

1394. Minimum Path Cost in a Grid

Difficulty : Medium

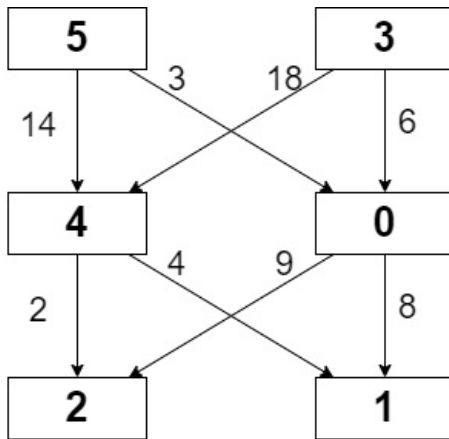
<https://leetcode.com/problems/minimum-path-cost-in-a-grid>

You are given a **0-indexed** $m \times n$ integer matrix `grid` consisting of **distinct** integers from 0 to $m * n - 1$. You can move in this matrix from a cell to any other cell in the **next** row. That is, if you are in cell (x, y) such that $x < m - 1$, you can move to any of the cells $(x + 1, 0), (x + 1, 1), \dots, (x + 1, n - 1)$. **Note** that it is not possible to move from cells in the last row.

Each possible move has a cost given by a **0-indexed** 2D array `moveCost` of size $(m * n) \times n$, where `moveCost[i][j]` is the cost of moving from a cell with value i to a cell in column j of the next row. The cost of moving from cells in the last row of `grid` can be ignored.

The cost of a path in `grid` is the **sum** of all values of cells visited plus the **sum** of costs of all the moves made. Return *the minimum cost of a path that starts from any cell in the first row and ends at any cell in the last row*.

Example 1:



Input: `grid = [[5,3],[4,0],[2,1]]`, `moveCost = [[9,8],[1,5],[10,12],[18,6],[2,4],[14,3]]`

Output: 17

Explanation: The path with the minimum possible cost is the path `5 -> 0 -> 1`.

- The sum of the values of cells visited is $5 + 0 + 1 = 6$.
 - The cost of moving from 5 to 0 is 3.
 - The cost of moving from 0 to 1 is 8.
- So the total cost of the path is $6 + 3 + 8 = 17$.

Example 2:

Input: `grid = [[5,1,2],[4,0,3]]`, `moveCost = [[12,10,15],[20,23,8],[21,7,1],[8,1,13],[9,10,25],[5,3,2]]`

Output: 6

Explanation: The path with the minimum possible cost is the path `2 -> 3`.

- The sum of the values of cells visited is $2 + 3 = 5$.
 - The cost of moving from 2 to 3 is 1.
- So the total cost of this path is $5 + 1 = 6$.

Constraints:

- $m == \text{grid.length}$
- $n == \text{grid}[i].\text{length}$
- $2 \leq m, n \leq 50$
- `grid` consists of distinct integers from 0 to $m * n - 1$.
- $\text{moveCost.length} == m * n$
- $\text{moveCost}[i].\text{length} == n$
- $1 \leq \text{moveCost}[i][j] \leq 100$