# Data Analysis and Machine Learning: Introduction and Representing data

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### What is Machine Learning?

Machine learning is the science of giving computers the ability to learn without being explicitly programmed. The idea is that there exist generic algorithms which can be used to find patterns in a broad class of data sets without having to write code specifically for each problem. The algorithm will build its own logic based on the

Machine learning is a subfield of computer science, and is closely related to computational statistics. It evolved from the study of pattern recognition in artificial intelligence (Al) research, and has made contributions to Al tasks like computer vision, natural language processing and speech recognition. It has also, especially in later years, found applications in a wide variety of other areas, including bioinformatics, economy, physics, finance and marketing.

### Types of Machine Learning

The approaches to machine learning are many, but are often split into two main categories. In supervised learning we know the answer to a problem, and let the computer deduce the logic behind it. On the other hand, unsupervised learning is a method for finding patterns and relationship in data sets without any prior knowledge of the system. Some authours also operate with a third category, namely reinforcement learning. This is a paradigm of learning inspired by behavioural psychology, where learning is achieved by trial-and-error, solely from rewards and punishment.

Another way to categorize machine learning tasks is to consider the desired output of a system. Some of the most common tasks are:

- Classification: Outputs are divided into two or more classes.
   The goal is to produce a model that assigns inputs into one of these classes. An example is to identify digits based on pictures of hand-written ones. Classification is typically supervised learning.
- Regression: Finding a functional relationship between an input

### Different algorithms

In this course we will build our machine learning approach on a statistical foundation, with elements from data analysis, stochastic processes etc before we proceed with the following machine learning algorithms

- Linear regression and its variants
- Decision tree algorithms, from simpler to more complex ones
- Nearest neighbors models
- Bayesian statistics
- Support vector machines and finally various variants of
- Artifical neural networks

Before we proceed however, there are several practicalities with data analysis and software tools we would like to present. These tools will help us in our understanding of various machine learning algorithms.

Our emphasis here is on understanding the mathematical aspects of different algorithms, however, where possible we will emphasize the importance of using available software.

### Software and needed installations

We will make intensive use of python as programming language and the myriad of available libraries. Furthermore, you will find IPython/Jupyter notebooks invaluable in your work. You can run R codes in the Jupyter/IPython notebooks, with the immediate benefit of visualizing your data.

If you have Python installed (we recommend Python3) and you feel pretty familiar with installing different packages, we recommend that you install the following Python packages via **pip** as

 pip install numpy scipy matplotlib ipython scikit-learn mglearn sympy pandas pillow

For Python3, replace pip with pip3.

For OSX users we recommend also, after having installed Xcode, to install **brew**. Brew allows for a seamless installation of additional software via for example

brew install python3

### Python installers

If you don't want to perform these operations separately, we recommend two widely used distrubutions which set up all relevant dependencies for Python, namely

- anaconda
- Enthought canopy

### Installing R, C++, cython or Julia

You will also find it convenient to utilize R. Say more about R. Jupyter/lpython notebook allows you run R code interactively in your browser. The software library R is tuned to statistically analysis and allows for an easy usage of the tools we will discuss in these texts.

For the C++ affecianodas, Jupyter/IPython notebook allows you also to install C++ and run codes written in this language interactively in the browser. Since we will emphasize writing many of the algorithms yourself, you can thus opt for either Python or C++ as programming languages.

To add more entropy, **cython** can also be used when running your notebooks. It means that Python with the Jupyter/IPython notebook setup allows you to integrate widely popular softwares and tools for scientific computing. With its versatility, including symbolic operations, Python offers a unique computational environment. Your Jupyter/IPython notebook can easily be converted into a nicely rendered **PDF** file or a Latex file for further

### Doing it in R

Use the Hudson bay model to load data and make plot in  $\ensuremath{\mathsf{R}}$  and with python

# import numpy as np import matplotlib.pyplot as plt from scipy import sparse import pandas as pd from IPython.display import display eye = np.eye(4) print(eye) sparse\_mtx = sparse.csr\_matrix(eye) print(sparse\_mtx) x = np.linspace(-10,10,100) y = np.sin(x) plt.plot(x,y,marker='x') plt.show() data = {'Name': ["John", "Anna", "Peter", "Linda"], 'Location': ["Roma data\_pandas = pd.DataFrame(data) display(data\_pandas)

# Representing data, more examples

```
import numpy as np
import matplotlib.pyplot as plt
from scipy import sparse
import pandas as pd
from IPython.display import display
import mglearn
import sklearn.linear_model import LinearRegression
from sklearn.linear_model import LinearRegression
from sklearn.tree import DecisionTreeRegressor
x, y = mglearn.dataets.make_vave(n_samples=100)
line = np.linspace(-3,3,1000,endpoint=False).reshape(-1,1)
reg = DecisionTreeRegressor(m.samples_split=3).fit(x,y)
plt.plot(line, reg.predict(line), label="decision tree")
regline = LinearRegression().fit(x,y)
plt.plot(line, regline.predict(line), label= "Linear Rgression")
plt.show()
```

### Binning of data

Use the Hudson bay model to load data and make plot in  $\ensuremath{\mathsf{R}}$  and with python

# Adding model complexity: Predator-Prey model from ecology

The population dynamics of a simple predator-prey system is a classical example shown in many biology textbooks when ecological systems are discussed. The system contains all elements of the scientific method:

- The set up of a specific hypothesis combined with
- the experimental methods needed (one can study existing data or perform experiments)
- analyzing and interpreting the data and performing further experiments if needed
- trying to extract general behaviors and extract eventual laws or patterns
- develop mathematical relations for the uncovered regularities/laws and test these by per forming new experiments

### Case study from Hudson bay

Lots of data about populations of hares and lynx collected from furs in Hudson Bay, Canada, are available. It is known that the populations oscillate. Why? We shall demonstrate the scientific method by

- plotting the data
- derive a simple model for the population dynamics
- (fitting parameters in the model to the data)
- using the model predict the evolution other predator-pray systems

### Hudson bay data

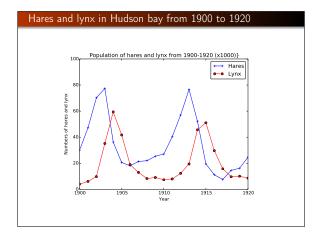
Most mammalian predators rely on a variety of prey, which complicates mathematical modeling; however, a few predators have become highly specialized and seek almost exclusively a single prey species. An example of this simplified predator-prey interaction is seen in Canadian northern forests, where the populations of the lynx and the snowshoe hare are intertwined in a life and death struggle. One reason that this particular system has been so extensively studied is that the Hudson Bay company kept careful records of all furs from the early 1800s into the 1900s. The records for the furs collected by the Hudson Bay company showed distinct oscillations (approximately 12 year periods), suggesting that these species caused almost periodic fluctuations of each other's populations. The table here shows data from 1900 to 1920.

he tal	ole here shows	data from 19
Year	Hares (x1000)	Lynx (x1000)
1900	30.0	4.0
1901	47.2	6.1
1902	70.2	9.8
1903	77.4	35.2
1904	36.3	59.4
1905	20.6	41.7

```
import numpy as np
from matplotlib import pyplot as plt

# Load in data file
data = np.loadtxt('Hudson_Bay.dat', delimiter=',', skiprows=1)
# Make arrays containing x-axis and hares and lynx populations
year = data[:,0]
hares = data[:,1]
lynx = data[:,2]

plt.plot(year, hares,'b-+', year, lynx, 'r-o')
plt.axis([1900,1920,0, 100.0])
plt.xlabel(r'Year')
plt.ylabel(r'Numbers of hares and lynx ')
plt.legend(('Hares','Lynx'), loc='upper right')
plt.tile(r'Population of hares and lynx from 1900-1920 (x1000)}
plt.savefig('Hudson_Bay_data.pdf')
plt.savefig('Hudson_Bay_data.png')
plt.show()
```



# Why now create a computer model for the hare and lynx populations?

We see from the plot that there are indeed fluctuations. We would like to create a mathematical model that explains these population fluctuations. Ecologists have predicted that in a simple predator-prey system that a rise in prey population is followed (with a lag) by a rise in the predator population. When the predator population is sufficiently high, then the prey population begins dropping. After the prey population falls, then the predator population falls, which allows the prey population to recover and complete one cycle of this interaction. Thus, we see that qualitatively oscillations occur. Can a mathematical model predict this? What causes cycles to slow or speed up? What affects the amplitude of the oscillation or do you expect to see the oscillations damp to a stable equilibrium? The models tend to ignore factors like climate and other complicating factors. How significant are these?

- We see oscillations in the data
- What causes suches to slow or speed up?

### The traditional (top-down) approach

The classical way (in all books) is to present the Lotka-Volterra equations:

$$\frac{dH}{dt} = H(a - bL)$$
$$\frac{dL}{dt} = -L(d - cH)$$

Here,

- ullet H is the number of preys
- L the number of predators
- a, b, d, c are parameters

Most books quickly establish the model and then use considerable space on discussing the qualitative properties of this *nonlinear system of ODEs* (which cannot be solved)

### The "new" discrete bottom-up approach

### The bottom-up approach

- Start with experimental data and discuss the methods which have been used to collect the data, the assumptions, the electronic devices, the aims etc. That is, expose the students to the theory and assumptions behind the data that have been collected and motivate for the scientific method.
- Where appropriate the students should do the experiment(s) needed to collect the data.
- The first programming tasks are to read and visualize the data to see if there are patterns or regularities. This strengthens a research-driven intuition.
- Now we want to increase the understanding through modeling.
- Most of the biology lies in the derivation of the model. We shall focus on an intuitive discrete approach that leads to difference equations that can be programmed and solved directly.

### Basic (computer-friendly) mathematics notation

- Time points:  $t_0, t_1, \ldots, t_m$
- Uniform distribution of time points:  $t_n = n\Delta t$
- $H^n$ : population of hares at time  $t_n$
- Ln: population of lynx at time tn
- We want to model the changes in populations,  $\Delta H = H^{n+1} H^n \text{ and } \Delta L = L^{n+1} L^n \text{ during a general time interval } [t_{n+1},t_n] \text{ of length } \Delta t = t_{n+1} t_n$

### Basic dynamics of the population of hares

The population of hares evolves due to births and deaths exactly as a bacteria population:

$$\Delta H = a\Delta t H^n$$

However, hares have an additional loss in the population because they are eaten by lynx. All the hares and lynx can form  $H \cdot L$  pairs in total. When such pairs meet during a time interval  $\Delta t$ , there is some small probablity that the lynx will eat the hare. So in fraction  $b\Delta tHL$ , the lynx eat hares. This loss of hares and must be accounted for: subtracted in the equation for hares:

$$\Delta H = a\Delta t H^n - b\Delta t H^n L^n$$

### Basic dynamics of the population of lynx

We assume that the primary growth for the lynx population depends on sufficient food for raising lynx kittens, which implies an adequate source of nutrients from predation on hares. Thus, the growth of the lynx population does not only depend of how many lynx there are, but on how many hares they can eat. In a time interval  $\Delta tHL$  hares and lynx can meet, and in a fraction  $b\Delta tHL$  the lynx eats the hare. All of this does not contribute to the growth of lynx, again just a fraction of  $b\Delta tHL$  that we write as  $d\Delta tHL$ . In addition, lynx die just as in the population dynamics with one isolated animal population, leading to a loss  $-c\Delta tL$ .

The accounting of lynx then looks like

$$\Delta L = d\Delta t H^n L^n - c\Delta t L^n$$

### Evolution equations

By writing up the definition of  $\Delta H$  and  $\Delta L$ , and putting all assumed known terms  $H^n$  and  $L^n$  on the right-hand side, we have

$$H^{n+1} = H^n + a\Delta tH^n - b\Delta tH^nL^n$$

$$L^{n+1} = L^n + d\Delta t H^n L^n - c\Delta t L^n$$

### Note:

- These equations are ready to be implemented!
- But to start, we need H<sup>0</sup> and L<sup>0</sup> (which we can get from the data)
- We also need values for a, b, d, c

### Adapt the model to the Hudson Bay case

- As always, models tend to be general as here, applicable to "all" predator-pray systems
- The critical issue is whether the *interaction* between hares and lynx is sufficiently well modeled by const*HL*
- ullet The parameters a, b, d, and c must be estimated from data
- Measure time in years
- $t_0 = 1900$ ,  $t_m = 1920$

```
import numpy as np
import matplotlib.pyplot as plt

def solver(m, H0, L0, dt, a, b, c, d, t0):
    """Solve the difference equations for H and L over m years
    with time step dt (measured in years."""

    num_intervals = int(m/float(dt))
    t = np.linspace(t0, t0 + m, num_intervals+1)
    H = np.zeros(t.size)
    L = np.zeros(t.size)

print 'Init:', H0, L0, dt
    H[0] = H0
    L[0] = L0

for n in range(0, len(t)-1):
    H[n+1] = H[n] + a+dt+H[n] + L[n] - c+dt+L[n]
    return H, L, t

# Load in data file
data = np.loadtxt('Hudson_Bay.csv', delimiter=',', skiprous=1)
# Make strays containing x-axis and hares and lynx populations
t_e = data[:,0]
H,e = data[:,2]
```

