## Monotonic Truncated Attention

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# 1 Backgrounds

Online automatic speech recognition (ASR) models transcribe speech to text as the speaker begins speaking. In attention-based encoder-decoder ASR models [1], the widely-used global attention network performs on top of the full sequential input representations, which hampers the online deployment of such ASR models. In [2], we have proposed a stable monotonic chunk-wise attention (sMoChA), which was designed for online attention-based encoder-decoder models. In this blog, we describe the monotonic truncated attention (MTA) network, which is in submission to a journal, to simplify the sMoChA and solve the training-and-decoding mismatch problem [3] of sMoChA. MTA truncates the sequential input representations and computes the attention weights from the truncation end-point to the beginning of input representation sequence. It should be noted that this is not a formal publication and just intends to show how MTA works.

### 2 Decoding of Monotonic Truncated Attention

In the decoding stage, MTA always begins a search from the previous end-point and decides the next qualified end-point. Suppose the encoder converts the audio frames into sequential input representations  $\mathbf{H} = (\mathbf{h}_1, \mathbf{h}_2, \cdots)$  and the decoder generates the sequential hidden state  $\mathbf{Q} = (\mathbf{q}_1, \mathbf{q}_2, \cdots)$  at the (i-1)-th step. We denote i and j as the indices of  $\mathbf{Q}$  and  $\mathbf{H}$ , respectively, and  $t_i$  as the truncation end-point in the input representation sequence for the i-th decoder step. MTA searches  $t_i$  as follows, for  $j = 1, 2, \cdots$ :

$$p_{i,j} = \operatorname{Sigmoid}(g \frac{\mathbf{v}^{\top}}{||\mathbf{v}||} \tanh(\mathbf{W}_1 \mathbf{q}_{i-1} + \mathbf{W}_2 \mathbf{h}_j + \mathbf{b}) + r),$$
 (1)

$$z_{i,j} = \mathbb{I}(p_{i,j} > 0.5 \land j \ge t_{i-1}),$$
 (2)

where matrices  $\mathbf{W}_1$ ,  $\mathbf{W}_2$ , vectors  $\mathbf{b}$ ,  $\mathbf{v}$  and scalar g, r are trainable parameters. In Eq. 1, we define  $p_{i,j}$  as the truncation probability. In Eq. 2, we define  $z_{i,j}$  as the indicator of truncating or not-truncating at  $\mathbf{h}_{\mathbf{j}}$ , and  $\mathbb{I}$  is an indicator function. When the truncation probability  $p_{i,j}$  is larger than the predefined threshold (i.e. 0.5) and the index j is greater or equal to the previous end-point  $t_{i-1}$ , we set  $t_i = j$ . Then, MTA computes a label-wise representation  $\mathbf{r}_i$  as follows, for  $j = 1, 2, \dots, t_i$ :

$$w_{i,j} = p_{i,j} \prod_{k=1}^{j-1} (1 - p_{i,k}),$$
(3)

$$\mathbf{r}_i = \sum_{j=1}^{t_i} w_{i,j} \mathbf{h}_j. \tag{4}$$

In Eq. 3, we denote  $w_{i,j}$  as the attention weights. In Eq. 4,  $\mathbf{r}_i$  is the weighted sum of the input representations before the truncation end-point. This label-wise representation  $\mathbf{r}_i$  are passed into the decoder to predict the *i*-th label.

### 3 Training of Monotonic Truncated Attention

In the training stage, the label-wise representation  $\mathbf{r}_i$  is computed based on the full sequential input representations as follows:

$$\mathbf{r}_i = \sum_{j=1}^T w_{i,j} \mathbf{h}_j, \tag{5}$$

where T denotes the length of input representation sequence. In Eq 3, the computation of  $w_{i,j}$  can be rewritten in the following recursive form:

$$w_{i,j} = \frac{p_{i,j}}{p_{i,j-1}} \cdot (1 - p_{i,j-1}) \cdot w_{i,j}.$$
 (6)

In Eq. 6,  $w_{i,j}$  exponentially decays by  $(1 - p_{i,j-1})$  along the index j. To prevent  $w_{i,j}$  from vanishing, we enforce the mean of  $(1 - p_{i,j-1})$  to be close to 1 by initializing r in Eq. 1 to a negative value, e.g. r = -4.

### 4 Experiments

We evaluated different attention networks on HKUST Mandarin conversational telephone (HKUST) [4] corpus. We used ESPnet [5] toolkit and followed the configurations on [6] to build the hybrid CTC/attention end-to-end models with recurrent neural networks [7]. We open source codes of sMoChA on [8]. The results are listed in Table 1. It shows that MTA outperformed sMoChA and exhibited comparable performance with location-aware attention network.

Table 1: Character error rates (CERs) of different attention types on HKUST.

Attention Type	Chunk Width	CER (%)	
		dev	eval
Location-aware Attention	_	28.7	27.6
Stable Monotonic Chunk-wise Attention (sMoChA)	1	28.8	27.8
	3	28.6	27.8
	6	28.9	27.7
Monotonic Truncated Attention (MTA)	_	28.5	27.6

#### References

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