

# **Developing FOB-CTMQC for use in simulating charge transport in organic semiconductors**

*Matt Ellis*

Supervisor: Jochen Blumberger

Second Supervisor: Graham Worth

**MPhil Upgrade Report**

Department of Physics and Astronomy  
University College London

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I, Matt Ellis, confirm that the work presented in this thesis is my own. Where information has been derived from other sources, I confirm that this has been indicated in the work.

# Abstract

Charge transfer in organic molecular systems are difficult to simulate due to (fast?) non-adiabatic transitions between Born-Oppenheimer energy surfaces. A range of techniques have been designed to overcome this, such as the Surface Hopping and Ehrenfest methods. However, they tend to suffer from unphysical overcoherence issues. In this report, I present an implementation of a fragment-orbital based coupled-trajectory mixed quantum-classical algorithm (FOB-CTMQC), which is designed for simulating charge transport in systems of tens to hundreds of organic molecules. This method uses an in-house analytical overlap method (AOM) within the framework of coupled-trajectory mixed quantum-classical (CTMQC) molecular dynamics. CTMQC enables the correct calculation of decoherence due to 2 new terms containing a quantity named the Quantum Momentum. While the AOM method allows the simulation of large systems, due to the method's analytic formulation of the off-diagonal elements of the Hamiltonian in terms of the overlap between singly occupied molecular orbitals. E.g.  $H_{kl} = CS_{kl}$ , where  $H_{kl}$  are the off-diagonal elements of the Hamiltonian,  $C$  is a constant of proportion and  $S_{kl}$  are the off-diagonal overlap elements. For many organic semiconductors we can assume pi-conjugation. Meaning only 1 optimized Slater p-orbital is needed for the calculation of the overlap.

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## Chapter 1

# Introduction

## 1.1 Charge Transport Regimes in Organic Semiconductors

### 1.1.1 Organic Semiconductors

Conductive polymers were first discovered in 1977 by Shirakawa et al [1, 2] for which they were awarded the Nobel prize in Chemistry. Recently these materials have become ubiquitous in many technologies, such as in organic solar cells[3], organic field-effect transistors (OFET) [4] and organic light-emitting diodes (OLED) [5]. While the other two technologies lag behind their inorganic counterparts, uptake of OLED screens is becoming increasingly popular especially in the smartphone and television market due to their flexibility, better colour representation and lower energy consumption than conventional backlit LCD displays. In fact IHS market's OLED market tracker predicts OLED to be the dominant technology in smartphone screens by 2020 [6] <sup>1</sup>. OLEDs have also found uses in lighting with their efficiency rivalling that of fluorescent tubes [7, 8]. Although, industry has made large strides in fabricating and using these materials the exact nature of the charge transport is still poorly understood. Conventional hopping and band theories break down in the regime of partial delocalisation of the charge carriers and atomistic simulations are required for a realistic picture.

Typically charge carrier mobilities in 'good' organic semiconductors (OSCs) fall

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<sup>1</sup>This is an online citation -Not sure whether I have cited correctly

between  $1\text{--}10\text{ cm}^2\text{ V}^{-1}\text{s}^{-1}$  [9]. This is just beyond the range of hopping model validity ( $\sim 1\text{ cm}^2\text{ V}^{-1}\text{s}^{-1}$ ) and below that of band theory ( $> 50\text{ cm}^2\text{ V}^{-1}\text{s}^{-1}$ ). In this intermediate regime the charge carriers are typically not completely delocalised at the valence band edges (band regime) or localised to a single site/molecule (hopping regime) but delocalised over a few molecules. Without current analytic approaches being valid in this regime many computational approaches have been developed to investigate the underlying charge transport mechanisms [10].

### 1.1.2 Band-like Transport

Band theory paragraph...

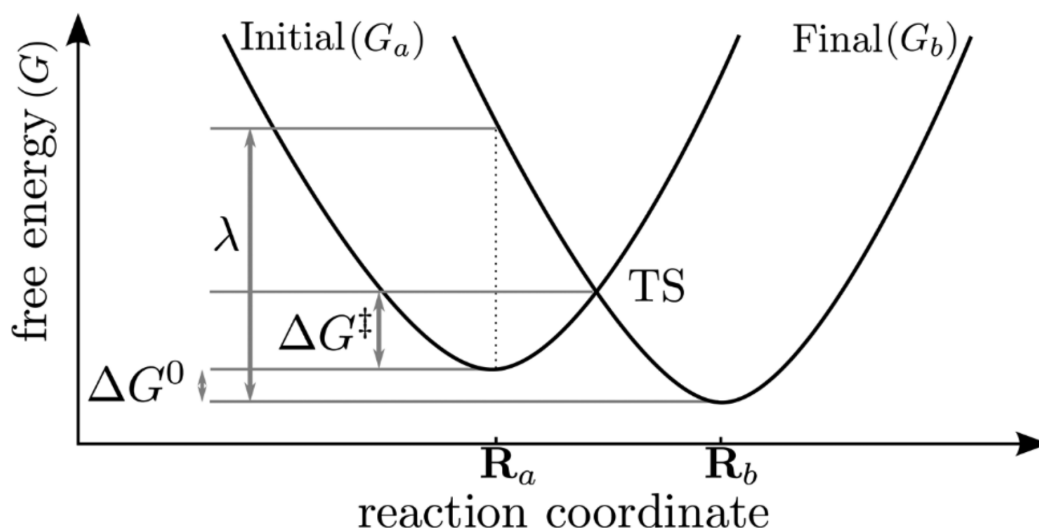
### 1.1.3 Hopping-like Transport

Need way more citations here -see Gajdos AOM paper it has lots of good references

Hopping theories assume the charge carrier is localised on one site and can hop from site to site in a series of discrete hops [10]. There are various underlying mechanisms for this. For example, the presence of the charge carrier at a site can alter the nuclear geometry. The distorted nuclear geometry can make it harder for the charge carrier to move onto the next site, creating a metastable state and trapping the charge carrier. The deformation in the nuclear geometry is called a small polaron.

Need a better connecting paragraph... Aim of the rest of this section is to lead on to the Born-Oppenheimer approx

Polaronic hopping theories have been used to relative success and one of the key tools used in visualising this process (assuming harmonic response) are the Marcus Parabolas. These show how the free energy and reaction coordinates change after a charge transfer i.e. from initial to final diabatic states. The term ‘diabatic state’ isn’t well defined and can refer to different things in different formulations. In this work a diabatic state can be imagined as the charge carrier localised on a single molecule. This is discussed later in more detail in 1.2.1

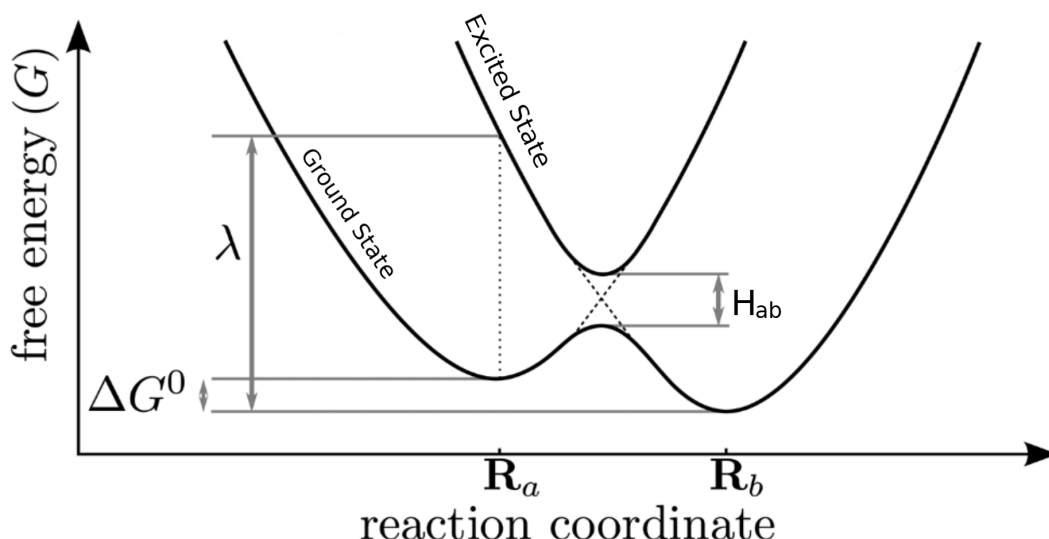


**Figure 1.1:** Marcus parabolas depicting the relationship between the free energy in the system and the reaction coordinate at 0 electronic coupling. This figure was taken from Oberhofer et al [10]

Figure 1.1 above defines various important quantities for calculating the mobility in materials displaying hopping-like transport. The initial parabola describes the change in free energy with respect to the reaction coordinate for the initial state, for example when the charge is located on site 1. The final parabola describes the change in free energy when the charge is located on site 2 e.g. when the charge has relocated to site 2. The transition state (TS) is a point where the energies of the initial and final states are the same. This degenerate point is the only point at which the charge can move from the initial to final state as other points would result in a

non-zero jump in energy between the 2 parabolas. The diabatic activation energy  $\Delta G^\ddagger$  defines the energy required to get to this transition state from the minima of the initial parabola. The driving force  $\Delta G^0$  is the difference in minima of the 2 parabolas, the reorganisation energy  $\lambda$  defines the energy required to change the reaction coordinate from the final state minima to the initial state minima without changing electronic state.

Figure 1.1 can change when there is a non-zero electronic coupling ( $H_{ab}$ ) between diabatic states. This parameter increases the chance of moving between the initial and final diabatic states by lowering the diabatic activation energy i.e. the energy required to transition from state 1 to 2. This is visualised in figure 1.2 In figure 1.2



**Figure 1.2:** Graph depicting the change in free energy for a change in reaction coordinate for non-zero electronic coupling. Adapted from [10]

above the diabatic activation energy has been lowered to  $\Delta G^\ddagger = \Delta G^\ddagger - H_{ab}$  making it easier for charge carriers to transition between diabatic states. In our formalism this means it is easier for charge carriers to move between sites i.e. delocalise. We see also that instead of being described totally by 2 parabolas there are 2 new adiabatic potential energy surfaces arising -the ground and excited state. The amount that these new potential energy surfaces diverge from the diabatic wells is dependent on an adiabaticity factor which is proportional to the ratio between the electronic



coupling,  $H_{ab}$ , and the re-organisation energy,  $\lambda$ . This has been discussed in detail in multiple papers [10–13].

In fact for systems with couplings larger than  $H_{ab} > \frac{3}{8}\lambda$  the diabatic activation energy vanishes completely [13], meaning that there is no energy cost in transitioning between diabatic states. Beyond this regime hopping theories cannot be accurately applied. Unfortunately, at room temperatures thermal fluctuations means the mean free path of the charge carriers is comparable to the intermolecular spacing. As such band theories too are inapplicable [10, 14, 15]. Much beyond this regime the energy cost to transition to higher adiabatic potential energy surfaces becomes prohibitively high and the system travels on a single state. In these situations the Born-Oppenheimer approximation is valid. However, in this work I will be looking into the regime in between the band and hopping-like transport where we currently don't have analytical theories to describe charge transport. For this I will be using non-adiabatic atomistic simulations, namely a technique called CTMQC.

## 1.2 Atomistic Simulations of Nonadiabatic Processes

In simulating processes involving electronic transfers a key approximation used in conventional molecular dynamics (MD) breaks down. That is the Born-Oppenheimer or adiabatic approximation [16]. This approximation relies on the fact that nuclei are more massive than electrons and are approximately stationary with respect to electron movement (need ref). This results in nuclear evolution that is governed by a single, adiabatic, potential energy surface. However, in many interesting processes, such as electron transfer, non-radiative decay and photochemical processes, electronic transitions between adiabatic potential energy surfaces occur (need ref). Simulating these processes requires non-adiabatic molecular dynamics (NAMD) techniques to be developed to correctly capture dynamical properties.

There have been many techniques proposed for use in NAMD such as the quantum classical Liouville equation (need ref), multiple spawning (need ref) or nonadiabatic Bohmian dynamics (need ref) <sup>2</sup>. However, two of the most popular are trajectory surface hopping (need ref) and mean-field approaches (need ref). This is probably due to their relative simplicity to implement (need ref), efficiency for large systems (need ref) and proven efficacy in a wide variety of situations (need ref). In all of these approaches the general aim is to treat as much of the system as possible with (computationally cheaper) classical mechanics. While handling all necessary parts with quantum mechanics [17]. In Surface Hopping, Ehrenfest and CTMQC one treats the nuclear subsystem classically and the electronic one quantum mechanically. The nuclei are propagated using a velocity verlet algorithm according to Newton's laws. The electrons are propagated using a fourth order Runge Kutta algorithm according to the time-dependent Schrödinger equation. This is normally expanded as a linear combination of adiabatic or diabatic states. The nuclei and electrons can also interact. Taking account of this interaction is where these different atomistic simulation techniques differ.

### 1.2.1 FOB Formalism

The effect of the nuclei on the electrons is normally handled via the Hamiltonian. This is dependent on nuclear positions and is in turn used in the Schrödinger equation to propagate the electron dynamics. Often the construction of the Hamiltonian is carried out using density function theory (DFT). However, for large, dynamic systems this becomes too computationally expensive and a different technique would have to be used. In this work I will rely on an Analytical Overlap Method (AOM) [14] to calculate the off-diagonal elements of the Hamiltonian and the diagonal elements will be calculated via a forcefield.

#### 1.2.1.1 AOM

AOM assumes that the off-diagonal elements of the Hamiltonian are proportional to the off-diagonal elements of the overlap matrix between 2 singly occupied

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<sup>2</sup>See first Frederica paper

molecular orbitals (SOMO). For  $\pi$ -conjugated systems,

### 1.2.2 Surface Hopping and Ehrenfest Dynamics

How surface hopping and ehrenfest alter the potential energy surface to affect the nuclear dynamics

## 1.3 CTMQC

CTMQC comes from taking the semi-classical limit of an exact factorisation of the molecular wavefunction into its constituent electronic and nuclear components [18]. Where the electronic component is parametrically dependent on the nuclear coordinates,  $\mathbf{R}$ . This is shown below in eq (1.1) where  $\chi$  is the nuclear wavefunction and  $\Phi$  is the electronic one.

$$\Psi(\mathbf{R}, \mathbf{r}, t) = \Phi_{\mathbf{R}}(\mathbf{r}, t) \chi(\mathbf{R}, t) \quad (1.1)$$

In the above equation (and throughout this report) I will denote nuclear coordinates and electronic coordinates  $R$  and  $r$  respectively. The nuclear and electronic wavefunctions then obey separate, but coupled, time-dependent schrödinger equations for spatial and temporal evolution. This representation has proven to be useful in furthering understanding through exact solutions of small toy-model systems (need ref<sup>3</sup>). However, in this report I will be focussing on the semi-classical limit of these equations (CTMQC) and give some early results of a combination of this and the AOM method explained previously in section 1.2.1.

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<sup>3</sup>see deconstruction paper

The equations for the evolution of the electronic and nuclear wavefunctions in the exact factorisation (need ref) are given below:

$$i\hbar\delta_t\Phi_{\mathbf{R}}(\mathbf{r},t) = (\hat{H}_{BO} + \hat{U}_{en}[\Phi_{\mathbf{R}},\chi] - \varepsilon(\mathbf{R},t))\Phi_{\mathbf{R}}(\mathbf{r},t) \quad (1.2)$$

$$i\hbar\delta_t\chi(\mathbf{R},t) = \left(\sum_{v=1}^{N_n} \frac{[-i\hbar\nabla_v + \mathbf{A}_v(\mathbf{R},t)]^2}{2M_v} + \varepsilon(\mathbf{R},t)\right)\chi(\mathbf{R},t) \quad (1.3)$$

In the above equations  $\Phi_{\mathbf{R}}$  is the electronic which is parametrically dependent on the nuclear positions,  $\mathbf{R}$  as well as being explicitly dependent on electronic positions,  $\mathbf{r}$  and time,  $t$ .  $\chi$  is the nuclear wavefunction.  $\hat{H}_{BO}$  is the Born-Oppenheimer Hamiltonian containing the electronic kinetic energy operator, and interactions between the nuclei and electrons as well as nuclear and electronic self-interactions. The  $M_v$  is the mass of nucleus,  $v$ . The  $\mathbf{A}_v$  is a time-dependent vector potential and  $\varepsilon$  is a time-dependent scalar potential. Finally the  $\hat{U}_{en}$  is an operator coupling the nuclear and electronic wavefunctions. In Agostini, 16 (need ref) it was shown after applying five approximations, which are justified for many cases <sup>4</sup>, we can get the semi-classical limit of the exact factorisation equations.

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<sup>4</sup>Will need to remember what these are, and how they are justified!

- Brief introduction to NAMD.
  - ~~Why isn't normal MD good enough?~~
  - ~~What sort of processes need NAMD to simulate them?~~
  - Characteristics of NAMD -Trivial Crossings, avoided crossings.
  - Give current standard methods and their advantages/disadvantages
- Briefly explain the AOM method.
  - How it works - The analytic off-diagonal elements of hamiltonian (Spencer -both)
  - What the alternatives are (Gajdos paper)
  - Why this is preferable (Gajdos)
  - What are the limitations
- Explain CTMQC
  - Intro -It was derived from exact factorisation (maybe put derivation in appendix)
  - Give the equations. -Ehrenfest + QM term
  - How does it compare to other techniques -decoherence, first principles
  - Why combine it with FOB-CTMQC? -Expensive DFT etc...
  - What sort of systems will I be looking at? Charge transfer in organic semiconductors -1D and 2D systems

Then Results

## Chapter 2

# My First Content Chapter

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## Chapter 3

# My Second Content Chapter

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## Chapter 4

# General Conclusions

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## **Appendix A**

# **An Appendix About Stuff**

(stuff)

## **Appendix B**

# **Another Appendix About Things**

(things)

## Appendix C

# Colophon

*This is a description of the tools you used to make your thesis. It helps people make future documents, reminds you, and looks good.*

(example) This document was set in the Times Roman typeface using  $\text{\LaTeX}$  and Bib $\text{\TeX}$ , composed with a text editor.

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