

# Visualizing Scalars, Vectors, and Tensors

# Data Objects in Space

# Objects in Two & Three Dimensional Space

Data Objects can contain  $n$ -dimensional information.

For visualization, information must be projected onto 1, 2, or 3 dimensional space.

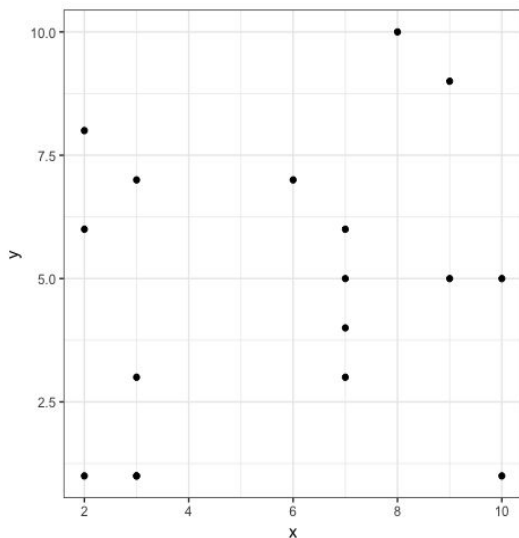
Each data entry is represented as a point in space.

Each point may contain extra dimensions of information, in addition to its position.

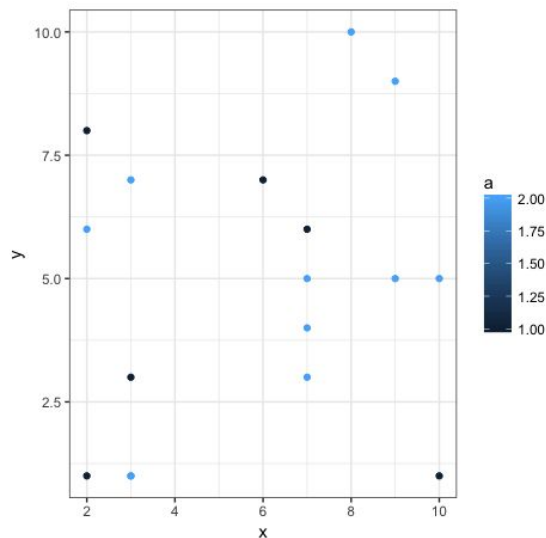
# Objects in Two & Three Dimensional Space

E.g. Data Objects in 2-Dimensional Space

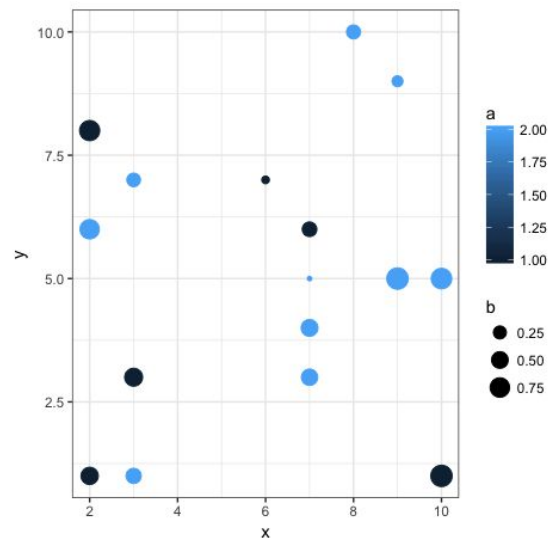
2 total dimensions:  
2-d position



3 total dimensions:  
2-d position +  
'a' dimension



4 total dimensions:  
2-d position +  
'a' + 'b' dimensions



# Scalars

# Scalars

A data object that contains information about only magnitude.

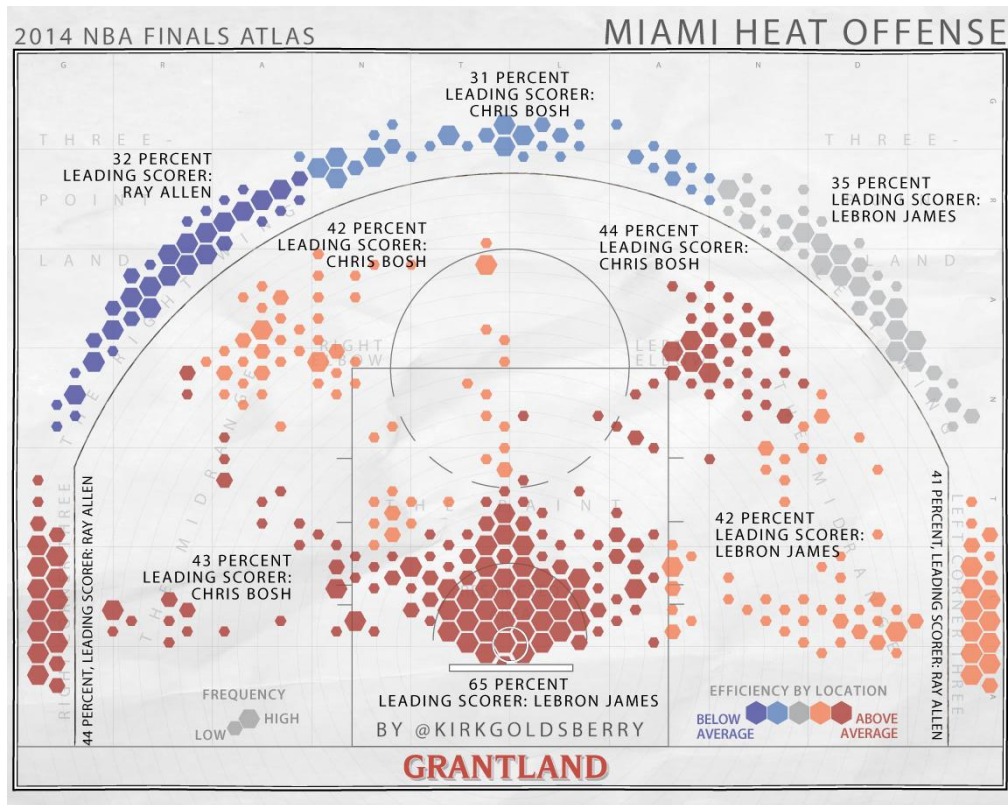
Scalars are quantitative data types that are typically continuous variables.

A scalar quantity has a one-dimensional visual representation at each point in space.

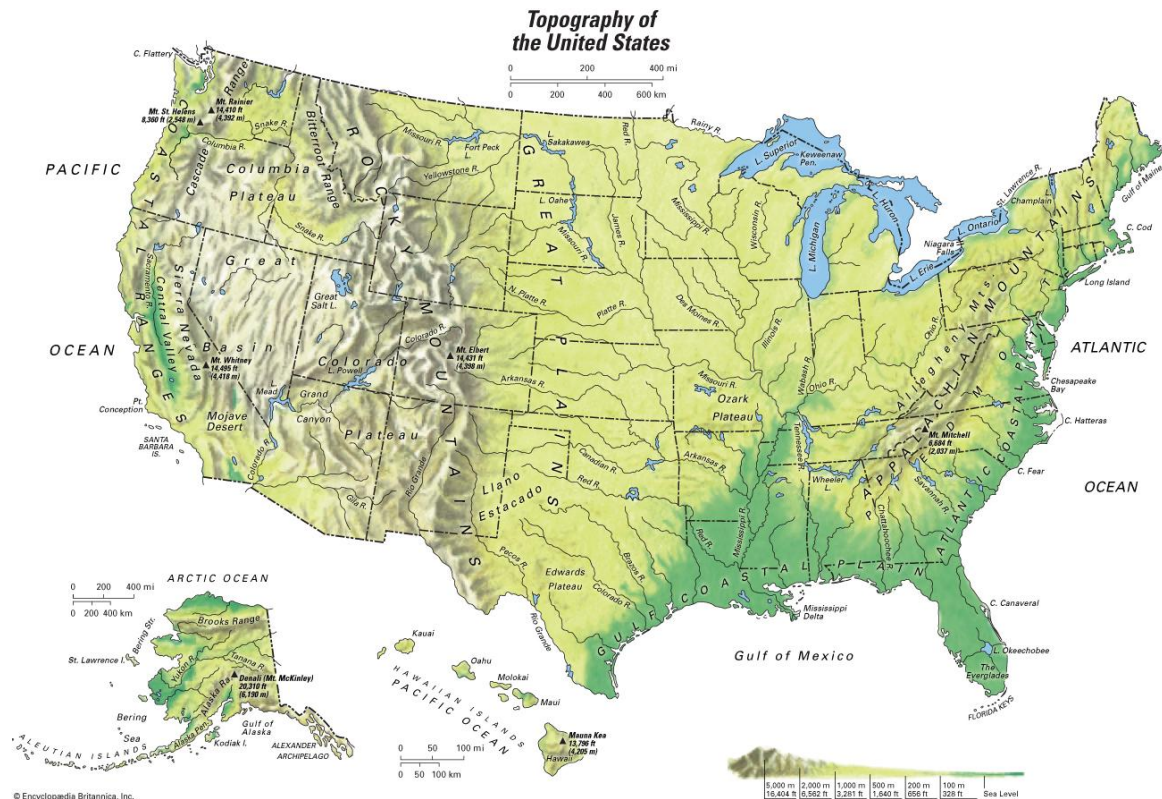
Examples of scalar data variables:

- Temperature
- Area
- Speed
- Density

# Scalars: Visual Examples

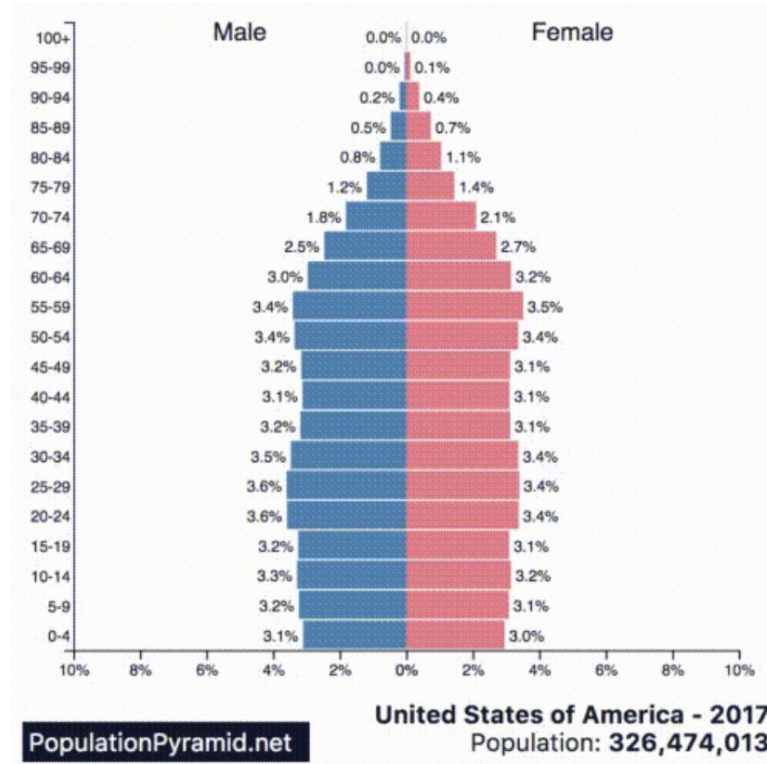


# Scalars: Visual Examples





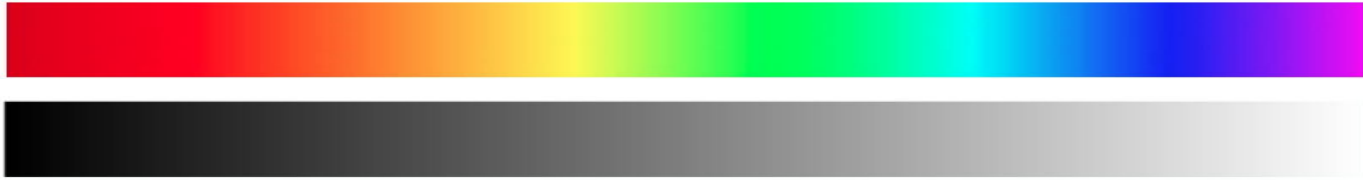
# Scalars: Visual Examples



# Scalars: Visual Variables Used

## 1. Color

- a. Hue
- b. Luminance



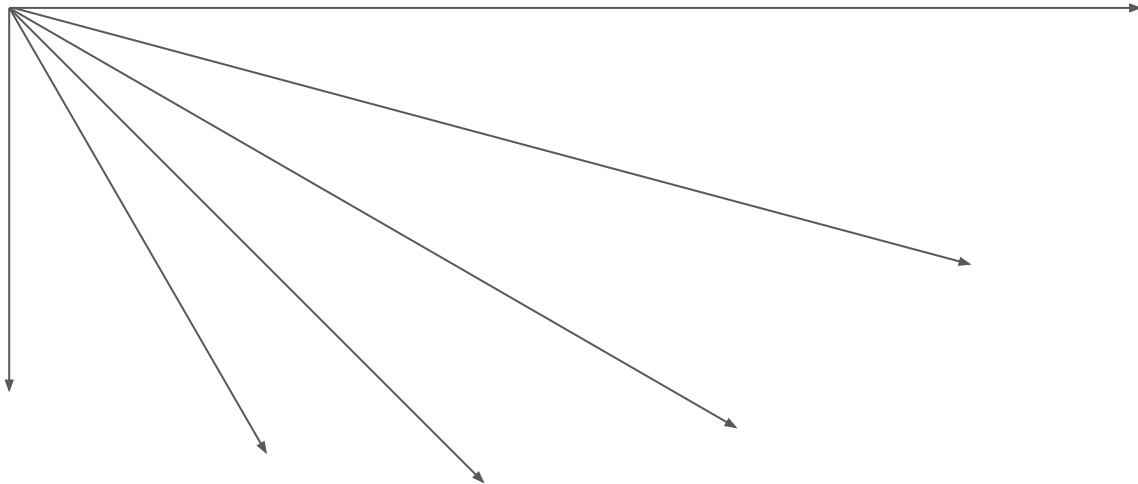
## 2. Size

- a. Area
- b. Length



# Vectors

# Vectors



# Vectors

A data object that contains information about magnitude and direction.

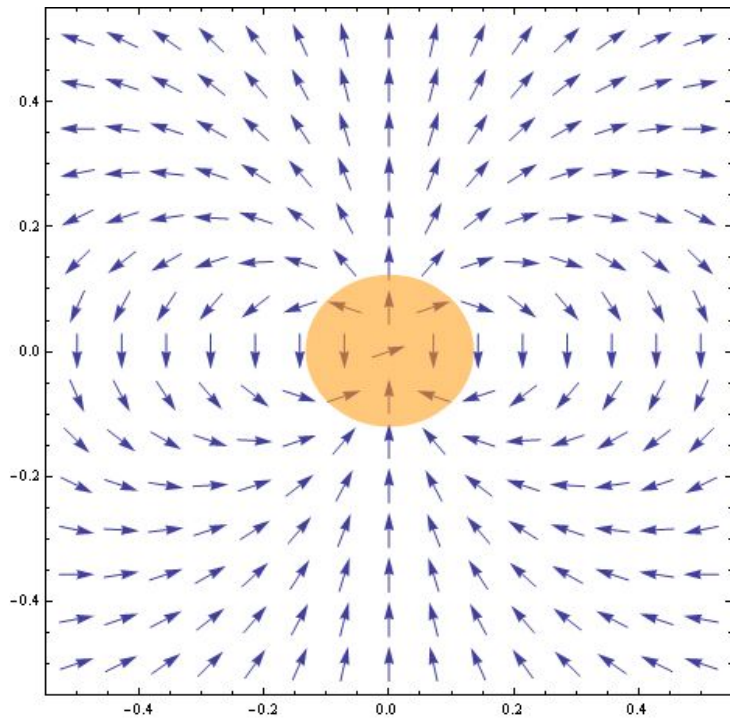
Vectors are quantitative data types that are typically continuous variables.

A vector quantity has a two-dimensional visual representation at each point in space.

Examples of vector data variables:

- Velocity (Speed + Direction)
- Force

# Vectors: Visual Examples



# Vectors: Visual Examples

Wind Vector Map: <http://hint.fm/wind/>

# Vectors: Visual Variables Used

1. Color
  - a. Hue
  - b. Luminance
2. Size
  - a. Area
  - b. Length
3. Orientation





# Tensors

# Tensors

Tensors are the generalized data object that scalars and vectors fit into.

Scalars: Rank 0 Tensors

Vectors: Rank 1 Tensors

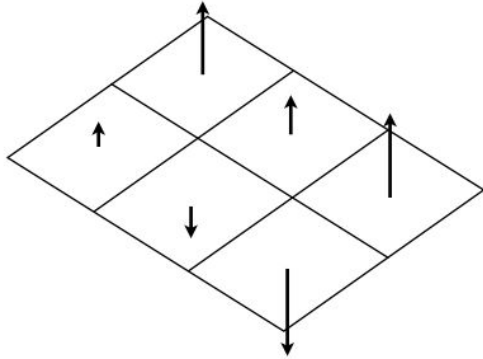
Matrices: Rank 2 Tensors

Higher-Dimensional Objects

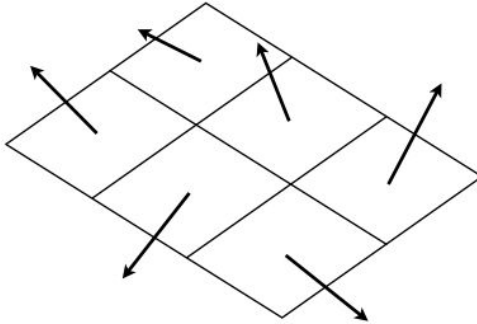
Typically in tensor visualization (non scalar/vector), a tensor quantity has a >two-dimensional visual representation at every point in space.

# Tensors

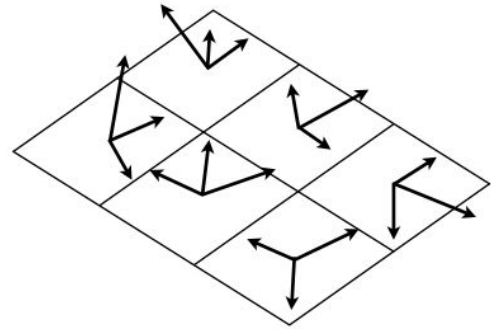
**Scalar field**



**Vector field**

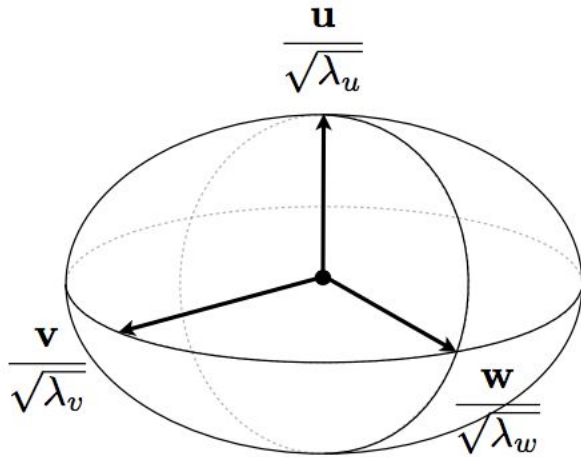


**Tensor field (Rank 2)**

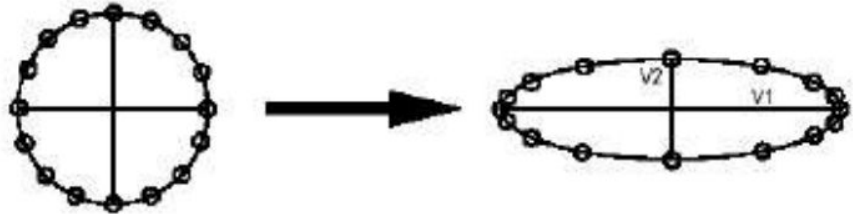


# Tensors: 'Common' Visualization Methods

Ellipsoid Glyphs

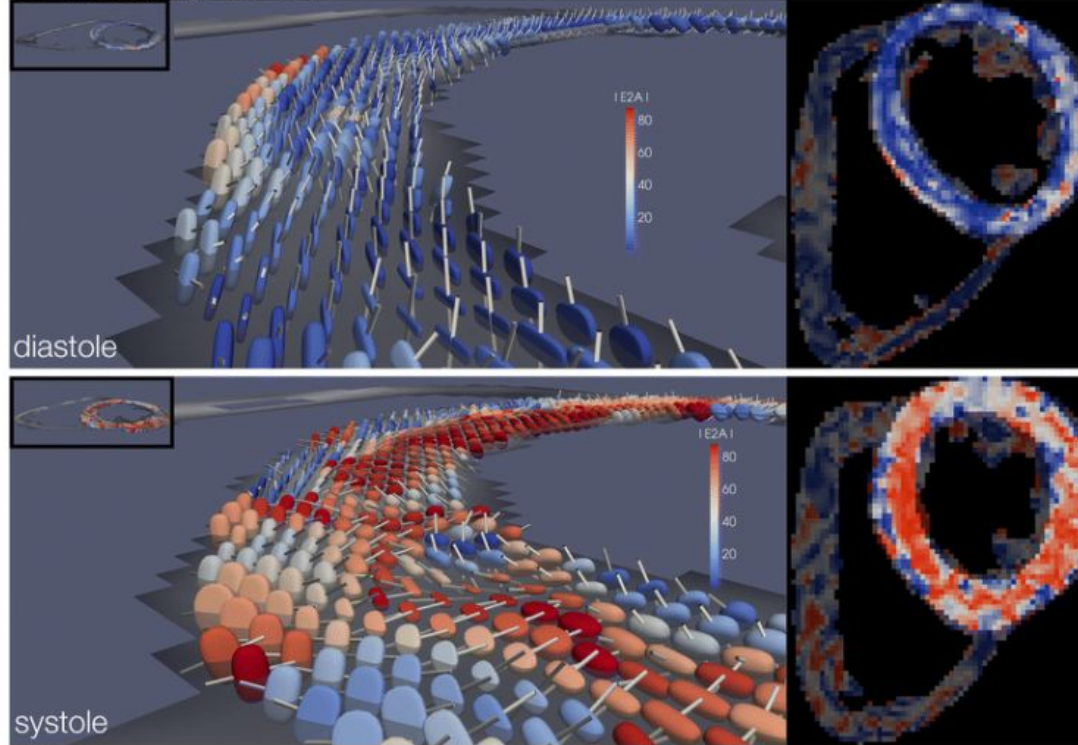


Hyperstreamlines

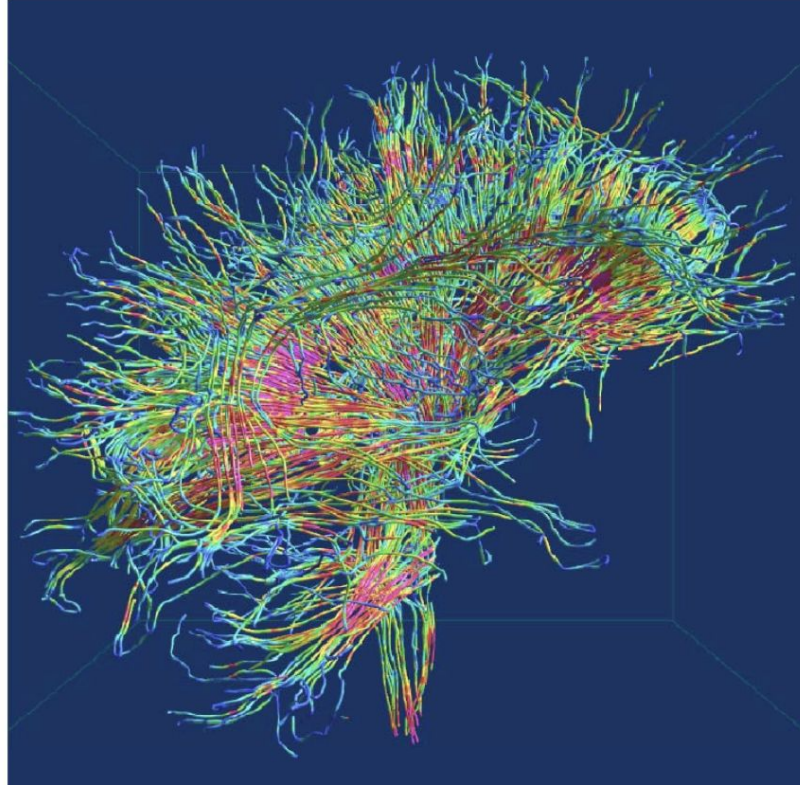


# Tensors: Visual Examples (Ellipsoid Glyphs)

Secondary eigenvector



# Tensors: Visual Examples (Hyperstreamlines)



# Tensors: Visual Examples

<https://youtu.be/wvsE8jm1GzE?t=18s>

# Scalars and Vectors in R