

# 二叉树与分治法

## Binary Tree & Divide Conquer

课程版本 v4.0    主讲 令狐冲



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官网: <http://www.jiuzhang.com>

- 时间复杂度训练 II
- 二叉树的遍历算法 Traverse in Binary Tree
  - Preorder / Inorder / Postorder
- 
- 二叉树的深度优先搜索 DFS in Binary Tree
  - 遍历问题 Preorder / Inorder / Postorder
  - 分治算法 Introduce Divide Conquer Algorithm
  - 非递归 遍历法 分治法 Non-recursion vs Traverse vs Divide Conquer
  - 二叉搜索树 Binary Search Tree
    - Insert / Remove / Find / Validate

# Time Complexity Training II

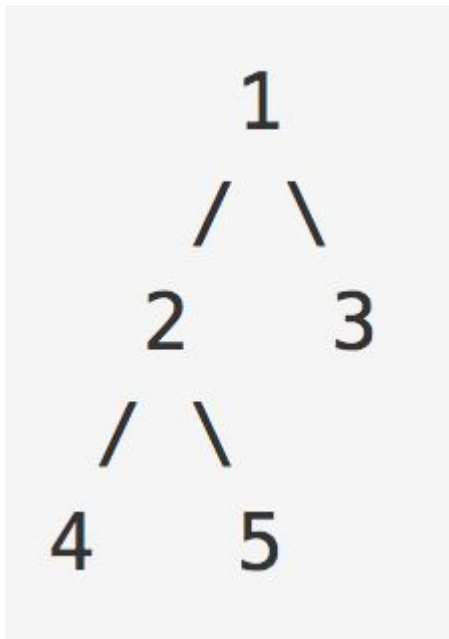
通过 $O(n)$ 的时间，把 $n$ 的问题，变为了两个 $n/2$ 的问题，复杂度是多少？

通过 $O(1)$ 的时间，把 $n$ 的问题，变成了两个 $n/2$ 的问题，复杂度是多少？



# Traverse a Binary Tree

- Preorder 前序遍历
  - 1 245 3 根左右
- Inorder 中序遍历
  - 425 1 3 左根右
- Postorder 后序遍历
  - 452 3 1 左右根



# Traverse a Binary Tree

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- Preorder:
  - <http://www.lintcode.com/problem/binary-tree-preorder-traversal/>
  - <http://www.jiuzhang.com/solutions/binary-tree-preorder-traversal/>
- Inorder
  - <http://www.lintcode.com/en/problem/binary-tree-inorder-traversal/>
  - <http://www.jiuzhang.com/solutions/binary-tree-inorder-traversal/>
- Postorder:
  - <http://www.lintcode.com/en/problem/binary-tree-postorder-traversal/>
  - <http://www.jiuzhang.com/solutions/binary-tree-postorder-traversal/>

# Divide Conquer Algorithm

- Traverse vs Divide Conquer
  - They are both Recursion Algorithm
  - Result in parameter vs Result in return value
  - Top down vs Bottom up
- Merge Sort / Quick Sort
- 90% Binary Tree Problems!

DFS 深度优先搜索

用递归实现

用非递归实现

遍历法

分治法

# 独孤九剑 —— 破枪式

碰到二叉树的问题，就想想整棵树在该问题上的结果  
和左右儿子在该问题上的结果之间的联系是什么

# Maximum Depth of Binary Tree

<http://www.lintcode.com/problem/maximum-depth-of-binary-tree/>  
<http://www.jiuzhang.com/solutions/maximum-depth-of-binary-tree/>

Divide Conquer vs Traverse



# 令狐大师兄手把手带你写代码

<http://www.lintcode.com/en/problem/binary-tree-paths/>

<http://www.jiuzhang.com/solutions/binary-tree-paths/>

# Minimum Subtree

<http://www.lintcode.com/en/problem/minimum-subtree/>

<http://www.jiuzhang.com/solutions/minimum-subtree/>

Traverse + Divide Conquer

课后作业: 只用 Divide Conquer 来实现

# 休息5分钟

Take a break

# Result Type

```
class ResultType { int var1, var2; }
```

# Balanced Binary Tree

<http://www.lintcode.com/problem/balanced-binary-tree/>

<http://www.jiuzhang.com/solutions/balanced-binary-tree/>

When we need ResultType?

# Subtree with Maximum Average

<http://www.lintcode.com/problem/subtree-with-maximum-average/>

<http://www.jiuzhang.com/solutions/subtree-with-maximum-average/>

# Flatten Binary Tree to Linked List

<http://www.lintcode.com/problem/flatten-binary-tree-to-linked-list/>

<http://www.jiuzhang.com/solutions/flatten-binary-tree-to-linked-list/>

# Lowest Common Ancestor

<http://www.lintcode.com/problem/lowest-common-ancestor/>

<http://www.jiuzhang.com/solutions/lowest-common-ancestor/>

with parent pointer vs no parent pointer

follow up: LCA II & III



# Binary Tree Longest Consecutive Sequence

<http://www.lintcode.com/problem/binary-tree-longest-consecutive-sequence/>

<http://www.jiuzhang.com/solutions/binary-tree-longest-consecutive-sequence/>

follow up: BT LCS II & III

# Binary Tree Path Sum I && II && III

<http://www.lintcode.com/problem/binary-tree-path-sum/>

<http://www.lintcode.com/problem/binary-tree-path-sum-ii/>

<http://www.lintcode.com/problem/binary-tree-path-sum-iii/>

# Binary Search Tree

二叉查找树，简称“BST”

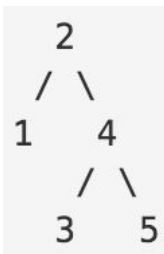
又名“二叉搜索树”“排序二叉树”

- 从定义出发:

- 左子树都比根节点小
- 右子树都不小于根节点

- 从效果出发:

- 中序遍历 in-order traversal 是“**不下降**”序列
- 如图, 中序遍历为 1 2 3 4 5



- 性质:

- 如果一棵二叉树的中序遍历不是“不下降”序列, 则一定不是BST
- 如果一棵二叉树的中序遍历是不下降, 也未必是BST
  - 比如下面这棵树就不是 BST, 但是它的中序遍历是不下降序列。
  - 1
  - / \
  - 1 1

# Validate Binary Search Tree

<http://www.lintcode.com/problem/validate-binary-search-tree/>

<http://www.jiuzhang.com/solutions/validate-binary-search-tree/>

traverse vs divide conquer

# Convert Binary Search Tree to Doubly Linked List

<http://www.lintcode.com/problem/convert-binary-search-tree-to-doubly-linked-list/>

<http://www.jiuzhang.com/solutions/convert-binary-search-tree-to-doubly-linked-list/>

## Related Questions

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- Binary Search Tree Iterator
- <http://www.lintcode.com/problem/binary-search-tree-iterator>
- <http://www.jiuzhang.com/solutions/binary-search-tree-iterator>
- In-order Successor in Binary Search Tree
- <http://www.lintcode.com/problem/inorder-successor-in-binary-search-tree/>
- <http://www.jiuzhang.com/solutions/inorder-successor-in-binary-search-tree/>
- Search Range in Binary Search Tree
- <http://www.lintcode.com/problem/search-range-in-binary-search-tree/>
- Insert Node in a Binary Search Tree
- <http://www.lintcode.com/problem/insert-node-in-a-binary-search-tree/>
- Remove Node in a Binary Search Tree
- <http://www.lintcode.com/problem/remove-node-in-binary-search-tree/>
- <http://www.mathcs.emory.edu/~cheung/Courses/171/Syllabus/9-BinTree/BST-delete.html>

# 今天学会了什么？

- 用树形分析法计算时间复杂度
- 递归是深度优先搜索算法(DFS)的一种实现形式
  - DFS可以使用非递归的方式实现
- 二叉树上的递归 Recursion in Binary Tree
  - 遍历法 Traverse
  - 分治法 Divide Conquer
- 二叉搜索树
  - 性质: 中序遍历是“不下降”序列
  - 功能:  $O(h)$ 的时间查找, 删除, 插入
- 必“背”程序:
  - 非递归版本的 Pre Order, In Order



# 点题时间

<http://www.jiuzhang.com/qa/983/>