PG4200: Algorithms And Data Structures

Lesson 06: Hash Maps and Sets

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Hash Function

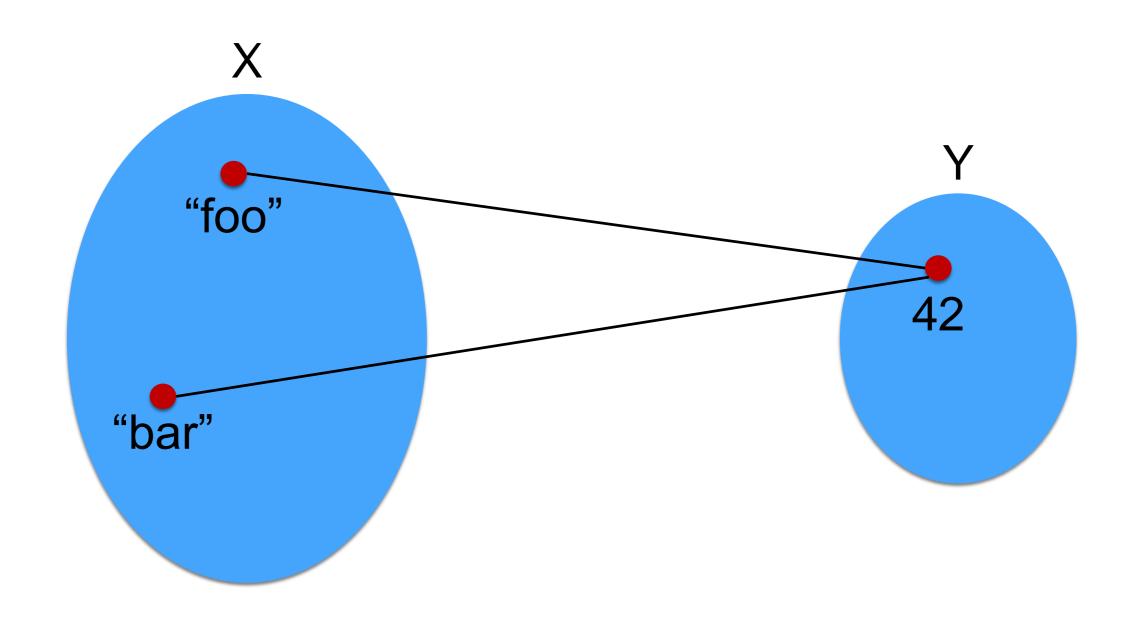
- A function that maps data from an arbitrary size to a specific size
 - eg, mapping strings to a int
- h(x)=y, mapping from domain X to a value in domain Y
- |X| is often much larger than |Y|

Hash Properties

- Deterministic: for a given input x', should always get the same output y'
- Uniform: mapping from X to Y should be ideally spread uniformly over Y,
 - ie the number of elements in X that map to a specific y' should be close to |X|/|Y|
- Performance: either fast (in this course) or slow (security, eg hashing of passwords)

Collisions

- If |X| > |Y|, you cannot avoid h(x') = h(x''), two different values in X mapping to the same value in Y
- Ideally, if uniform, no more than |X|/|Y| collisions per element



Hash Maps

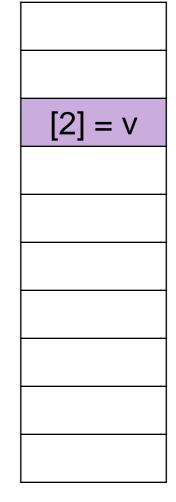
- Still a map from a K key to a V value
- No requirement on ordering of K keys, just being able to compute an hash of it
- In Java, all objects inherits from java.lang.Object, which defines a hashCode() method
- Hash code used as an index for an internal array

Example

put("foo", v)

Internal array buffer of size M=10

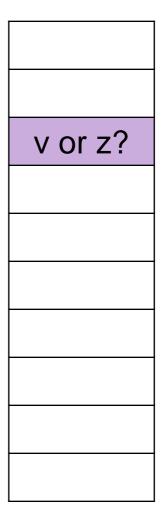
- h("foo")=42
- h("foo")%10 = 2
- Benefit: operations
 (insert/search/etc) have
 cost due to hash
 independent of size N of
 the collection



What About Collisions?

- put("foo", v)
- put("bar", z)
- h("foo")=h("bar")
 - ie, collision due to same hash
- h("foo")%10 = 2
- What to do?

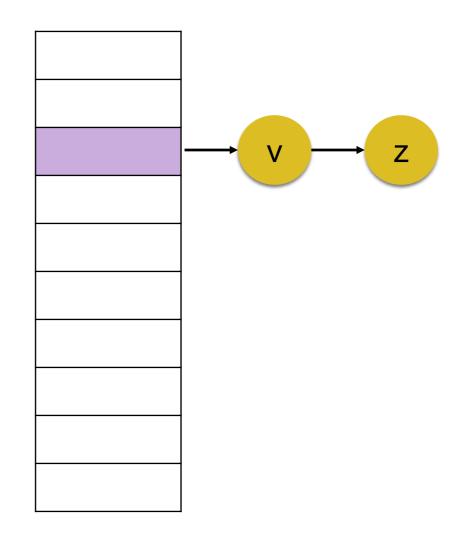
Internal array buffer of size M=10



Different Strategies

- put("foo", v)
- put("bar", z)
- h("foo")=h("bar")
 - ie, collision due to same hash
- Use list at each position sharing same hash

Internal array buffer of size M=10



Cost

- Worst case: O(N) if all elements end up in same "bucket" (ie same value for h()%M), the map would be equivalent to a list
 - operations to search on list would be O(N), albeit insert would be O(1)
- But, if M large enough compared to N, and hash function is uniform enough, you can have a O(1) cost in many cases
 - even if you have some collisions, it will not be a problem, as you
 would have a small number of elements in the list

Hash or RBT?

- Hash Maps is the most popular and widely used
- If you know how much data you II insert at most, can choose a good large enough M
- So in most cases, we are in O(1) Hash vs O(log N) RBT
- But Hash can be O(N) in worst case, vs RBT guarantees
 O(log N) in all cases
 - eg, in critical systems where you MUST guarantee a response within a certain amount of time, might want to use RBT
- Hash does not need ordering of keys

Set

- In mathematics, a set is a collection of elements where:
 - 1) ordering is not important: ie {1,2,3} is equivalent to {2,3,1}
 - 2) no repetitions: ie {1,2} is the same as {2,1,1,2,2,1,1,2,1}
- How to implement a Set in Java?
- Easy: use an internal Map<K,V> were your values in the set are the keys K, and you just ignore the values V

Keys and Immutability

- Immutable Object: an object whose state cannot be changed once created
- Example: Strings are immutable
 - eg, concatenation with + and methods like toUpperCase() and substring() do NOT change the String, but rather create a NEW one
- Keys in a Map/Set MUST be immutable... why?

Different Hash

foo

miss

- Foo foo = new Foo();
- set.add(foo);
- assertTrue(set.contains(foo));
- // h(foo) = 42 , 42 % M = 5
- foo.setSomeVariable(...);
- // h(foo) = 55 , 55 % M = 5
- assertFalse(set.contains(foo));

java.lang.Object

- Object does define two methods: hashCode() and equals()
- Those methods will depend on the internal fields of the object
- Important: if two objects are equals, then they MUST have same hash code
 - A.equals(B) implies A.hashCode()==B.hashCode()
 - The vice-versa is not necessarily true, ie A.hashCode()==B.hashCode()
 does not imply A.equals(B), although that could happen
- What if constraint is not satisfied? Expect weird bugs when using maps and sets...

Homework

- Study Book Chapter 3.4 and 3.5
- Study code in the org.pg4200.les06 package
- Do exercises in exercises/ex06
- Extra: do exercises in the book