AI5002: Assignment 7

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Download all latex codes from

https://github.com/96143/Assignment-7/blob/main/ assignment%207.tex

Download all Python codes from

https://github.com/96143/Assignment-7/blob/main/ Assignment 7.ipynb

1 Problem

Find the probability distribution of number of doublets in three throws of a pair of dice.

2 Solution

Let X denotes the number of doublets. X can take : The required probabilities are shown in the figure the value 0,1,2 or 3.

Possible doublets are (1,1), (2,2), (3,3), (4,4), (5,5) and (6,6)

Probability of getting a doublet = $\frac{6}{36} = \frac{1}{6}$ Probability of not getting a doublet = 1 - $\frac{1}{6} = \frac{5}{6}$ Now,

P(X = 0) = P(No doublet)

$$= \frac{5}{6} \times \frac{5}{6} \times \frac{5}{6}$$

$$= \frac{125}{216}$$
(2.0.1)

P(X = 1) = P(One doublet and two non doublet)

$$= \frac{1}{6} \times \frac{5}{6} \times \frac{5}{6} + \frac{5}{6} \times \frac{1}{6} \times \frac{5}{6} + \frac{5}{6} \times \frac{5}{6} \times \frac{1}{6}$$
 (2.0.3)
$$= \frac{25}{216} + \frac{25}{216} + \frac{25}{216}$$
 (2.0.4)

$$=\frac{75}{216}\tag{2.0.5}$$

P(X=2) = P(Two doublet and one non doublet)

$$= \frac{1}{6} \times \frac{1}{6} \times \frac{5}{6} + \frac{1}{6} \times \frac{5}{6} \times \frac{1}{6} + \frac{5}{6} \times \frac{1}{6} \times \frac{1}{6}$$
 (2.0.6)

$$=\frac{5}{216} + \frac{5}{216} + \frac{5}{216} \tag{2.0.7}$$

$$=\frac{15}{216}\tag{2.0.8}$$

P(X=3)=P(Three doublets)

$$= \frac{1}{6} \times \frac{1}{6} \times \frac{1}{6} \tag{2.0.9}$$

$$=\frac{1}{216}\tag{2.0.10}$$

X	0	1	2	3
P(X)	125/216	75/216	15/216	1/216