positive and negative partial interpretations. S_M consists of a set of normal rules, choice rules and constraints. S_M is specified by *language bias* of the learning task using *mode declaration*. Mode declaration specifies what can occur in a hypothesis by specifying the predicates, and consists of two parts: *modeh* and *modeb*. *modeh* and *modeb* are the predicates that can occur in the head of the rule and body of the rule respectively. Language bias is the specification of the language in the hypothesis in order to reduce the search space for the hypothesis.

Definition 2.12. Learning from Answer Sets (LAS)

Given a learning task T , the set of all possible inductive solutions of T , denoted $ILP_{LAS}(T)$, and a hypothesis H is an inductive solution of $ILP_{LAS}(T) \langle B, S_M, E^+, E^- \rangle$ such that:

1. $H \subseteq S_M$
2. $\forall e^+ \in E^+ : \exists A \in \text{Answer Sets}(B \cup H)$ such that A extends e^+
3. $\forall e^- \in E^- : \nexists A \in \text{Answer Sets}(B \cup H)$ such that A extends e^-

Inductive Learning of Answer Set Programs (ILASP)

Inductive Learning of Answer Set Programs (ILASP) is an algorithm that is capable of solving LAS tasks, and is based on two fundamental concepts: *positive solutions* and *violating solutions*.

A hypothesis H is a positive solution if and only if

1. $H \subseteq S_M$
2. $\forall e^+ \in E^+ \exists A \in \text{Answer Sets}(B \cup H)$ such that A extends e^+

A hypothesis H is a violating solution if and only if

1. $H \subseteq S_M$
2. $\forall e^+ \in E^+ \exists A \in \text{Answer Sets}(B \cup H)$ such that A extends e^+
3. $\exists e^- \in E^- \exists A \in \text{Answer Sets}(B \cup H)$ such that A extends e^-

Given both definitions of positive and violating solutions, $ILP_{LAS} \langle B, S_M, E^+, E^- \rangle$ is positive solutions that are not violating solutions.

Example 2.2.5. (ILASP).

XXX

A Context-dependent Learning from Answer Sets

Context-dependent learning from answer sets ($ILP_{LAS}^{context}$) is a further generalisation of ILP_{LAS} with *context dependent examples*[?] ². *Context-dependent examples* are examples that each unique background knowledge, or *context*, only applies to specific examples. This way the background knowledge is more structured rather than one fixed background knowledge that are applied to all examples.

Formally, partial interpretation is called *context-dependent partial interpretation (CDPI)*, which is of the form:

$$\langle e, C \rangle \tag{2.8}$$

²The original paper developed the framework called *learning from ordered answer sets* ($ILP_{LOAS}^{context}$). In this paper, we do not use ordered answer sets and therefore simplify it to $ILP_{LAS}^{context}$.

where e is a partial interpretation and C is a context, or an ASP program without weak constraints.

Definition 2.13. $ILP_{LAS}^{context}$ task is of the form $T = \langle B, S_M, E^+, E^- \rangle$. A hypothesis H is an inductive solution of T if and only if:

1. $H \subseteq S_M$
2. $\forall \langle e, C \rangle \in E^+, \exists A \in \text{Answer Sets } (B \cup C \cup H) \text{ such that } A \text{ extends } e$
3. $\forall \langle e, C \rangle \in E^-, \nexists A \in \text{Answer Sets } (B \cup C \cup H) \text{ such that } A \text{ extends } e$

One of the main advantages of using context dependent examples is that when a hypothesis is computed, only the relevant set of examples are used for search rather than using all examples at once. Relevant examples are counterexamples for the previously computed hypothesis in the previous iterations. This iterative approach increases the efficiency of solving learning tasks, and enables more expressive structure of the background knowledge to particular examples.

$ILP_{LAS}^{context}$ is used in ILASP2i, which we use for our new framework.

Example 2.2.6. ($ILP_{LAS}^{context}$).

XXX

2.3 Reinforcement Learning (RL)

Reinforcement learning (RL) is a subfield of machine learning regarding how an agent behaves in an environment in order to maximise its total reward. As shown in Figure ??, the agent interacts with an environment, and at each time step the agent takes an action and receives observation, which affects the environment state and the reward (or penalty) it receives as the action outcome. In this section, we briefly introduce the background of RL necessary for our new framework as well as benchmarks of the experiments discussed in Chapter ??.

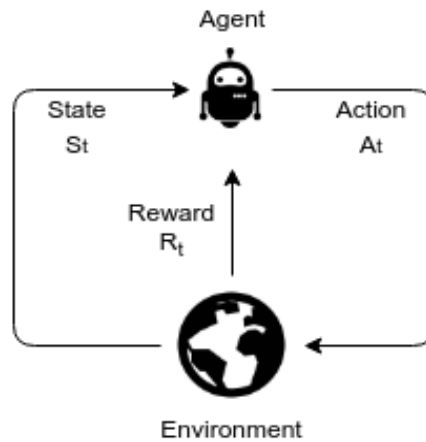


Figure 2.1: The interaction between an agent and an environment

2.3.1 Markov Decision Process (MDP)

An agent interacts with an environment at a sequence of discrete time step, which is part of the sequential history of observations, actions and rewards. The sequential history is formalised as

$$H_t = S_1, R_1, A_1, \dots, A_{t-1}, S_t, R_t. \quad (2.9)$$

where S is *states*, R is *rewards* and A is *actions*. A state S_t determines the next environment and has a *Markov property* if and only if

$$P[S_{t+1}|S_t] = P[S_{t+1}|S_1, \dots, S_t]. \quad (2.10)$$

In other words, the probability of reaching S_{t+1} depends only on S_t , which captures all the relevant information from the earlier history ([?]). When an agent must make a sequence of decision, the sequential decision problem can be formalised using *Markov decision process (MDP)*. MDP formally represents a fully observable environment of an agent for RL.

Definition 2.14. Markov Decision Process (MDP)

Markov decision process (MDP) is defined in the form of a tuple $\langle S, A, T, R \rangle$ where:

- S is the set of finite states that is observable in the environment.
- A is the set of finite actions taken by the agent.
- T is a *state transition function*: $S \times A \times S \rightarrow [0,1]$, which is a probability of reaching a future state $s' \in S$ by taking an action $a \in A$ in the current state $s \in S$.
- R is a reward function $R_a(s, s') = \mathbb{E}[R_{t+1} | S_t = s, A_t = a]$, the expected immediate reward that action a in state s at time t will return.

The objective of an agent is to solve an MDP by taking a sequence of actions to maximise the total cumulative reward it receives. A method to find the optimal solution of an MDP is Reinforcement Learning (RL). Formally, the objective of a RL agent is to maximise *expected discounted return*, which is defined as:

$$G_t = R_{t+1} + \gamma R_{t+2} + \dots = \sum_{k=0}^{\infty} \gamma^k R_{t+k+1} \quad (2.11)$$

where γ is a discount rate $\gamma \in [0,1]$, a parameter, which represents the preference of the agent for the present reward over future rewards. If γ is low, the agent is more interested in maximising immediate rewards.

For RL programs, it is not necessary for the agent to know T and R in advance, but they are present in the environment and can be realised each time the agent takes an action.

2.3.2 Policies and Value Functions

Most of RL algorithms are concerned with estimating *Value functions*. Value functions estimate the expected return, or expected future reward, for a given action in a given state. The expected reward for an agent is dependent on the agent's action. Value functions are defined by *policies*, which maps from states to probabilities of choosing each action. The state value function $v_\pi(s)$ of an MDP under a policy π is the expected return starting from state s , which is of the form:

$$v_\pi(s) = \mathbb{E}[G_t | S_t = s] \text{ for all } s \in \mathcal{S} \quad (2.12)$$

The optimal state-value function $v^*(s)$ maximises the value function over all policies in the MDP, which is of the form:

$$v^*(s) = \max_{\pi} v_\pi(s) \quad (2.13)$$

Example 2.3.1. (Value Functions).

XXX

Similar to the state value function v_π , we define a *action-value function* under a policy π , which represents the value of taking action a in state s following a policy π .

$$q_\pi(s, a) = \mathbb{E}[G_t | S_t = s, A_t = a] \text{ for all } s \in \mathcal{S} \quad (2.14)$$

The optimal state-action-value function $q^*(s, a)$ maximises the action-value function over all policies in the MDP, which is of the form:

$$q^*(s, a) = \max_{\pi} q_\pi(s, a) \quad (2.15)$$

A solution to MDP is called a *policy* π , a sequence of actions that leads to a solution. An optimal policy achieves the optimal value function (or action-value function), and it can be computed by maximising over the optimal value function (or action-value function).

Example 2.3.2. (Action-value Functions).

XXX

2.3.3 Model-based and Model-free RL

A *model* is a representation of an environment that an agent can use to understand how the environment should look like. There are two different types of RL methods: *model-based* and *model-free* RL method. Model-based RL is that, given a model of the environment is known, the agent uses the model to plan for a series of actions to achieve the agent's goal. The model itself can be learnt by interacting with the environment by taking actions, which returns states and rewards, and the parameters of the action models can be estimated by maximum likelihood methods [?]. Using a model, an agent can do planning to generate or improve a policy for the modeled environment. Most of the RL methods are model-free RL, where the model is unknown

and the agent learns to achieve the goal by solely interacting with the environment. Thus the agent knows only possible states and actions, and the transition state and reward probability functions are unknown. When the model of the environment is correct, unlike model-free RL, the agent does not require trial-and-error interactions with the environment and therefore model-based RL is faster to reach an optimal policy. However, when the model is not a true representation of the environment, or the true MDP, the planning algorithms will not lead to the optimal policy, but a suboptimal policy.

One algorithm which combine both aspects of model-based and model-free learning to solve the issue of sub-optimality is called Dyna [?]. Dyna learns a model from real experience and use the model to generate simulated experience to update the evaluation functions. This approach is more efficient because the simulated experiences are relatively easy to generate compared to real experiences, thus less iterations are required.

This idea of learning a model of the environment and use it to execute planning is a core idea of our new framework.

2.3.4 Temporal-Difference (TD) Learning

One of the RL approaches for solving a MDP is called *Temporal-Difference (TD) Learning*. TD learning is an online model-free RL and learns directly from episodes of incomplete experiences without a model of the environment. TD updates the estimates of value function as follow:

$$V(S_t) \leftarrow V(S_t) + \alpha[R_{t+1} + \gamma V(S_{t+1}) - V(S_t)] \quad (2.16)$$

where $R_{t+1} + \gamma V(S_{t+1})$ is the target for TD update, which is biased estimated of $v_\pi(S_t)$, and $\delta = R_{t+1} + \gamma V(S_{t+1}) - V(S_t)$ is called *TD error*, which is the error in $V(S_t)$ available at time $t+1$. Since TD method only needs to know the estimate of one step ahead and does not need the final outcome of the episodes (also called TD(0)), it can learn online after every time step. TD also works without the terminal state, which is the goal for an agent. TD(0) is proved to converge to v_π in the table-based case (non-function approximation).

Q-learning is off-policy TD learning defined in [?], where the agent only knows about the possible states and actions. The transition states and reward probability functions are unknown to the agent. The update rule for the state-action value function, called *Q function*, is of the form:

$$Q(s_t, a_t) \leftarrow Q(s_t, a_t) + \alpha(R_{t+1} + \gamma \max(a, t)Q(s_{t+1}, a_{t+1}) - Q(s_t, a_t)) \quad (2.17)$$

where α is a constant step-size parameter, or learning rate, α between 0 and 1, and γ is a discount rate. The function $Q(S, A)$ predicts the best action A in state S to maximise the total cumulative rewards.

$$Q(s_t, a_t) = E[R_{t+1} + \gamma R_{t+2} + \gamma^2 R_{t+3} + \dots | s_t, a_t] \quad (2.18)$$

Q-learning is guaranteed to converge to a optimal policy in a finite tabular representation. Since Q-learning is one of the most widely used RL methods and our

experiments are conducted in a tabular representation, we use it as one of the benchmarks for our new framework.

2.3.5 Function Approximation

Q-learning with a tabular representation works when every state-action value can be represented. In case of very large MDPs, however, it may not be possible to represent all state-action values with a tabular representation. For example, robot arms has a continuous states in 3D dimensional space. This problem motivates the use of *function approximation*, which estimates value function with function approximation. Not only is it represented in tabular form, but also in the form of a parameterized function with *weight vector* w . Unlike Q-table, changing one weight updates the estimated value of not only one state, but many states, and this generalisation makes it more flexible to apply different scenarios that tabular approach could not be applied.

The reason we are introducing the function approximation is that it is used as another benchmark for our new framework.

The Prediction Objective (\overline{VE})

With function approximation, an update at one state changes many other states, and therefore the values of all states will not be exactly accurate, and there is a tradeoff among states as to which state we make it more accurate, while other might be less accurate. The error in a state s is the square of the difference between the approximate value $\hat{v}(s, w)$ and the true value $v_\pi(s)$. The objective function can be defined by weighting it over the state space by μ , the *Mean Squared Value Error*, denoted \overline{VE} .

$$\overline{VE}(w) \doteq \sum_{s \in S} \mu(s) [v_\pi(s) - \hat{v}(s, w)]^2. \quad (2.19)$$

Stochastic gradient descent (SGD)

Stochastic gradient descent (SGD) methods are commonly used to learn function approximation in value prediction, which works well for online reinforcement learning. The weight vector w in SGD is defined as:

$$w \doteq \begin{pmatrix} w_1 \\ w_2 \\ \vdots \\ w_n \end{pmatrix} \quad (2.20)$$

and $\hat{v}(s, w)$ is a differentiable function of w for all $s \in S$. SGD adjusts the weights vector by a fraction of α , a step-size parameter, in the direction what reduces the

error on that example the most. Formally, it is defined as:

$$\begin{aligned} w_{t+1} &\doteq w_t - \frac{1}{2}\alpha \nabla [v_\pi(S_t) - \hat{v}(S_t, w_t)]^2. \\ &= w_t + \alpha [v_\pi(S_t) - \hat{v}(S_t, w_t)] \nabla \hat{v}(S_t, w_t). \end{aligned} \quad (2.21)$$

The gradient of $J(w)$, which is the vector of partial derivatives with respect to each weight vector, is defined as:

$$\nabla_w J(w) = \begin{pmatrix} \frac{\partial J(w)}{\partial w_1} \\ \vdots \\ \frac{\partial J(w)}{\partial w_n} \end{pmatrix} \quad (2.22)$$

Linear Value Function Approximation

A *linear function* of a weight vector is a type of simple function approximation to approximate action-value function.

$$\hat{q}(s, a) \approx q_\pi(s, a) \quad (2.23)$$

The vector $x(s, a)$ represents a *feature vector*, which is of the form:

$$x(S, A) = \begin{pmatrix} x_1(S, A) \\ \vdots \\ x_n(S, A) \end{pmatrix} \quad (2.24)$$

where each $x(s, a)$ is a feature of corresponding action-state pair.

Using SGD update with linear function approximation, the gradient of the approximate value function with respect to w is:

$$\nabla \hat{q}(s, a, w) = x(s, a) \quad (2.25)$$

Thus the general SGD update defined in (??) can be simplified to the following:

$$w_{t+1} = w_t + \alpha [q_\pi(S_t, A_t) - \hat{q}(S_t, A_t, w_t)] x(S_t, A_t) \quad (2.26)$$

Unlike non-linear value function approximation, linear method is guaranteed to converge to a global optimum. One disadvantage of the linear method is that it cannot express any relationship between features. For example, it cannot represent that feature i is useful only if feature j is not present. Nevertheless, this approach is sufficient enough for our experiments, which is described in Chapter ??.

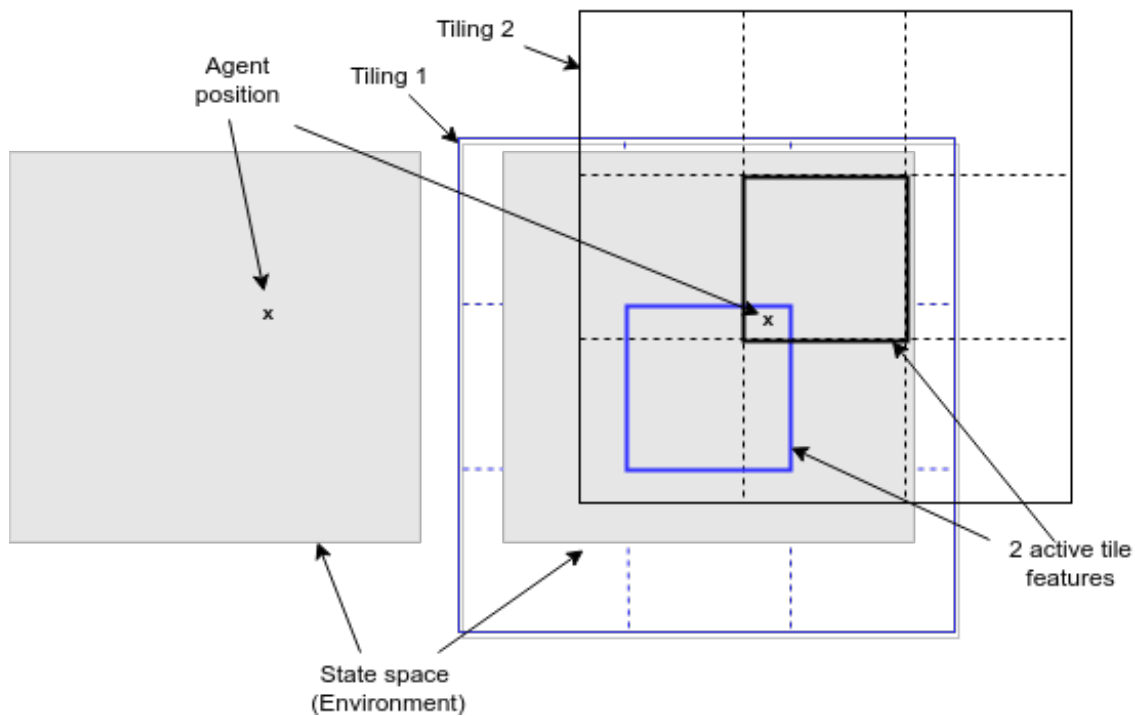


Figure 2.2: Tiling coding illustration

Tile Coding (TBD)

There are different linear function approximation methods to represent states as features. Feature construction depends on a problem you are solving. We introduce *Tile Coding* which will be used for our benchmark.

Illustration of tile coding is shown in Figure ???. In Tile Coding, state set is represented as a continuous two-dimensional space. If a state is within the space, then the value of the corresponding feature is set to be 1 to indicate that the feature is present, while 0 indicates that the feature is absent. This way of representing the feature is called *binary feature*. *Coarse coding* represents a state with which binary features are present within the space. One area is associated with one weight w , and training at a state will affect the weight of all the areas overlapping that state. The approximate value function will be updated within at all states within the union of the areas, and a point that has more overlap will be more affected. The size and shape of the areas will determine the degree of the generalisation. Large areas will have more generalisation. In addition, tiles can be overlap, and the change of the weight in that state will affect all other states within the intersection of the spaces. The degree of overlap within a space will determine the degree of the generalisation. The shape of the space also affects how it is generalised.

Tile coding is a type of coarse coding. *Tiling* is a partition of state space, and each element of the partition is called a *tile*.

The state space is partitioned into multiple tiles with multiple tilings. Each tile in each tiling is associated with

In order to do coarse coding with tile coding, multiple tilings are required, each tiling is offset from one another by a fraction of a tile width.

As illustrated in Figure XXX, when a state occurs, several features with corresponding tiles become active,

Tile coding has computational advantage, since each component of tiling is binary value, XXXX.

a trained state will be generalised to other states if they are within any of the same tiles.

Similar to coarse coding, the size and shape of tiles will determine the degree of approximation.

Example 2.3.3. (Tile Coding).

XXX

2.3.6 Transfer Learning (TBD)

Transfer learning is a method that knowledge learnt in one or more tasks can be used to learn a new task better than if without the knowlege in the first task.

Transfer learning is an active research areas in machine learning, but not many have been done in RL. Since training tend to be time consuming and computational expensive, transfer learning allow the trained model to be applied in a different setting.

Transfer learning in RL is particularly important since most of the RL research have been done in a simulation or game scenarios, and training RL models in a real physical environment is more expensive to conduct.

Even in a virtual environments like games, the transfer learning between different tasks will greatly will have a big impact on potential applications.

This will also speed up learning

Transfer learning in ILP domain have been proved to be successful in many fields,

Since this project is combining ILP into RL senarios, this has a potential for extending this particular research.

We conducted experiements on transfer learning capabilities, which we describe in XXX.

One of the purposes of transfer learning is so that the agent requires less time to learn a new task with the help of what was learn in previous tasks.

Another goal would be to measure how effectively the agent reuses its knoledge in a new task. In this case the performan of learningon the first task is usally not measured.

There are many different matrices used to measure the performance of the transfer learning. Five common matrices are defined in XX as follow.

TODO source task selection

Since each matric measures different aspect of transfer learning, using multiple metrics would provide more comprehensive views of the performance of an RL algorithm.

Chapter 3

Framework

3.1 Overview

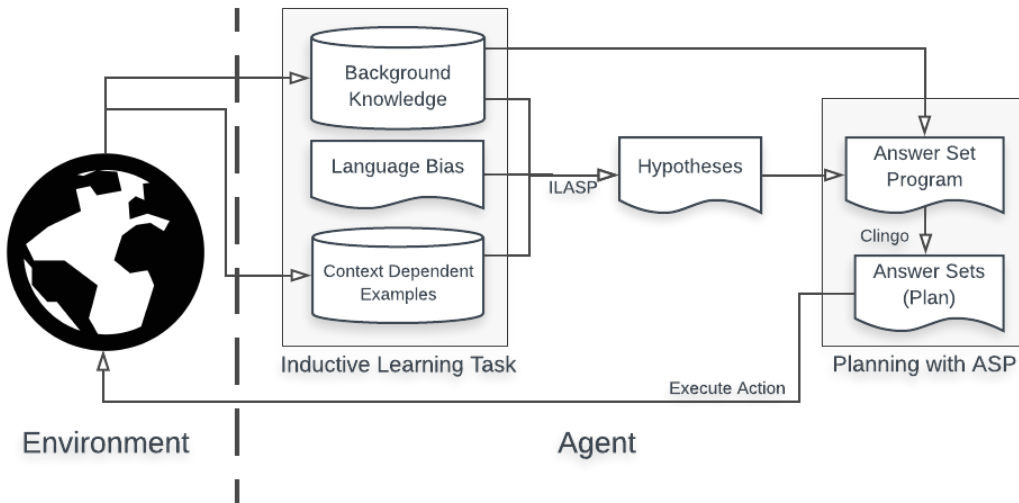


Figure 3.1: ILP(RL) overview

The overall architecture of the learning framework, called *ILP(RL)*, is shown in Figure ???. By interacting with the environment, an agent receives state transition experiences as positive examples, which is used by ILASP, together with pre-defined background knowledge and language bias, to learn and improve hypotheses. The agent also remembers surrounding information it has seen as background knowledge, which is used to make an action plan together using the learnt hypotheses by solving an answer set program. Mechanisms of each step is explained in details in the following sections.

3.2 Inductive Learning Task

The first step is to translate experiences generated by the interaction with an environment into ASP syntax. Similar to an existing RL, an agent explores an environment following an exploration strategy. Every time the agent takes an action, these experiences are recorded in two different forms: a positive example and background knowledge. Positive examples and background knowledge are used by ILASP for inductive learning, and background knowledge is used by both ILASP and ASP for solving for answer sets. Thus it is necessary to convert them into ASP syntax. The full details for ILASP learning tasks is described in Appendix XXX.

3.2.1 Context Dependent Examples

Context dependent examples contain information about how the state transitions between the current state and the next state. They are equivalent to context-dependent partial interpretation (CDPI) in $ILLP_{LAS}^{context}$. As defined in the Equation ??, CDPI is of the form $\langle e, C \rangle$ where $e = \langle e^{inc}, e^{exc} \rangle$. Each of the components in CDPI is defined as follows:

Definition 3.1. e^{inc} of CDPI for ILP(RL) is the next state of an agent $\forall s_{t+1} \in S$ such that answer sets of $B \cup H$ does not cover.

Definition 3.2. e^{exc} of CDPI for ILP(RL) is the next state of an agent $\forall s_{t+1} \notin S$ such that answer sets of $B \cup H$ covers, as well as $\forall s'_{t+1} \in S_{neighbor}$ such that $s_{t+1} \neq s'_{t+1}$.

where B is the current background knowledge, H is the current hypotheses learnt by previous inductive learning using ILASP, S is all the states in the environment, and $S_{neighbor}$ is all adjacent states of s_t as well as s_t itself.

Definition 3.3. Context C of CDPI for ILP(RL) contains an action a_t , a state s_t , and adjacent walls of s_t .

In this paper, we assume that part of context contains only whether a wall exists or not, with the presence of a wall, the agent cannot move to the state where a wall exist.

Positive examples in ASP syntax

A positive example is expressed as a following ASP form:

$$\#pos(\{e^{inc}\}, \{e^{exc}\}, \{C\}) \quad (3.1)$$

For e^{inc} and e^{exc} , s_{t+1} is expressed as *state_after((x,y))*, where x and y represent coordinates of X and Y axis in an environment respectively. Thus both e^{inc} and e^{exc} contain only *state_after((x,y))* or empty. For context C , a_t is translated into *action((a))*, s_t is translated into *state_before((x,y))*, and adjacent walls of s_t are translated into *wall((x',y'))*.

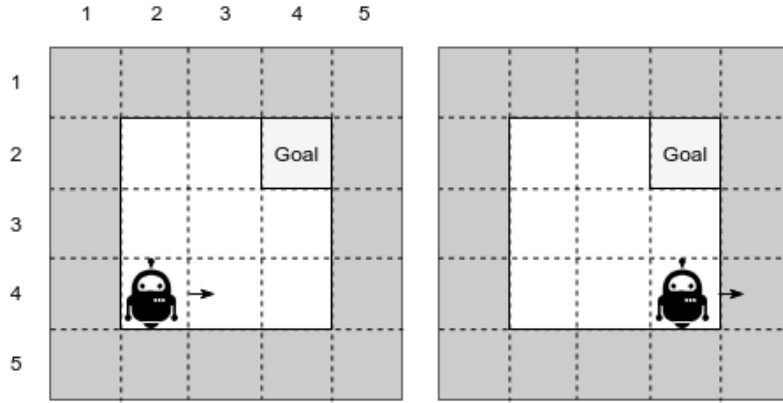


Figure 3.2: 5×5 grid world example

Example 3.2.1. (Positive examples).

We use a simple 5x5 gridworld environment to highlight how an agent gains a positive example, suppose the agent takes an action "right" to move from (2,4) to (3,4) cell, as shown on Figure ?? on the right. All other alternative states that the agent could have ended up by taking different actions (down, up, and left) are in the exclusions. Context examples are the state that the agent is before taking an action and surrounding walls information. The following positive example is generated.

```
#pos({state_after((3,4))},
    {state_after((2,4)),state_after((1,5)),state_after((0,4)),state_after((1,4))}, (3.2)
    {state_before((2,4)). action(right). wall((1, 4)). wall((4, 2)).})
```

This example will be used to learn how to move up as one of the agent's hypotheses. Similarly, the agent is at (4,4) and tries to move right, as shown on the left on Figure ??. In this case, however, there is a wall at (5,4) and therefore the agent ends up in the same state. From this example, the following positive example is generated:

```
#pos({state_after((4,4))},
    {state_after((4,3)),state_after((3,4)),state_after((5,4)),state_after((4,5))} (3.3)
    {state_before((4,4)). action(right). wall((5,4)). wall((4,5)).}).
```

3.2.2 Background Knowledge

Having defined the positive examples, we now define necessary background knowledge for inductive learning. In order to learn valid move for each direction in the form of state transition, it needs to know how it means to be "being next to XX". The

definition of adjacent is given as follows:

$$\begin{aligned}
 \text{adjacent}(\text{right}, (X+1,Y),(X,Y)) &:- \text{cell}((X,Y)), \text{cell}((X+1,Y)). \\
 \text{adjacent}(\text{left},(X,Y), (X+1,Y)) &:- \text{cell}((X,Y)), \text{cell}((X+1,Y)). \\
 \text{adjacent}(\text{down}, (X,Y+1),(X,Y)) &:- \text{cell}((X,Y)), \text{cell}((X,Y+1)). \\
 \text{adjacent}(\text{up}, (X,Y), (X,Y+1)) &:- \text{cell}((X,Y)), \text{cell}((X,Y+1)).
 \end{aligned} \tag{3.4}$$

In existing RL methods, the agent is only able to see the state where the agent is at, and this is an additional assumption that the agent is able to see surrounding states. These adjacent concepts themselves could be learnt using ILASP separately, but in this preliminary research we focus on learning valid move, and this extension will be discussed in Further Research in XX. In addition, $\text{cell}((X,Y))$ is defined as follows:

$$\text{cell}((0..X, 0..Y)). \tag{3.5}$$

where, $0..X$ defines the range of X coordinates and X and Y are the size of width and height of the environment respectively. For 5x5 gridworld environment, for example, cell is defined as $\text{cell}((0..5, 0..5))$.

Example 3.2.2. (Background Knowledge).

XXX

3.2.3 Language Bias

Recall in ?? that $H \subseteq S_M$ for $ILP_{LAS}^{context}$, thus we define a search space using a language bias specified by *mode declaration*. We define S_M as follows:

$$\begin{aligned}
 \#modeh(\text{state_after}(\text{var}(\text{cell}))). \\
 \#modeb(1, \text{adjacent}(\text{const}(\text{action}), \text{var}(\text{cell}), \text{var}(\text{cell})), (\text{positive})). \\
 \#modeb(1, \text{state_before}(\text{var}(\text{cell})), (\text{positive})). \\
 \#modeb(1, \text{action}(\text{const}(\text{action})), (\text{positive})). \\
 \#modeb(1, \text{wall}(\text{var}(\text{cell}))).
 \end{aligned} \tag{3.6}$$

$\#modeh$ and $\#modeb$ are the *normal head* declarations and the body declarations. The first argument of each $\#modeb$ specifies the maximum number of times that $\#modeb$ can be used in each rule (also called *recall*), which is 1 in our case.

$\text{var}(t)$ is a placeholder for variable of type t . In ??, we use cell for a variable type, which is based on any cell defined in ?. $\text{const}(t)$ is a placeholder for constant term of type t , and type t must be specified as $\#constant(t, c)$, where c is a constant term., $\text{const}(t)$ is defined as follow:

$$\begin{aligned}
 \#constant(\text{action}, \text{right}). \\
 \#constant(\text{action}, \text{left}). \\
 \#constant(\text{action}, \text{down}). \\
 \#constant(\text{action}, \text{up}).
 \end{aligned} \tag{3.7}$$

action type is specified as constant since ILASP should learn different hypothesis for each action, and can be found in each context as specified in Definition ??.

(positive) in `#modeb` specifies that the predicates only appears as positive and not negation as failure, which reduces the search space. In this case, `#modeb(1, wall(var(cell)))` could appears as not wall, and all other body declaration should be positive.

Finally, we define `#max_penalty` to specify the maximum size of the hypothesis. By default it is 15, and we increased to 50 as the maximum. Increasing `#max_penalty` allows ILASP to learn longer hypothesis in expense of longer computation.

Example 3.2.3. (Language Bias).

XXX

3.2.4 Hypothesis

Having defined the $ILP_{LAS}^{context}$ task T, ILP(RL) is able to learn an hypothesis H. Since B and S_M are fixed, the learnt H varies depending on positive examples that the agent receives. In the early phase of learning, the agent does not have many positive examples, and learns an hypothesis that is part of the full hypothesis that the agent can run in the environment. Therefore it is important to iteratively improve hypotheses. Inductive learning algorithm is executed by the following rule.

Definition 3.4. ILP(RL) runs $ILP_{LAS}^{context}$ to relearn H_{new} if and only if $\forall \langle e, C \rangle \in E^+$, $\exists A \in \text{Answer Sets}(B \cup C \cup H)$ such that A extends e

where H is the current hypothesis that the agent has learnt so far. Learnt hypotheses are improved when a new positive example is added and the current hypothesis does not cover the new positive example. If it does cover it, there is no need to rerun ILASP again.

The learnt hypothesis will be used to generate a plan, which we describe in the next section.

Example 3.2.4. (Hypothesis).

For example, if the agent has only one positive example,

XXX This hypothesis, for example, does not explain how to move "down". In order to learn how to move "down", it needs an positive example of moving up.

3.3 Planning with Answer Set Programming

Having learnt hypothesis using $ILP_{LAS}^{context}$, we can use the learnt hypotheses to generate a sequence of actions in the form of answer sets that the agent should follow. In the following subsections, we explain how to create a answer set program and use the answer sets to make a plan in a maze.

3.3.1 Answer Set Program

The ASP should be constructed such that answer sets of ASP are a sequence of actions and the next state by taking each action. We explain the details of how the ASP is constructed in the planning phase.

First, we use the learnt hypotheses by $ILP_{LAS}^{context}$ as rules for solving ASP. In the $ILP_{LAS}^{context}$, we only need to differentiate between s_t and s_{t+1} as `state_before(T)` and `state_after(T+1)` respectively. However, for ASP planning, the answer sets contains a sequence of actions and states at each time steps. In order to capture the notion of time sequences, we modify the ASP syntax slightly by introducing T . Specifically, the following mapping is required

$$\begin{aligned}
 \text{state_after}(V0) &:- \text{adjacent}(\text{right}, V0, V1), \text{state_before}(V1), \text{action}(\text{right}), \text{not wall}(V0). \\
 \text{state_after}(V0) &:- \text{adjacent}(\text{left}, V0, V1), \text{state_before}(V1), \text{action}(\text{left}), \text{not wall}(V0). \\
 \text{state_after}(V0) &:- \text{adjacent}(\text{down}, V0, V1), \text{state_before}(V1), \text{action}(\text{down}), \text{not wall}(V0). \\
 \text{state_after}(V0) &:- \text{adjacent}(\text{up}, V0, V1), \text{state_before}(V1), \text{action}(\text{up}), \text{not wall}(V0).
 \end{aligned} \tag{3.8}$$

Example 3.3.1. (Mapping of ASP syntax between $ILP_{LAS}^{context}$ and ASP).

XXX

Second, we define a rule for action, which is of the form:

$$\begin{aligned}
 &1\{\text{action}(\text{down}, T); \text{action}(\text{up}, T); \text{action}(\text{right}, T); \text{action}(\text{left}, T)\}1 \\
 &:- \text{time}(T), \text{not finished}(T).
 \end{aligned} \tag{3.9}$$

Action is given as a choice rule, and this choice rule states that action must be one of four actions: down, up, right, or left. at each time step T , as defined maximum and minimum numbers in 1. One of four actions must be selected unless `not finished(T)` or `time(T)` are satisfied, as defined in the body of the rule. In RL scenarios, this means there is always action to be taken until the agent reaches a goal, thus `finished(T)` is satisfied, or time step T exceeds a maximum time step.

$$\text{time}(T_t..T_{\max}) \tag{3.10}$$

where T_t is the current time step and T_{\max} is the maximum time steps. For example, if an agent is at time step 0, and can take actions 100 times to find a goal time is defined as `time(0..100)`.

`finished(T)` determines whether the agent reaches the goal, which is defined in the following ASP form:

$$\begin{aligned}
 \text{finished}(T) &:- \text{goal}(T2), \text{time}(T), T \geq T2. \\
 \text{goal}(T) &:- \text{state_at}((X_{\text{goal}}, Y_{\text{goal}}), T), \text{not finished}(T-1). \\
 \text{goalMet} &:- \text{goal}(T). \\
 &:- \text{not goalMet}.
 \end{aligned} \tag{3.11}$$

$state_at((X_{goal}, Y_{goal}))$ is the location of the goal, which is unknown to the agent in the beginning of the training. The agent explores the environment until it finds the goal location. In the other word, the agent cannot generate a plan to the goal until the goal is found. Once the agent reaches the goal and $finished(T)$ is satisfied, there will not be any actions at time $T+1$ since the body of the action choice rule defined in ?? is not satisfied.

Next, facts of walls information is provided as follows:

$$wall((X,Y)) \quad (3.12)$$

As defined in Definition ??, the agent is assumed to be able to see adjacent walls and used it as a context in positive examples in $ILP_{LAS}^{context}$. For ASP planning part, these wall information is accumulated as background knowledge as a separate repository, and used it for solving ASP.

Next, the starting state for the planning provided as part of ASP. It is simply the current location of the agent where the actions plan is a starting point.

$$state_at((X_{start}, Y_{start}), T) \quad (3.13)$$

In addition, the definition of adjacent and cell type are also provided, which are the same as what was defined as background knoweldge of $ILP_{LAS}^{context}$ (Equation ?? and ??) ajacents.

Next, we need to incorporate a nortion of rewards in each state. Instead of maximising the total rewards, which is the objectives of most RL methods, we use optimisation statements as follow.

$$\#minimize\{1, X, T: action(X,T)\}. \quad (3.14)$$

The use of optimisation staetment is based on the assumption that the total rewards can be maximised by searching for optimal answer sets. While this works only subset of MDP, our preliminary research focuses on solving this particular MDP problem. Finally, we are only interested in a sequecne of actions and corresponding state as answer sets. Clingo can selectively include the atoms of certain predicates in the output and hide unselected ones. This is defined as follows:

$$\begin{aligned} \#show\ state_at/2. \\ \#show\ action/2. \end{aligned} \quad (3.15)$$

Example 3.3.2. (Answer Set Program).

$$\begin{aligned} &state_at((X_{start}, Y_{start}), T) \\ &\#minimize\{1, X, T: action(X,T)\}. \\ &\#show\ state_at/2. \\ &\#show\ action/2. \\ &wall((X,Y)) \end{aligned} \quad (3.16)$$

3.3.2 Plan Execution

Having defined the ASP, we explain the answer sets generated by the ASP and how to use the answer sets to execute the planning.

Since the rules ?? involves $\text{state_at}((X_{\text{goal}}, Y_{\text{goal}}))$ and it is found only when the agent reaches the goal state, the plan generation is executed only after the agent finds the goal. Until the goal is found, the agent continues to explore the environment while improving the hypotheses and collecting surrounding information. Once the agent reaches the goal, the agent is told whether the state is a terminal state, and can generate a plan using the current hypotheses by solving Answer Set Program defined in ??.

The output of the ASP is of the form:

$$\begin{aligned}
 &\text{state_at}((x_t, y_t), t), \text{ action}(a_t, t), \\
 &\text{state_at}((x_{t+1}, y_{t+1}), t+1), \text{ action}(a_{t+1}, t+1), \\
 &\text{state_at}((x_{t+2}, y_{t+2}), t+2), \text{ action}(a_{t+2}, t+2), \\
 &\dots \\
 &\text{state_at}((x_{t+n}, y_{t+n}), t+n), \text{ action}(a_{t+n}, t+n), \\
 &\text{state_at}((x_{\text{goal}}, y_{\text{goal}}), t+n+1).
 \end{aligned} \tag{3.17}$$

where n is the number of time steps to take to reach the goal. $\text{action}(A, T)$ tells which action the agent should take at each time. Given the answer set planning is correct, the agent follows the plan and reach the goal. The correctness of the planning is based on the correctness of the hypotheses as well as the wall surrounding information in the agent's background knowledge. For the correctness of the hypotheses, since the agent does not know all the information about the environment in the beginning of the learning, clingo might not generate correct sequence of actions leading to the goals. Also if the agent has not seen enough surrounding walls, the plan of actions might be blocked by a wall that the agent has not seen.

Example 3.3.3. (Plan Execution).

Together with hypothesis, the background knowledge will used to solve for answer sets program. However, since hypothesis is not complete, there is more than one answer set at each time step. Since one of the answer sets state_at is correct, the rest will be in the exclusions in the answer set, which is used to further improve the hypothesis in the next iteration of inductive learning.

In this example, the following is the answer set program

The answer set using the hypothesis XXX is

XXX. The answer set using the improved hypothesis is XXX, Which correctly returns a sequence of actions and predicted states.

This uncorrect plan is also a source for learning a better hypothesis. As shown in Example XX, if the hypothesis is not a full hypotheses, outputs of ASP contain lots of $\text{state_at}((X, Y), T)$ at the same states. Given the agent is at one state at each time step, these duplicates are all included in exclusions, as defined in Definition ??.

3.4 Exploration

Exploration is one of the active research areas in RL, and is often discussed as a tradeoff between exploration and exploitation. While the agent exploits what is already learnt and follows the best policy and action selection so far. It also needs to explore by taking a new action to discover a new state, which might make the agent discover an even shorter path and therefore higher total rewards in the future or in the long term. One of the most commonly used strategies is ϵ -greedy strategy. As described in Chapter XXX, the agent takes a random action with a probability of ϵ , which is a hyper-parameter.

ILP(RL) planning starts once the agent reaches a goal once. However it is likely that the agent has not seen all the environment and therefore is likely to generate a sub-optimal plan. Therefore, similar to RL algorithms, the agent also has to explore a new state.

In our case, given the goal is found and the model is correct, it is likely that following the plan will maximize the total rewards. To avoid the agent from being stuck in a sub-optimal plan, the agent deliberately discards the plan and takes a random action with a probability of epsilon (which is less than 1) TODO define this mathematically.

When the agent deviates from the planning, it discovers new information, which will be added to B. Exploration is therefore necessary to make sure that the agent might discover a shorter path than the current plan, which will be demonstrated in the experiment.

Example 3.4.1. (Plan Generation). Suppose the plan of the agent is the following. Suppose the agent decides to take a random action and moves "up", which may help it discover a new state. From the new state, the agent again plans to the goal from the current state. In this case, the new plan is Sub-optimal plan -> random exploration -> optimal policy.

While statistical RL algorithms, such as Q-learning or Tile-coding explained in XX, update Q-value by a factor of alpha, ILP(RL) tends to strictly follow the plan the generated. Also it is known that model-based RL tends to get stuck in a sub-optimal if the model is incorrect, ILP(RL) also needs a exploration And since the agent does not know when the perfect hypothesis in a particular environment is fully realised, it needs to keep exploring the environment even though

This strategy may not be appropriate in cases where safety is a priority (since it is random action.)

When the agent takes a random action and moves into a new state, the agent creates a new plan from the new state and continues to move forward.

It is simple to implement.

The reason for using random exploration is that it can be used for both benchmark and ILP(RL) and thus enables us to do a fair comparison between them. In the further research, we could experiment with a more sophisticated exploration strategy, such as Boltzman approach, Count-based and Optimistic Initial value TODO REFERENCE).

After taking an random action, the agent again has a probably of epsilon for taking an random action. Throughout following the new plan, there is a small probalbility of chance that the agent takes an random action.

The current framework simply uses a simple random exploration, therefore even if the agent takes an random action and goes to a different state other than the planed one, the agent does the replan from the new state and quickly correct to the original plan path. This means it is likely that the agent of ILP(RL) only explores the adjacent cells and if there is a shorter path or new state In other words, if the shorter path is far from the current state, the agent is unlikely be able to find the new state unless epsilon value is very high.

3.5 Implementation

As shown in Figure ??, there are mainly three different components that need to be communicated: inductive learning with ILASP, planning with ASP and the external environment platform provided by VGDL with OpenAI interface. All of them are communicated through the main driver written in Python. In the following section, part of low-level implementation of each part of the framework.

3.5.1 Inductive Learning with ILASP

We use ILASP2i, a inductive learning system developed in XX. ILASP2i is an interative version of ILASP2, and is designed to scale with the numbers of examples. ILASP2i also introduces the use of context dependent examples. The latest ILASP officially available at the time of writing is ILASP3, which is designed to work on a noisy examples. Our positive examples do not contain noise, state transition positive examples, and ILASP2i was sufficient for our implemnetation. which is discussed in Section XX. Although ILASP2i is designed to work with a large number of examples, inductive learning part is the bottleneck of our framework in terms of computational time. We did a number of optimisation in order to mitigate this.

The first optimastion is the frequency of running ILASP. As already described in Definition ??, ILASP is ran only if the current hypothesis does not cover all the examples accumulated so far. Because of this, inductive learning takes place at the very early stage of learning, which is highlighted in the experiments in Chapter XX.

The next optimisation is through the command line. ILASP2i has a number of options, and we explain each option using the actual command we use to run ILASP

```
ILASP --version=2i FILENAME.las -ml=8 -nc --clingo5
--clingo "clingo5 --opt-strat=usc, stratify"
--cached-ref=PATH --max-rule-length=8
```

where,

- `--version=2i` specifies that we use ILASP2i.
- `-ml=8` specified the maximum numbers of body that each rule can have. The default length is XX.

- `-nc` means no constrains, and omits constrains from the search space. Since our target hypothesis is not a constraint, this option recudes the search space.
- `-clingo5` generates clingo 5 programs, which is faster, instead of clingo 4.3.
- `-clingo "clingo5 --opt-strat=usc,stratify"` specifies clingo executable with the specified options. `usc`, `stratify` is unsatisfiable-core base optimisation with stratification using Gringo [?], a core XXX introduced in gringo version 3. REFERENCE.
- `-cached-ref=PATH` enables the iterative mode, and keeps the output of the relevant example to a specified path, and start the learning from where it left before rather than going through all the examples.
- `-max-rule-length=8` The default maximum number is 5.

Last optimisation is specifying search space.

Complexity.

TODO the number of search space XX.

3.5.2 Planning with ASP

Planning is computed using Clingo 5.

```
clingo5 --opt-strat=usc,stratify -n 0 FILENAME.lp
--opt-mode=opt --outf=2
```

- `-clingo "clingo5 --opt-strat=usc,stratify"` specifies clingo executable with the specified options. `usc`, `stratify` is unsatisfiable-core base optimisation with stratification using Gringo [?], a core XXX introduced in gringo version 3. REFERENCE.
- `-n 0` `-n` is an abbreviation of models to specify the maximum number of answer sets to be computed. `-n 0` means to compute all answer sets.
- `--opt-mode=opt` computes optimal answer sets
- `--outf=2` makes the output in JSON¹ format

3.5.3 Environment Platform

We use the Video Game Definition Language (VGDL), which is a high-level description language for 2D video games providing a platform for computational intelligence research ([?]). The VGDL allows users to easily craft their own environments, which makes us possible to do various experiments without relying on a default environment. The VGDL platform provides an interface with OpenAI Gym ([?]), which is a commonly used benchmark platform. The base game is a simple maze as shown in Figure ???. There are 3 different types of cells: a goal cell, walls and paths. The agent can take 4 different actions: up, down, right and left. The environment is not

¹<http://json.org/>

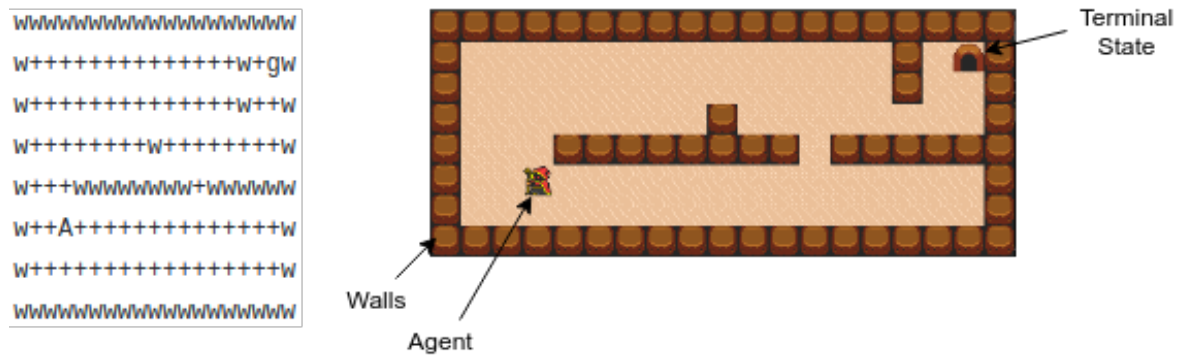


Figure 3.3: The VGDL (Video Game Definition Language) environment example

known to the agent in advance, and it attempts to find the goal by exploring the environment. In all experiments, the agent receives -1 in any states except the goal state, where it gains a reward of 10. Once the agent reaches the goal, or termination state, that episode is finished and the agent start the next episode from the starting point.

Chapter 4

Evaluation

4.1 Setting

4.1.1 Evaluation Metrics

As introduced in ??, our motivation is to improve the RL learning efficiency and capability of transfer learning. Therefore, these are the two main measurements for the performance of ILP(RL).

The learning efficiencies are measured in two different ways. First, the performance of ILP(RL) is compared with benchmarks in terms of convergence rate, which is measured in terms of the number of episodes that the agent requires to get to an optimal policy. The optimal policy can be measured in terms of the total reward that the agent gains at each episodes. Throughout the experiments, we designed the environment such that the agent receives reward of -1 for any state except the terminal state, and receives reward of + 10 for the terminal state, or the goal. For example, if the agent needs the shortest 10 actions to get to the terminal state, the maximum reward the agent could get per episode is 0 (-1 reward at each action + 10 for reaching the goal). We log the reward at each time step and calculate the total reward at each episode.

At each episode, we also measure the performance without exploration to see the pure optimal policy.

Second, the convergence of learning by ILASP is measured to see the learning curve of ILP(RL), which is defined as follows:

$$\frac{\text{The cumulative number of inductive learning per time step at episode 0}}{\text{The total number of inductive learning at all episodes}} \quad (4.1)$$

The reason we are measuring it only at episode 0 is that empirically the agent learns most of the target hypotheses within episode 0 and there is no hypothesis refinement after episode 0. This gives a normalised convergence rate of ILASP learning with the maximum 1, and we plot it across each time steps. If an inductive learning happens after episode 0, this included in the denominator, and the maximum convergence plot is strictly less than 1.

RUNTIME

4.1.2 Benchmarks

We use different benchmarks for learning evaluation and transfer learning evaluation.

For learning evaluation, we use two existing RL methods as benchmarks: Q-learning and tile-coding. Q-learning is widely used RL technique, and given the environments used for the experiments are discrete and deterministic, this method is sufficient for our experiments. XX the Q-values are initialised as XX. (Optimistic and pessimistic initialisation.)

Another benchmark is tile coding, which is a type of linear function approximation techniques described in Chapter XX. The reason for using an extra benchmark is that the performance comparison of ILP(RL) with q-learning might not be a fair comparison, since ILP(RL) has one extra assumption: the agent knows surrounding information (whether there are walls in adjacent cells), which is not a common assumption for Q-learning. Thus we incorporate the same surrounding information as features, and update the weights of each feature as a learning. We compare the performance of ILP(RL) with these two methods.

TODO Details of tile-coding configuration

For transfer learning evaluation,

4.1.3 Parameters

Parameter	ILP(RL)	Benchmarks
The number of episode	100	100
Time steps per episode	250	250
The number of experiments	30	30
Alpha	N/A	0.5
Epsilon	0.1	0.1

Table 4.1: List of parameters used in the experiments

All the matrices used in the experiments are summarised in Table ???. The number of episode is set such that both the benchmarks as well as ILP(RL) eventually reaches the optimal policy. The number of time steps should be sufficient for the both algorithms to reach the terminal state by the random exploration, which we set 250 time steps for all experiments. If the agent does not find the terminal state by 250 time steps, the agent receives the reward of -250 and start the next episode from the starting point. If the agent reaches the terminal state within 250 time steps, it receives the reward of 10 and start the next episode with the same starting point.

Starting point is fixed every episode. We conducted several experiments using different environments to highlight each aspect of the algorithm.

Each experiment is conducted 30 times and the performance is averaged across the experiments, since the performance of the agent is affected by the randomness of the exploration, and ILP(RL) is highly dependent on how quickly the agent finds the goal.

4.2 Learning Evaluation

4.2.1 Experiment Result 1

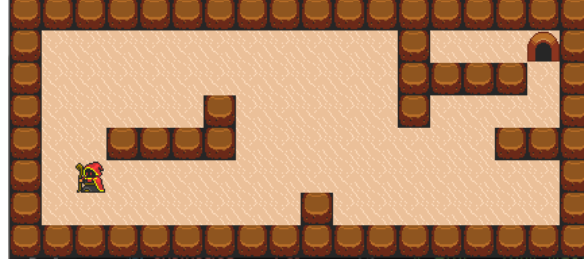


Figure 4.2: Game environment for experiment 1

The purpose of the first experiment is to highlight how ILP(RL) agent learns hypotheses in ILASP. The environment are designed as a simple maze where the goal is located the right uppper corner as shown in Figure ??.

The shortest path is 18 steps, thus the maximum total reward the agent could gain is -8.

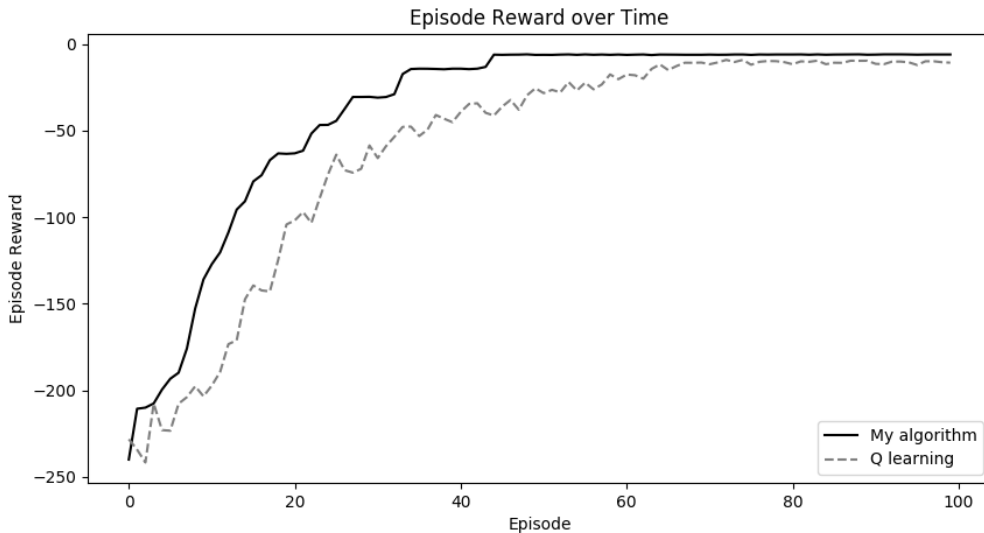


Figure 4.3: Result of experiment 1 (learning curve)

Figure ?? shows the traning performance between ILP(RL) and Q-learning. The convergence rate of ILP(RL) is faster than Q-learning: ILP(RL) reaches the maximum reward between 40 and 50 episodes, whereas Q-learning reaches the same level at between 60 and 70 episodes. This is because unlike Q-learning where the value function is updated with the rate of α , whereas ILP(RL) gradually builds the model of the environment and use the background knowledge to accurately plan. This result is also consistent with the general notion that model-based learning (ILP(RL)) is more data-efficient than model-free learning (Q-learning). The same trend is also

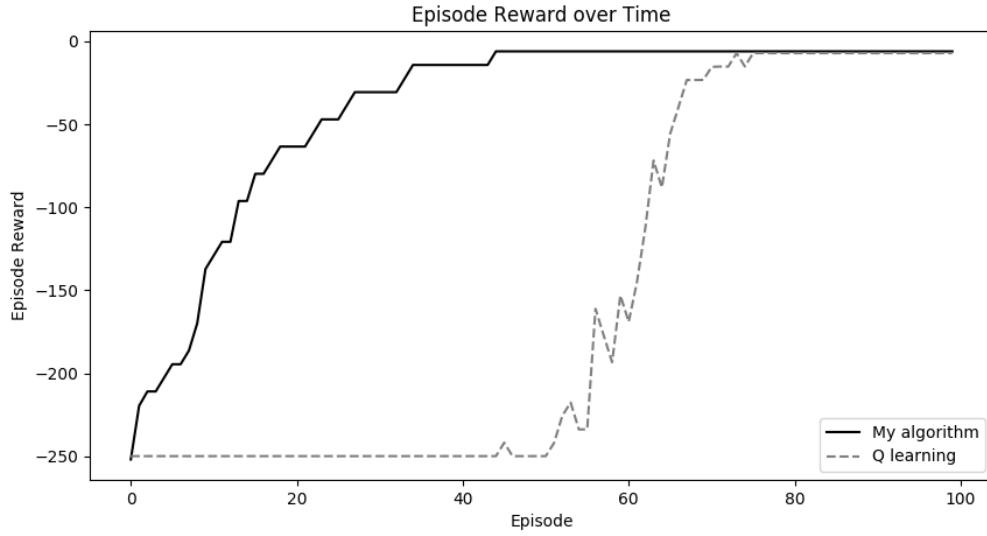


Figure 4.4: Result of experiment 1 (performance)

shown in Figure ??, where we measure only the performance of the policy without random exploration.

Overall this results shows that ILP(RL) converges to the optimal policy faster than benchmarks in a simple scenarios, achieving more data-efficient learning.

In addition to the data-efficient learning, what the agent has learnt with ILP(RL) is expressive. Learnt hypotheses are shown in ??, which is the rule of the game and easy to understand for human users. Since the learnt hypothesis is a general concept, which can be used in a different environmet. This transfer learning capability is also described in Experiement 3 and 4.

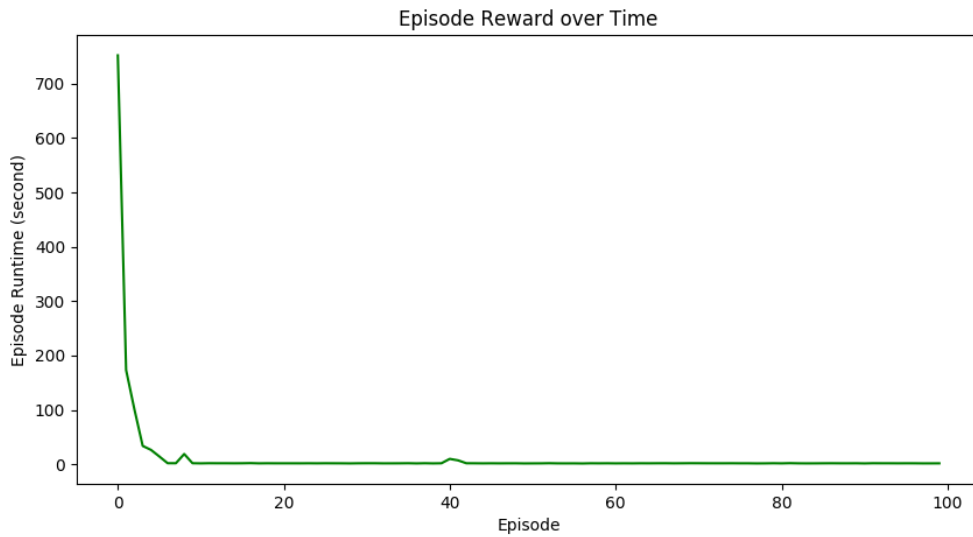


Figure 4.5: Runtime comparision

```

state_after(V1) :- adjacent(right, V0, V1), state_before(V1), action(right), wall(V0).
state_after(V0) :- adjacent(right, V0, V1), state_before(V0), action(left), wall(V1).
state_after(V1) :- adjacent(down, V0, V1), state_before(V1), action(down), wall(V0).
state_after(V1) :- adjacent(up, V0, V1), state_before(V1), action(up), wall(V0).
state_after(V0) :- adjacent(right, V0, V1), state_before(V1), action(right), not wall(V0).
state_after(V0) :- adjacent(left, V0, V1), state_before(V1), action(left), not wall(V0).
state_after(V0) :- adjacent(down, V0, V1), state_before(V1), action(down), not wall(V0).
state_after(V0) :- adjacent(up, V0, V1), state_before(V1), action(up), not wall(V0).

```

(4.2)

In addition, we plot the learning convergence for ILASP at episode 0 in Figure ??, measured in terms of the number of hypothesis refinement to reach the final hypothesis as shown in ??. This shows that the agent quickly learns the hypothesis at the episode 0. The reason that the agent reaches the maximum reward at between 40 and 50 episodes, is mostly dependent on how quickly the agent finds the goal location, which enables it to plan. Since our exploration strategy is expilon random choice, there is a promissing that a better exploration strategy further accelerates the learning process.

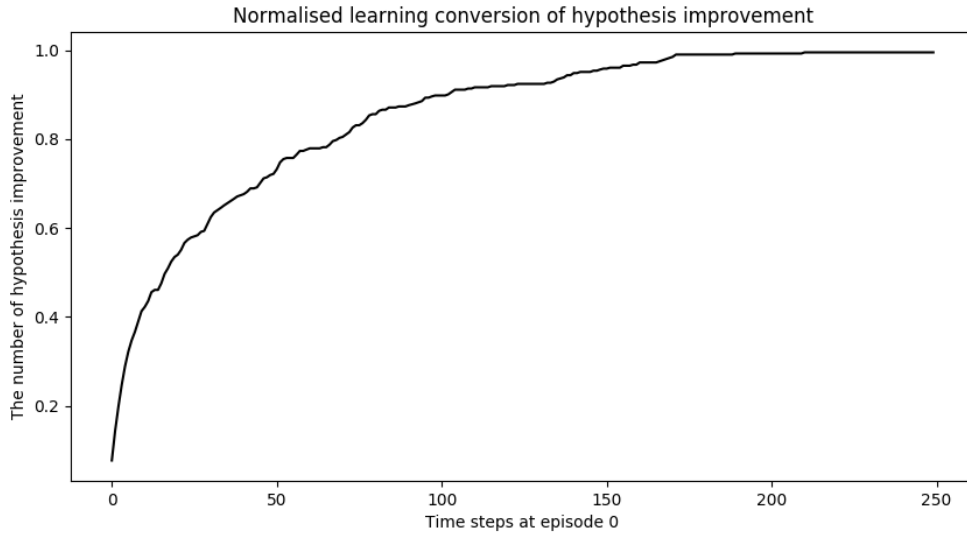


Figure 4.6: Normalised learning convergence by ILASP for experiment 1

4.2.2 Experiment Result 2

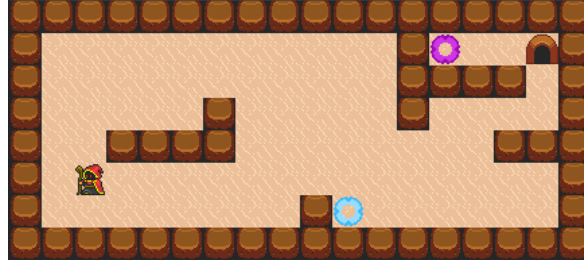


Figure 4.7: Game environment for experiment 2

Experiment 2 was conducted to see if the agent find a optimal path of using a tele-port. In the environment shown in Figure ??, there are two ways to reach the goal: using a normal path to get the goal located on the top right corner, or using a tel-port. The environment is designed such that using a teleport is a shorter path and therefore gives higher total reward. Compared to Experiment 1, two extra search spaces and concepts are added as follow:

```
#modeb(1, link_start(var(cell)), (positive)).
#modeb(1, link_dest(var(cell)), (positive)).
```

Where teleport links are added to the environment. The teleport link is one-way: link_start takes the agent to link_dest, but link_dest does not take the agent back to link_start. The allows ILASP to learn additional hypothesis. The full learning task for this experiment is in Appendix XX.

Once the agent steps onto a state where link_start is located, it gets two positive experiences. In this game environment, the agent moves two cells in one time step instead of one cell per time step.

Also link_start and link_dest need to be stored in background knowledge rather than as contex examples, because ILASP needs to learn different hypothesis for link and non-link case. link locations need to be available for all positive examples so that ILASP correctly learn non-link, which is shown in Figure XX below.

The training performance shown in XX, which converges faster than XX.

```
state_after(V1) :- link_dest(V1).
state_after(V0) :- link_dest(V0), state_before(V0), action(right).
state_after(V1) :- adjacent(left, V0, V1), state_before(V0), action(right), not wall(V1).
state_after(V0) :- adjacent(left, V0, V1), state_before(V1), action(left), not wall(V0).
state_after(V1) :- adjacent(up, V0, V1), state_before(V0), action(down), not wall(V1).
state_after(V0) :- adjacent(up, V0, V1), state_before(V1), action(up), not wall(V0).
state_after(V1) :- adjacent(left, V0, V1), state_before(V1), action(left), wall(V0).
state_after(V1) :- adjacent(down, V0, V1), state_before(V1), action(down), wall(V0).
state_after(V1) :- adjacent(up, V0, V1), state_before(V1), action(up), wall(V0).
```

(4.3)

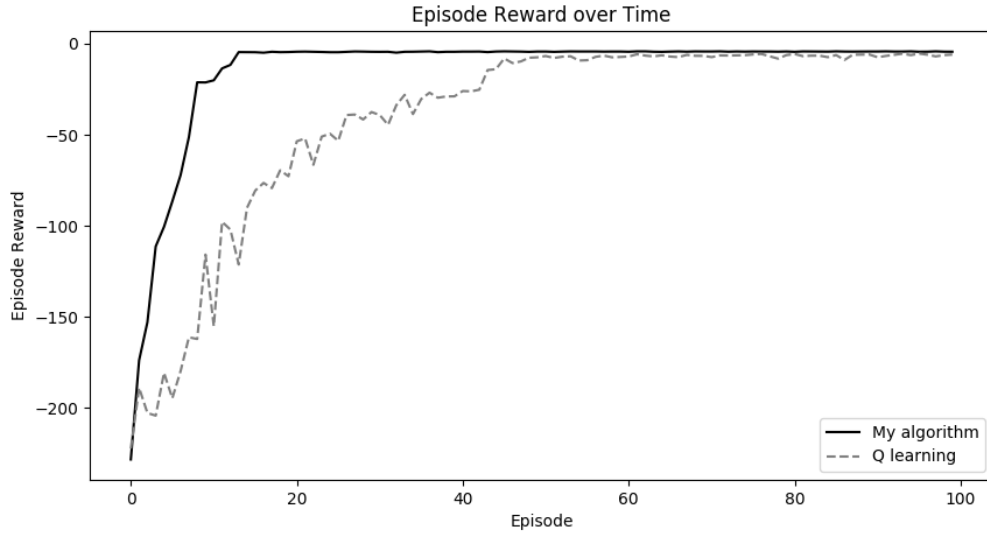


Figure 4.8: Result of experiment 2 (learning curve)

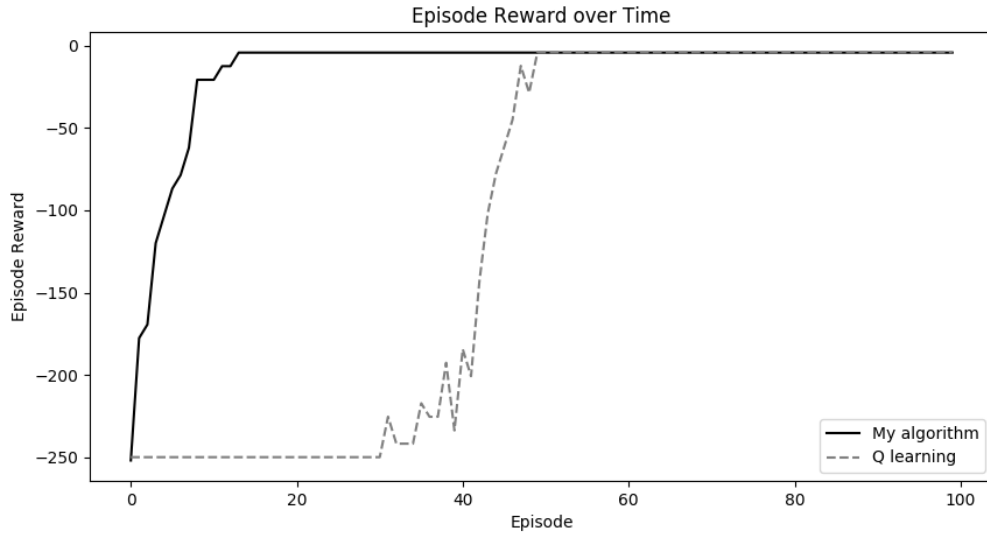


Figure 4.9: Result of experiment 2 (performance)

To highlight the learning the new concept of teleport link, Figure ?? is an intermediate incomplete hypothesis learnt by ILASP. These hypotheses are generated just after the agent steps onto the link. However, the first hypothesis says when `link_dest` is available `state_after` is true. Since `link_dest` is available in background knowledge rather than context, when solving for answer sets to generate a plan, it generates incorrect `state_after` at every time step. However, as shown in Algorithms XX, these generated `state_after` are all incorrect and therefore will be added to exclusions of the next positive examples. These exclusions will later refine hypotheses and results in Figure ??, the final complete hypotheses.

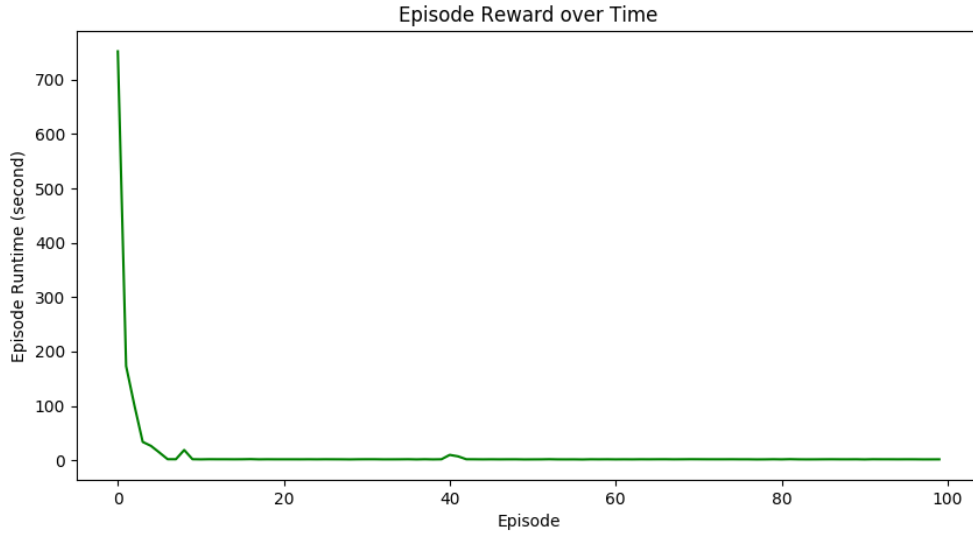


Figure 4.10: Runtime comparison

Learnt hypotheses are as follow:

```

state_after(V1) :- link_start(V0), link_dest(V1), state_before(V0).
state_after(V0) :- link_dest(V0), state_before(V0), action(right).
state_after(V1) :- adjacent(left, V0, V1), state_before(V0), action(right), not wall(V1).
state_after(V0) :- adjacent(left, V0, V1), state_before(V1), action(left), not wall(V0).
state_after(V1) :- adjacent(up, V0, V1), state_before(V0), action(down), not wall(V1).
state_after(V0) :- adjacent(up, V0, V1), state_before(V1), action(up), not wall(V0).
state_after(V1) :- adjacent(left, V0, V1), state_before(V1), action(left), wall(V0).
state_after(V1) :- adjacent(down, V0, V1), state_before(V1), action(down), wall(V0).
state_after(V1) :- adjacent(up, V0, V1), state_before(V1), action(up), wall(V0).

```

(4.4)

Compared the Experiment 1, there are two new hypotheses due to the presence of the teleport links. These learnt hypotheses are also applicables to an environment where there is no link, such as a game in experiment 1. In this case, the first two hypotheses in Figure XX are never be used since the body predicates relating to `link_start(V0)`, `link_dest(V1)` are never be satisfied.

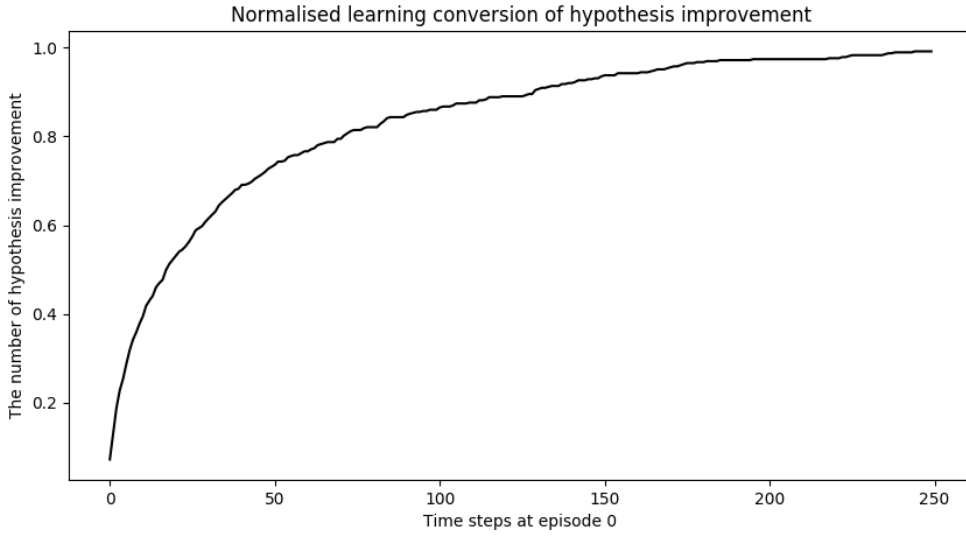


Figure 4.11: Normalised learning convergence by ILASP for experiment 2

4.3 Transfer Learning Evaluation

4.3.1 Experiment Result 3

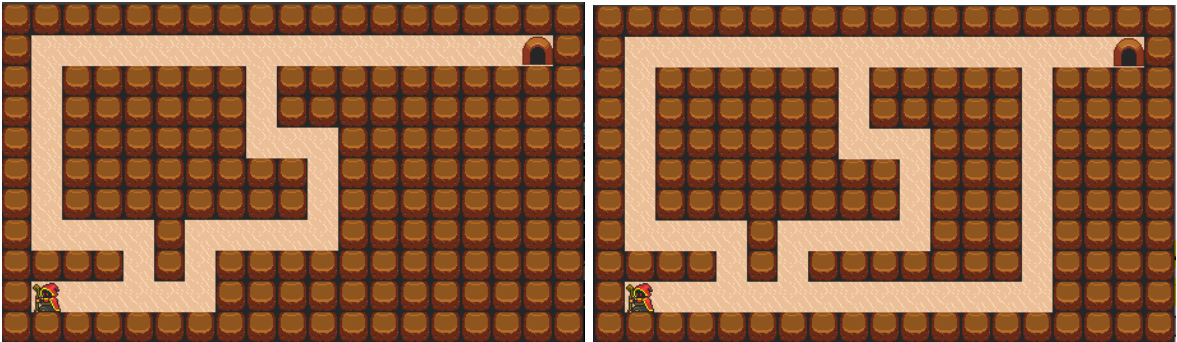


Figure 4.12: Game environment for experiment 3: before (left) and after (right) transfer learning

In Experiment 3, we investigated the potentials of transfer learning between similar environments. We trained the agent using the environment on the left in Figure ??, and transfer the learnt hypothesis as well as positive examples to a new environment. The learnt hypothesis is valid move of the game and a general concept that is applicable to any similar games. Positive examples are also transferred since if there is a new concept that the agent needs to learn in a new environment, the agent needs to refine the hypothesis by running ILASP, thus the all the positice examples are also transferred as well as hypotheses. Background knowledge are not transferred since these information are different in a new environment. The agent starts with an empty background knowledge in the new environment and gradually collects them as it explore the environment. The goal position is the same as in the

first game and we assume that the transferred agent already knows the goal location, but the routes to the goal may be different. While this is a limited transfer learning since the goal position is known in advance, this is still a useful transfer in cases where the rest of the environment changes. In this experiment, we compare the two learning performance: one with transfer learning and one without it. The result is shown in Figure ?? and ??.

These are the hypotheses we are transferring to a new environment. Since the complete hypothesis is already known to the agent, it can do planning from the beginning.

```

state_after(V0) :- adjacent(right, V0, V1), state_before(V1), action(right), not wall(V0).
state_after(V0) :- adjacent(left, V0, V1), state_before(V1), action(left), not wall(V0).
state_after(V1) :- adjacent(down, V0, V1), state_before(V0), action(up), not wall(V1).
state_after(V0) :- adjacent(down, V0, V1), state_before(V1), action(down), not wall(V0).
state_after(V1) :- adjacent(right, V0, V1), state_before(V1), action(right), wall(V0).
state_after(V1) :- adjacent(left, V0, V1), state_before(V1), action(left), wall(V0).
state_after(V0) :- adjacent(up, V0, V1), state_before(V0), action(down), wall(V1).
state_after(V1) :- adjacent(up, V0, V1), state_before(V1), action(up), wall(V0).

```

(4.5)

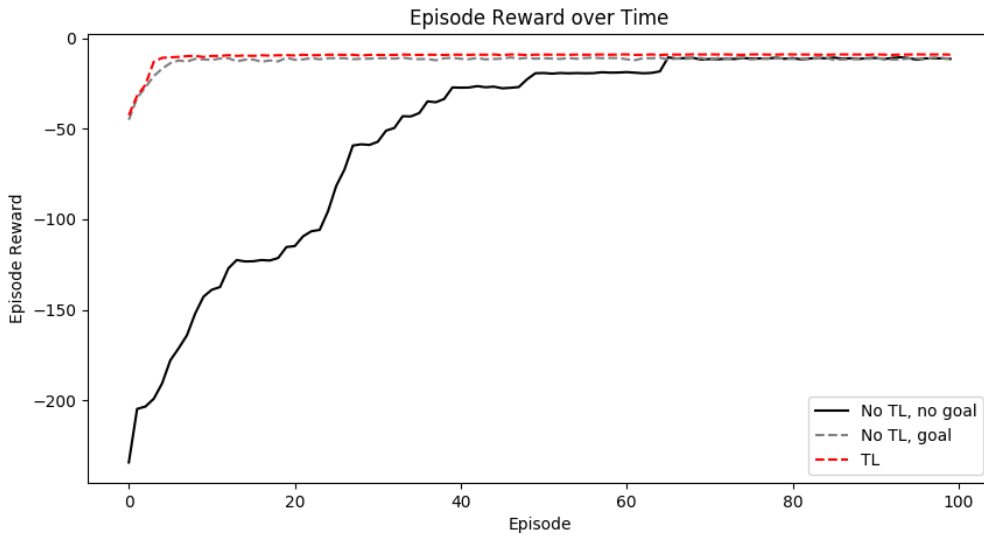


Figure 4.13: Result of experiment 3 (learning curve)

4.3.2 Experiment Result 4

Finally the hypothesis is transferred to a new environment where there is a new concept that did not exist in the first environment and therefore the agent needs to learn it after the hypothesis is transferred.

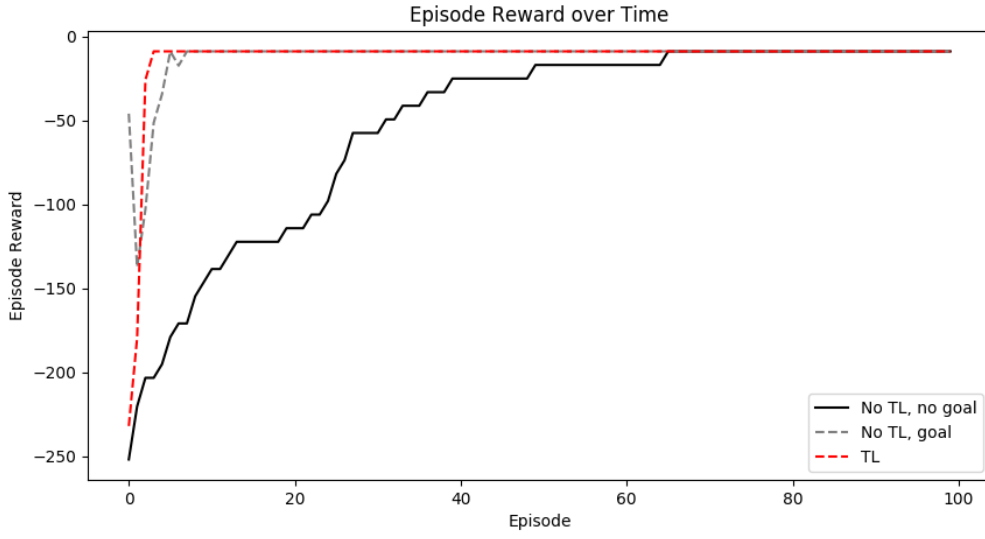


Figure 4.14: Result of experiment 3 (performance)

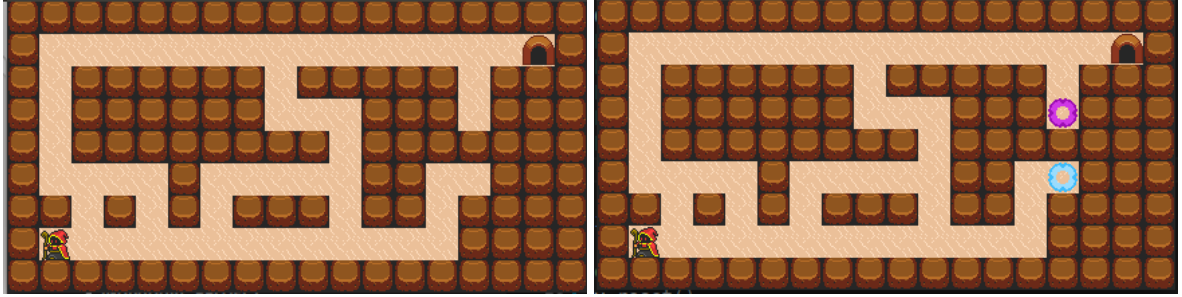


Figure 4.15: Game environment for experiment 4: before (left) and after (right) transfer learning

```

state_after(V1) :- link_start(V0), link_dest(V1), state_before(V0).
state_after(V1) :- adjacent(left, V0, V1), state_before(V0), action(right), not wall(V1).
state_after(V0) :- adjacent(left, V0, V1), state_before(V1), action(left), not wall(V0).
state_after(V1) :- adjacent(up, V0, V1), state_before(V0), action(down), not wall(V1).
state_after(V0) :- adjacent(up, V0, V1), state_before(V1), action(up), not wall(V0).
state_after(V0) :- adjacent(left, V0, V1), state_before(V0), action(right), wall(V1).
state_after(V1) :- adjacent(left, V0, V1), state_before(V1), action(left), wall(V0).
state_after(V0) :- adjacent(up, V0, V1), state_before(V0), action(down), wall(V1).
state_after(V1) :- adjacent(up, V0, V1), state_before(V1), action(up), wall(V0).

```

(4.6)

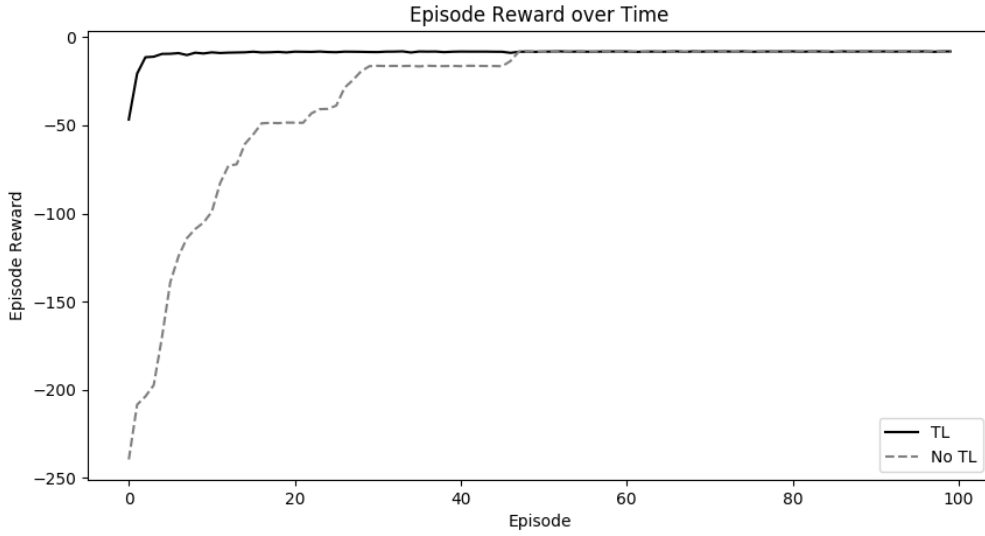


Figure 4.16: Result of experiment 4 (learning curve)

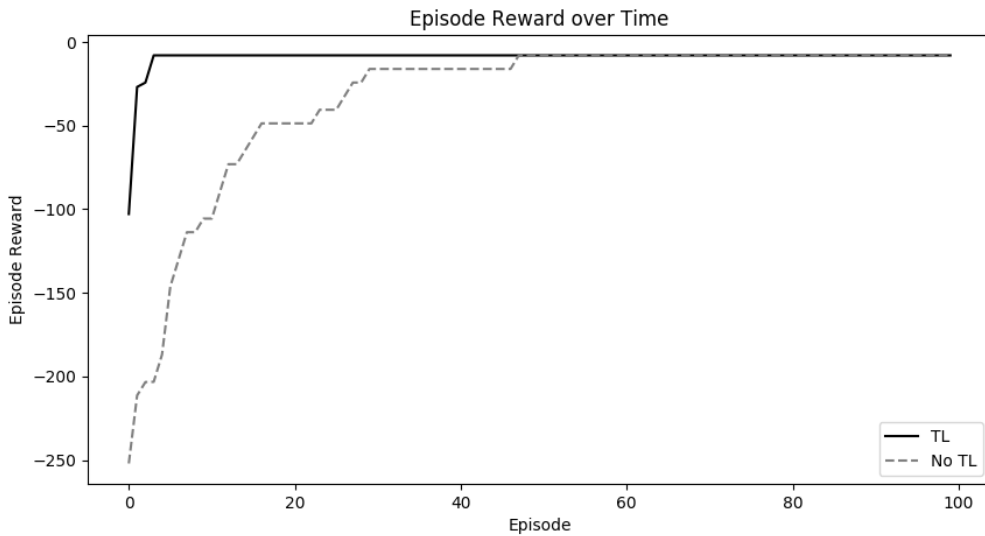


Figure 4.17: Result of experiment 4 (performance)

4.4 Discussion

Although this is the first time and inductive logic programming is applied into reinforcement learning and there are new interesting property for ILP(RL), there are two major limitations with the current framework.

4.4.1 Scalability

The first limitation is scalability. As pointed in XXX or XXX, ILP framework is known to be less scalable. The current framework is tested in a relatively simple environ-

ments, and proven to be work better than RL algorithm in terms of the number of episodes that is needed to converge to an optimal policy. However, learning in each episode is relatively slower than that of RL. This is shown in XXX, which shows average learnint time for ILASP.

This limitation is theoretically discussed in XXX, where the complexity of deciding satisfiability is \sum_2^P -complete. Since there is no negative examples used in our current framework, the complexity is NP-complete.

Whereas Q-learning update value function in the same way whether there is a new concept such as teleport links.

Figure XXX shows traning times for Experiment 1 and 2.

ILASP learning time for Experiment 1 and 2.

Unlike existing reinforcement learning, out algorithm refines hypothesis at every time steps within the same episode. Thus even though the efficiency in terms of the number of iteration is higher, training time within each iteration tends to be lower.

4.4.2 Flexibility

While most of existing reinforcement learning works in different kinds of environment without pre-configuration, our algorithm needs to define search space for learning hypothesis. As explained in the experiment 3, it was necessary to add two extra modeb before training. Thus the algorithm may not be feasible in cases where these learning concepts were unknown or difficult to define. In addition, not only it needs search space, surrounding information is assumed to be known to the agent. While this assumption may be reasonable in many cases, this is not common in traditional reinforcement learning setting.

The current framework does not make use of rewards the agent collects and mainly uses the location of the goal for planning. In some senarios, there may not be a termination state (goal) and instead there may be a different purpose to gain these rewards. Since the current implementation is dependent on finding the goal for planning rather than maximizing total rewards, which is the common objective for most of RL algorithms, the application of the current framework may be limited to particular types of problems.

Another question remains to how to extend the framework to more realistic senarios. RL works in more complex environments such as 3D or real physical environment, whereas the experiences of the agent in the current framework need to be expressed as ASP syntax, thus expressing continuous states rather than discrete states is challenging.

Chapter 5

Related Work

In this section, I summarise recent studies related to symbolic (deep) reinforcement learning.

[?] introduced Deep Symbolic Reinforcement Learning (DSRL), a proof of concept for incorporating symbolic front end as a means of converting low-dimensional symbolic representation into spatio-temporal representations, which will be the state transitions input of reinforcement learning. DSRL extracts features using convolutional neural networks (CNNs) [?] and an autoencoder, which are transformed into symbolic representations for relevant object types and positions of the objects. These symbolic representations represent abstract state-space, which are the inputs for the Q-learning algorithm to learn a policy on this particular state-space. DSRL was shown to outperform DRL in stochastic variant environments. However, there are a number of drawbacks to this approach. First, the extraction of the individual objects was done by manually defined threshold of feature activation values, given that the games were geometrically simple. Thus this approach would not scale in geometrically complex games. Second, using deep neural network front-end might also cause a problem. As demonstrated in [?], a single irrelevant pixel could dramatically influence the state through the change in CNNs. In addition, while proposed method successfully used symbolic representations to achieve more data-efficient learning, there is still the potential to apply symbolic learning to those symbolic representations to further improve the learning efficiency, which is what we attempt to do in this paper. [?] further explored this symbolic abstraction approach by incorporating the relative position of each object with respect to every other object rather than absolute object position. They also assign priority to each Q-value function based on the relative distance of objects from an agent.

[?] added relational reinforcement learning, a classical subfield of research aiming to combining reinforcement learning with relational learning or Inductive Logic Programming, which added more abstract planning on top of DSRL approach. The new mode was then applied to much more complicate game environment than that used by [?]. This idea of adding planning capability align with our approach of using ILP to improve a RL agent. We explore how to effectively learn the model of the environment and effectively use it to facilitate data-efficient learning and transfer learning capability.

Another approach for using symbolic reinforcement learning is storing heuristics

expressed by knowledge bases [[?]]. An agent learns the concept of *Hierarchical Knowledge Bases (HKBs)* (which is defined in more details in [?] and [?]) at every iteration of training, which contain multiple rules (state-action pairs). The agent then is able to decide itself when it should exploit the heuristic rather than the state-action pairs of the RL using *Strategic Depth*. This approach effectively uses the heuristic knowledge bases, which acts as a sym-symbolic model of the game.

Another field related to our research is the combining of ASP and RL. The original concept of combining ASP and RL was in [?], where they developed an algorithm that efficiently finds the optimal solution of an MDP of non-stationary domains by using ASP to find the possible trajectories of an MDP. This approach focused more on efficient update of the Q function rather than inductive learning. In order to find stationary sets, an extension of ASP called BC^+ , an action language, was used. BC^+ can directly translate the agent's actions into ASP form, and provide sequences of actions in answer sets.

Chapter 6

Conclusion

6.1 Summary of Work

In this paper, we developed a new RL algorithm by applying ILP to develop a new learning process. We used a latest ILP algorithm called ILASP, Learning from Answer Set Program to iteratively improve hypotheses.

6.2 Further Research

Having stated the limitations of the current framework, we discuss some of the possible improvements and further research in this section.

This is a proof of concept, a new type of model-based reinforcement learning using inductive logic programming.

More complicated environment

More general transfer learning.

Only empirically correct, no theoretical guarantee

Dynamic environment like moving enemy etc.

Non-stationality possible to be handled??

Our approach is similar to experience replay ??

More promising approach is to combine RL algorithm and using ILP approach to complement each other, rather than replacing the bellman equation altogether.

6.2.1 Value Iteration Approach

The proposed architecture is not finalised and will be reviewed regularly as we do more research. More research needs to be devoted to finalising the overall architecture, and the following issues in particular need to be considered.

6.2.2 Weak Constraint

- Further investigation of whether ILASP can learn the concept of adjacent, which is crucial concept to know in any environment.

- How to generalise the agent's model when the environment changes. The new environment could be very similar to the previous one, or could be a completely different environment thus the agent should create a new internal model rather than generalising the existing model.
- The current proposed architecture is based on Dyna with simulated experiences. However, this might not be the best overall architecture, and the feasibility of using simulated experience with the learnt model with ILASP needs to be further investigated.
- Possibility of using other representational concepts such as *Predictive Representations of State* or *Affordance* [?] for the agent's learning task. These concept have not been considered at the moment, but could help better transfer learning.
- Preparation for a backup plan in case ILASP approach does not work, so that the researchs feasible within 3 months of the research period.

6.2.3 Generalisation of the Current Approach

Learning the concept of being adjacent

Appendix A

Ethics

To our best knowledge, there is no particular ethical considerations for this particular research listed in Table XX. However, the field of RL is an active research area and has been increasingly applied in industries these days, and therefore ethical frameworks for RL will be required for both academic research as well as industry applications.

Also the experiments of our algorithm were conducted using a game environment rather than real applications (e.g. robots).

Rather compared to existing reinforcement learning methodologies.

Also there are a number of AI researchers discussing the ethics of AI in general. Since RL is considered to be part of AI research, these ethical considerations might be also applied.

	Yes	No
Section 1: HUMAN EMBRYOS/FOETUSES		
Does your project involve Human Embryonic Stem Cells?		✓
Does your project involve the use of human embryos?		✓
Does your project involve the use of human foetal tissues / cells?		✓
Section 2: HUMANS		
Does your project involve human participants?		✓
Section 3: HUMAN CELLS / TISSUES		
Does your project involve human cells or tissues? (Other than from Human Embryos/Foetuses i.e. Section 1)?		✓
Section 4: PROTECTION OF PERSONAL DATA		
Does your project involve personal data collection and/or processing?		✓
Does it involve the collection and/or processing of sensitive personal data (e.g. health, sexual lifestyle, ethnicity, political opinion, religious or philosophical conviction)?		✓
Does it involve processing of genetic information?		✓

Does it involve tracking or observation of participants? It should be noted that this issue is not limited to surveillance or localization data. It also applies to Wan data such as IP address, MACs, cookies etc.		✓
Does your project involve further processing of previously collected personal data (secondary use)? For example Does your project involve merging existing data sets?		✓
Section 5: ANIMALS		
Does your project involve animals?		✓
Section 6: DEVELOPING COUNTRIES		
Does your project involve developing countries?		✓
If your project involves low and/or lower-middle income countries, are any benefit-sharing actions planned?		✓
Could the situation in the country put the individuals taking part in the project at risk?		✓
Section 7: ENVIRONMENTAL PROTECTION AND SAFETY		
Does your project involve the use of elements that may cause harm to the environment, animals or plants?		✓
Does your project deal with endangered fauna and/or flora /protected areas?		✓
Does your project involve the use of elements that may cause harm to humans, including project staff?		✓
Does your project involve other harmful materials or equipment, e.g. high-powered laser systems?		✓
Section 8: DUAL USE		
Does your project have the potential for military applications?		✓
Does your project have an exclusive civilian application focus?		✓
Will your project use or produce goods or information that will require export licenses in accordance with legislation on dual use items?		✓
Does your project affect current standards in military ethics e.g., global ban on weapons of mass destruction, issues of proportionality, discrimination of combatants and accountability in drone and autonomous robotics developments, incendiary or laser weapons?		✓
Section 9: MISUSE		
Does your project have the potential for malevolent/criminal/terrorist abuse?		✓
Does your project involve information on/or the use of biological-, chemical-, nuclear/radiological-security sensitive materials and explosives, and means of their delivery?		✓

Does your project involve the development of technologies or the creation of information that could have severe negative impacts on human rights standards (e.g. privacy, stigmatization, discrimination), if misapplied?		✓
Does your project have the potential for terrorist or criminal abuse e.g. infrastructural vulnerability studies, cybersecurity related project?		✓
Section 10: LEGAL ISSUES		
Will your project use or produce software for which there are copyright licensing implications?		✓
Will your project use or produce goods or information for which there are data protection, or other legal implications?		✓
Section 11: OTHER ETHICS ISSUES		
Are there any other ethics issues that should be taken into consideration?		✓

Table A.1: Ethics Checklist

Appendix B

Learning tasks

This is the full learning task for ILASP in the experiment 1.

```
state_after(V1) :- link_dest(V1).
cell((0..7, 0..6)).
adjacent(right, (X+1,Y),(X,Y)):- cell((X,Y)), cell((X+1,Y)).
adjacent(left,(X,Y), (X+1,Y)) :- cell((X,Y)), cell((X+1,Y)).
adjacent(down, (X,Y+1),(X,Y)) :- cell((X,Y)), cell((X,Y+1)).
adjacent(up, (X,Y), (X,Y+1)) :- cell((X,Y)), cell((X,Y+1)).
#modeh(state_after(var(cell))).
#modeb(1, adjacent(const(action), var(cell), var(cell))).
#modeb(1, state_before(var(cell)), (positive)).
#modeb(1, action(const(action)),(positive)).
#modeb(1, wall(var(cell))).
#max_penalty(50).
#constant(action, right).
#constant(action, left).
#constant(action, down).
#constant(action, up).
```

Appendix C

Answer Set Program

This is the full learning task for ILASP in the experiment 1. The syntax and time are added for planning purpose.

TODO put comment on the code

```
1{action(down,T); action(up,T); action(right,T); action(left,T); action(non,T)}1 :-  
time(T), not finished(T).
```

```
#show state_at/2.
```

```
#show action/2.
```

```
finished(T):- goal(T2), time(T), T <= T2.
```

```
goal(T):- state_at((5, 1), T), not finished(T-1).
```

```
goalMet:- goal(T).
```

```
:- not goalMet.
```

```
time(0..30).
```

```
cell((0..6, 0..5)).
```

```
#minimize1, X, T: action(X,T).
```

```
adjacent(right, (X+1,Y),(X,Y)) :- cell((X,Y)), cell((X+1,Y)).
```

```
adjacent(left,(X,Y), (X+1,Y)) :- cell((X,Y)), cell((X+1,Y)).
```

```
adjacent(down, (X,Y+1),(X,Y)) :- cell((X,Y)), cell((X,Y+1)).
```

```
adjacent(up, (X,Y), (X,Y+1)) :- cell((X,Y)), cell((X,Y+1)).
```

```
state_at((1, 4), 3).
```