

# 2nd Partial Project

Computational Mathematics

October 10, 2016

## 1 Introduction

The Cocke–Younger–Kasami algorithm (also called CYK) is a parsing algorithm for context-free grammars (CFG), named after its inventors, John Cocke, Daniel Younger and Tadao Kasami [2]. It is considered a bottom-up parser that uses dynamic programming to build an AST of a given input string. The standard version of CYK works only on CFG given in Chomsky normal form (CNF).

In the worst case, this algorithm has a running time of  $\Theta(n^3 \cdot |G|)$ , where  $n$  is the length of the parsed string and  $|G|$  is the size of the CNF grammar  $G$ . Therefore, it is one of the most efficient parsing algorithms in terms of worst-case asymptotic complexity, although other algorithms exist with better average running time [1].

## 2 Algorithm Description

The input is a context-free grammar in CNF  $G$  and an input string  $x$ . This means  $G$  will contain production rules of the forms  $A \rightarrow \alpha$  and  $A \rightarrow BC$ .

The basic idea of this algorithm is to find for each substring  $w$  of  $x$  the set of all non-terminals ( $V_t$ ) that generate  $w$ . This is done by building a data structure that will contain all the  $V_t$  that leads the creation of  $w$ . If at the top of this structure, the start symbol  $S$  is present, this means such a string  $x$  can be built using  $G$ . Therefore,  $w$  can be generated by  $G$ .

Listing 1: Algorithm 1

```
CYK ( $G < V_n, V_t, P, S >, x$ )
for i=0 to n-1 do
     $T_{i,i+1} = \emptyset$ 
    for  $A \rightarrow a$  do
        if  $a = x_{i,i+1}$  then
             $T_{i,i+1} = T_{i,i+1} \cup \{A\}$ 
        end if
    end for
end for
for m=0 to n do
```

```

for i=0 to n-m do
   $T_{i,i+m} = \emptyset$ 
  for j=i+1 to i+m-1 do
    for  $A \rightarrow BC$  do
      if  $B \in T_{i,j}$  and  $C \in T_{j,i+m}$  then
         $T_{i,i+m} = T_{i,i+m} \cup \{A\}$ 
      end if
    end for
  end for
end for
end for
end for

```

### 3 Deliverables

As part of this project, you and your team have to submit the following:

1. The executable file of your implementation using the programming language you like.
2. The source code of such an implementation.
3. The following testing case:
  - Given the grammar:

$S$	$\rightarrow$	$A B$		$B C$
$A$	$\rightarrow$	$B A$		$a$
$B$	$\rightarrow$	$C C$		$b$
$C$	$\rightarrow$	$A B$		$a$

Verify if  $w_1 = baaba$  and  $w_2 = ababa$  are both accepted. *The solution has to contain the generated AST.*

The solution has to be presented by the complete team at a date and time previously agreed on. Without this, your project cannot be marked. You should present before **October 26th**.

### References

- [1] John E. Hopcroft, Rajeev Motwani, Rotwani, and Jeffrey D. Ullman. *Introduction to Automata Theory, Languages and Computability*. Addison-Wesley Longman Publishing Co., Inc., Boston, MA, USA, 2nd edition, 2000.
- [2] Daniel H. Younger. Recognition and parsing of context-free languages in time  $n^3$ . *Information and Control*, 10(2):189 – 208, 1967.