

489. Kth Smallest Instructions

Difficulty : Hard

<https://leetcode.com/problems/kth-smallest-instructions>

Bob is standing at cell $(0, 0)$, and he wants to reach destination: $(row, column)$. He can only travel **right** and **down**. You are going to help Bob by providing **instructions** for him to reach destination.

The **instructions** are represented as a string, where each character is either:

- 'H', meaning move horizontally (go **right**), or
- 'V', meaning move vertically (go **down**).

Multiple **instructions** will lead Bob to destination. For example, if destination is $(2, 3)$, both "HHHV" and "HVHV" are valid **instructions**.

However, Bob is very picky. Bob has a lucky number k , and he wants the k^{th} **lexicographically smallest instructions** that will lead him to destination. k is **1-indexed**.

Given an integer array `destination` and an integer k , return *the k^{th} lexicographically smallest instructions that will take Bob to destination*.

Example 1:

(0,0)	(0,1)	(0,2)	(0,3)
(1,0)	(1,1)	(1,2)	(1,3)
(2,0)	(2,1)	(2,2)	(2,3)

Input: `destination = [2,3], k = 1`

Output: "HHHV"

Explanation: All the instructions that reach $(2, 3)$ in lexicographic order are as follows:
["HHHV", "HHVH", "HHVV", "HVHV", "HVHH", "HVVH", "VHHV", "VHHH", "VHVH", "VVHH"].

Example 2:

(0,0)	(0,1)	(0,2)	(0,3)
(1,0)	(1,1)	(1,2)	(1,3)
(2,0)	(2,1)	(2,2)	(2,3)

Input: `destination = [2,3], k = 2`

Output: "HHVH"

Example 3:

(0,0)	(0,1)	(0,2)	(0,3)
(1,0)	(1,1)	(1,2)	(1,3)
(2,0)	(2,1)	(2,2)	(2,3)

Input: destination = [2,3], k = 3

Output: "HHVVH"

Constraints:

- destination.length == 2
- 1 <= row, column <= 15
- 1 <= k <= nCr(row + column, row), where nCr(a, b) denotes a choose b