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AI5002: Assignment 8

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Download all latex codes from

https://github.com/96143/Assignment-8/blob/main/Latex.tex

Download all Python codes from

https://github.com/96143/Assignment-8/blob/main/Code.py

1 Problem

Let U and V be two independent zero mean Gaussian random variables of variances $\frac{1}{4}$ and $\frac{1}{9}$ respectively. The probability $\Pr(3V \ge 2U)$ is

2 Solution

$$U = \mathcal{N}\left(0, \frac{1}{4}\right)$$
$$V = \mathcal{N}\left(0, \frac{1}{9}\right)$$

To determine-

$$Pr(3V \ge 2U) = Pr(3V - 2U \ge 0)$$

Let Y = 3V - 2U

$$\therefore E[Y] = 3E[V] - 2E[U]$$

$$\implies E[Y] = 0$$

Also,

$$Var[Y] = 3^{2}Var[V] + 2^{2}Var[U]$$

$$\implies Var[Y] = 9 \times \frac{1}{9} + 4 \times \frac{1}{4}$$

$$\implies Var[Y] = 2$$

$$\therefore Y = \mathcal{N}(0,2)$$

W is a Gaussian Random variable with mean zero and variance 2.

$$Pr(3V - 2U \ge 0) = Pr(Y \ge 0)$$

Since, Y is symmetric about the zero mean axis

$$\therefore \Pr(Y \ge 0) = \frac{1}{2}$$