

```

1: ICPC Library @ tapu
2: -----
3: |                                tree                                |
4: -----
5:
6: #####
7: ##### tree-diameter.cpp #####
8: #####
9:
10: template< typename T >
11: pair< T, int > dfs(const WeightedGraph< T > &g, int idx, int par) {
12:     pair< T, int > ret(0, idx);
13:     for(auto &e : g[idx]) {
14:         if(e.to == par) continue;
15:         auto cost = dfs(g, e.to, idx);
16:         cost.first += e.cost;
17:         ret = max(ret, cost);
18:     }
19:     return ret;
20: }
21:
22: template< typename T >
23: T tree_diameter(const WeightedGraph< T > &g) {
24:     auto p = dfs(g, 0, -1);
25:     auto q = dfs(g, p.second, -1);
26:     return (q.first);
27: }
28:
29:
30: #####
31: ##### doubling-lowest-common-ancestor.cpp #####
32: #####
33:
34: template< typename G >
35: struct DoublingLowestCommonAncestor {
36:     const int LOG;
37:     vector< int > dep;
38:     const G &g;
39:     vector< vector< int > > table;
40:
41:     DoublingLowestCommonAncestor(const G &g) : g(g), dep(g.size()), LOG(32 - __built
in_clz(g.size())) {
42:         table.assign(LOG, vector< int >(g.size(), -1));
43:     }
44:
45:     void dfs(int idx, int par, int d) {
46:         table[0][idx] = par;
47:         dep[idx] = d;
48:         for(auto &to : g[idx]) {
49:             if(to != par) dfs(to, idx, d + 1);
50:         }
51:     }
52:
53:     void build() {
54:         dfs(0, -1, 0);
55:         for(int k = 0; k + 1 < LOG; k++) {
56:             for(int i = 0; i < table[k].size(); i++) {
57:                 if(table[k][i] == -1) table[k + 1][i] = -1;
58:                 else table[k + 1][i] = table[k][table[k][i]];
59:             }
60:         }
61:     }
62:
63:     int query(int u, int v) {
64:         if(dep[u] > dep[v]) swap(u, v);
65:         for(int i = LOG - 1; i >= 0; i--) {
66:             if(((dep[v] - dep[u]) >> i) & 1) v = table[i][v];
67:         }
68:         if(u == v) return u;
69:         for(int i = LOG - 1; i >= 0; i--) {

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70:         if(table[i][u] != table[i][v]) {
71:             u = table[i][u];
72:             v = table[i][v];
73:         }
74:     }
75:     return table[0][u];
76: }
77: };
78:
79:
80: #####
81: ##### tree-isomorphism.cpp #####
82: #####
83:
84: template< typename G >
85: bool tree_isomorphism(const G &a, const G &b) {
86:     if(a.size() != b.size()) return false;
87:
88:     const int N = (int) a.size();
89:     using pvi = pair< vector< int >, vector< int > >;
90:
91:     auto get_uvu = [&](const G &t, int e) {
92:         stack< pair< int, int > > st;
93:         st.emplace(e, -1);
94:         vector< int > dep(N, -1), par(N);
95:         while(!st.empty()) {
96:             auto p = st.top();
97:             if(dep[p.first] == -1) {
98:                 dep[p.first] = p.second == -1 ? 0 : dep[p.second] + 1;
99:                 for(auto &to : t[p.first]) if(to != p.second) st.emplace(to, p.first);
100:             } else {
101:                 par[p.first] = p.second;
102:                 st.pop();
103:             }
104:         }
105:         return make_pair(dep, par);
106:     };
107:
108:     auto solve = [&](const pvi &latte, const pvi &malta) {
109:
110:         int d = *max_element(begin(latte.first), end(latte.first));
111:         if(d != *max_element(begin(malta.first), end(malta.first))) return false;
112:
113:         vector< vector< int > > latte_d(d + 1), malta_d(d + 1), latte_key(N), malta_ke
y(N);
114:
115:         for(int i = 0; i < N; i++) latte_d[latte.first[i]].emplace_back(i);
116:         for(int i = 0; i < N; i++) malta_d[malta.first[i]].emplace_back(i);
117:
118:         for(int i = d; i >= 0; i--) {
119:             map< vector< int >, int > ord;
120:             for(auto &idx : latte_d[i]) {
121:                 sort(begin(latte_key[idx]), end(latte_key[idx]));
122:                 ord[latte_key[idx]]++;
123:             }
124:             for(auto &idx : malta_d[i]) {
125:                 sort(begin(malta_key[idx]), end(malta_key[idx]));
126:                 if(--ord[malta_key[idx]] < 0) return false;
127:             }
128:             if(i == 0) return ord.size() == 1;
129:
130:             int ptr = 0;
131:             for(auto &p : ord) {
132:                 if(p.second != 0) return false;
133:                 p.second = ptr++;
134:             }
135:             for(auto &idx : latte_d[i]) {
136:                 latte_key[latte.second[idx]].emplace_back(ord[latte_key[idx]]);
137:             }
138:             for(auto &idx : malta_d[i]) {

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139:         malta_key[malta.second[idx]].emplace_back(ord[malta_key[idx]]);
140:     }
141: }
142:     assert(0);
143: };
144: auto p = centroid(a), q = centroid(b);
145: if(p.size() != q.size()) return false;
146: auto a1 = get_uku(a, p[0]);
147: auto b1 = get_uku(b, q[0]);
148: if(solve(a1, b1)) return true;
149: if(p.size() == 1) return false;
150: auto a2 = get_uku(a, p[1]);
151: return solve(a2, b1);
152: }
153:
154:
155: #####
156: ##### heavy-light-decomposition.cpp #####
157: #####
158:
159: template< typename G >
160: struct HeavyLightDecomposition {
161:     G &g;
162:     vector< int > sz, in, out, head, rev, par;
163:
164:     HeavyLightDecomposition(G &g) :
165:         g(g), sz(g.size()), in(g.size()), out(g.size()), head(g.size()), rev(g.size(
166: )), par(g.size()) {}
167:
168:     void dfs_sz(int idx, int p) {
169:         par[idx] = p;
170:         sz[idx] = 1;
171:         if(g[idx].size() && g[idx][0] == p) swap(g[idx][0], g[idx].back());
172:         for(auto &to : g[idx]) {
173:             if(to == p) continue;
174:             dfs_sz(to, idx);
175:             sz[idx] += sz[to];
176:             if(sz[g[idx][0]] < sz[to]) swap(g[idx][0], to);
177:         }
178:     }
179:
180:     void dfs_hld(int idx, int par, int &times) {
181:         in[idx] = times++;
182:         rev[in[idx]] = idx;
183:         for(auto &to : g[idx]) {
184:             if(to == par) continue;
185:             head[to] = (g[idx][0] == to ? head[idx] : to);
186:             dfs_hld(to, idx, times);
187:         }
188:         out[idx] = times;
189:     }
190:
191:     void build() {
192:         dfs_sz(0, -1);
193:         int t = 0;
194:         dfs_hld(0, -1, t);
195:     }
196:
197:     int la(int v, int k) {
198:         while(1) {
199:             int u = head[v];
200:             if(in[v] - k >= in[u]) return rev[in[v] - k];
201:             k -= in[v] - in[u] + 1;
202:             v = par[u];
203:         }
204:     }
205:
206:     int lca(int u, int v) {
207:         for(;; v = par[head[v]]) {
208:             if(in[u] > in[v]) swap(u, v);

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208:         if(head[u] == head[v]) return u;
209:     }
210: }
211:
212: template< typename T, typename Q, typename F >
213: T query(int u, int v, const T &ti, const Q &q, const F &f, bool edge = false) {
214:     T l = ti, r = ti;
215:     for(;; v = par[head[v]]) {
216:         if(in[u] > in[v]) swap(u, v), swap(l, r);
217:         if(head[u] == head[v]) break;
218:         l = f(q(in[head[v]], in[v] + 1), l);
219:     }
220:     return f(f(q(in[u] + edge, in[v] + 1), l), r);
221: // return {f(q(in[u] + edge, in[v] + 1), l), r};
222: }
223:
224: template< typename Q >
225: void add(int u, int v, const Q &q, bool edge = false) {
226:     for(;; v = par[head[v]]) {
227:         if(in[u] > in[v]) swap(u, v);
228:         if(head[u] == head[v]) break;
229:         q(in[head[v]], in[v] + 1);
230:     }
231:     q(in[u] + edge, in[v] + 1);
232: }
233: };
234:
235:
236: #####
237: ##### rerooting.cpp #####
238: #####
239:
240: template< typename Data, typename T >
241: struct ReRooting {
242:
243:     struct Node {
244:         int to, rev;
245:         Data data;
246:     };
247:
248:     using F1 = function< T(T, T) >;
249:     using F2 = function< T(T, Data) >;
250:
251:     vector< vector< Node > > g;
252:     vector< vector< T > > ldp, rdp;
253:     vector< int > lptr, rptr;
254:     const F1 f1;
255:     const F2 f2;
256:     const T ident;
257:
258:     ReRooting(int n, const F1 &f1, const F2 &f2, const T &ident) :
259:         g(n), ldp(n), rdp(n), lptr(n), rptr(n), f1(f1), f2(f2), ident(ident) {}
260:
261:     void add_edge(int u, int v, const Data &d) {
262:         g[u].emplace_back((Node) {v, (int) g[v].size(), d});
263:         g[v].emplace_back((Node) {u, (int) g[u].size() - 1, d});
264:     }
265:
266:     void add_edge_bi(int u, int v, const Data &d, const Data &e) {
267:         g[u].emplace_back((Node) {v, (int) g[v].size(), d});
268:         g[v].emplace_back((Node) {u, (int) g[u].size() - 1, e});
269:     }
270:
271:
272:     T dfs(int idx, int par) {
273:
274:         while(lptr[idx] != par && lptr[idx] < g[idx].size()) {
275:             auto &e = g[idx][lptr[idx]];
276:             ldp[idx][lptr[idx] + 1] = f1(ldp[idx][lptr[idx]], f2(dfs(e.to, e.rev), e.dat
a));

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277:         ++lptr[idx];
278:     }
279:     while(rptr[idx] != par && rptr[idx] >= 0) {
280:         auto &e = g[idx][rptr[idx]];
281:         rdp[idx][rptr[idx]] = f1(rdp[idx][rptr[idx] + 1], f2(dfs(e.to, e.rev), e.data));
282:         --rptr[idx];
283:     }
284:     if(par < 0) return rdp[idx][0];
285:     return f1(ldp[idx][par], rdp[idx][par + 1]);
286: }
287:
288: vector< T > solve() {
289:     for(int i = 0; i < g.size(); i++) {
290:         ldp[i].assign(g[i].size() + 1, ident);
291:         rdp[i].assign(g[i].size() + 1, ident);
292:         lptr[i] = 0;
293:         rptr[i] = (int) g[i].size() - 1;
294:     }
295:     vector< T > ret;
296:     for(int i = 0; i < g.size(); i++) {
297:         ret.push_back(dfs(i, -1));
298:     }
299:     return ret;
300: }
301: };
302:
303:
304: #####
305: ##### convert-rooted-tree.cpp #####
306: #####
307:
308: template< typename G >
309: G convert_rooted_tree(const G &g, int r = 0) {
310:     int N = (int) g.size();
311:     G rg(N);
312:     vector< int > v(N);
313:     v[r] = 1;
314:     queue< int > que;
315:     que.emplace(r);
316:     while(!que.empty()) {
317:         auto p = que.front();
318:         que.pop();
319:         for(auto &to : g[p]) {
320:             if(v[to] == 0) {
321:                 v[to] = 1;
322:                 que.emplace(to);
323:                 rg[p].emplace_back(to);
324:             }
325:         }
326:     }
327:     return rg;
328: }
329:
330:
331: #####
332: ##### centroid-decomposition.cpp #####
333: #####
334:
335: template< typename G >
336: struct CentroidDecomposition {
337:     const G &g;
338:     vector< int > sub;
339:     vector< vector< int > > belong;
340:     vector< bool > v;
341:
342:     CentroidDecomposition(const G &g) : g(g), sub(g.size()), v(g.size()), belong(g.size()) {}
343:
344:     inline int build_dfs(int idx, int par) {

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345:     sub[idx] = 1;
346:     for(auto &to : g[idx]) {
347:         if(to == par || v[to]) continue;
348:         sub[idx] += build_dfs(to, idx);
349:     }
350:     return sub[idx];
351: }
352:
353: inline int search_centroid(int idx, int par, const int mid) {
354:     for(auto &to : g[idx]) {
355:         if(to == par || v[to]) continue;
356:         if(sub[to] > mid) return search_centroid(to, idx, mid);
357:     }
358:     return idx;
359: }
360:
361: inline void belong_dfs(int idx, int par, int centroid) {
362:     belong[idx].emplace_back(centroid);
363:     for(auto &to : g[idx]) {
364:         if(to == par || v[to]) continue;
365:         belong_dfs(to, idx, centroid);
366:     }
367: }
368:
369: inline int build(UnWeightedGraph &t, int idx) {
370:     int centroid = search_centroid(idx, -1, build_dfs(idx, -1) / 2);
371:     v[centroid] = true;
372:     belong_dfs(centroid, -1, centroid);
373:     for(auto &to : g[centroid]) {
374:         if(!v[to]) t[centroid].emplace_back(build(t, to));
375:     }
376:     v[centroid] = false;
377:     return centroid;
378: }
379:
380: inline int build(UnWeightedGraph &t) {
381:     t.resize(g.size());
382:     return build(t, 0);
383: }
384: };
385:
386:
387: #####
388: ##### centroid.cpp #####
389: #####
390:
391: template< typename G >
392: vector< int > centroid(const G &g) {
393:     const int N = (int) g.size();
394:
395:     stack< pair< int, int > > st;
396:     st.emplace(0, -1);
397:     vector< int > sz(N), par(N);
398:     while(!st.empty()) {
399:         auto p = st.top();
400:         if(sz[p.first] == 0) {
401:             sz[p.first] = 1;
402:             for(auto &to : g[p.first]) if(to != p.second) st.emplace(to, p.first);
403:         } else {
404:             for(auto &to : g[p.first]) if(to != p.second) sz[p.first] += sz[to];
405:             par[p.first] = p.second;
406:             st.pop();
407:         }
408:     }
409:
410:     vector< int > ret;
411:     int size = N;
412:     for(int i = 0; i < N; i++) {
413:         int val = N - sz[i];
414:         for(auto &to : g[i]) if(to != par[i]) val = max(val, sz[to]);

```

```

415:         if(val < size) size = val, ret.clear();
416:         if(val == size) ret.emplace_back(i);
417:     }
418:
419:     return ret;
420: }
421:
422:
423: -----
424: |                                     graph                                     |
425: -----
426:
427: #####
428: ##### boruvka.cpp #####
429: #####
430:
431: template< typename T, typename F >
432: T boruvka(int N, F f) {
433:     vector< int > rev(N), belong(N);
434:     UnionFind uf(N);
435:     T ret = T();
436:     while(uf.size(0) != N) {
437:         int ptr = 0;
438:         for(int i = 0; i < N; i++) {
439:             if(uf.find(i) == i) {
440:                 belong[i] = ptr++;
441:                 rev[belong[i]] = i;
442:             }
443:         }
444:         for(int i = 0; i < N; i++) {
445:             belong[i] = belong[uf.find(i)];
446:         }
447:         auto v = f(ptr, belong);
448:         bool update = false;
449:         for(int i = 0; i < ptr; i++) {
450:             if(~v[i].second && uf.unite(rev[i], rev[v[i].second])) {
451:                 ret += v[i].first;
452:                 update = true;
453:             }
454:         }
455:         if(!update) return -1; // notice!!
456:     }
457:     return ret;
458: }
459:
460:
461: #####
462: ##### dijkstra.cpp #####
463: #####
464:
465: template< typename T >
466: vector< T > dijkstra(WeightedGraph< T > &g, int s) {
467:     const auto INF = numeric_limits< T >::max();
468:     vector< T > dist(g.size(), INF);
469:
470:     using Pi = pair< T, int >;
471:     priority_queue< Pi, vector< Pi >, greater< Pi > > que;
472:     dist[s] = 0;
473:     que.emplace(dist[s], s);
474:     while(!que.empty()) {
475:         T cost;
476:         int idx;
477:         tie(cost, idx) = que.top();
478:         que.pop();
479:         if(dist[idx] < cost) continue;
480:         for(auto &e : g[idx]) {
481:             auto next_cost = cost + e.cost;
482:             if(dist[e.to] <= next_cost) continue;
483:             dist[e.to] = next_cost;
484:             que.emplace(dist[e.to], e.to);

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485:     }
486:   }
487:   return dist;
488: }
489:
490:
491: #####
492: ##### template.cpp #####
493: #####
494:
495: template< typename T >
496: struct edge {
497:   int src, to;
498:   T cost;
499:
500:   edge(int to, T cost) : src(-1), to(to), cost(cost) {}
501:
502:   edge(int src, int to, T cost) : src(src), to(to), cost(cost) {}
503:
504:   edge &operator=(const int &x) {
505:     to = x;
506:     return *this;
507:   }
508:
509:   operator int() const { return to; }
510: };
511:
512: template< typename T >
513: using Edges = vector< edge< T > >;
514: template< typename T >
515: using WeightedGraph = vector< Edges< T > >;
516: using UnWeightedGraph = vector< vector< int > >;
517: template< typename T >
518: using Matrix = vector< vector< T > >;
519:
520:
521: #####
522: ##### bipartite-matching.cpp #####
523: #####
524:
525: struct BipartiteMatching {
526:   vector< vector< int > > graph;
527:   vector< int > match, alive, used;
528:   int timestamp;
529:
530:   BipartiteMatching(int n) : graph(n), alive(n, 1), used(n, 0), match(n, -1), time
stamp(0) {}
531:
532:   void add_edge(int u, int v) {
533:     graph[u].push_back(v);
534:     graph[v].push_back(u);
535:   }
536:
537:   bool dfs(int idx) {
538:     used[idx] = timestamp;
539:     for(auto &to : graph[idx]) {
540:       int to_match = match[to];
541:       if(alive[to] == 0) continue;
542:       if(to_match == -1 || (used[to_match] != timestamp && dfs(to_match))) {
543:         match[idx] = to;
544:         match[to] = idx;
545:         return true;
546:       }
547:     }
548:     return false;
549:   }
550:
551:   int bipartite_matching() {
552:     int ret = 0;
553:     for(int i = 0; i < graph.size(); i++) {
```



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554:         if(alive[i] == 0) continue;
555:         if(match[i] == -1) {
556:             ++timestamp;
557:             ret += dfs(i);
558:         }
559:     }
560:     return ret;
561: }
562:
563: void output() {
564:     for(int i = 0; i < graph.size(); i++) {
565:         if(i < match[i]) {
566:             cout << i << "-" << match[i] << endl;
567:         }
568:     }
569: }
570: };
571:
572:
573:
574: #####
575: ##### warshall-floyd.cpp #####
576: #####
577:
578: template< typename T >
579: void warshall_floyd(Matrix< T > &g, T INF) {
580:     for(int k = 0; k < g.size(); k++) {
581:         for(int i = 0; i < g.size(); i++) {
582:             for(int j = 0; j < g.size(); j++) {
583:                 if(g[i][k] == INF || g[k][j] == INF) continue;
584:                 g[i][j] = min(g[i][j], g[i][k] + g[k][j]);
585:             }
586:         }
587:     }
588: }
589:
590:
591: #####
592: ##### gabow-edmonds.cpp #####
593: #####
594:
595: // https://qiita.com/Kutimoti\_T/items/5b579773e0a24d650bdf
596: struct GabowEdmonds {
597:
598:     struct edge {
599:         int to, idx;
600:     };
601:
602:     vector< vector< edge > > g;
603:     vector< pair< int, int > > edges;
604:     vector< int > mate, label, first;
605:     queue< int > que;
606:
607:     GabowEdmonds(int n) : g(n + 1), mate(n + 1), label(n + 1, -1), first(n + 1) {}
608:
609:     void add_edge(int u, int v) {
610:         ++u, ++v;
611:         g[u].push_back((edge) {v, (int) (edges.size() + g.size())});
612:         g[v].push_back((edge) {u, (int) (edges.size() + g.size())});
613:         edges.emplace_back(u, v);
614:     }
615:
616:     int find(int x) {
617:         if(label[first[x]] < 0) return first[x];
618:         first[x] = find(first[x]);
619:         return first[x];
620:     }
621:
622:     void rematch(int v, int w) {
623:         int t = mate[v];

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624:     mate[v] = w;
625:     if(mate[t] != v) return;
626:     if(label[v] < g.size()) {
627:         mate[t] = label[v];
628:         rematch(label[v], t);
629:     } else {
630:         int x = edges[label[v] - g.size()].first;
631:         int y = edges[label[v] - g.size()].second;
632:         rematch(x, y);
633:         rematch(y, x);
634:     }
635: }
636:
637: void assign_label(int x, int y, int num) {
638:     int r = find(x);
639:     int s = find(y);
640:     int join = 0;
641:     if(r == s) return;
642:     label[r] = -num;
643:     label[s] = -num;
644:     while(true) {
645:         if(s != 0) swap(r, s);
646:         r = find(label[mate[r]]);
647:         if(label[r] == -num) {
648:             join = r;
649:             break;
650:         }
651:         label[r] = -num;
652:     }
653:     int v = first[x];
654:     while(v != join) {
655:         que.push(v);
656:         label[v] = num;
657:         first[v] = join;
658:         v = first[label[mate[v]]];
659:     }
660:     v = first[y];
661:     while(v != join) {
662:         que.push(v);
663:         label[v] = num;
664:         first[v] = join;
665:         v = first[label[mate[v]]];
666:     }
667: }
668:
669: bool augment_check(int u) {
670:     que = queue< int >();
671:     first[u] = 0;
672:     label[u] = 0;
673:     que.push(u);
674:     while(!que.empty()) {
675:         int x = que.front();
676:         que.pop();
677:         for(auto e : g[x]) {
678:             int y = e.to;
679:             if(mate[y] == 0 && y != u) {
680:                 mate[y] = x;
681:                 rematch(x, y);
682:                 return true;
683:             } else if(label[y] >= 0) {
684:                 assign_label(x, y, e.idx);
685:             } else if(label[mate[y]] < 0) {
686:                 label[mate[y]] = x;
687:                 first[mate[y]] = y;
688:                 que.push(mate[y]);
689:             }
690:         }
691:     }
692:     return false;
693: }

```

```

694:
695:     vector< pair< int, int > > max_matching() {
696:         for(int i = 1; i < g.size(); i++) {
697:             if(mate[i] != 0) continue;
698:             if(augment_check(i)) label.assign(g.size(), -1);
699:         }
700:         vector< pair< int, int > > ret;
701:         for(int i = 1; i < g.size(); i++) {
702:             if(i < mate[i]) ret.emplace_back(i - 1, mate[i] - 1);
703:         }
704:         return ret;
705:     }
706: };
707:
708:
709: #####
710: ##### maxflow-lower-bound.cpp #####
711: #####
712:
713: template< typename flow_t, template< typename > class F >
714: struct MaxFlowLowerBound {
715:     F< flow_t > flow;
716:     vector< flow_t > in, up;
717:     typename F< flow_t >::edge *latte, *malta;
718:     int X, Y, V;
719:     flow_t sum;
720:
721:     MaxFlowLowerBound(int V) : V(V), flow(V + 2), X(V), Y(V + 1), sum(0), in(V) {}
722:
723:     void add_edge(int from, int to, flow_t low, flow_t high) {
724:         assert(from != to);
725:         flow.add_edge(from, to, high - low, up.size());
726:         in[from] -= low;
727:         in[to] += low;
728:         up.emplace_back(high);
729:     }
730:
731:     void build() {
732:         for(int i = 0; i < V; i++) {
733:             if(in[i] > 0) {
734:                 flow.add_edge(X, i, in[i]);
735:                 sum += in[i];
736:             } else if(in[i] < 0) {
737:                 flow.add_edge(i, Y, -in[i]);
738:             }
739:         }
740:     }
741:
742:     bool can_flow(int s, int t) {
743:         assert(s != t);
744:         flow.add_edge(t, s, flow.INF);
745:         latte = &flow.graph[t].back();
746:         malta = &flow.graph[s].back();
747:         return can_flow();
748:     }
749:
750:     bool can_flow() {
751:         build();
752:         auto ret = flow.max_flow(X, Y);
753:         return ret >= sum;
754:     }
755:
756:     flow_t max_flow(int s, int t) {
757:         if(can_flow(s, t)) {
758:             return flow.max_flow(s, t);
759:         } else {
760:             return -1;
761:         }
762:     }
763:

```

```

764:   flow_t min_flow(int s, int t) {
765:       if(can_flow(s, t)) {
766:           auto ret = flow.INF - latte->cap;
767:           latte->cap = malta->cap = 0;
768:           return ret - flow.max_flow(t, s);
769:       } else {
770:           return -1;
771:       }
772:   }
773:
774:   void output(int M) {
775:       vector< flow_t > ans(M);
776:       for(int i = 0; i < flow.graph.size(); i++) {
777:           for(auto &e : flow.graph[i]) {
778:               if(!e.isrev && ~e.idx) ans[e.idx] = up[e.idx] - e.cap;
779:           }
780:       }
781:       for(auto &p : ans) cout << p << endl;
782:   }
783: };
784:
785:
786: #####
787: ##### primal-dual.cpp #####
788: #####
789:
790: template< typename flow_t, typename cost_t >
791: struct PrimalDual {
792:     const cost_t INF;
793:
794:     struct edge {
795:         int to;
796:         flow_t cap;
797:         cost_t cost;
798:         int rev;
799:         bool isrev;
800:     };
801:     vector< vector< edge > > graph;
802:     vector< cost_t > potential, min_cost;
803:     vector< int > prevv, preve;
804:
805:     PrimalDual(int V) : graph(V), INF(numeric_limits< cost_t >::max()) {}
806:
807:     void add_edge(int from, int to, flow_t cap, cost_t cost) {
808:         graph[from].emplace_back((edge) {to, cap, cost, (int) graph[to].size(), false}
);
809:         graph[to].emplace_back((edge) {from, 0, -cost, (int) graph[from].size() - 1, true});
810:     }
811:
812:     cost_t min_cost_flow(int s, int t, flow_t f) {
813:         int V = (int) graph.size();
814:         cost_t ret = 0;
815:         using Pi = pair< cost_t, int >;
816:         priority_queue< Pi, vector< Pi >, greater< Pi > > que;
817:         potential.assign(V, 0);
818:         preve.assign(V, -1);
819:         prevv.assign(V, -1);
820:
821:         while(f > 0) {
822:             min_cost.assign(V, INF);
823:             que.emplace(0, s);
824:             min_cost[s] = 0;
825:             while(!que.empty()) {
826:                 Pi p = que.top();
827:                 que.pop();
828:                 if(min_cost[p.second] < p.first) continue;
829:                 for(int i = 0; i < graph[p.second].size(); i++) {
830:                     edge &e = graph[p.second][i];
831:                     cost_t nextCost = min_cost[p.second] + e.cost + potential[p.second] - po

```

```

tential[e.to];
832:         if(e.cap > 0 && min_cost[e.to] > nextCost) {
833:             min_cost[e.to] = nextCost;
834:             prevv[e.to] = p.second, preve[e.to] = i;
835:             que.emplace(min_cost[e.to], e.to);
836:         }
837:     }
838: }
839: if(min_cost[t] == INF) return -1;
840: for(int v = 0; v < V; v++) potential[v] += min_cost[v];
841: flow_t addflow = f;
842: for(int v = t; v != s; v = prevv[v]) {
843:     addflow = min(addflow, graph[prevv[v]][preve[v]].cap);
844: }
845: f -= addflow;
846: ret += addflow * potential[t];
847: for(int v = t; v != s; v = prevv[v]) {
848:     edge &e = graph[prevv[v]][preve[v]];
849:     e.cap -= addflow;
850:     graph[v][e.rev].cap += addflow;
851: }
852: }
853: return ret;
854: }
855:
856: void output() {
857:     for(int i = 0; i < graph.size(); i++) {
858:         for(auto &e : graph[i]) {
859:             if(e.isrev) continue;
860:             auto &rev_e = graph[e.to][e.rev];
861:             cout << i << "->" << e.to << " (flow: " << rev_e.cap << "/" << rev_e.cap +
e.cap << ")" << endl;
862:         }
863:     }
864: }
865: };
866:
867:
868: #####
869: ##### bellman-ford.cpp #####
870: #####
871:
872: template< typename T >
873: vector< T > bellman_ford(Edges< T > &edges, int V, int s) {
874:     const auto INF = numeric_limits< T >::max();
875:     vector< T > dist(V, INF);
876:     dist[s] = 0;
877:     for(int i = 0; i < V - 1; i++) {
878:         for(auto &e : edges) {
879:             if(dist[e.src] == INF) continue;
880:             dist[e.to] = min(dist[e.to], dist[e.src] + e.cost);
881:         }
882:     }
883:     for(auto &e : edges) {
884:         if(dist[e.src] == INF) continue;
885:         if(dist[e.src] + e.cost < dist[e.to]) return vector< T >();
886:     }
887:     return dist;
888: }
889:
890:
891:
892: #####
893: ##### hungarian.cpp #####
894: #####
895:
896: template< typename T >
897: T hungarian(Matrix< T > &A) {
898:     const T infy = numeric_limits< T >::max();
899:     const int N = (int) A.size();

```

```

900:  const int M = (int) A[0].size();
901:  vector< int > P(M), way(M);
902:  vector< T > U(N, 0), V(M, 0), minV;
903:  vector< bool > used;
904:
905:  for(int i = 1; i < N; i++) {
906:      P[0] = i;
907:      minV.assign(M, infity);
908:      used.assign(M, false);
909:      int j0 = 0;
910:      while(P[j0] != 0) {
911:          int i0 = P[j0], j1 = 0;
912:          used[j0] = true;
913:          T delta = infity;
914:          for(int j = 1; j < M; j++) {
915:              if(used[j]) continue;
916:              T curr = A[i0][j] - U[i0] - V[j];
917:              if(curr < minV[j]) minV[j] = curr, way[j] = j0;
918:              if(minV[j] < delta) delta = minV[j], j1 = j;
919:          }
920:          for(int j = 0; j < M; j++) {
921:              if(used[j]) U[P[j]] += delta, V[j] -= delta;
922:              else minV[j] -= delta;
923:          }
924:          j0 = j1;
925:      }
926:      do {
927:          P[j0] = P[way[j0]];
928:          j0 = way[j0];
929:      } while(j0 != 0);
930:  }
931:  return -V[0];
932: }
933:
934:
935: #####
936: ##### maximum-independent-set.cpp #####
937: #####
938:
939: template< typename T >
940: vector< int > maximum_independent_set(const Matrix< T > &g, int trial = 1000000) {
941:
942:     int N = (int) g.size();
943:     vector< uint64_t > bit(N);
944:
945:     assert(N <= 64);
946:     for(int i = 0; i < N; i++) {
947:         for(int j = 0; j < N; j++) {
948:             if(i != j) {
949:                 assert(g[i][j] == g[j][i]);
950:                 if(g[i][j]) bit[i] |= uint64_t(1) << j;
951:             }
952:         }
953:     }
954:
955:     vector< int > ord(N);
956:     iota(begin(ord), end(ord), 0);
957:     mt19937 mt(chrono::steady_clock::now().time_since_epoch().count());
958:     int ret = 0;
959:     uint64_t ver;
960:     for(int i = 0; i < trial; i++) {
961:         shuffle(begin(ord), end(ord), mt);
962:         uint64_t used = 0;
963:         int add = 0;
964:         for(int j : ord) {
965:             if(used & bit[j]) continue;
966:             used |= uint64_t(1) << j;
967:             ++add;
968:         }
969:         if(ret < add) {

```

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```
970:         ret = add;
971:         ver = used;
972:     }
973: }
974: vector< int > ans;
975: for(int i = 0; i < N; i++) {
976:     if((ver >> i) & 1) ans.emplace_back(i);
977: }
978: return ans;
979: }
980:
981:
982: #####
983: ##### push-relabel.cpp #####
984: #####
985:
986: template< typename flow_t >
987: struct PushRelabel {
988:     const flow_t INF;
989:
990:     struct edge {
991:         int to;
992:         flow_t cap;
993:         int rev;
994:         bool isrev;
995:         int idx;
996:     };
997:     vector< vector< edge > > graph;
998:     vector< flow_t > ex;
999:     int relabels, high;
1000:     vector< int > cnt, h;
1001:     vector< vector< int > > hs;
1002:
1003:     PushRelabel(int V) : graph(V), INF(numeric_limits< flow_t >::max()), hs(V + 1),
high(0) {}
1004:
1005:
1006:     void add_edge(int from, int to, flow_t cap, int idx = -1) {
1007:         graph[from].emplace_back((edge) {to, cap, (int) graph[to].size(), false, idx})
;
1008:         graph[to].emplace_back((edge) {from, 0, (int) graph[from].size() - 1, true, id
x});
1009:     }
1010:
1011:     void update_height(int idx, int nxt_height) {
1012:         ++relabels;
1013:         if(h[idx] != graph.size() + 1) {
1014:             --cnt[h[idx]];
1015:         }
1016:         h[idx] = nxt_height;
1017:         if(h[idx] != graph.size() + 1) {
1018:             high = nxt_height;
1019:             ++cnt[nxt_height];
1020:             if(ex[idx] > 0) hs[nxt_height].emplace_back(idx);
1021:         }
1022:     }
1023:
1024:     void global_relabel(int idx) {
1025:         for(int i = 0; i <= high; i++) hs[i].clear();
1026:         relabels = 0;
1027:         high = 0;
1028:         h.assign(graph.size(), graph.size() + 1);
1029:         cnt.assign(graph.size(), 0);
1030:         queue< int > que;
1031:         que.emplace(idx);
1032:         h[idx] = 0;
1033:         while(que.size()) {
1034:             int p = que.front();
1035:             que.pop();
1036:             for(auto &e : graph[p]) {
```

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```
1037:         if(h[e.to] == graph.size() + 1 && graph[e.to][e.rev].cap > 0) {
1038:             que.emplace(e.to);
1039:             high = h[p] + 1;
1040:             update_height(e.to, high);
1041:         }
1042:     }
1043: }
1044: }
1045:
1046:
1047: void push(int idx, edge &e) {
1048:     if(h[e.to] == graph.size() + 1) return;
1049:     if(ex[e.to] == 0) {
1050:         hs[h[e.to]].emplace_back(e.to);
1051:     }
1052:     flow_t df = min(ex[idx], e.cap);
1053:     e.cap -= df;
1054:     graph[e.to][e.rev].cap += df;
1055:     ex[idx] -= df;
1056:     ex[e.to] += df;
1057: }
1058:
1059: void discharge(int idx) {
1060:     int next_height = (int) graph.size() + 1;
1061:     for(auto &e : graph[idx]) {
1062:         if(e.cap > 0) {
1063:             if(h[idx] == h[e.to] + 1) {
1064:                 push(idx, e);
1065:                 if(ex[idx] <= 0) return;
1066:             } else {
1067:                 next_height = min(next_height, h[e.to] + 1);
1068:             }
1069:         }
1070:     }
1071:     if(cnt[h[idx]] > 1) {
1072:         update_height(idx, next_height);
1073:     } else {
1074:         for(; high >= h[idx]; hs[high--].clear()) {
1075:             for(int j : hs[high]) update_height(j, graph.size() + 1);
1076:         }
1077:     }
1078: }
1079:
1080: flow_t max_flow(int s, int t) {
1081:     ex.assign(graph.size(), 0);
1082:     ex[s] = INF;
1083:     ex[t] = -INF;
1084:     global_relabel(t);
1085:     for(auto &e : graph[s]) push(s, e);
1086:     for(; high >= 0; high--) {
1087:         while(!hs[high].empty()) {
1088:             int idx = hs[high].back();
1089:             hs[high].pop_back();
1090:             discharge(idx);
1091:             if(relabels >= graph.size() * 4) global_relabel(t);
1092:         }
1093:     }
1094:     return ex[t] + INF;
1095: }
1096:
1097: void output() {
1098:     for(int i = 0; i < graph.size(); i++) {
1099:         for(auto &e : graph[i]) {
1100:             if(e.isrev) continue;
1101:             auto &rev_e = graph[e.to][e.rev];
1102:             cout << i << "->" << e.to << " (flow: " << rev_e.cap << "/" << e.cap + rev_e.cap << ")" << endl;
1103:         }
1104:     }
1105: }
```



```

1106: };
1107:
1108:
1109: #####
1110: ##### kruskal.cpp #####
1111: #####
1112:
1113: template< typename T >
1114: T kruskal(Edges< T > &edges, int V) {
1115:     sort(begin(edges), end(edges), [](const edge< T > &a, const edge< T > &b) {
1116:         return (a.cost < b.cost);
1117:     });
1118:     UnionFind tree(V);
1119:     T ret = 0;
1120:     for(auto &e : edges) {
1121:         if(tree.unite(e.src, e.to)) ret += e.cost;
1122:     }
1123:     return (ret);
1124: }
1125:
1126:
1127: #####
1128: ##### ford-fulkerson.cpp #####
1129: #####
1130:
1131: template< typename flow_t >
1132: struct FordFulkerson {
1133:     struct edge {
1134:         int to;
1135:         flow_t cap;
1136:         int rev;
1137:         bool isrev;
1138:         int idx;
1139:     };
1140:
1141:     vector< vector< edge > > graph;
1142:     vector< int > used;
1143:     const flow_t INF;
1144:     int timestamp;
1145:
1146:     FordFulkerson(int n) : INF(numeric_limits< flow_t >::max()), timestamp(0) {
1147:         graph.resize(n);
1148:         used.assign(n, -1);
1149:     }
1150:
1151:     void add_edge(int from, int to, flow_t cap, int idx = -1) {
1152:         graph[from].emplace_back((edge) {to, cap, (int) graph[to].size(), false, idx});
1153:         graph[to].emplace_back((edge) {from, 0, (int) graph[from].size() - 1, true, id
x});
1154:     }
1155:
1156:     flow_t dfs(int idx, const int t, flow_t flow) {
1157:         if(idx == t) return flow;
1158:         used[idx] = timestamp;
1159:         for(auto &e : graph[idx]) {
1160:             if(e.cap > 0 && used[e.to] != timestamp) {
1161:                 flow_t d = dfs(e.to, t, min(flow, e.cap));
1162:                 if(d > 0) {
1163:                     e.cap -= d;
1164:                     graph[e.to][e.rev].cap += d;
1165:                     return d;
1166:                 }
1167:             }
1168:         }
1169:         return 0;
1170:     }
1171:
1172:     flow_t max_flow(int s, int t) {
1173:         flow_t flow = 0;

```

```

1174:     for(flow_t f; (f = dfs(s, t, INF)) > 0; timestamp++) {
1175:         flow += f;
1176:     }
1177:     return flow;
1178: }
1179:
1180: void output() {
1181:     for(int i = 0; i < graph.size(); i++) {
1182:         for(auto &e : graph[i]) {
1183:             if(e.isrev) continue;
1184:             auto &rev_e = graph[e.to][e.rev];
1185:             cout << i << "->" << e.to << " (flow: " << rev_e.cap << "/" << e.cap + rev
_e.cap << ")" << endl;
1186:         }
1187:     }
1188: }
1189: };
1190:
1191:
1192: #####
1193: ##### offline-dag-reachability.cpp #####
1194: #####
1195:
1196: template< typename G >
1197: vector< int > offline_dag_reachability(const G &g, vector< pair< int, int > > &qs)
{
1198:     const int N = (int) g.size();
1199:     const int Q = (int) qs.size();
1200:     auto ord = topological_sort(g);
1201:     vector< int > ans(Q);
1202:     for(int l = 0; l < Q; l += 64) {
1203:         int r = min(Q, l + 64);
1204:         vector< int64_t > dp(N);
1205:         for(int k = l; k < r; k++) {
1206:             dp[qs[k].first] |= int64_t(1) << (k - l);
1207:         }
1208:         for(auto &idx : ord) {
1209:             for(auto &to : g[idx]) dp[to] |= dp[idx];
1210:         }
1211:         for(int k = l; k < r; k++) {
1212:             ans[k] = (dp[qs[k].second] >> (k - l)) & 1;
1213:         }
1214:     }
1215:     return ans;
1216: }
1217:
1218:
1219: #####
1220: ##### chromatic-number.cpp #####
1221: #####
1222:
1223: int chromatic_number(const Matrix< bool > &g) {
1224:     int N = (int) g.size();
1225:     vector< int > es(N);
1226:     for(int i = 0; i < g.size(); i++) {
1227:         for(int j = 0; j < g.size(); j++) {
1228:             es[i] |= g[i][j] << j;
1229:         }
1230:     }
1231:     int ret = N;
1232:     for(int d : {7, 11, 21}) {
1233:         int mod = 1e9 + d;
1234:         vector< int > ind(1 << N), aux(1 << N, 1);
1235:         ind[0] = 1;
1236:         for(int S = 1; S < 1 << N; S++) {
1237:             int u = __builtin_ctz(S);
1238:             ind[S] = ind[S ^ (1 << u)] + ind[(S ^ (1 << u)) & ~es[u]];
1239:         }
1240:         for(int i = 1; i < ret; i++) {
1241:             int64_t all = 0;

```

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```
1242:         for(int j = 0; j < 1 << N; j++) {
1243:             int S = j ^ (j >> 1);
1244:             aux[S] = (1LL * aux[S] * ind[S]) % mod;
1245:             all += j & 1 ? aux[S] : mod - aux[S];
1246:         }
1247:         if(all % mod) ret = i;
1248:     }
1249: }
1250: return ret;
1251: }
1252:
1253:
1254:
1255: #####
1256: ##### grid-bfs.cpp #####
1257: #####
1258:
1259: vector< vector< int > > grid_bfs(vector< string > &s, char start, const string &wall = "#") {
1260:     const int vx[] = {0, 1, 0, -1}, vy[] = {1, 0, -1, 0};
1261:     vector< vector< int > > min_cost(s.size(), vector< int >(s[0].size(), -1));
1262:     queue< pair< int, int > > que;
1263:     for(int i = 0; i < s.size(); i++) {
1264:         for(int j = 0; j < s[i].size(); j++) {
1265:             if(s[i][j] == start) {
1266:                 que.emplace(i, j);
1267:                 min_cost[i][j] = 0;
1268:             }
1269:         }
1270:     }
1271:     while(!que.empty()) {
1272:         auto p = que.front();
1273:         que.pop();
1274:         for(int i = 0; i < 4; i++) {
1275:             int ny = p.first + vy[i], nx = p.second + vx[i];
1276:             if(nx < 0 || ny < 0 || nx >= s[0].size() || ny >= s.size()) continue;
1277:             if(min_cost[ny][nx] != -1) continue;
1278:             if(wall.find(s[ny][nx]) != string::npos) continue;
1279:             min_cost[ny][nx] = min_cost[p.first][p.second] + 1;
1280:             que.emplace(ny, nx);
1281:         }
1282:     }
1283:     return min_cost;
1284: }
1285:
1286:
1287: #####
1288: ##### two-edge-connected-components.cpp #####
1289: #####
1290:
1291: template< typename G >
1292: struct TwoEdgeConnectedComponents : LowLink< G > {
1293:     using LL = LowLink< G >;
1294:     vector< int > comp;
1295:
1296:     TwoEdgeConnectedComponents(const G &g) : LL(g) {}
1297:
1298:     int operator[](const int &k) {
1299:         return comp[k];
1300:     }
1301:
1302:     void dfs(int idx, int par, int &k) {
1303:         if(~par && this->ord[par] >= this->low[idx]) comp[idx] = comp[par];
1304:         else comp[idx] = k++;
1305:         for(auto &to : this->g[idx]) {
1306:             if(comp[to] == -1) dfs(to, idx, k);
1307:         }
1308:     }
1309:
1310:     void build(UnWeightedGraph &t) {
```

```

1311:     LL::build();
1312:     comp.assign(this->g.size(), -1);
1313:     int k = 0;
1314:     for(int i = 0; i < comp.size(); i++) {
1315:         if(comp[i] == -1) dfs(i, -1, k);
1316:     }
1317:     t.resize(k);
1318:     for(auto &e : this->bridge) {
1319:         int x = comp[e.first], y = comp[e.second];
1320:         t[x].push_back(y);
1321:         t[y].push_back(x);
1322:     }
1323: }
1324: };
1325:
1326:
1327: #####
1328: ##### dinic-capacity-scaling.cpp #####
1329: #####
1330:
1331: template< typename flow_t >
1332: struct DinicCapacityScaling {
1333:
1334:     const flow_t INF;
1335:
1336:     struct edge {
1337:         int to;
1338:         flow_t cap;
1339:         int rev;
1340:         bool isrev;
1341:     };
1342:
1343:     vector< vector< edge > > graph;
1344:     vector< int > min_cost, iter;
1345:     flow_t max_cap;
1346:
1347:     DinicCapacityScaling(int V) : INF(numeric_limits< flow_t >::max()), graph(V), ma
x_cap(0) {}
1348:
1349:     void add_edge(int from, int to, flow_t cap) {
1350:         max_cap = max(max_cap, cap);
1351:         graph[from].emplace_back(edge) {to, cap, (int) graph[to].size(), false};
1352:         graph[to].emplace_back(edge) {from, 0, (int) graph[from].size() - 1, true};
1353:     }
1354:
1355:     bool bfs(int s, int t, const flow_t &base) {
1356:         min_cost.assign(graph.size(), -1);
1357:         queue< int > que;
1358:         min_cost[s] = 0;
1359:         que.push(s);
1360:         while(!que.empty() && min_cost[t] == -1) {
1361:             int p = que.front();
1362:             que.pop();
1363:             for(auto &e : graph[p]) {
1364:                 if(e.cap >= base && min_cost[e.to] == -1) {
1365:                     min_cost[e.to] = min_cost[p] + 1;
1366:                     que.push(e.to);
1367:                 }
1368:             }
1369:         }
1370:         return min_cost[t] != -1;
1371:     }
1372:
1373:     flow_t dfs(int idx, const int t, const flow_t base, flow_t flow) {
1374:         if(idx == t) return flow;
1375:         flow_t sum = 0;
1376:         for(int &i = iter[idx]; i < graph[idx].size(); i++) {
1377:             edge &e = graph[idx][i];
1378:             if(e.cap >= base && min_cost[idx] < min_cost[e.to]) {
1379:                 flow_t d = dfs(e.to, t, base, min(flow - sum, e.cap));

```

```

1380:         if(d > 0) {
1381:             e.cap -= d;
1382:             graph[e.to][e.rev].cap += d;
1383:             sum += d;
1384:             if(flow - sum < base) break;
1385:         }
1386:     }
1387: }
1388: return sum;
1389: }
1390:
1391: flow_t max_flow(int s, int t) {
1392:     if(max_cap == flow_t(0)) return flow_t(0);
1393:     flow_t flow = 0;
1394:     for(int i = 63 - __builtin_clzll(max_cap); i >= 0; i--) {
1395:         flow_t now = flow_t(1) << i;
1396:         while(bfs(s, t, now)) {
1397:             iter.assign(graph.size(), 0);
1398:             flow += dfs(s, t, now, INF);
1399:         }
1400:     }
1401:     return flow;
1402: }
1403:
1404: void output() {
1405:     for(int i = 0; i < graph.size(); i++) {
1406:         for(auto &e : graph[i]) {
1407:             if(e.isrev) continue;
1408:             auto &rev_e = graph[e.to][e.rev];
1409:             cout << i << "->" << e.to << " (flow: " << rev_e.cap << "/" << e.cap + rev
_e.cap << ")" << endl;
1410:         }
1411:     }
1412: }
1413: };
1414:
1415:
1416:
1417: #####
1418: ##### bi-connected-components.cpp #####
1419: #####
1420:
1421: template< typename G >
1422: struct BiConnectedComponents : LowLink< G > {
1423:     using LL = LowLink< G >;
1424:
1425:     vector< int > used;
1426:     vector< vector< pair< int, int > > > bc;
1427:     vector< pair< int, int > > tmp;
1428:
1429:     BiConnectedComponents(const G &g) : LL(g) {}
1430:
1431:     void dfs(int idx, int par) {
1432:         used[idx] = true;
1433:         for(auto &to : this->g[idx]) {
1434:             if(to == par) continue;
1435:             if(!used[to] || this->ord[to] < this->ord[idx]) {
1436:                 tmp.emplace_back(minmax(idx, to));
1437:             }
1438:             if(!used[to]) {
1439:                 dfs(to, idx);
1440:                 if(this->low[to] >= this->ord[idx]) {
1441:                     bc.emplace_back();
1442:                     for(;;) {
1443:                         auto e = tmp.back();
1444:                         bc.back().emplace_back(e);
1445:                         tmp.pop_back();
1446:                         if(e.first == min(idx, to) && e.second == max(idx, to)) {
1447:                             break;
1448:                         }

```

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```
1449:         }
1450:     }
1451: }
1452: }
1453: }
1454:
1455: void build() override {
1456:     LL::build();
1457:     used.assign(this->g.size(), 0);
1458:     for(int i = 0; i < used.size(); i++) {
1459:         if(!used[i]) dfs(i, -1);
1460:     }
1461: }
1462: };
1463:
1464:
1465: #####
1466: ##### strongly-connected-components.cpp #####
1467: #####
1468:
1469: template< typename G >
1470: struct StronglyConnectedComponents {
1471:     const G &g;
1472:     UnWeightedGraph gg, rg;
1473:     vector< int > comp, order, used;
1474:
1475:     StronglyConnectedComponents(G &g) : g(g), gg(g.size()), rg(g.size()), comp(g.siz
e(), -1), used(g.size()) {
1476:         for(int i = 0; i < g.size(); i++) {
1477:             for(auto e : g[i]) {
1478:                 gg[i].emplace_back((int) e);
1479:                 rg[(int) e].emplace_back(i);
1480:             }
1481:         }
1482:     }
1483:
1484:     int operator[] (int k) {
1485:         return comp[k];
1486:     }
1487:
1488:     void dfs(int idx) {
1489:         if(used[idx]) return;
1490:         used[idx] = true;
1491:         for(int to : gg[idx]) dfs(to);
1492:         order.push_back(idx);
1493:     }
1494:
1495:     void rdfs(int idx, int cnt) {
1496:         if(comp[idx] != -1) return;
1497:         comp[idx] = cnt;
1498:         for(int to : rg[idx]) rdfs(to, cnt);
1499:     }
1500:
1501:     void build(UnWeightedGraph &t) {
1502:         for(int i = 0; i < gg.size(); i++) dfs(i);
1503:         reverse(begin(order), end(order));
1504:         int ptr = 0;
1505:         for(int i : order) if(comp[i] == -1) rdfs(i, ptr), ptr++;
1506:
1507:         t.resize(ptr);
1508:         for(int i = 0; i < g.size(); i++) {
1509:             for(auto &to : g[i]) {
1510:                 int x = comp[i], y = comp[to];
1511:                 if(x == y) continue;
1512:                 t[x].push_back(y);
1513:             }
1514:         }
1515:     }
1516: };
1517:
```

```

1518:
1519: #####
1520: ##### dominator-tree.cpp #####
1521: #####
1522:
1523: template< typename G >
1524: struct DominatorTree {
1525:
1526:     struct UnionFind {
1527:         const vector< int > &semi;
1528:         vector< int > par, m;
1529:
1530:         UnionFind(const vector< int > &semi) : semi(semi), par(semi.size()), m(semi.si
ze()) {
1531:             iota(begin(par), end(par), 0);
1532:             iota(begin(m), end(m), 0);
1533:         }
1534:
1535:         int find(int v) {
1536:             if(par[v] == v) return v;
1537:             int r = find(par[v]);
1538:             if(semi[m[v]] > semi[m[par[v]]]) m[v] = m[par[v]];
1539:             return par[v] = r;
1540:         }
1541:
1542:         int eval(int v) {
1543:             find(v);
1544:             return m[v];
1545:         }
1546:
1547:         void link(int p, int c) {
1548:             par[c] = p;
1549:         }
1550:     };
1551:
1552:     const G &g;
1553:     vector< vector< int > > rg;
1554:     vector< int > ord, par;
1555:     vector< int > idom, semi;
1556:     UnionFind uf;
1557:
1558:     DominatorTree(G &g) : g(g), rg(g.size()), par(g.size()), idom(g.size(), -1), sem
i(g.size(), -1), uf(semi) {
1559:         ord.reserve(g.size());
1560:     }
1561:
1562:
1563:     void dfs(int idx) {
1564:         semi[idx] = (int) ord.size();
1565:         ord.emplace_back(idx);
1566:         for(auto &to : g[idx]) {
1567:             if(~semi[to]) continue;
1568:             dfs(to);
1569:             par[to] = idx;
1570:         }
1571:     }
1572:
1573:     void build(int root) {
1574:         const int N = (int) g.size();
1575:         dfs(root);
1576:         for(int i = 0; i < N; i++) {
1577:             for(auto &to : g[i]) {
1578:                 if(~semi[i]) rg[to].emplace_back(i);
1579:             }
1580:         }
1581:
1582:         vector< vector< int > > bucket(N);
1583:         vector< int > U(N);
1584:         for(int i = (int) ord.size() - 1; i >= 0; i--) {
1585:             int x = ord[i];

```

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```

1586:         for(int v : rg[x]) {
1587:             v = uf.eval(v);
1588:             if(semi[x] > semi[v]) semi[x] = semi[v];
1589:         }
1590:         bucket[ord[semi[x]]].emplace_back(x);
1591:         for(int v : bucket[par[x]]) U[v] = uf.eval(v);
1592:         bucket[par[x]].clear();
1593:         uf.link(par[x], x);
1594:     }
1595:     for(int i = 1; i < ord.size(); i++) {
1596:         int x = ord[i], u = U[x];
1597:         idom[x] = semi[x] == semi[u] ? semi[x] : idom[u];
1598:     }
1599:     for(int i = 1; i < ord.size(); i++) {
1600:         int x = ord[i];
1601:         idom[x] = ord[idom[x]];
1602:     }
1603:     idom[root] = root;
1604: }
1605:
1606: int operator[](const int &k) {
1607:     return idom[k];
1608: }
1609: };
1610:
1611:
1612: #####
1613: ##### prim.cpp #####
1614: #####
1615:
1616: template< typename T >
1617: T prim(WeightedGraph< T > &g) {
1618:     using Pi = pair< T, int >;
1619:
1620:     T total = 0;
1621:     vector< bool > used(g.size(), false);
1622:     priority_queue< Pi, vector< Pi >, greater< Pi > > que;
1623:     que.emplace(0, 0);
1624:     while(!que.empty()) {
1625:         auto p = que.top();
1626:         que.pop();
1627:         if(used[p.second]) continue;
1628:         used[p.second] = true;
1629:         total += p.first;
1630:         for(auto &e : g[p.second]) {
1631:             que.emplace(e.cost, e.to);
1632:         }
1633:     }
1634:     return total;
1635: }
1636:
1637:
1638: #####
1639: ##### eulerian-trail.cpp #####
1640: #####
1641:
1642: template< typename T >
1643: vector< edge< T > > eulerian_path(Edges< T > es, int s, bool directed) {
1644:     int V = 0;
1645:     for(auto &e : es) V = max(V, max(e.to, e.src) + 1);
1646:     vector< vector< pair< edge< T >, int > > > g(V);
1647:     for(auto &e : es) {
1648:         int sz_to = (int) g[e.to].size();
1649:         g[e.src].emplace_back(e, sz_to);
1650:         if(!directed) {
1651:             int sz_src = (int) g[e.src].size() - 1;
1652:             swap(e.src, e.to);
1653:             g[e.src].emplace_back(e, sz_src);
1654:         }
1655:     }

```



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```
1656: vector< edge< T > > ord;
1657: stack< pair< int, edge< T > > > st;
1658: st.emplace(s, edge< T >(-1, -1));
1659: while(st.size()) {
1660:     int idx = st.top().first;
1661:     if(g[idx].empty()) {
1662:         ord.emplace_back(st.top().second);
1663:         st.pop();
1664:     } else {
1665:         auto e = g[idx].back();
1666:         g[idx].pop_back();
1667:         if(e.second == -1) continue;
1668:         if(!directed) g[e.first.to][e.second].second = -1;
1669:         st.emplace(e.first.to, e.first);
1670:     }
1671: }
1672: ord.pop_back();
1673: reverse(begin(ord), end(ord));
1674: if(ord.size() != es.size()) return {};
1675: return ord;
1676: }
1677:
1678:
1679: #####
1680: ##### dinic.cpp #####
1681: #####
1682:
1683: template< typename flow_t >
1684: struct Dinic {
1685:     const flow_t INF;
1686:
1687:     struct edge {
1688:         int to;
1689:         flow_t cap;
1690:         int rev;
1691:         bool isrev;
1692:         int idx;
1693:     };
1694:
1695:     vector< vector< edge > > graph;
1696:     vector< int > min_cost, iter;
1697:
1698:     Dinic(int V) : INF(numeric_limits< flow_t >::max()), graph(V) {}
1699:
1700:     void add_edge(int from, int to, flow_t cap, int idx = -1) {
1701:         graph[from].emplace_back((edge) {to, cap, (int) graph[to].size(), false, idx})
;
1702:         graph[to].emplace_back((edge) {from, 0, (int) graph[from].size() - 1, true, id
x});
1703:     }
1704:
1705:     bool bfs(int s, int t) {
1706:         min_cost.assign(graph.size(), -1);
1707:         queue< int > que;
1708:         min_cost[s] = 0;
1709:         que.push(s);
1710:         while(!que.empty() && min_cost[t] == -1) {
1711:             int p = que.front();
1712:             que.pop();
1713:             for(auto &e : graph[p]) {
1714:                 if(e.cap > 0 && min_cost[e.to] == -1) {
1715:                     min_cost[e.to] = min_cost[p] + 1;
1716:                     que.push(e.to);
1717:                 }
1718:             }
1719:         }
1720:         return min_cost[t] != -1;
1721:     }
1722:
1723:     flow_t dfs(int idx, const int t, flow_t flow) {
```

```

1724:         if(idx == t) return flow;
1725:         for(int &i = iter[idx]; i < graph[idx].size(); i++) {
1726:             edge &e = graph[idx][i];
1727:             if(e.cap > 0 && min_cost[idx] < min_cost[e.to]) {
1728:                 flow_t d = dfs(e.to, t, min(flow, e.cap));
1729:                 if(d > 0) {
1730:                     e.cap -= d;
1731:                     graph[e.to][e.rev].cap += d;
1732:                     return d;
1733:                 }
1734:             }
1735:         }
1736:         return 0;
1737:     }
1738:
1739:     flow_t max_flow(int s, int t) {
1740:         flow_t flow = 0;
1741:         while(bfs(s, t)) {
1742:             iter.assign(graph.size(), 0);
1743:             flow_t f = 0;
1744:             while((f = dfs(s, t, INF)) > 0) flow += f;
1745:         }
1746:         return flow;
1747:     }
1748:
1749:     void output() {
1750:         for(int i = 0; i < graph.size(); i++) {
1751:             for(auto &e : graph[i]) {
1752:                 if(e.isrev) continue;
1753:                 auto &rev_e = graph[e.to][e.rev];
1754:                 cout << i << "->" << e.to << " (flow: " << rev_e.cap << "/" << e.cap + rev
_e.cap << ")" << endl;
1755:             }
1756:         }
1757:     }
1758: };
1759:
1760:
1761: #####
1762: ##### topological-sort.cpp #####
1763: #####
1764:
1765: template< typename G >
1766: vector< int > topological_sort(const G &g) {
1767:     const int N = (int) g.size();
1768:     vector< int > deg(N);
1769:     for(int i = 0; i < N; i++) {
1770:         for(auto &to : g[i]) ++deg[to];
1771:     }
1772:     stack< int > st;
1773:     for(int i = 0; i < N; i++) {
1774:         if(deg[i] == 0) st.emplace(i);
1775:     }
1776:     vector< int > ord;
1777:     while(!st.empty()) {
1778:         auto p = st.top();
1779:         st.pop();
1780:         ord.emplace_back(p);
1781:         for(auto &to : g[p]) {
1782:             if(--deg[to] == 0) st.emplace(to);
1783:         }
1784:     }
1785:     return ord;
1786: }
1787:
1788:
1789: #####
1790: ##### chu-liu-edmond.cpp #####
1791: #####
1792:

```

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```
1793: template< typename T >
1794: struct MinimumSpanningTreeArborescence
1795: {
1796:     using Pi = pair< T, int >;
1797:     using Heap = SkewHeap< Pi, int >;
1798:     using Node = typename Heap::Node;
1799:     const Edges< T > &es;
1800:     const int V;
1801:     T INF;
1802:
1803:     MinimumSpanningTreeArborescence(const Edges< T > &es, int V) :
1804:         INF(numeric_limits< T >::max()), es(es), V(V) {}
1805:
1806:     T build(int start)
1807:     {
1808:         auto g = [] (const Pi &a, const T &b) { return Pi(a.first + b, a.second); };
1809:         auto h = [] (const T &a, const T &b) { return a + b; };
1810:         Heap heap(g, h);
1811:         vector< Node * > heaps(V, heap.makeheap());
1812:         for(auto &e : es) heap.push(heaps[e.to], {e.cost, e.src});
1813:         UnionFind uf(V);
1814:         vector< int > used(V, -1);
1815:         used[start] = start;
1816:
1817:         T ret = 0;
1818:         for(int s = 0; s < V; s++) {
1819:             stack< int > path;
1820:             for(int u = s; used[u] < 0;) {
1821:                 path.push(u);
1822:                 used[u] = s;
1823:                 if(heap.empty(heaps[u])) return -1;
1824:                 auto p = heap.top(heaps[u]);
1825:                 ret += p.first;
1826:                 heap.add(heaps[u], -p.first);
1827:                 heap.pop(heaps[u]);
1828:                 int v = uf.find(p.second);
1829:                 if(used[v] == s) {
1830:                     int w;
1831:                     Node *nextheap = heap.makeheap();
1832:                     do {
1833:                         w = path.top();
1834:                         path.pop();
1835:                         nextheap = heap.merge(nextheap, heaps[w]);
1836:                     } while(uf.unite(v, w));
1837:                     heaps[uf.find(v)] = nextheap;
1838:                     used[uf.find(v)] = -1;
1839:                 }
1840:                 u = uf.find(v);
1841:             }
1842:         }
1843:         return ret;
1844:     }
1845: };
1846:
1847:
1848: #####
1849: ##### shortest-path-faster-algorithm.cpp #####
1850: #####
1851:
1852: template< typename T >
1853: vector< T > shortest_path_faster_algorithm(WeightedGraph< T > &g, int s) {
1854:     const auto INF = numeric_limits< T >::max();
1855:     vector< T > dist(g.size(), INF);
1856:     vector< int > pending(g.size(), 0), times(g.size(), 0);
1857:     queue< int > que;
1858:
1859:     que.emplace(s);
1860:     pending[s] = true;
1861:     ++times[s];
1862:     dist[s] = 0;
```

```

1863:
1864:     while(!que.empty()) {
1865:         int p = que.front();
1866:         que.pop();
1867:         pending[p] = false;
1868:         for(auto &e : g[p]) {
1869:             T next_cost = dist[p] + e.cost;
1870:             if(next_cost >= dist[e.to]) continue;
1871:             dist[e.to] = next_cost;
1872:             if(!pending[e.to]) {
1873:                 if(++times[e.to] >= g.size()) return vector< T >();
1874:                 pending[e.to] = true;
1875:                 que.emplace(e.to);
1876:             }
1877:         }
1878:     }
1879:     return dist;
1880: }
1881:
1882:
1883: #####
1884: ##### hopcroft-karp.cpp #####
1885: #####
1886:
1887: struct HopcroftKarp {
1888:     vector< vector< int > > graph;
1889:     vector< int > dist, match;
1890:     vector< bool > used, vv;
1891:
1892:     HopcroftKarp(int n, int m) : graph(n), match(m, -1), used(n) {}
1893:
1894:     void add_edge(int u, int v) {
1895:         graph[u].push_back(v);
1896:     }
1897:
1898:     void bfs() {
1899:         dist.assign(graph.size(), -1);
1900:         queue< int > que;
1901:         for(int i = 0; i < graph.size(); i++) {
1902:             if(!used[i]) {
1903:                 que.emplace(i);
1904:                 dist[i] = 0;
1905:             }
1906:         }
1907:
1908:         while(!que.empty()) {
1909:             int a = que.front();
1910:             que.pop();
1911:             for(auto &b : graph[a]) {
1912:                 int c = match[b];
1913:                 if(c >= 0 && dist[c] == -1) {
1914:                     dist[c] = dist[a] + 1;
1915:                     que.emplace(c);
1916:                 }
1917:             }
1918:         }
1919:     }
1920:
1921:     bool dfs(int a) {
1922:         vv[a] = true;
1923:         for(auto &b : graph[a]) {
1924:             int c = match[b];
1925:             if(c < 0 || (!vv[c] && dist[c] == dist[a] + 1 && dfs(c))) {
1926:                 match[b] = a;
1927:                 used[a] = true;
1928:                 return (true);
1929:             }
1930:         }
1931:         return (false);
1932:     }

```

```

1933:
1934:     int bipartite_matching() {
1935:         int ret = 0;
1936:         while(true) {
1937:             bfs();
1938:             vv.assign(graph.size(), false);
1939:             int flow = 0;
1940:             for(int i = 0; i < graph.size(); i++) {
1941:                 if(!used[i] && dfs(i)) ++flow;
1942:             }
1943:             if(flow == 0) return (ret);
1944:             ret += flow;
1945:         }
1946:     }
1947:
1948:     void output() {
1949:         for(int i = 0; i < match.size(); i++) {
1950:             if(~match[i]) {
1951:                 cout << match[i] << "-" << i << endl;
1952:             }
1953:         }
1954:     }
1955: };
1956:
1957:
1958: #####
1959: ##### lowlink.cpp #####
1960: #####
1961:
1962: template< typename G >
1963: struct LowLink {
1964:     const G &g;
1965:     vector< int > used, ord, low;
1966:     vector< int > articulation;
1967:     vector< pair< int, int > > bridge;
1968:
1969:     LowLink(const G &g) : g(g) {}
1970:
1971:     int dfs(int idx, int k, int par) {
1972:         used[idx] = true;
1973:         ord[idx] = k++;
1974:         low[idx] = ord[idx];
1975:         bool is_articulation = false;
1976:         int cnt = 0;
1977:         for(auto &to : g[idx]) {
1978:             if(!used[to]) {
1979:                 ++cnt;
1980:                 k = dfs(to, k, idx);
1981:                 low[idx] = min(low[idx], low[to]);
1982:                 is_articulation |= ~par && low[to] >= ord[idx];
1983:                 if(ord[idx] < low[to]) bridge.emplace_back(minmax(idx, (int) to));
1984:             } else if(to != par) {
1985:                 low[idx] = min(low[idx], ord[to]);
1986:             }
1987:         }
1988:         is_articulation |= par == -1 && cnt > 1;
1989:         if(is_articulation) articulation.push_back(idx);
1990:         return k;
1991:     }
1992:
1993:     virtual void build() {
1994:         used.assign(g.size(), 0);
1995:         ord.assign(g.size(), 0);
1996:         low.assign(g.size(), 0);
1997:         int k = 0;
1998:         for(int i = 0; i < g.size(); i++) {
1999:             if(!used[i]) k = dfs(i, k, -1);
2000:         }
2001:     }
2002: };

```

```

2003:
2004:
2005: #####
2006: ##### maximum-clique.cpp #####
2007: #####
2008:
2009: template< typename T >
2010: T maximum_clique(Matrix< bool > g, function< T(vector< int >) > f) {
2011:
2012:     int N = (int) g.size(), M = 0;
2013:     vector< int > deg(N), v(N);
2014:     for(int i = 0; i < N; i++) {
2015:         for(int j = 0; j < i; j++) {
2016:             assert(g[i][j] == g[j][i]);
2017:             if(g[i][j]) {
2018:                 ++deg[i];
2019:                 ++M;
2020:             }
2021:         }
2022:     }
2023:     T t = 0;
2024:     int lim = (int) sqrt(2 * M);
2025:
2026:     for(int i = 0; i < N; i++) {
2027:         vector< int > notice;
2028:         for(int j = 0; j < N; j++) {
2029:             if(!v[j] && deg[j] < lim) {
2030:                 for(int k = 0; k < N; k++) {
2031:                     if(j == k) continue;
2032:                     if(g[j][k]) notice.emplace_back(k);
2033:                 }
2034:                 notice.emplace_back(j);
2035:                 break;
2036:             }
2037:         }
2038:         if(notice.empty()) break;
2039:         int neighbor = (int) notice.size() - 1;
2040:         vector< int > bit(neighbor);
2041:         for(int j = 0; j < neighbor; j++) {
2042:             for(int k = 0; k < j; k++) {
2043:                 if(!g[notice[j]][notice[k]]) {
2044:                     bit[j] |= 1 << k;
2045:                     bit[k] |= 1 << j;
2046:                 }
2047:             }
2048:         }
2049:         for(int j = 0; j < (1 << neighbor); j++) {
2050:             bool ok = true;
2051:             for(int k = 0; k < neighbor; k++) {
2052:                 if((j >> k) & 1) ok &= (j & bit[k]) == 0;
2053:             }
2054:             if(ok) {
2055:                 vector< int > stock{notice.back()};
2056:                 for(int k = 0; k < neighbor; k++) {
2057:                     if((j >> k) & 1) stock.emplace_back(notice[k]);
2058:                 }
2059:                 t = max(t, f(stock));
2060:             }
2061:         }
2062:         v[notice.back()] = true;
2063:         for(int j = 0; j < N; j++) {
2064:             if(g[j][notice.back()]) {
2065:                 --deg[j];
2066:                 g[notice.back()][j] = g[j][notice.back()] = false;
2067:             }
2068:         }
2069:     }
2070:
2071:     vector< int > notice;
2072:     for(int j = 0; j < N; j++) {

```

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```

2073:     if(!v[j]) notice.emplace_back(j);
2074: }
2075: int neighbor = (int) notice.size();
2076: vector< int > bit(neighbor);
2077: for(int j = 0; j < neighbor; j++) {
2078:     for(int k = 0; k < j; k++) {
2079:         if(!g[notice[j]][notice[k]]) {
2080:             bit[j] |= 1 << k;
2081:             bit[k] |= 1 << j;
2082:         }
2083:     }
2084: }
2085: for(int j = 0; j < (1 << neighbor); j++) {
2086:     bool ok = true;
2087:     for(int k = 0; k < neighbor; k++) {
2088:         if((j >> k) & 1) ok &= (j & bit[k]) == 0;
2089:     }
2090:     if(ok) {
2091:         vector< int > stock;
2092:         for(int k = 0; k < neighbor; k++) {
2093:             if((j >> k) & 1) stock.emplace_back(notice[k]);
2094:         }
2095:         t = max(t, f(stock));
2096:     }
2097: }
2098: return t;
2099: }
2100:
2101:
2102:
2103: -----
2104: |                                other                                |
2105: -----
2106:
2107: #####
2108: ##### mo.cpp #####
2109: #####
2110:
2111: struct Mo {
2112:     using ADD = function< void(int) >;
2113:     using DEL = function< void(int) >;
2114:     using REM = function< void(int) >;
2115:
2116:     int width;
2117:     vector< int > left, right, order;
2118:     vector< bool > v;
2119:
2120:     Mo(int N, int Q) : width((int) sqrt(N)), order(Q), v(N) {
2121:         iota(begin(order), end(order), 0);
2122:     }
2123:
2124:     void add(int l, int r) { /* [l, r) */
2125:         left.emplace_back(l);
2126:         right.emplace_back(r);
2127:     }
2128:
2129:     int run(const ADD &add, const DEL &del, const REM &rem) {
2130:         assert(left.size() == order.size());
2131:         sort(begin(order), end(order), [&](int a, int b) {
2132:             int ablock = left[a] / width, bblock = left[b] / width;
2133:             if(ablock != bblock) return ablock < bblock;
2134:             if(ablock & 1) return right[a] < right[b];
2135:             return right[a] > right[b];
2136:         });
2137:         int nl = 0, nr = 0;
2138:         auto push = [&](int idx) {
2139:             v[idx].flip();
2140:             if(v[idx]) add(idx);
2141:             else del(idx);
2142:         };

```

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```
2143:     for(auto idx : order) {
2144:         while(nl > left[idx]) push(--nl);
2145:         while(nr < right[idx]) push(nr++);
2146:         while(nl < left[idx]) push(nl++);
2147:         while(nr > right[idx]) push(--nr);
2148:         rem(idx);
2149:     }
2150: }
2151: };
2152:
2153:
2154: #####
2155: ##### dice.cpp #####
2156: #####
2157:
2158: struct Dice
2159: {
2160:     // int x, y;
2161:     int l, r, f, b, d, u;
2162:
2163:     void RollN()
2164:     {
2165:         // --y;
2166:         int buff = d;
2167:         d = f;
2168:         f = u;
2169:         u = b;
2170:         b = buff;
2171:     }
2172:
2173:     void RollS()
2174:     {
2175:         // ++y;
2176:         int buff = d;
2177:         d = b;
2178:         b = u;
2179:         u = f;
2180:         f = buff;
2181:     }
2182:
2183:     void RollL() // ---->
2184:     {
2185:         int buff = f;
2186:         f = l;
2187:         l = b;
2188:         b = r;
2189:         r = buff;
2190:     }
2191:
2192:     void RollR() // <-----
2193:     {
2194:         int buff = f;
2195:         f = r;
2196:         r = b;
2197:         b = l;
2198:         l = buff;
2199:     }
2200:
2201:     void RollE() // .o -> o.
2202:     {
2203:         // --x;
2204:         int buff = d;
2205:         d = l;
2206:         l = u;
2207:         u = r;
2208:         r = buff;
2209:     }
2210:
2211:
2212:     void RollW() // o. -> .o
```



```

2213: {
2214:     // ++x;
2215:     int buff = d;
2216:     d = r;
2217:     r = u;
2218:     u = l;
2219:     l = buff;
2220: }
2221:
2222:
2223: vector< Dice > makeDice()
2224: {
2225:     vector< Dice > ret;
2226:     for(int i = 0; i < 6; i++) {
2227:         Dice d(*this);
2228:         if(i == 1) d.RollN();
2229:         if(i == 2) d.RollS();
2230:         if(i == 3) d.RollS(), d.RollS();
2231:         if(i == 4) d.RollL();
2232:         if(i == 5) d.RollR();
2233:         for(int j = 0; j < 4; j++) {
2234:             ret.emplace_back(d);
2235:             d.RollE();
2236:         }
2237:     }
2238:     return (ret);
2239: }
2240: };
2241:
2242:
2243: #####
2244: ##### timer.cpp #####
2245: #####
2246:
2247: struct Timer {
2248:     chrono::high_resolution_clock::time_point st;
2249:
2250:     Timer() { reset(); }
2251:
2252:     void reset() {
2253:         st = chrono::high_resolution_clock::now();
2254:     }
2255:
2256:     chrono::milliseconds::rep elapsed() {
2257:         auto ed = chrono::high_resolution_clock::now();
2258:         return chrono::duration_cast< chrono::milliseconds >(ed - st).count();
2259:     }
2260: };
2261:
2262:
2263: #####
2264: ##### fast-input.cpp #####
2265: #####
2266:
2267: template< int sz >
2268: struct FastInput {
2269:     char buf[sz + 1];
2270:     char *o;
2271:
2272:     FastInput() { init(); }
2273:
2274:     void init() {
2275:         o = buf;
2276:         buf[fread(buf, sizeof(char), sizeof(char) * sz, stdin)] = '\0';
2277:     }
2278:
2279:     int64_t read() {
2280:         int64_t ret = 0, sign = 1;
2281:         while(*o && *o <= 32) ++o;
2282:         if(*o == '-') sign *= -1, ++o;

```

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```
2283:     while(*o >= '0' && *o <= '9') {
2284:         ret *= 10;
2285:         ret += *o++ - '0';
2286:     }
2287:     return ret * sign;
2288: }
2289: };
2290:
2291:
2292: #####
2293: ##### offline-dynamic-connectivity.cpp #####
2294: #####
2295:
2296: struct OfflineDynamicConnectivity {
2297:     using edge = pair< int, int >;
2298:
2299:     UnionFindUndo uf;
2300:     int V, Q, segsz;
2301:     vector< vector< edge > > seg;
2302:     int comp;
2303:
2304:     vector< pair< pair< int, int >, edge > > pend;
2305:     map< edge, int > cnt, appear;
2306:
2307:     OfflineDynamicConnectivity(int V, int Q) : uf(V), V(V), Q(Q), comp(V) {
2308:         segsz = 1;
2309:         while(segsz < Q) segsz <= 1;
2310:         seg.resize(2 * segsz - 1);
2311:     }
2312:
2313:     void insert(int idx, int s, int t) {
2314:         auto e = minmax(s, t);
2315:         if(cnt[e]++ == 0) appear[e] = idx;
2316:     }
2317:
2318:     void erase(int idx, int s, int t) {
2319:         auto e = minmax(s, t);
2320:         if(--cnt[e] == 0) pend.emplace_back(make_pair(appear[e], idx), e);
2321:     }
2322:
2323:     void add(int a, int b, const edge &e, int k, int l, int r) {
2324:         if(r <= a || b <= l) return;
2325:         if(a <= l && r <= b) {
2326:             seg[k].emplace_back(e);
2327:             return;
2328:         }
2329:         add(a, b, e, 2 * k + 1, l, (l + r) >> 1);
2330:         add(a, b, e, 2 * k + 2, (l + r) >> 1, r);
2331:     }
2332:
2333:     void add(int a, int b, const edge &e) {
2334:         add(a, b, e, 0, 0, segsz);
2335:     }
2336:
2337:     void build() {
2338:         for(auto &p : cnt) {
2339:             if(p.second > 0) pend.emplace_back(make_pair(appear[p.first], Q), p.first);
2340:         }
2341:         for(auto &s : pend) {
2342:             add(s.first.first, s.first.second, s.second);
2343:         }
2344:     }
2345:
2346:     int run(const function< void(int) > &f, int k = 0) {
2347:         int add = 0;
2348:         for(auto &e : seg[k]) {
2349:             add += uf.unite(e.first, e.second);
2350:         }
2351:         comp -= add;
2352:         if(k < segsz - 1) {
```

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```
2353:         run(f, 2 * k + 1);
2354:         run(f, 2 * k + 2);
2355:     } else if(k - (segsz - 1) < Q) {
2356:         int query_index = k - (segsz - 1);
2357:         f(query_index);
2358:     }
2359:     for(auto &e : seg[k]) {
2360:         uf.undo();
2361:     }
2362:     comp += add;
2363: }
2364: };
2365:
2366:
2367: #####
2368: ##### random-number-generator.cpp #####
2369: #####
2370:
2371: struct RandomNumberGenerator {
2372:     mt19937 mt;
2373:
2374:     RandomNumberGenerator() : mt(chrono::steady_clock::now().time_since_epoch().count()) {}
2375:
2376:     int operator()(int a, int b) { // [a, b)
2377:         uniform_int_distribution< int > dist(a, b - 1);
2378:         return dist(mt);
2379:     }
2380:
2381:     int operator()(int b) { // [0, b)
2382:         return (*this)(0, b);
2383:     }
2384: };
2385:
2386:
2387: #####
2388: ##### mo-rollback.cpp #####
2389: #####
2390:
2391: struct MoRollBack {
2392:     using ADD = function< void(int) >;
2393:     using REM = function< void(int) >;
2394:     using RESET = function< void() >;
2395:     using SNAPSHOT = function< void() >;
2396:     using ROLLBACK = function< void() >;
2397:
2398:     int width;
2399:     vector< int > left, right, order;
2400:
2401:     MoRollBack(int N, int Q) : width((int) sqrt(N)), order(Q) {
2402:         iota(begin(order), end(order), 0);
2403:     }
2404:
2405:     void add(int l, int r) { /* [l, r) */
2406:         left.emplace_back(l);
2407:         right.emplace_back(r);
2408:     }
2409:
2410:     int run(const ADD &add, const REM &rem, const RESET &reset, const SNAPSHOT &snapshot, const ROLLBACK &rollback) {
2411:         assert(left.size() == order.size());
2412:         sort(begin(order), end(order), [&](int a, int b) {
2413:             int ablock = left[a] / width, bblock = left[b] / width;
2414:             if(ablock != bblock) return ablock < bblock;
2415:             return right[a] < right[b];
2416:         });
2417:         reset();
2418:         for(auto idx : order) {
2419:             if(right[idx] - left[idx] < width) {
2420:                 for(int i = left[idx]; i < right[idx]; i++) add(i);
```

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```
2421:         rem(idx);
2422:         rollback();
2423:     }
2424: }
2425: int nr = 0, last_block = -1;
2426: for(auto idx : order) {
2427:     if(right[idx] - left[idx] < width) continue;
2428:     int block = left[idx] / width;
2429:     if(last_block != block) {
2430:         reset();
2431:         last_block = block;
2432:         nr = (block + 1) * width;
2433:     }
2434:     while(nr < right[idx]) add(nr++);
2435:     snapshot();
2436:     for(int j = (block + 1) * width - 1; j >= left[idx]; j--) add(j);
2437:     rem(idx);
2438:     rollback();
2439: }
2440: }
2441: };
2442:
2443:
2444:
2445: #####
2446: ##### compress.cpp #####
2447: #####
2448:
2449: template< typename T >
2450: struct Compress {
2451:     vector< T > xs;
2452:
2453:     Compress() = default;
2454:
2455:     Compress(const vector< T > &vs) {
2456:         add(vs);
2457:     }
2458:
2459:     Compress(const initializer_list< vector< T > > &vs) {
2460:         for(auto &p : vs) add(p);
2461:     }
2462:
2463:     void add(const vector< T > &vs) {
2464:         copy(begin(vs), end(vs), back_inserter(xs));
2465:     }
2466:
2467:     void add(const T &x) {
2468:         xs.emplace_back(x);
2469:     }
2470:
2471:     void build() {
2472:         sort(begin(xs), end(xs));
2473:         xs.erase(unique(begin(xs), end(xs)), end(xs));
2474:     }
2475:
2476:     vector< int > get(const vector< T > &vs) const {
2477:         vector< int > ret;
2478:         transform(begin(vs), end(vs), back_inserter(ret), [&](const T &x) {
2479:             return lower_bound(begin(xs), end(xs), x) - begin(xs);
2480:         });
2481:         return ret;
2482:     }
2483:
2484:     int get(const T &x) const {
2485:         return lower_bound(begin(xs), end(xs), x) - begin(xs);
2486:     }
2487:
2488:     const T &operator[](int k) const {
2489:         return xs[k];
2490:     }
}
```

```

2491: };
2492:
2493:
2494: -----
2495: |                                template                                |
2496: -----
2497:
2498: #####
2499: ##### template.cpp #####
2500: #####
2501:
2502: #include<bits/stdc++.h>
2503:
2504: using namespace std;
2505:
2506: using int64 = long long;
2507: const int mod = 1e9 + 7;
2508:
2509: const int64 infll = (1LL << 62) - 1;
2510: const int inf = (1 << 30) - 1;
2511:
2512: struct IoSetup {
2513:     IoSetup() {
2514:         cin.tie(nullptr);
2515:         ios::sync_with_stdio(false);
2516:         cout << fixed << setprecision(10);
2517:         cerr << fixed << setprecision(10);
2518:     }
2519: } iosetup;
2520:
2521:
2522: template< typename T1, typename T2 >
2523: ostream &operator<<(ostream &os, const pair< T1, T2 >& p) {
2524:     os << p.first << " " << p.second;
2525:     return os;
2526: }
2527:
2528: template< typename T1, typename T2 >
2529: istream &operator>>(istream &is, pair< T1, T2 > &p) {
2530:     is >> p.first >> p.second;
2531:     return is;
2532: }
2533:
2534: template< typename T >
2535: ostream &operator<<(ostream &os, const vector< T > &v) {
2536:     for(int i = 0; i < (int) v.size(); i++) {
2537:         os << v[i] << (i + 1 != v.size() ? " " : "");
2538:     }
2539:     return os;
2540: }
2541:
2542: template< typename T >
2543: istream &operator>>(istream &is, vector< T > &v) {
2544:     for(T &in : v) is >> in;
2545:     return is;
2546: }
2547:
2548: template< typename T1, typename T2 >
2549: inline bool chmax(T1 &a, T2 b) { return a < b && (a = b, true); }
2550:
2551: template< typename T1, typename T2 >
2552: inline bool chmin(T1 &a, T2 b) { return a > b && (a = b, true); }
2553:
2554: template< typename T = int64 >
2555: vector< T > make_v(size_t a) {
2556:     return vector< T >(a);
2557: }
2558:
2559: template< typename T, typename... Ts >
2560: auto make_v(size_t a, Ts... ts) {

```

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```
2561:     return vector< decltype(make_v< T >(ts...)) >(a, make_v< T >(ts...));
2562: }
2563:
2564: template< typename T, typename V >
2565: typename enable_if< is_class< T >::value == 0 >::type fill_v(T &t, const V &v) {
2566:     t = v;
2567: }
2568:
2569: template< typename T, typename V >
2570: typename enable_if< is_class< T >::value != 0 >::type fill_v(T &t, const V &v) {
2571:     for(auto &e : t) fill_v(e, v);
2572: }
2573:
2574: template< typename F >
2575: struct FixPoint : F {
2576:     FixPoint(F &&f) : F(forward< F >(f)) {}
2577:
2578:     template< typename... Args >
2579:     decltype(auto) operator()(Args &&... args) const {
2580:         return F::operator()(*this, forward< Args >(args)...);
2581:     }
2582: };
2583:
2584: template< typename F >
2585: inline decltype(auto) MFP(F &&f) {
2586:     return FixPoint< F >{forward< F >(f)};
2587: }
2588:
2589:
2590: -----
2591: |                                     math                                     |
2592: -----
2593:
2594: #####
2595: ##### prime-factor.cpp #####
2596: #####
2597:
2598: map< int64_t, int > prime_factor(int64_t n) {
2599:     map< int64_t, int > ret;
2600:     for(int64_t i = 2; i * i <= n; i++) {
2601:         while(n % i == 0) {
2602:             ret[i]++;
2603:             n /= i;
2604:         }
2605:     }
2606:     if(n != 1) ret[n] = 1;
2607:     return ret;
2608: }
2609:
2610:
2611: #####
2612: ##### stirling-number-second.cpp #####
2613: #####
2614:
2615: template< typename T >
2616: T stirling_number_second(int n, int k) {
2617:     Combination< T > table(k);
2618:     T ret = 0;
2619:     for(int i = 0; i <= k; i++) {
2620:         auto add = T(i).pow(n) * table.C(k, i);
2621:         if((k - i) & 1) ret -= add;
2622:         else ret += add;
2623:     }
2624:     return ret * table.rfact(k);
2625: }
2626:
2627:
2628:
2629: #####
2630: ##### mod-int.cpp #####
```

```

2631: #####
2632:
2633: template< int mod >
2634: struct ModInt {
2635:     int x;
2636:
2637:     ModInt() : x(0) {}
2638:
2639:     ModInt(int64_t y) : x(y >= 0 ? y % mod : (mod - (-y) % mod) % mod) {}
2640:
2641:     ModInt &operator+=(const ModInt &p) {
2642:         if((x += p.x) >= mod) x -= mod;
2643:         return *this;
2644:     }
2645:
2646:     ModInt &operator-=(const ModInt &p) {
2647:         if((x += mod - p.x) >= mod) x -= mod;
2648:         return *this;
2649:     }
2650:
2651:     ModInt &operator*=(const ModInt &p) {
2652:         x = (int) (1LL * x * p.x % mod);
2653:         return *this;
2654:     }
2655:
2656:     ModInt &operator/=(const ModInt &p) {
2657:         *this *= p.inverse();
2658:         return *this;
2659:     }
2660:
2661:     ModInt operator-() const { return ModInt(-x); }
2662:
2663:     ModInt operator+(const ModInt &p) const { return ModInt(*this) += p; }
2664:
2665:     ModInt operator-(const ModInt &p) const { return ModInt(*this) -= p; }
2666:
2667:     ModInt operator*(const ModInt &p) const { return ModInt(*this) *= p; }
2668:
2669:     ModInt operator/(const ModInt &p) const { return ModInt(*this) /= p; }
2670:
2671:     bool operator==(const ModInt &p) const { return x == p.x; }
2672:
2673:     bool operator!=(const ModInt &p) const { return x != p.x; }
2674:
2675:     ModInt inverse() const {
2676:         int a = x, b = mod, u = 1, v = 0, t;
2677:         while(b > 0) {
2678:             t = a / b;
2679:             swap(a -= t * b, b);
2680:             swap(u -= t * v, v);
2681:         }
2682:         return ModInt(u);
2683:     }
2684:
2685:     ModInt pow(int64_t n) const {
2686:         ModInt ret(1), mul(x);
2687:         while(n > 0) {
2688:             if(n & 1) ret *= mul;
2689:             mul *= mul;
2690:             n >>= 1;
2691:         }
2692:         return ret;
2693:     }
2694:
2695:     friend ostream &operator<<(ostream &os, const ModInt &p) {
2696:         return os << p.x;
2697:     }
2698:
2699:     friend istream &operator>>(istream &is, ModInt &a) {
2700:         int64_t t;

```

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```
2701:     is >> t;
2702:     a = ModInt< mod >(t);
2703:     return (is);
2704: }
2705:
2706: static int get_mod() { return mod; }
2707: };
2708:
2709: using modint = ModInt< mod >;
2710:
2711:
2712: #####
2713: ##### binomial.cpp #####
2714: #####
2715:
2716: template< typename T >
2717: T binomial(int64_t N, int64_t K) {
2718:     if(K < 0 || N < K) return 0;
2719:     T ret = 1;
2720:     for(T i = 1; i <= K; ++i) {
2721:         ret *= N--;
2722:         ret /= i;
2723:     }
2724:     return ret;
2725: }
2726:
2727:
2728: #####
2729: ##### factorial.cpp #####
2730: #####
2731:
2732: template< typename T >
2733: T factorial(int64_t n) {
2734:     if(n >= T::get_mod()) return 0;
2735:     if(n == 0) return 1;
2736:
2737:     const int64_t sn = sqrt(n);
2738:     const T sn_inv = T(1) / sn;
2739:
2740:     Combination< modint > comb(sn);
2741:     using P = vector< T >;
2742:
2743:     ArbitraryModConvolution< T > fft;
2744:     using FPS = FormalPowerSeries< T >;
2745:     auto mult = [&](const typename FPS::P &a, const typename FPS::P &b) {
2746:         auto ret = fft.multiply(a, b);
2747:         return typename FPS::P(ret.begin(), ret.end());
2748:     };
2749:     FPS::set_fft(mult);
2750:
2751:
2752:     auto shift = [&](const P &f, T dx) {
2753:         int n = (int) f.size();
2754:         T a = dx * sn_inv;
2755:         auto p1 = P(f);
2756:         for(int i = 0; i < n; i++) {
2757:             T d = comb.rfact(i) * comb.rfact((n - 1) - i);
2758:             if(((n - 1 - i) & 1)) d = -d;
2759:             p1[i] *= d;
2760:         }
2761:         auto p2 = P(2 * n);
2762:         for(int i = 0; i < p2.size(); i++) {
2763:             p2[i] = (a.x + i - n) <= 0 ? 1 : a + i - n;
2764:         }
2765:         for(int i = 1; i < p2.size(); i++) {
2766:             p2[i] *= p2[i - 1];
2767:         }
2768:         T prod = p2[2 * n - 1];
2769:         T prod_inv = T(1) / prod;
2770:         for(int i = 2 * n - 1; i > 0; --i) {
```



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```

2771:     p2[i] = prod_inv * p2[i - 1];
2772:     prod_inv *= a + i - n;
2773: }
2774: p2[0] = prod_inv;
2775: auto p3 = fft.multiply(p1, p2, (int) p2.size());
2776: p1 = P(p3.begin() + p1.size(), p3.begin() + p2.size());
2777: prod = 1;
2778: for(int i = 0; i < n; i++) {
2779:     prod *= a + n - 1 - i;
2780: }
2781: for(int i = n - 1; i >= 0; --i) {
2782:     p1[i] *= prod;
2783:     prod *= p2[n + i] * (a + i - n);
2784: }
2785: return p1;
2786: };
2787: function< P(int) > rec = [&](int64_t n) {
2788:     if(n == 1) return P({1, 1 + sn});
2789:     int64_t nh = n >> 1;
2790:     auto a1 = rec(nh);
2791:     auto a2 = shift(a1, nh);
2792:     auto b1 = shift(a1, sn * nh);
2793:     auto b2 = shift(a1, sn * nh + nh);
2794:     for(int i = 0; i <= nh; i++) a1[i] *= a2[i];
2795:     for(int i = 1; i <= nh; i++) a1.emplace_back(b1[i] * b2[i]);
2796:     if(n & 1) {
2797:         for(int64_t i = 0; i < n; i++) {
2798:             a1[i] *= n + 1LL * sn * i;
2799:         }
2800:         T prod = 1;
2801:         for(int64_t i = 1LL * n * sn; i < 1LL * n * sn + n; i++) {
2802:             prod *= (i + 1);
2803:         }
2804:         a1.push_back(prod);
2805:     }
2806:     return a1;
2807: };
2808: auto vs = rec(sn);
2809: T ret = 1;
2810: for(int64_t i = 0; i < sn; i++) ret *= vs[i];
2811: for(int64_t i = 1LL * sn * sn + 1; i <= n; i++) ret *= i;
2812: return ret;
2813: }
2814:
2815:
2816: #####
2817: ##### binomial-table.cpp #####
2818: #####
2819:
2820: template< typename T >
2821: vector< vector< T > > binomial_table(int N) {
2822:     vector< vector< T > > mat(N + 1, vector< T >(N + 1));
2823:     for(int i = 0; i <= N; i++) {
2824:         for(int j = 0; j <= i; j++) {
2825:             if(j == 0 || j == i) mat[i][j] = 1;
2826:             else mat[i][j] = mat[i - 1][j - 1] + mat[i - 1][j];
2827:         }
2828:     }
2829:     return mat;
2830: }
2831:
2832:
2833: #####
2834: ##### polynomial-interpolation.cpp #####
2835: #####
2836:
2837: template< class T >
2838: FormalPowerSeries< T > polynomial_interpolation(const FormalPowerSeries< T > &xs,
const vector< T > &ys) {
2839:     assert(xs.size() == ys.size());

```

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```
2840: using FPS = FormalPowerSeries< T >;
2841: PolyBuf< T > buf(xs);
2842: FPS w = buf.query(0, xs.size()).diff();
2843: auto vs = multipoint_evaluation(w, xs, buf);
2844: function< FPS(int, int) > rec = [&](int l, int r) -> FPS {
2845:     if(r - 1 == 1) return {ys[l] / vs[l]};
2846:     int m = (l + r) >> 1;
2847:     return rec(l, m) * buf.query(m, r) + rec(m, r) * buf.query(l, m);
2848: };
2849: return rec(0, xs.size());
2850: }
2851:
2852:
2853: #####
2854: ##### bell-number.cpp #####
2855: #####
2856:
2857: template< typename T >
2858: T bell_number(int n, int k) {
2859:     if(n == 0) return 1;
2860:     k = min(k, n);
2861:     Combination< T > uku(k);
2862:     T ret = 0;
2863:     vector< T > pref(k + 1);
2864:     pref[0] = 1;
2865:     for(int i = 1; i <= k; i++) {
2866:         if(i & 1) pref[i] = pref[i - 1] - uku.rfact(i);
2867:         else pref[i] = pref[i - 1] + uku.rfact(i);
2868:     }
2869:     for(int i = 1; i <= k; i++) {
2870:         ret += T(i).pow(n) * uku.rfact(i) * pref[k - i];
2871:     }
2872:     return ret;
2873: }
2874:
2875:
2876: #####
2877: ##### divisor.cpp #####
2878: #####
2879:
2880: vector< int64_t > divisor(int64_t n) {
2881:     vector< int64_t > ret;
2882:     for(int64_t i = 1; i * i <= n; i++) {
2883:         if(n % i == 0) {
2884:             ret.push_back(i);
2885:             if(i * i != n) ret.push_back(n / i);
2886:         }
2887:     }
2888:     sort(begin(ret), end(ret));
2889:     return (ret);
2890: }
2891:
2892:
2893: #####
2894: ##### arbitrary-mod-convolution-long.cpp #####
2895: #####
2896:
2897: template< typename T >
2898: struct ArbitraryModConvolutionLong {
2899:     using real = FastFourierTransform::real;
2900:     using C = FastFourierTransform::C;
2901:
2902:     ArbitraryModConvolutionLong() = default;
2903:
2904:     vector< T > multiply(const vector< T > &a, const vector< T > &b, int need = -1)
2905:     {
2906:         if(need == -1) need = a.size() + b.size() - 1;
2907:         int nbase = 0;
2908:         while((1 << nbase) < need) nbase++;
2909:         FastFourierTransform::ensure_base(nbase);
```

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```
2909:     int sz = 1 << nbase;
2910:     vector< C > fa(sz);
2911:     for(int i = 0; i < a.size(); i++) {
2912:         fa[i] = C(a[i].x & ((1 << 19) - 1), a[i].x >> 19);
2913:     }
2914:     fft(fa, sz);
2915:     vector< C > fb(sz);
2916:     if(a == b) {
2917:         fb = fa;
2918:     } else {
2919:         for(int i = 0; i < b.size(); i++) {
2920:             fb[i] = C(b[i].x & ((1 << 19) - 1), b[i].x >> 19);
2921:         }
2922:         fft(fb, sz);
2923:     }
2924:     real ratio = 0.25 / sz;
2925:     C r2(0, -1), r3(ratio, 0), r4(0, -ratio), r5(0, 1);
2926:     for(int i = 0; i <= (sz >> 1); i++) {
2927:         int j = (sz - i) & (sz - 1);
2928:         C a1 = (fa[i] + fa[j].conj());
2929:         C a2 = (fa[i] - fa[j].conj()) * r2;
2930:         C b1 = (fb[i] + fb[j].conj()) * r3;
2931:         C b2 = (fb[i] - fb[j].conj()) * r4;
2932:         if(i != j) {
2933:             C c1 = (fa[j] + fa[i].conj());
2934:             C c2 = (fa[j] - fa[i].conj()) * r2;
2935:             C d1 = (fb[j] + fb[i].conj()) * r3;
2936:             C d2 = (fb[j] - fb[i].conj()) * r4;
2937:             fa[i] = c1 * d1 + c2 * d2 * r5;
2938:             fb[i] = c1 * d2 + c2 * d1;
2939:         }
2940:         fa[j] = a1 * b1 + a2 * b2 * r5;
2941:         fb[j] = a1 * b2 + a2 * b1;
2942:     }
2943:     fft(fa, sz);
2944:     fft(fb, sz);
2945:     vector< T > ret(need);
2946:     auto mul1 = T(2).pow(19);
2947:     auto mul2 = T(2).pow(38);
2948:     for(int i = 0; i < need; i++) {
2949:         int64_t aa = llround(fa[i].x);
2950:         int64_t bb = llround(fb[i].x);
2951:         int64_t cc = llround(fa[i].y);
2952:         aa = T(aa).x, bb = T(bb).x, cc = T(cc).x;
2953:         ret[i] = (mul1 * bb) + (mul2 * cc) + aa;
2954:     }
2955:     return ret;
2956: }
2957: };
2958:
2959:
2960: #####
2961: ##### mod-pow.cpp #####
2962: #####
2963:
2964: template< typename T >
2965: T mod_pow(T x, T n, const T &p) {
2966:     T ret = 1;
2967:     while(n > 0) {
2968:         if(n & 1) (ret *= x) %= p;
2969:         (x *= x) %= p;
2970:         n >>= 1;
2971:     }
2972:     return ret;
2973: }
2974:
2975:
2976:
2977: #####
2978: ##### prime-table.cpp #####
```

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```
2979: #####
2980:
2981: vector< bool > prime_table(int n) {
2982:     vector< bool > prime(n + 1, true);
2983:     if(n >= 0) prime[0] = false;
2984:     if(n >= 1) prime[1] = false;
2985:     for(int i = 2; i * i <= n; i++) {
2986:         if(!prime[i]) continue;
2987:         for(int j = i + i; j <= n; j += i) {
2988:             prime[j] = false;
2989:         }
2990:     }
2991:     return prime;
2992: }
2993:
2994:
2995: #####
2996: ##### multipoint-evaluation.cpp #####
2997: #####
2998:
2999: template< typename T >
3000: struct PolyBuf {
3001:     using FPS = FormalPowerSeries< T >;
3002:     const FPS xs;
3003:     using pi = pair< int, int >;
3004:     map< pi, FPS > buf;
3005:
3006:     PolyBuf(const FPS &xs) : xs(xs) {}
3007:
3008:     const FPS &query(int l, int r) {
3009:         if(buf.count({l, r})) return buf[{l, r}];
3010:         if(l + 1 == r) return buf[{l, r}] = {-xs[l], 1};
3011:         return buf[{l, r}] = query(l, (l + r) >> 1) * query((l + r) >> 1, r);
3012:     }
3013: };
3014:
3015:
3016: template< typename T >
3017: FormalPowerSeries< T > multipoint_evaluation(const FormalPowerSeries< T > &as, const
st FormalPowerSeries< T > &xs, PolyBuf< T > &buf) {
3018:     using FPS = FormalPowerSeries< T >;
3019:     FPS ret;
3020:     const int B = 64;
3021:     function< void(FPS, int, int) > rec = [&](FPS a, int l, int r) -> void {
3022:         a %= buf.query(l, r);
3023:         if(a.size() <= B) {
3024:             for(int i = l; i < r; i++) ret.emplace_back(a.eval(xs[i]));
3025:             return;
3026:         }
3027:         rec(a, l, (l + r) >> 1);
3028:         rec(a, (l + r) >> 1, r);
3029:     };
3030:     rec(as, 0, xs.size());
3031:     return ret;
3032: };
3033:
3034: template< typename T >
3035: FormalPowerSeries< T > multipoint_evaluation(const FormalPowerSeries< T > &as, const
st FormalPowerSeries< T > &xs) {
3036:     PolyBuf< T > buff(xs);
3037:     return multipoint_evaluation(as, xs, buff);
3038: }
3039:
3040:
3041:
3042: #####
3043: ##### mod-sqrt.cpp #####
3044: #####
3045:
3046: template< typename T >
```

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```
3047: T mod_sqrt(const T &a, const T &p) {
3048:     if(a == 0) return 0;
3049:     if(p == 2) return a;
3050:     if(mod_pow(a, (p - 1) >> 1, p) != 1) return -1;
3051:     T b = 1;
3052:     while(mod_pow(b, (p - 1) >> 1, p) == 1) ++b;
3053:     T e = 0, m = p - 1;
3054:     while(m % 2 == 0) m >>= 1, ++e;
3055:     T x = mod_pow(a, (m - 1) >> 1, p);
3056:     T y = a * (x * x % p) % p;
3057:     (x *= a) %= p;
3058:     T z = mod_pow(b, m, p);
3059:     while(y != 1) {
3060:         T j = 0, t = y;
3061:         while(t != 1) {
3062:             j += 1;
3063:             (t *= z) %= p;
3064:         }
3065:         z = mod_pow(z, T(1) << (e - j - 1), p);
3066:         (x *= z) %= p;
3067:         (z *= z) %= p;
3068:         (y *= z) %= p;
3069:         e = j;
3070:     }
3071:     return x;
3072: }
3073:
3074:
3075: #####
3076: ##### arbitrary-mod-convolution.cpp #####
3077: #####
3078:
3079: template< typename T >
3080: struct ArbitraryModConvolution {
3081:     using real = FastFourierTransform::real;
3082:     using C = FastFourierTransform::C;
3083:
3084:     ArbitraryModConvolution() = default;
3085:
3086:     vector< T > multiply(const vector< T > &a, const vector< T > &b, int need = -1)
3087:     {
3088:         if(need == -1) need = a.size() + b.size() - 1;
3089:         int nbase = 0;
3090:         while((1 << nbase) < need) nbase++;
3091:         FastFourierTransform::ensure_base(nbase);
3092:         int sz = 1 << nbase;
3093:         vector< C > fa(sz);
3094:         for(int i = 0; i < a.size(); i++) {
3095:             fa[i] = C(a[i].x & ((1 << 15) - 1), a[i].x >> 15);
3096:         }
3097:         fft(fa, sz);
3098:         vector< C > fb(sz);
3099:         if(a == b) {
3100:             fb = fa;
3101:         } else {
3102:             for(int i = 0; i < b.size(); i++) {
3103:                 fb[i] = C(b[i].x & ((1 << 15) - 1), b[i].x >> 15);
3104:             }
3105:             fft(fb, sz);
3106:         }
3107:         real ratio = 0.25 / sz;
3108:         C r2(0, -1), r3(ratio, 0), r4(0, -ratio), r5(0, 1);
3109:         for(int i = 0; i <= (sz >> 1); i++) {
3110:             int j = (sz - i) & (sz - 1);
3111:             C a1 = (fa[i] + fa[j].conj());
3112:             C a2 = (fa[i] - fa[j].conj()) * r2;
3113:             C b1 = (fb[i] + fb[j].conj()) * r3;
3114:             C b2 = (fb[i] - fb[j].conj()) * r4;
3115:             if(i != j) {
```

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```
3116:         C c2 = (fa[j] - fa[i].conj()) * r2;
3117:         C d1 = (fb[j] + fb[i].conj()) * r3;
3118:         C d2 = (fb[j] - fb[i].conj()) * r4;
3119:         fa[i] = c1 * d1 + c2 * d2 * r5;
3120:         fb[i] = c1 * d2 + c2 * d1;
3121:     }
3122:     fa[j] = a1 * b1 + a2 * b2 * r5;
3123:     fb[j] = a1 * b2 + a2 * b1;
3124: }
3125: fft(fa, sz);
3126: fft(fb, sz);
3127: vector< T > ret(need);
3128: for(int i = 0; i < need; i++) {
3129:     int64_t aa = llround(fa[i].x);
3130:     int64_t bb = llround(fb[i].x);
3131:     int64_t cc = llround(fa[i].y);
3132:     aa = T(aa).x, bb = T(bb).x, cc = T(cc).x;
3133:     ret[i] = aa + (bb << 15) + (cc << 30);
3134: }
3135: return ret;
3136: }
3137: };
3138:
3139:
3140: #####
3141: number-theoretic-transform-friendly-mod-int.cpp #
3142: #####
3143:
3144: template< typename Mint >
3145: struct NumberTheoreticTransformFriendlyModInt {
3146:
3147:     vector< int > rev;
3148:     vector< Mint > rts;
3149:     int base, max_base;
3150:     Mint root;
3151:
3152:     NumberTheoreticTransformFriendlyModInt() : base(1), rev{0, 1}, rts{0, 1} {
3153:         const int mod = Mint::get_mod();
3154:         assert(mod >= 3 && mod % 2 == 1);
3155:         auto tmp = mod - 1;
3156:         max_base = 0;
3157:         while(tmp % 2 == 0) tmp >>= 1, max_base++;
3158:         root = 2;
3159:         while(root.pow((mod - 1) >> 1) == 1) root += 1;
3160:         assert(root.pow(mod - 1) == 1);
3161:         root = root.pow((mod - 1) >> max_base);
3162:     }
3163:
3164:     void ensure_base(int nbase) {
3165:         if(nbase <= base) return;
3166:         rev.resize(1 << nbase);
3167:         rts.resize(1 << nbase);
3168:         for(int i = 0; i < (1 << nbase); i++) {
3169:             rev[i] = (rev[i >> 1] >> 1) + ((i & 1) << (nbase - 1));
3170:         }
3171:         assert(nbase <= max_base);
3172:         while(base < nbase) {
3173:             Mint z = root.pow(1 << (max_base - 1 - base));
3174:             for(int i = 1 << (base - 1); i < (1 << base); i++) {
3175:                 rts[i << 1] = rts[i];
3176:                 rts[(i << 1) + 1] = rts[i] * z;
3177:             }
3178:             ++base;
3179:         }
3180:     }
3181:
3182:
3183:     void ntt(vector< Mint > &a) {
3184:         const int n = (int) a.size();
3185:         assert((n & (n - 1)) == 0);
```

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```

3186:     int zeros = __builtin_ctz(n);
3187:     ensure_base(zeros);
3188:     int shift = base - zeros;
3189:     for(int i = 0; i < n; i++) {
3190:         if(i < (rev[i] >> shift)) {
3191:             swap(a[i], a[rev[i] >> shift]);
3192:         }
3193:     }
3194:     for(int k = 1; k < n; k <= 1) {
3195:         for(int i = 0; i < n; i += 2 * k) {
3196:             for(int j = 0; j < k; j++) {
3197:                 Mint z = a[i + j + k] * rts[j + k];
3198:                 a[i + j + k] = a[i + j] - z;
3199:                 a[i + j] = a[i + j] + z;
3200:             }
3201:         }
3202:     }
3203: }
3204:
3205:
3206: void intt(vector< Mint > &a) {
3207:     const int n = (int) a.size();
3208:     ntt(a);
3209:     reverse(a.begin() + 1, a.end());
3210:     Mint inv_sz = Mint(1) / n;
3211:     for(int i = 0; i < n; i++) a[i] *= inv_sz;
3212: }
3213:
3214: vector< Mint > multiply(vector< Mint > a, vector< Mint > b) {
3215:     int need = a.size() + b.size() - 1;
3216:     int nbase = 1;
3217:     while((1 << nbase) < need) nbase++;
3218:     ensure_base(nbase);
3219:     int sz = 1 << nbase;
3220:     a.resize(sz, 0);
3221:     b.resize(sz, 0);
3222:     ntt(a);
3223:     ntt(b);
3224:     Mint inv_sz = Mint(1) / sz;
3225:     for(int i = 0; i < sz; i++) {
3226:         a[i] *= b[i] * inv_sz;
3227:     }
3228:     reverse(a.begin() + 1, a.end());
3229:     ntt(a);
3230:     a.resize(need);
3231:     return a;
3232: }
3233: };
3234:
3235:
3236: #####
3237: ##### euler-phi.cpp #####
3238: #####
3239:
3240: int64_t euler_phi(int64_t n) {
3241:     int64_t ret = n;
3242:     for(int64_t i = 2; i * i <= n; i++) {
3243:         if(n % i == 0) {
3244:             ret -= ret / i;
3245:             while(n % i == 0) n /= i;
3246:         }
3247:     }
3248:     if(n > 1) ret -= ret / n;
3249:     return ret;
3250: }
3251:
3252:
3253: #####
3254: ##### lagrange-polynomial.cpp #####
3255: #####

```

```

3256:
3257: template< typename T >
3258: T lagrange_polynomial(const vector< T > &y, int64_t t) {
3259:     int N = y.size() - 1;
3260:     Combination< T > comb(N);
3261:     if(t <= N) return y[t];
3262:     T ret(0);
3263:     vector< T > dp(N + 1, 1), pd(N + 1, 1);
3264:     for(int i = 0; i < N; i++) dp[i + 1] = dp[i] * (t - i);
3265:     for(int i = N; i > 0; i--) pd[i - 1] = pd[i] * (t - i);
3266:     for(int i = 0; i <= N; i++) {
3267:         T tmp = y[i] * dp[i] * pd[i] * comb.rfact(i) * comb.rfact(N - i);
3268:         if((N - i) & 1) ret -= tmp;
3269:         else ret += tmp;
3270:     }
3271:     return ret;
3272: }
3273:
3274:
3275: #####
3276: ##### combination.cpp #####
3277: #####
3278:
3279: template< typename T >
3280: struct Combination {
3281:     vector< T > _fact, _rfact, _inv;
3282:
3283:     Combination(int sz) : _fact(sz + 1), _rfact(sz + 1), _inv(sz + 1) {
3284:         _fact[0] = _rfact[sz] = _inv[0] = 1;
3285:         for(int i = 1; i <= sz; i++) _fact[i] = _fact[i - 1] * i;
3286:         _rfact[sz] /= _fact[sz];
3287:         for(int i = sz - 1; i >= 0; i--) _rfact[i] = _rfact[i + 1] * (i + 1);
3288:         for(int i = 1; i <= sz; i++) _inv[i] = _rfact[i] * _fact[i - 1];
3289:     }
3290:
3291:     inline T fact(int k) const { return _fact[k]; }
3292:
3293:     inline T rfact(int k) const { return _rfact[k]; }
3294:
3295:     inline T inv(int k) const { return _inv[k]; }
3296:
3297:     T P(int n, int r) const {
3298:         if(r < 0 || n < r) return 0;
3299:         return fact(n) * rfact(n - r);
3300:     }
3301:
3302:     T C(int p, int q) const {
3303:         if(q < 0 || p < q) return 0;
3304:         return fact(p) * rfact(q) * rfact(p - q);
3305:     }
3306:
3307:     T H(int n, int r) const {
3308:         if(n < 0 || r < 0) return (0);
3309:         return r == 0 ? 1 : C(n + r - 1, r);
3310:     }
3311: };
3312:
3313:
3314: #####
3315: ##### mod-log.cpp #####
3316: #####
3317:
3318: int64_t mod_log(int64_t a, int64_t b, int64_t p) {
3319:     int64_t g = 1;
3320:
3321:     for(int64_t i = p; i; i /= 2) (g *= a) %= p;
3322:     g = __gcd(g, p);
3323:
3324:     int64_t t = 1, c = 0;
3325:     for(; t % g; c++) {

```



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```
3326:     if(t == b) return c;
3327:     (t *= a) %= p;
3328: }
3329: if(b % g) return -1;
3330:
3331: t /= g;
3332: b /= g;
3333:
3334: int64_t n = p / g, h = 0, gs = 1;
3335:
3336: for(; h * h < n; h++) (gs *= a) %= n;
3337:
3338: unordered_map< int64_t, int64_t > bs;
3339: for(int64_t s = 0, e = b; s < h; bs[e] = ++s) {
3340:     (e *= a) %= n;
3341: }
3342:
3343: for(int64_t s = 0, e = t; s < n;) {
3344:     (e *= gs) %= n;
3345:     s += h;
3346:     if(bs.count(e)) return c + s - bs[e];
3347: }
3348: return -1;
3349: }
3350:
3351:
3352: #####
3353: ##### quotient-range.cpp #####
3354: #####
3355:
3356: template< typename T >
3357: vector< pair< pair< T, T >, T > > quotient_range(T N) {
3358:     T M;
3359:     vector< pair< pair< T, T >, T > > ret;
3360:     for(M = 1; M * M <= N; M++) {
3361:         ret.emplace_back(make_pair(M, M), N / M);
3362:     }
3363:     for(T i = M; i >= 1; i--) {
3364:         T L = N / (i + 1) + 1;
3365:         T R = N / i;
3366:         if(L <= R && ret.back().first.second < L) ret.emplace_back(make_pair(L, R), N
/ L);
3367:     }
3368:     return ret;
3369: }
3370:
3371:
3372: #####
3373: ##### formal-power-series-seq.cpp #####
3374: #####
3375:
3376: template< typename T >
3377: FormalPowerSeries< T > bernoulli(int N) {
3378:     FormalPowerSeries< T > poly(N + 1);
3379:     poly[0] = T(1);
3380:     for(int i = 1; i <= N; i++) {
3381:         poly[i] = poly[i - 1] / T(i + 1);
3382:     }
3383:     poly = poly.inv();
3384:     T tmp(1);
3385:     for(int i = 1; i <= N; i++) {
3386:         tmp *= T(i);
3387:         poly[i] *= tmp;
3388:     }
3389:     return poly;
3390: }
3391:
3392: template< typename T >
3393: FormalPowerSeries< T > partition(int N) {
3394:     FormalPowerSeries< T > poly(N + 1);
```

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```
3395: poly[0] = 1;
3396: for(int k = 1; k <= N; k++) {
3397:     if(1LL * k * (3 * k + 1) / 2 <= N) poly[k * (3 * k + 1) / 2] += (k % 2 ? -1 :
1);
3398:     if(1LL * k * (3 * k - 1) / 2 <= N) poly[k * (3 * k - 1) / 2] += (k % 2 ? -1 :
1);
3399: }
3400: return poly.inv();
3401: }
3402:
3403: template< typename T >
3404: FormalPowerSeries< T > bell(int N) {
3405:     FormalPowerSeries< T > poly(N + 1), ret(N + 1);
3406:     poly[1] = 1;
3407:     poly = poly.exp();
3408:     poly[0] -= 1;
3409:     poly = poly.exp();
3410:     T mul = 1;
3411:     for(int i = 0; i <= N; i++) {
3412:         ret[i] = poly[i] * mul;
3413:         mul *= i + 1;
3414:     }
3415:     return ret;
3416: }
3417:
3418: template< typename T >
3419: FormalPowerSeries< T > stirling_first(int N) {
3420:     if(N == 0) return {1};
3421:     int M = N / 2;
3422:     FormalPowerSeries< T > A = stirling_first< T >(M), B, C(N - M + 1);
3423:
3424:     if(N % 2 == 0) {
3425:         B = A;
3426:     } else {
3427:         B.resize(M + 2);
3428:         B[M + 1] = 1;
3429:         for(int i = 1; i < M + 1; i++) B[i] = A[i - 1] + A[i] * M;
3430:     }
3431:
3432:     T tmp = 1;
3433:     for(int i = 0; i <= N - M; i++) {
3434:         C[N - M - i] = T(M).pow(i) / tmp;
3435:         B[i] *= tmp;
3436:         tmp *= T(i + 1);
3437:     }
3438:     C *= B;
3439:     tmp = 1;
3440:     for(int i = 0; i <= N - M; i++) {
3441:         B[i] = C[N - M + i] / tmp;
3442:         tmp *= T(i + 1);
3443:     }
3444:     return A * B;
3445: }
3446:
3447: template< typename T >
3448: FormalPowerSeries< T > stirling_second(int N) {
3449:     FormalPowerSeries< T > A(N + 1), B(N + 1);
3450:     modint tmp = 1;
3451:     for(int i = 0; i <= N; i++) {
3452:         T rev = T(1) / tmp;
3453:         A[i] = T(i).pow(N) * rev;
3454:         B[i] = T(1) * rev;
3455:         if(i & 1) B[i] *= -1;
3456:         tmp *= i + 1;
3457:     }
3458:     return (A * B).pre(N + 1);
3459: }
3460:
3461: template< typename T >
3462: FormalPowerSeries< T > stirling_second_kth_column(int N, int K) {
```

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```
3463: FormalPowerSeries< T > poly(N + 1), ret(N + 1);
3464: poly[1] = 1;
3465: poly = poly.exp();
3466: poly[0] -= 1;
3467: poly = poly.pow(K);
3468: T rev = 1, mul = 1;
3469: for(int i = 2; i <= K; i++) rev *= i;
3470: rev = T(1) / rev;
3471: poly *= rev;
3472: for(int i = 0; i <= N; i++) {
3473:     ret[i] = poly[i] * mul;
3474:     mul *= i + 1;
3475: }
3476: return ret;
3477: }
3478:
3479: template< typename T >
3480: FormalPowerSeries< T > eulerian(int N) {
3481:     vector< T > fact(N + 2), rfact(N + 2);
3482:     fact[0] = rfact[N + 1] = 1;
3483:     for(int i = 1; i <= N + 1; i++) fact[i] = fact[i - 1] * i;
3484:     rfact[N + 1] /= fact[N + 1];
3485:     for(int i = N; i >= 0; i--) rfact[i] = rfact[i + 1] * (i + 1);
3486:
3487:     FormalPowerSeries< T > A(N + 1), B(N + 1);
3488:     for(int i = 0; i <= N; i++) {
3489:         A[i] = fact[N + 1] * rfact[i] * rfact[N + 1 - i];
3490:         if(i & 1) A[i] *= -1;
3491:         B[i] = T(i + 1).pow(N);
3492:     }
3493:     return (A * B).pre(N + 1);
3494: }
3495:
3496:
3497: #####
3498: ##### fast-prime-factorization.cpp #####
3499: #####
3500:
3501: namespace FastPrimeFactorization {
3502:
3503:     template< typename word, typename dword, typename sword >
3504:     struct UnsafeMod {
3505:         UnsafeMod() : x(0) {}
3506:
3507:         UnsafeMod(word _x) : x(init(_x)) {}
3508:
3509:         bool operator==(const UnsafeMod &rhs) const {
3510:             return x == rhs.x;
3511:         }
3512:
3513:         bool operator!=(const UnsafeMod &rhs) const {
3514:             return x != rhs.x;
3515:         }
3516:
3517:         UnsafeMod &operator+=(const UnsafeMod &rhs) {
3518:             if((x += rhs.x) >= mod) x -= mod;
3519:             return *this;
3520:         }
3521:
3522:         UnsafeMod &operator-=(const UnsafeMod &rhs) {
3523:             if(sword(x -= rhs.x) < 0) x += mod;
3524:             return *this;
3525:         }
3526:
3527:         UnsafeMod &operator*=(const UnsafeMod &rhs) {
3528:             x = reduce(dword(x) * rhs.x);
3529:             return *this;
3530:         }
3531:
3532:         UnsafeMod operator+(const UnsafeMod &rhs) const {
```

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```
3533:         return UnsafeMod(*this) += rhs;
3534:     }
3535:
3536:     UnsafeMod operator-(const UnsafeMod &rhs) const {
3537:         return UnsafeMod(*this) -= rhs;
3538:     }
3539:
3540:     UnsafeMod operator*(const UnsafeMod &rhs) const {
3541:         return UnsafeMod(*this) *= rhs;
3542:     }
3543:
3544:     UnsafeMod pow(uint64_t e) const {
3545:         UnsafeMod ret(1);
3546:         for(UnsafeMod base = *this; e; e >>= 1, base *= base) {
3547:             if(e & 1) ret *= base;
3548:         }
3549:         return ret;
3550:     }
3551:
3552:     word get() const {
3553:         return reduce(x);
3554:     }
3555:
3556:     static constexpr int word_bits = sizeof(word) * 8;
3557:
3558:     static word modulus() {
3559:         return mod;
3560:     }
3561:
3562:     static word init(word w) {
3563:         return reduce(dword(w) * r2);
3564:     }
3565:
3566:     static void set_mod(word m) {
3567:         mod = m;
3568:         inv = mul_inv(mod);
3569:         r2 = -dword(mod) % mod;
3570:     }
3571:
3572:     static word reduce(dword x) {
3573:         word y = word(x >> word_bits) - word((dword(word(x) * inv) * mod) >> word_bits);
3574:         return sword(y) < 0 ? y + mod : y;
3575:     }
3576:
3577:     static word mul_inv(word n, int e = 6, word x = 1) {
3578:         return !e ? x : mul_inv(n, e - 1, x * (2 - x * n));
3579:     }
3580:
3581:     static word mod, inv, r2;
3582:
3583:     word x;
3584: };
3585:
3586: using uint128_t = __uint128_t;
3587:
3588: using Mod64 = UnsafeMod< uint64_t, uint128_t, int64_t >;
3589: template<> uint64_t Mod64::mod = 0;
3590: template<> uint64_t Mod64::inv = 0;
3591: template<> uint64_t Mod64::r2 = 0;
3592:
3593: using Mod32 = UnsafeMod< uint32_t, uint64_t, int32_t >;
3594: template<> uint32_t Mod32::mod = 0;
3595: template<> uint32_t Mod32::inv = 0;
3596: template<> uint32_t Mod32::r2 = 0;
3597:
3598: bool miller_rabin_primality_test_uint64(uint64_t n) {
3599:     Mod64::set_mod(n);
3600:     uint64_t d = n - 1;
3601:     while(d % 2 == 0) d /= 2;
```

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```
3602:     Mod64 e{1}, rev{n - 1};
3603:     // http://miller-rabin.appspot.com/ < 2^64
3604:     for(uint64_t a : {2, 325, 9375, 28178, 450775, 9780504, 1795265022}) {
3605:         if(n <= a) break;
3606:         uint64_t t = d;
3607:         Mod64 y = Mod64(a).pow(t);
3608:         while(t != n - 1 && y != e && y != rev) {
3609:             y *= y;
3610:             t *= 2;
3611:         }
3612:         if(y != rev && t % 2 == 0) return false;
3613:     }
3614:     return true;
3615: }
3616:
3617: bool miller_rabin_primality_test_uint32(uint32_t n) {
3618:     Mod32::set_mod(n);
3619:     uint32_t d = n - 1;
3620:     while(d % 2 == 0) d /= 2;
3621:     Mod32 e{1}, rev{n - 1};
3622:     for(uint32_t a : {2, 7, 61}) {
3623:         if(n <= a) break;
3624:         uint32_t t = d;
3625:         Mod32 y = Mod32(a).pow(t);
3626:         while(t != n - 1 && y != e && y != rev) {
3627:             y *= y;
3628:             t *= 2;
3629:         }
3630:         if(y != rev && t % 2 == 0) return false;
3631:     }
3632:     return true;
3633: }
3634:
3635: bool is_prime(uint64_t n) {
3636:     if(n == 2) return true;
3637:     if(n == 1 || n % 2 == 0) return false;
3638:     if(n < uint64_t(1) << 31) return miller_rabin_primality_test_uint32(n);
3639:     return miller_rabin_primality_test_uint64(n);
3640: }
3641:
3642: uint64_t pollard_rho(uint64_t n) {
3643:     if(is_prime(n)) return n;
3644:     if(n % 2 == 0) return 2;
3645:     Mod64::set_mod(n);
3646:     uint64_t d;
3647:     Mod64 one{1};
3648:     for(Mod64 c{one};; c += one) {
3649:         Mod64 x{2}, y{2};
3650:         do {
3651:             x = x * x + c;
3652:             y = y * y + c;
3653:             y = y * y + c;
3654:             d = __gcd((x - y).get(), n);
3655:         } while(d == 1);
3656:         if(d < n) return d;
3657:     }
3658:     assert(0);
3659: }
3660:
3661: vector< uint64_t > prime_factor(uint64_t n) {
3662:     if(n <= 1) return {};
3663:     uint64_t p = pollard_rho(n);
3664:     if(p == n) return {p};
3665:     auto l = prime_factor(p);
3666:     auto r = prime_factor(n / p);
3667:     copy(begin(r), end(r), back_inserter(l));
3668:     return l;
3669: }
3670: };
3671:
```

```

3672:
3673: #####
3674: ##### is-prime.cpp #####
3675: #####
3676:
3677: bool is_prime(int64_t x) {
3678:     for(int64_t i = 2; i * i <= x; i++) {
3679:         if(x % i == 0) return false;
3680:     }
3681:     return true;
3682: }
3683:
3684:
3685: #####
3686: ##### sparse-matrix.cpp #####
3687: #####
3688:
3689: template< typename T >
3690: using FPSGraph = vector< vector< pair< int, T > > >;
3691:
3692: template< typename T >
3693: FormalPowerSeries< T > random_poly(int n) {
3694:     mt19937 mt(1333333);
3695:     FormalPowerSeries< T > res(n);
3696:     uniform_int_distribution< int > rand(0, T::get_mod() - 1);
3697:     for(int i = 0; i < n; i++) res[i] = rand(mt);
3698:     return res;
3699: }
3700:
3701: template< typename T >
3702: FormalPowerSeries< T > next_poly(const FormalPowerSeries< T > &dp, const FPSGraph<
T > &g) {
3703:     const int N = (int) dp.size();
3704:     FormalPowerSeries< T > nxt(N);
3705:     for(int i = 0; i < N; i++) {
3706:         for(auto &p : g[i]) nxt[p.first] += p.second * dp[i];
3707:     }
3708:     return nxt;
3709: }
3710:
3711: template< typename T >
3712: FormalPowerSeries< T > minimum_poly(const FPSGraph< T > &g) {
3713:     const int N = (int) g.size();
3714:     auto dp = random_poly< T >(N), u = random_poly< T >(N);
3715:     FormalPowerSeries< T > f(2 * N);
3716:     for(int i = 0; i < 2 * N; i++) {
3717:         for(auto &p : u.dot(dp)) f[i] += p;
3718:         dp = next_poly(dp, g);
3719:     }
3720:     return berlekamp_massey(f);
3721: }
3722:
3723: /* O(N(N+S) + N log N log Q) (O(S): time complexity of nex) */
3724: template< typename T >
3725: FormalPowerSeries< T > sparse_pow(int64_t Q, FormalPowerSeries< modint > dp, const
FPSGraph< T > &g) {
3726:     const int N = (int) dp.size();
3727:     auto A = FormalPowerSeries< T >({0, 1}).pow_mod(Q, minimum_poly(g));
3728:     FormalPowerSeries< T > res(N);
3729:     for(int i = 0; i < A.size(); i++) {
3730:         res += dp * A[i];
3731:         dp = next_poly(dp, g);
3732:     }
3733:     return res;
3734: }
3735:
3736: /* O(N(N+S)) (S: none-zero elements)*/
3737: template< typename T >
3738: T sparse_determinant(FPSGraph< T > g) {
3739:     using FPS = FormalPowerSeries< T >;

```

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```
3740:     int N = (int) g.size();
3741:     auto C = random_poly< T >(N);
3742:     for(int i = 0; i < N; i++) for(auto &p : g[i]) p.second *= C[i];
3743:     auto u = minimum_poly(g);
3744:     T acdet = u[0];
3745:     if(N % 2 == 0) acdet *= -1;
3746:     T cdet = 1;
3747:     for(int i = 0; i < N; i++) cdet *= C[i];
3748:     return acdet / cdet;
3749: }
3750:
3751:
3752: #####
3753: ##### convert-base.cpp #####
3754: #####
3755:
3756: template< typename T >
3757: vector< T > convert_base(T x, T b) {
3758:     vector< T > ret;
3759:     T t = 1, k = abs(b);
3760:     while(x) {
3761:         ret.emplace_back((x * t) % k);
3762:         if(ret.back() < 0) ret.back() += k;
3763:         x -= ret.back() * t;
3764:         x /= k;
3765:         t *= b / k;
3766:     }
3767:     if(ret.empty()) ret.emplace_back(0);
3768:     reverse(begin(ret), end(ret));
3769:     return ret;
3770: }
3771:
3772:
3773: #####
3774: ##### partition-table.cpp #####
3775: #####
3776:
3777: template< typename T >
3778: vector< vector< T > > get_partition(int n, int k) {
3779:     vector< vector< T > > dp(n + 1, vector< T >(k + 1));
3780:     dp[0][0] = 1;
3781:     for(int i = 0; i <= n; i++) {
3782:         for(int j = 1; j <= k; j++) {
3783:             if(i - j >= 0) dp[i][j] = dp[i][j - 1] + dp[i - j][j];
3784:             else dp[i][j] = dp[i][j - 1];
3785:         }
3786:     }
3787:     return dp;
3788: }
3789:
3790:
3791: #####
3792: ##### fast-fourier-transform.cpp #####
3793: #####
3794:
3795: namespace FastFourierTransform {
3796:     using real = double;
3797:
3798:     struct C {
3799:         real x, y;
3800:
3801:         C() : x(0), y(0) {}
3802:
3803:         C(real x, real y) : x(x), y(y) {}
3804:
3805:         inline C operator+(const C &c) const { return C(x + c.x, y + c.y); }
3806:
3807:         inline C operator-(const C &c) const { return C(x - c.x, y - c.y); }
3808:
3809:         inline C operator*(const C &c) const { return C(x * c.x - y * c.y, x * c.y + y
```

```

* c.x); }
3810:
3811:     inline C conj() const { return C(x, -y); }
3812: };
3813:
3814: const real PI = acos(-1);
3815: int base = 1;
3816: vector< C > rts = { {0, 0},
3817:                   {1, 0} };
3818: vector< int > rev = {0, 1};
3819:
3820:
3821: void ensure_base(int nbase) {
3822:     if(nbase <= base) return;
3823:     rev.resize(1 << nbase);
3824:     rts.resize(1 << nbase);
3825:     for(int i = 0; i < (1 << nbase); i++) {
3826:         rev[i] = (rev[i >> 1] >> 1) + ((i & 1) << (nbase - 1));
3827:     }
3828:     while(base < nbase) {
3829:         real angle = PI * 2.0 / (1 << (base + 1));
3830:         for(int i = 1 << (base - 1); i < (1 << base); i++) {
3831:             rts[i << 1] = rts[i];
3832:             real angle_i = angle * (2 * i + 1 - (1 << base));
3833:             rts[(i << 1) + 1] = C(cos(angle_i), sin(angle_i));
3834:         }
3835:         ++base;
3836:     }
3837: }
3838:
3839: void fft(vector< C > &a, int n) {
3840:     assert((n & (n - 1)) == 0);
3841:     int zeros = __builtin_ctz(n);
3842:     ensure_base(zeros);
3843:     int shift = base - zeros;
3844:     for(int i = 0; i < n; i++) {
3845:         if(i < (rev[i] >> shift)) {
3846:             swap(a[i], a[rev[i] >> shift]);
3847:         }
3848:     }
3849:     for(int k = 1; k < n; k <= 1) {
3850:         for(int i = 0; i < n; i += 2 * k) {
3851:             for(int j = 0; j < k; j++) {
3852:                 C z = a[i + j + k] * rts[j + k];
3853:                 a[i + j + k] = a[i + j] - z;
3854:                 a[i + j] = a[i + j] + z;
3855:             }
3856:         }
3857:     }
3858: }
3859:
3860: vector< int64_t > multiply(const vector< int > &a, const vector< int > &b) {
3861:     int need = (int) a.size() + (int) b.size() - 1;
3862:     int nbase = 1;
3863:     while((1 << nbase) < need) nbase++;
3864:     ensure_base(nbase);
3865:     int sz = 1 << nbase;
3866:     vector< C > fa(sz);
3867:     for(int i = 0; i < sz; i++) {
3868:         int x = (i < (int) a.size() ? a[i] : 0);
3869:         int y = (i < (int) b.size() ? b[i] : 0);
3870:         fa[i] = C(x, y);
3871:     }
3872:     fft(fa, sz);
3873:     C r(0, -0.25 / (sz >> 1)), s(0, 1), t(0.5, 0);
3874:     for(int i = 0; i <= (sz >> 1); i++) {
3875:         int j = (sz - i) & (sz - 1);
3876:         C z = (fa[j] * fa[j] - (fa[i] * fa[i]).conj()) * r;
3877:         fa[j] = (fa[i] * fa[i] - (fa[j] * fa[j]).conj()) * r;
3878:         fa[i] = z;

```



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```
3879:     }
3880:     for(int i = 0; i < (sz >> 1); i++) {
3881:         C A0 = (fa[i] + fa[i + (sz >> 1)]) * t;
3882:         C A1 = (fa[i] - fa[i + (sz >> 1)]) * t * rts[(sz >> 1) + i];
3883:         fa[i] = A0 + A1 * s;
3884:     }
3885:     fft(fa, sz >> 1);
3886:     vector< int64_t > ret(need);
3887:     for(int i = 0; i < need; i++) {
3888:         ret[i] = llround(i & 1 ? fa[i >> 1].y : fa[i >> 1].x);
3889:     }
3890:     return ret;
3891: }
3892: };
3893:
3894:
3895: #####
3896: ##### extgcd.cpp #####
3897: #####
3898:
3899: template< typename T >
3900: T extgcd(T a, T b, T &x, T &y) {
3901:     T d = a;
3902:     if(b != 0) {
3903:         d = extgcd(b, a % b, y, x);
3904:         y -= (a / b) * x;
3905:     } else {
3906:         x = 1;
3907:         y = 0;
3908:     }
3909:     return d;
3910: }
3911:
3912:
3913: #####
3914: ##### formal-power-series.cpp #####
3915: #####
3916:
3917: template< typename T >
3918: struct FormalPowerSeries : vector< T > {
3919:     using vector< T >::vector;
3920:     using P = FormalPowerSeries;
3921:
3922:     using MULT = function< P(P, P) >;
3923:     using FFT = function< void(P &) >;
3924:
3925:     static MULT &get_mult() {
3926:         static MULT mult = nullptr;
3927:         return mult;
3928:     }
3929:
3930:     static void set_mult(MULT f) { get_mult() = f; }
3931:
3932:     static FFT &get_fft() {
3933:         static FFT fft = nullptr;
3934:         return fft;
3935:     }
3936:
3937:     static FFT &get_ifft() {
3938:         static FFT ifft = nullptr;
3939:         return ifft;
3940:     }
3941:
3942:     static void set_fft(FFT f, FFT g) {
3943:         get_fft() = f;
3944:         get_ifft() = g;
3945:     }
3946:
3947:     void shrink() {
3948:         while(this->size() && this->back() == T(0)) this->pop_back();
```

```

3949:     }
3950:
3951: P operator+(const P &r) const { return P(*this) += r; }
3952:
3953: P operator+(const T &v) const { return P(*this) += v; }
3954:
3955: P operator-(const P &r) const { return P(*this) -= r; }
3956:
3957: P operator-(const T &v) const { return P(*this) -= v; }
3958:
3959: P operator*(const P &r) const { return P(*this) *= r; }
3960:
3961: P operator*(const T &v) const { return P(*this) *= v; }
3962:
3963: P operator/(const P &r) const { return P(*this) /= r; }
3964:
3965: P operator%(const P &r) const { return P(*this) %= r; }
3966:
3967: P &operator+=(const P &r) {
3968:     if(r.size() > this->size()) this->resize(r.size());
3969:     for(int i = 0; i < r.size(); i++) (*this)[i] += r[i];
3970:     return *this;
3971: }
3972:
3973: P &operator+=(const T &r) {
3974:     if(this->empty()) this->resize(1);
3975:     (*this)[0] += r;
3976:     return *this;
3977: }
3978:
3979: P &operator-=(const P &r) {
3980:     if(r.size() > this->size()) this->resize(r.size());
3981:     for(int i = 0; i < r.size(); i++) (*this)[i] -= r[i];
3982:     shrink();
3983:     return *this;
3984: }
3985:
3986: P &operator-=(const T &r) {
3987:     if(this->empty()) this->resize(1);
3988:     (*this)[0] -= r;
3989:     shrink();
3990:     return *this;
3991: }
3992:
3993: P &operator*=(const T &v) {
3994:     const int n = (int) this->size();
3995:     for(int k = 0; k < n; k++) (*this)[k] *= v;
3996:     return *this;
3997: }
3998:
3999: P &operator*=(const P &r) {
4000:     if(this->empty() || r.empty()) {
4001:         this->clear();
4002:         return *this;
4003:     }
4004:     assert(get_mult() != nullptr);
4005:     return *this = get_mult()(*this, r);
4006: }
4007:
4008: P &operator%=(const P &r) { return *this -= *this / r * r; }
4009:
4010: P operator-() const {
4011:     P ret(this->size());
4012:     for(int i = 0; i < this->size(); i++) ret[i] = -(*this)[i];
4013:     return ret;
4014: }
4015:
4016: P &operator/=(const P &r) {
4017:     if(this->size() < r.size()) {
4018:         this->clear();

```

```

4019:         return *this;
4020:     }
4021:     int n = this->size() - r.size() + 1;
4022:     return *this = (rev().pre(n) * r.rev().inv(n)).pre(n).rev(n);
4023: }
4024:
4025: P dot(P r) const {
4026:     P ret(min(this->size(), r.size()));
4027:     for(int i = 0; i < ret.size(); i++) ret[i] = (*this)[i] * r[i];
4028:     return ret;
4029: }
4030:
4031: P pre(int sz) const { return P(begin(*this), begin(*this) + min((int) this->size
(), sz)); }
4032:
4033: P operator>>(int sz) const {
4034:     if(this->size() <= sz) return {};
4035:     P ret(*this);
4036:     ret.erase(ret.begin(), ret.begin() + sz);
4037:     return ret;
4038: }
4039:
4040: P operator<<(int sz) const {
4041:     P ret(*this);
4042:     ret.insert(ret.begin(), sz, T(0));
4043:     return ret;
4044: }
4045:
4046: P rev(int deg = -1) const {
4047:     P ret(*this);
4048:     if(deg != -1) ret.resize(deg, T(0));
4049:     reverse(begin(ret), end(ret));
4050:     return ret;
4051: }
4052:
4053: P diff() const {
4054:     const int n = (int) this->size();
4055:     P ret(max(0, n - 1));
4056:     for(int i = 1; i < n; i++) ret[i - 1] = (*this)[i] * T(i);
4057:     return ret;
4058: }
4059:
4060: P integral() const {
4061:     const int n = (int) this->size();
4062:     P ret(n + 1);
4063:     ret[0] = T(0);
4064:     for(int i = 0; i < n; i++) ret[i + 1] = (*this)[i] / T(i + 1);
4065:     return ret;
4066: }
4067:
4068: // F(0) must not be 0
4069: P inv(int deg = -1) const {
4070:     assert((*this)[0] != T(0));
4071:     const int n = (int) this->size();
4072:     if(deg == -1) deg = n;
4073:     if(get_fft() != nullptr) {
4074:         P ret(*this);
4075:         ret.resize(deg, T(0));
4076:         return ret.inv_fast();
4077:     }
4078:     P ret({T(1) / (*this)[0]});
4079:     for(int i = 1; i < deg; i <= 1) {
4080:         ret = (ret + ret - ret * ret * pre(i << 1)).pre(i << 1);
4081:     }
4082:     return ret.pre(deg);
4083: }
4084:
4085: // F(0) must be 1
4086: P log(int deg = -1) const {
4087:     assert((*this)[0] == 1);

```

```

4088:     const int n = (int) this->size();
4089:     if(deg == -1) deg = n;
4090:     return (this->diff() * this->inv(deg)).pre(deg - 1).integral();
4091: }
4092:
4093: P sqrt(int deg = -1) const {
4094:     const int n = (int) this->size();
4095:     if(deg == -1) deg = n;
4096:     if((*this)[0] == T(0)) {
4097:         for(int i = 1; i < n; i++) {
4098:             if((*this)[i] != T(0)) {
4099:                 if(i & 1) return {};
4100:                 if(deg - i / 2 <= 0) break;
4101:                 auto ret = (*this >> i).sqrt(deg - i / 2) << (i / 2);
4102:                 if(ret.size() < deg) ret.resize(deg, T(0));
4103:                 return ret;
4104:             }
4105:         }
4106:         return P(deg, 0);
4107:     }
4108:
4109:     P ret({T(1)});
4110:     T inv2 = T(1) / T(2);
4111:     for(int i = 1; i < deg; i <= 1) {
4112:         ret = (ret + pre(i < 1) * ret.inv(i < 1)) * inv2;
4113:     }
4114:     return ret.pre(deg);
4115: }
4116:
4117: // F(0) must be 0
4118: P exp(int deg = -1) const {
4119:     assert((*this)[0] == T(0));
4120:     const int n = (int) this->size();
4121:     if(deg == -1) deg = n;
4122:     if(get_fft() != nullptr) {
4123:         P ret(*this);
4124:         ret.resize(deg, T(0));
4125:         return ret.exp_rec();
4126:     }
4127:     P ret({T(1)});
4128:     for(int i = 1; i < deg; i <= 1) {
4129:         ret = (ret * (pre(i < 1) + T(1) - ret.log(i < 1))).pre(i < 1);
4130:     }
4131:     return ret.pre(deg);
4132: }
4133:
4134:
4135: P online_convolution_exp(const P &conv_coeff) const {
4136:     const int n = (int) conv_coeff.size();
4137:     assert((n & (n - 1)) == 0);
4138:     vector< P > conv_ntt_coeff;
4139:     for(int i = n; i >= 1; i >= 1) {
4140:         P g(conv_coeff.pre(i));
4141:         get_fft()(g);
4142:         conv_ntt_coeff.emplace_back(g);
4143:     }
4144:     P conv_arg(n), conv_ret(n);
4145:     auto rec = [&](auto rec, int l, int r, int d) -> void {
4146:         if(r - l <= 16) {
4147:             for(int i = l; i < r; i++) {
4148:                 T sum = 0;
4149:                 for(int j = l; j < i; j++) sum += conv_arg[j] * conv_coeff[i - j];
4150:                 conv_ret[i] += sum;
4151:                 conv_arg[i] = i == 0 ? T(1) : conv_ret[i] / i;
4152:             }
4153:         } else {
4154:             int m = (l + r) / 2;
4155:             rec(rec, l, m, d + 1);
4156:             P pre(r - 1);
4157:             for(int i = 0; i < m - 1; i++) pre[i] = conv_arg[l + i];

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4158:         get_fft()(pre);
4159:         for(int i = 0; i < r - 1; i++) pre[i] *= conv_ntt_coeff[d][i];
4160:         get_ifft()(pre);
4161:         for(int i = 0; i < r - m; i++) conv_ret[m + i] += pre[m + i - 1];
4162:         rec(rec, m, r, d + 1);
4163:     }
4164: };
4165: rec(rec, 0, n, 0);
4166: return conv_arg;
4167: }
4168:
4169: P exp_rec() const {
4170:     assert((*this)[0] == T(0));
4171:     const int n = (int) this->size();
4172:     int m = 1;
4173:     while(m < n) m *= 2;
4174:     P conv_coeff(m);
4175:     for(int i = 1; i < n; i++) conv_coeff[i] = (*this)[i] * i;
4176:     return online_convolution_exp(conv_coeff).pre(n);
4177: }
4178:
4179:
4180: P inv_fast() const {
4181:     assert((*this)[0] != T(0));
4182:
4183:     const int n = (int) this->size();
4184:     P res{T(1) / (*this)[0]};
4185:
4186:     for(int d = 1; d < n; d <= 1) {
4187:         P f(2 * d), g(2 * d);
4188:         for(int j = 0; j < min(n, 2 * d); j++) f[j] = (*this)[j];
4189:         for(int j = 0; j < d; j++) g[j] = res[j];
4190:         get_fft()(f);
4191:         get_fft()(g);
4192:         for(int j = 0; j < 2 * d; j++) f[j] *= g[j];
4193:         get_ifft()(f);
4194:         for(int j = 0; j < d; j++) {
4195:             f[j] = 0;
4196:             f[j + d] = -f[j + d];
4197:         }
4198:         get_fft()(f);
4199:         for(int j = 0; j < 2 * d; j++) f[j] *= g[j];
4200:         get_ifft()(f);
4201:         for(int j = 0; j < d; j++) f[j] = res[j];
4202:         res = f;
4203:     }
4204:     return res.pre(n);
4205: }
4206:
4207: P pow(int64_t k, int deg = -1) const {
4208:     const int n = (int) this->size();
4209:     if(deg == -1) deg = n;
4210:     for(int i = 0; i < n; i++) {
4211:         if((*this)[i] != T(0)) {
4212:             T rev = T(1) / (*this)[i];
4213:             P ret = (((*this * rev) >> i).log() * k).exp() * ((*this)[i].pow(k));
4214:             if(i * k > deg) return P(deg, T(0));
4215:             ret = (ret << (i * k)).pre(deg);
4216:             if(ret.size() < deg) ret.resize(deg, T(0));
4217:             return ret;
4218:         }
4219:     }
4220:     return *this;
4221: }
4222:
4223: T eval(T x) const {
4224:     T r = 0, w = 1;
4225:     for(auto &v : *this) {
4226:         r += w * v;
4227:         w *= x;

```

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```
4228:     }
4229:     return r;
4230: }
4231:
4232: P pow_mod(int64_t n, P mod) const {
4233:     P modinv = mod.rev().inv();
4234:     auto get_div = [&](P base) {
4235:         if(base.size() < mod.size()) {
4236:             base.clear();
4237:             return base;
4238:         }
4239:         int n = base.size() - mod.size() + 1;
4240:         return (base.rev().pre(n) * modinv.pre(n)).pre(n).rev(n);
4241:     };
4242:     P x(*this), ret{1};
4243:     while(n > 0) {
4244:         if(n & 1) {
4245:             ret *= x;
4246:             ret -= get_div(ret) * mod;
4247:         }
4248:         x *= x;
4249:         x -= get_div(x) * mod;
4250:         n >>= 1;
4251:     }
4252:     return ret;
4253: }
4254: };
4255:
4256:
4257: #####
4258: ##### matrix.cpp #####
4259: #####
4260:
4261: template< class T >
4262: struct Matrix {
4263:     vector< vector< T > > A;
4264:
4265:     Matrix() {}
4266:
4267:     Matrix(size_t n, size_t m) : A(n, vector< T >(m, 0)) {}
4268:
4269:     Matrix(size_t n) : A(n, vector< T >(n, 0)) {}
4270:
4271:     size_t height() const {
4272:         return (A.size());
4273:     }
4274:
4275:     size_t width() const {
4276:         return (A[0].size());
4277:     }
4278:
4279:     inline const vector< T > &operator[](int k) const {
4280:         return (A.at(k));
4281:     }
4282:
4283:     inline vector< T > &operator[](int k) {
4284:         return (A.at(k));
4285:     }
4286:
4287:     static Matrix I(size_t n) {
4288:         Matrix mat(n);
4289:         for(int i = 0; i < n; i++) mat[i][i] = 1;
4290:         return (mat);
4291:     }
4292:
4293:     Matrix &operator+=(const Matrix &B) {
4294:         size_t n = height(), m = width();
4295:         assert(n == B.height() && m == B.width());
4296:         for(int i = 0; i < n; i++)
4297:             for(int j = 0; j < m; j++)
```

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```

4298:         (*this)[i][j] += B[i][j];
4299:     return (*this);
4300: }
4301:
4302: Matrix &operator+=(const Matrix &B) {
4303:     size_t n = height(), m = width();
4304:     assert(n == B.height() && m == B.width());
4305:     for(int i = 0; i < n; i++)
4306:         for(int j = 0; j < m; j++)
4307:             (*this)[i][j] += B[i][j];
4308:     return (*this);
4309: }
4310:
4311: Matrix &operator*=(const Matrix &B) {
4312:     size_t n = height(), m = B.width(), p = width();
4313:     assert(p == B.height());
4314:     vector< vector< T > > C(n, vector< T >(m, 0));
4315:     for(int i = 0; i < n; i++)
4316:         for(int j = 0; j < m; j++)
4317:             for(int k = 0; k < p; k++)
4318:                 C[i][j] = (C[i][j] + (*this)[i][k] * B[k][j]);
4319:     A.swap(C);
4320:     return (*this);
4321: }
4322:
4323: Matrix &operator^=(long long k) {
4324:     Matrix B = Matrix::I(height());
4325:     while(k > 0) {
4326:         if(k & 1) B *= *this;
4327:         *this *= *this;
4328:         k >>= 1LL;
4329:     }
4330:     A.swap(B.A);
4331:     return (*this);
4332: }
4333:
4334: Matrix operator+(const Matrix &B) const {
4335:     return (Matrix(*this) += B);
4336: }
4337:
4338: Matrix operator-(const Matrix &B) const {
4339:     return (Matrix(*this) -= B);
4340: }
4341:
4342: Matrix operator*(const Matrix &B) const {
4343:     return (Matrix(*this) *= B);
4344: }
4345:
4346: Matrix operator^(const long long k) const {
4347:     return (Matrix(*this) ^= k);
4348: }
4349:
4350: friend ostream &operator<<(ostream &os, Matrix &p) {
4351:     size_t n = p.height(), m = p.width();
4352:     for(int i = 0; i < n; i++) {
4353:         os << "[";
4354:         for(int j = 0; j < m; j++) {
4355:             os << p[i][j] << (j + 1 == m ? "]\n" : ",");
4356:         }
4357:     }
4358:     return (os);
4359: }
4360:
4361:
4362: T determinant() {
4363:     Matrix B(*this);
4364:     assert(width() == height());
4365:     T ret = 1;
4366:     for(int i = 0; i < width(); i++) {
4367:         int idx = -1;

```

```

4368:     for(int j = i; j < width(); j++) {
4369:         if(B[j][i] != 0) idx = j;
4370:     }
4371:     if(idx == -1) return (0);
4372:     if(i != idx) {
4373:         ret *= -1;
4374:         swap(B[i], B[idx]);
4375:     }
4376:     ret *= B[i][i];
4377:     T vv = B[i][i];
4378:     for(int j = 0; j < width(); j++) {
4379:         B[i][j] /= vv;
4380:     }
4381:     for(int j = i + 1; j < width(); j++) {
4382:         T a = B[j][i];
4383:         for(int k = 0; k < width(); k++) {
4384:             B[j][k] -= B[i][k] * a;
4385:         }
4386:     }
4387: }
4388: return (ret);
4389: }
4390: };
4391:
4392:
4393: #####
4394: ##### berlekamp-massey.cpp #####
4395: #####
4396:
4397: template< class T >
4398: FormalPowerSeries< T > berlekamp_massey(const FormalPowerSeries< T > &s) {
4399:     const int N = (int) s.size();
4400:     FormalPowerSeries< T > b = {T(-1)}, c = {T(-1)};
4401:     T y = T(1);
4402:     for(int ed = 1; ed <= N; ed++) {
4403:         int l = int(c.size()), m = int(b.size());
4404:         T x = 0;
4405:         for(int i = 0; i < l; i++) x += c[i] * s[ed - 1 + i];
4406:         b.emplace_back(0);
4407:         m++;
4408:         if(x == T(0)) continue;
4409:         T freq = x / y;
4410:         if(l < m) {
4411:             auto tmp = c;
4412:             c.insert(begin(c), m - 1, T(0));
4413:             for(int i = 0; i < m; i++) c[m - 1 - i] -= freq * b[m - 1 - i];
4414:             b = tmp;
4415:             y = x;
4416:         } else {
4417:             for(int i = 0; i < m; i++) c[l - 1 - i] -= freq * b[m - 1 - i];
4418:         }
4419:     }
4420:     return c;
4421: }
4422:
4423:
4424: #####
4425: ##### euler-phi-table.cpp #####
4426: #####
4427:
4428: vector< int > euler_phi_table(int n) {
4429:     vector< int > euler(n + 1);
4430:     for(int i = 0; i <= n; i++) {
4431:         euler[i] = i;
4432:     }
4433:     for(int i = 2; i <= n; i++) {
4434:         if(euler[i] == i) {
4435:             for(int j = i; j <= n; j += i) {
4436:                 euler[j] = euler[j] / i * (i - 1);
4437:             }

```



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```
4438:     }
4439: }
4440: return euler;
4441: }
4442:
4443:
4444: #####
4445: ##### number-theoretic-transform.cpp #####
4446: #####
4447:
4448: template< int mod >
4449: struct NumberTheoreticTransform {
4450:
4451:     vector< int > rev, rts;
4452:     int base, max_base, root;
4453:
4454:     NumberTheoreticTransform() : base(1), rev{0, 1}, rts{0, 1} {
4455:         assert(mod >= 3 && mod % 2 == 1);
4456:         auto tmp = mod - 1;
4457:         max_base = 0;
4458:         while(tmp % 2 == 0) tmp >>= 1, max_base++;
4459:         root = 2;
4460:         while(mod_pow(root, (mod - 1) >> 1) == 1) ++root;
4461:         assert(mod_pow(root, mod - 1) == 1);
4462:         root = mod_pow(root, (mod - 1) >> max_base);
4463:     }
4464:
4465:     inline int mod_pow(int x, int n) {
4466:         int ret = 1;
4467:         while(n > 0) {
4468:             if(n & 1) ret = mul(ret, x);
4469:             x = mul(x, x);
4470:             n >>= 1;
4471:         }
4472:         return ret;
4473:     }
4474:
4475:     inline int inverse(int x) {
4476:         return mod_pow(x, mod - 2);
4477:     }
4478:
4479:     inline unsigned add(unsigned x, unsigned y) {
4480:         x += y;
4481:         if(x >= mod) x -= mod;
4482:         return x;
4483:     }
4484:
4485:     inline unsigned mul(unsigned a, unsigned b) {
4486:         return lull * a * b % (unsigned long long) mod;
4487:     }
4488:
4489:     void ensure_base(int nbase) {
4490:         if(nbase <= base) return;
4491:         rev.resize(1 << nbase);
4492:         rts.resize(1 << nbase);
4493:         for(int i = 0; i < (1 << nbase); i++) {
4494:             rev[i] = (rev[i >> 1] >> 1) + ((i & 1) << (nbase - 1));
4495:         }
4496:         assert(nbase <= max_base);
4497:         while(base < nbase) {
4498:             int z = mod_pow(root, 1 << (max_base - 1 - base));
4499:             for(int i = 1 << (base - 1); i < (1 << base); i++) {
4500:                 rts[i << 1] = rts[i];
4501:                 rts[(i << 1) + 1] = mul(rts[i], z);
4502:             }
4503:             ++base;
4504:         }
4505:     }
4506:
4507: }
```

```

4508: void ntt(vector< int > &a) {
4509:     const int n = (int) a.size();
4510:     assert((n & (n - 1)) == 0);
4511:     int zeros = __builtin_ctz(n);
4512:     ensure_base(zeros);
4513:     int shift = base - zeros;
4514:     for(int i = 0; i < n; i++) {
4515:         if(i < (rev[i] >> shift)) {
4516:             swap(a[i], a[rev[i] >> shift]);
4517:         }
4518:     }
4519:     for(int k = 1; k < n; k <= 1) {
4520:         for(int i = 0; i < n; i += 2 * k) {
4521:             for(int j = 0; j < k; j++) {
4522:                 int z = mul(a[i + j + k], rts[j + k]);
4523:                 a[i + j + k] = add(a[i + j], mod - z);
4524:                 a[i + j] = add(a[i + j], z);
4525:             }
4526:         }
4527:     }
4528: }
4529:
4530:
4531: vector< int > multiply(vector< int > a, vector< int > b) {
4532:     int need = a.size() + b.size() - 1;
4533:     int nbase = 1;
4534:     while((1 < nbase) < need) nbase++;
4535:     ensure_base(nbase);
4536:     int sz = 1 << nbase;
4537:     a.resize(sz, 0);
4538:     b.resize(sz, 0);
4539:     ntt(a);
4540:     ntt(b);
4541:     int inv_sz = inverse(sz);
4542:     for(int i = 0; i < sz; i++) {
4543:         a[i] = mul(a[i], mul(b[i], inv_sz));
4544:     }
4545:     reverse(a.begin() + 1, a.end());
4546:     ntt(a);
4547:     a.resize(need);
4548:     return a;
4549: }
4550: };
4551:
4552:
4553: #####
4554: ##### arbitrary-mod-int.cpp #####
4555: #####
4556:
4557: struct ArbitraryModInt {
4558:
4559:     int x;
4560:
4561:     ArbitraryModInt() : x(0) {}
4562:
4563:     ArbitraryModInt(int64_t y) : x(y >= 0 ? y % mod() : (mod() - (-y) % mod()) % mod
4564: ()) {}
4565:
4566:     static int &mod() {
4567:         static int mod = 0;
4568:         return mod;
4569:     }
4570:
4571:     static int set_mod(int md) {
4572:         mod() = md;
4573:     }
4574:
4575:     ArbitraryModInt &operator+=(const ArbitraryModInt &p) {
4576:         if((x += p.x) >= mod()) x -= mod();
4577:         return *this;

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```
4577:     }
4578:
4579: ArbitraryModInt &operator==(const ArbitraryModInt &p) {
4580:     if((x += mod() - p.x) >= mod()) x -= mod();
4581:     return *this;
4582: }
4583:
4584: ArbitraryModInt &operator*=(const ArbitraryModInt &p) {
4585:     unsigned long long a = (unsigned long long) x * p.x;
4586:     unsigned xh = (unsigned) (a >> 32), xl = (unsigned) a, d, m;
4587:     asm("divl %4; \n\t" : "=a" (d), "=d" (m) : "d" (xh), "a" (xl), "r" (mod()));
4588:     x = m;
4589:     return *this;
4590: }
4591:
4592: ArbitraryModInt &operator/=(const ArbitraryModInt &p) {
4593:     *this *= p.inverse();
4594:     return *this;
4595: }
4596:
4597: ArbitraryModInt operator-() const { return ArbitraryModInt(-x); }
4598:
4599: ArbitraryModInt operator+(const ArbitraryModInt &p) const { return ArbitraryModInt(*this) += p; }
4600:
4601: ArbitraryModInt operator-(const ArbitraryModInt &p) const { return ArbitraryModInt(*this) -= p; }
4602:
4603: ArbitraryModInt operator*(const ArbitraryModInt &p) const { return ArbitraryModInt(*this) *= p; }
4604:
4605: ArbitraryModInt operator/(const ArbitraryModInt &p) const { return ArbitraryModInt(*this) /= p; }
4606:
4607: bool operator==(const ArbitraryModInt &p) const { return x == p.x; }
4608:
4609: bool operator!=(const ArbitraryModInt &p) const { return x != p.x; }
4610:
4611: ArbitraryModInt inverse() const {
4612:     int a = x, b = mod(), u = 1, v = 0, t;
4613:     while(b > 0) {
4614:         t = a / b;
4615:         swap(a -= t * b, b);
4616:         swap(u -= t * v, v);
4617:     }
4618:     return ArbitraryModInt(u);
4619: }
4620:
4621: ArbitraryModInt pow(int64_t n) const {
4622:     ArbitraryModInt ret(1), mul(x);
4623:     while(n > 0) {
4624:         if(n & 1) ret *= mul;
4625:         mul *= mul;
4626:         n >>= 1;
4627:     }
4628:     return ret;
4629: }
4630:
4631: friend ostream &operator<<(ostream &os, const ArbitraryModInt &p) {
4632:     return os << p.x;
4633: }
4634:
4635: friend istream &operator>>(istream &is, ArbitraryModInt &a) {
4636:     int64_t t;
4637:     is >> t;
4638:     a = ArbitraryModInt(t);
4639:     return (is);
4640: }
4641: };
4642:
```

```

4643:
4644: -----
4645: |                                     dp                                     |
4646: -----
4647:
4648: #####
4649: ##### knapsack-limitations.cpp #####
4650: #####
4651:
4652: template< typename T, typename Compare = greater< T > >
4653: vector< T > knapsack_limitations(const vector< int > &w, const vector< int > &m, c
4654: onst vector< T > &v,
4655:                                const int &W, const T &NG, const Compare &comp =
4656: Compare()) {
4657:     const int N = (int) w.size();
4658:     vector< T > dp(W + 1, NG), deqv(W + 1);
4659:     dp[0] = T();
4660:     vector< int > deq(W + 1);
4661:     for(int i = 0; i < N; i++) {
4662:         for(int a = 0; a < w[i]; a++) {
4663:             int s = 0, t = 0;
4664:             for(int j = 0; w[i] * j + a <= W; j++) {
4665:                 if(dp[w[i] * j + a] != NG) {
4666:                     auto val = dp[w[i] * j + a] - j * v[i];
4667:                     while(s < t && comp(val, deqv[t - 1])) --t;
4668:                     deq[t] = j;
4669:                     deqv[t++] = val;
4670:                 }
4671:                 if(s < t) {
4672:                     dp[j * w[i] + a] = deqv[s] + j * v[i];
4673:                     if(deq[s] == j - m[i]) ++s;
4674:                 }
4675:             }
4676:         }
4677:     }
4678:     return dp;
4679: }
4680: #####
4681: ##### online-offline-dp.cpp #####
4682: #####
4683:
4684: template< typename T, typename Compare = less< T > >
4685: vector< T > online_offline_dp(int W, const function< T(int, int) > &f, const Compa
4686: re &comp = Compare()) {
4687:     vector< T > dp(W + 1);
4688:     vector< int > isset(W + 1);
4689:     int y_base = -1, x_base = -1;
4690:     function< T(int, int) > get_cost = [&](int y, int x) { // return dp[0, x+x_base]
4691:         +f[x+x_base, y+y_base]
4692:     };
4693:     return dp[x + x_base] + f(x + x_base, y + y_base);
4694: };
4695: function< void(int, int, int) > induce = [&](int l, int m, int r) { // dp[l, m)
4696:     -> dp[m, r)
4697:     x_base = l, y_base = m;
4698:     auto ret = monotone_minima(r - m, m - l, get_cost, comp);
4699:     for(int i = 0; i < ret.size(); i++) {
4700:         if(!isset[m + i] || comp(ret[i].second, dp[m + i])) {
4701:             isset[m + i] = true;
4702:             dp[m + i] = ret[i].second;
4703:         }
4704:     }
4705: };
4706: function< void(int, int) > dfs = [&](int l, int r) {
4707:     if(l + 1 == r) {
4708:         x_base = l, y_base = l;
4709:         T cst = l ? get_cost(0, -1) : 0;
4710:         if(!isset[l] || comp(cst, dp[l])) {
4711:             isset[l] = true;

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```
4708:         dp[l] = cst;
4709:     }
4710: } else {
4711:     int mid = (l + r) / 2;
4712:     dfs(l, mid);
4713:     induce(l, mid, r);
4714:     dfs(mid, r);
4715: }
4716: };
4717: dfs(0, W + 1);
4718: return dp;
4719: };
4720:
4721:
4722: #####
4723: ##### cumulative-sum.cpp #####
4724: #####
4725:
4726: template< class T >
4727: struct CumulativeSum {
4728:     vector< T > data;
4729:
4730:     CumulativeSum(int sz) : data(sz, 0) {};
4731:
4732:     void add(int k, T x) {
4733:         data[k] += x;
4734:     }
4735:
4736:     void build() {
4737:         for(int i = 1; i < data.size(); i++) {
4738:             data[i] += data[i - 1];
4739:         }
4740:     }
4741:
4742:     T query(int k) {
4743:         if(k < 0) return (0);
4744:         return (data[min(k, (int) data.size() - 1)]);
4745:     }
4746: };
4747:
4748:
4749: #####
4750: ##### cumulative-sum-2d.cpp #####
4751: #####
4752:
4753: template< class T >
4754: struct CumulativeSum2D {
4755:     vector< vector< T > > data;
4756:
4757:     CumulativeSum2D(int W, int H) : data(W + 1, vector< int >(H + 1, 0)) {}
4758:
4759:     void add(int x, int y, T z) {
4760:         ++x, ++y;
4761:         if(x >= data.size() || y >= data[0].size()) return;
4762:         data[x][y] += z;
4763:     }
4764:
4765:     void build() {
4766:         for(int i = 1; i < data.size(); i++) {
4767:             for(int j = 1; j < data[i].size(); j++) {
4768:                 data[i][j] += data[i][j - 1] + data[i - 1][j] - data[i - 1][j - 1];
4769:             }
4770:         }
4771:     }
4772:
4773:     T query(int sx, int sy, int gx, int gy) {
4774:         return (data[gx][gy] - data[sx][gy] - data[gx][sy] + data[sx][sy]);
4775:     }
4776: };
4777:
```

```

4778:
4779: #####
4780: ##### largest-rectangle.cpp #####
4781: #####
4782:
4783: template< typename T >
4784: int64_t largest_rectangle(vector< T > height)
4785: {
4786:     stack< int > st;
4787:     height.push_back(0);
4788:     vector< int > left(height.size());
4789:     int64_t ret = 0;
4790:     for(int i = 0; i < height.size(); i++) {
4791:         while(!st.empty() && height[st.top()] >= height[i]) {
4792:             ret = max(ret, (int64_t) (i - left[st.top()] - 1) * height[st.top()]);
4793:             st.pop();
4794:         }
4795:         left[i] = st.empty() ? -1 : st.top();
4796:         st.emplace(i);
4797:     }
4798:     return ret;
4799: }
4800:
4801:
4802: #####
4803: ##### slide-min.cpp #####
4804: #####
4805:
4806: template< typename T >
4807: vector< T > slide_min(const vector< T > &v, int k)
4808: {
4809:     deque< int > deq;
4810:     vector< T > ret;
4811:     for(int i = 0; i < v.size(); i++) {
4812:         while(!deq.empty() && v[deq.back()] >= v[i]) {
4813:             deq.pop_back();
4814:         }
4815:         deq.push_back(i);
4816:         if(i - k + 1 >= 0) {
4817:             ret.emplace_back(v[deq.front()]);
4818:             if(deq.front() == i - k + 1) deq.pop_front();
4819:         }
4820:     }
4821:     return ret;
4822: }
4823:
4824:
4825: #####
4826: ##### longest-increasing-subsequence.cpp #####
4827: #####
4828:
4829: template< typename T >
4830: size_t longest_increasing_subsequence(const vector< T > &a, bool strict) {
4831:     vector< T > lis;
4832:     for(auto &p : a) {
4833:         typename vector< T >::iterator it;
4834:         if(strict) it = lower_bound(begin(lis), end(lis), p);
4835:         else it = upper_bound(begin(lis), end(lis), p);
4836:         if(end(lis) == it) lis.emplace_back(p);
4837:         else *it = p;
4838:     }
4839:     return lis.size();
4840: }
4841:
4842:
4843: #####
4844: ##### monotone-minima.cpp #####
4845: #####
4846:
4847: template< typename T, typename Compare = less< T > >

```

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```
4848: vector< pair< int, T > > monotone_minima(int H, int W, const function< T(int, int)
> &f, const Compare &comp = Compare()) {
4849:     vector< pair< int, T > > dp(H);
4850:     function< void(int, int, int, int) > dfs = [&](int top, int bottom, int left, in
t right) {
4851:         if(top > bottom) return;
4852:         int line = (top + bottom) / 2;
4853:         T ma;
4854:         int mi = -1;
4855:         for(int i = left; i <= right; i++) {
4856:             T cst = f(line, i);
4857:             if(mi == -1 || comp(cst, ma)) {
4858:                 ma = cst;
4859:                 mi = i;
4860:             }
4861:         }
4862:         dp[line] = make_pair(mi, ma);
4863:         dfs(top, line - 1, left, mi);
4864:         dfs(line + 1, bottom, mi, right);
4865:     };
4866:     dfs(0, H - 1, 0, W - 1);
4867:     return dp;
4868: }
4869:
4870:
4871:
4872: #####
4873: ##### knapsack-limitations-2.cpp #####
4874: #####
4875:
4876: template< typename T >
4877: T knapsack_limitations(const vector< T > &w, const vector< T > &m, const vector< i
nt > &v,
4878:                     const T &W) {
4879:     const int N = (int) w.size();
4880:     auto v_max = *max_element(begin(v), end(v));
4881:     if(v_max == 0) return 0;
4882:     vector< int > ma(N);
4883:     vector< T > mb(N);
4884:     for(int i = 0; i < N; i++) {
4885:         ma[i] = min< T >(m[i], v_max - 1);
4886:         mb[i] = m[i] - ma[i];
4887:     }
4888:     T sum = 0;
4889:     for(int i = 0; i < N; i++) sum += ma[i] * v[i];
4890:     auto dp = knapsack_limitations(v, ma, w, sum, T(-1), less<>());
4891:     vector< int > ord(N);
4892:     iota(begin(ord), end(ord), 0);
4893:     sort(begin(ord), end(ord), [&](int a, int b) {
4894:         return v[a] * w[b] > v[b] * w[a];
4895:     });
4896:     T ret = T();
4897:     for(int i = 0; i < dp.size(); i++) {
4898:         if(dp[i] > W || dp[i] == -1) continue;
4899:         T rest = W - dp[i], cost = i;
4900:         for(auto &p : ord) {
4901:             auto get = min(mb[p], rest / w[p]);
4902:             if(get == 0) break;
4903:             cost += get * v[p];
4904:             rest -= get * w[p];
4905:         }
4906:         ret = max(ret, cost);
4907:     }
4908:     return ret;
4909: }
4910:
4911:
4912: #####
4913: ##### divide-and-conquer-optimization.cpp #####
4914: #####
```

```

4915:
4916: template< typename T, typename Compare = less< T > >
4917: vector< vector< T > > divide_and_conquer_optimization(int H, int W, T INF, const f
unction< T(int, int) > &f, const Compare &comp = Compare()) {
4918:     vector< vector< T > > dp(H + 1, vector< T >(W + 1, INF));
4919:     dp[0][0] = 0;
4920:     for(int i = 1; i <= H; i++) {
4921:         function< T(int, int) > get_cost = [&](int y, int x) {
4922:             if(x >= y) return INF;
4923:             return dp[i - 1][x] + f(x, y);
4924:         };
4925:         auto ret = monotone_minima(W + 1, W + 1, get_cost, comp);
4926:         for(int j = 0; j <= W; j++) dp[i][j] = ret[j].second;
4927:     }
4928:     return dp;
4929: }
4930:
4931:
4932: #####
4933: ##### hu-tucker.cpp #####
4934: #####
4935:
4936: te< typename Heap, typename T >
4937: T hu_tucker(vector< T > vs, T INF) {
4938:     int N = (int) vs.size();
4939:     Heap heap;
4940:     vector< typename Heap::Node * > hs(N - 1, heap.makeheap());
4941:     vector< int > ls(N), rs(N);
4942:     vector< T > cs(N - 1);
4943:     using pi = pair< T, int >;
4944:     priority_queue< pi, vector< pi >, greater< pi > > que;
4945:     for(int i = 0; i + 1 < N; i++) {
4946:         ls[i] = i - 1;
4947:         rs[i] = i + 1;
4948:         cs[i] = vs[i] + vs[i + 1];
4949:         que.emplace(cs[i], i);
4950:     }
4951:     T ret = 0;
4952:     for(int k = 0; k + 1 < N; k++) {
4953:         T c;
4954:         int i;
4955:         do {
4956:             tie(c, i) = que.top();
4957:             que.pop();
4958:         } while(rs[i] < 0 || cs[i] != c);
4959:
4960:         bool ml = false, mr = false;
4961:         if(!heap.empty(hs[i]) && vs[i] + heap.top(hs[i]) == c) {
4962:             heap.pop(hs[i]);
4963:             ml = true;
4964:         } else if(vs[i] + vs[rs[i]] == c) {
4965:             ml = mr = true;
4966:         } else {
4967:             auto top = heap.pop(hs[i]);
4968:             if(!heap.empty(hs[i]) && heap.top(hs[i]) + top == c) {
4969:                 heap.pop(hs[i]);
4970:             } else {
4971:                 mr = true;
4972:             }
4973:         }
4974:         ret += c;
4975:         heap.push(hs[i], c);
4976:         if(ml) vs[i] = INF;
4977:         if(mr) vs[rs[i]] = INF;
4978:
4979:         if(ml && i > 0) {
4980:             int j = ls[i];
4981:             hs[j] = heap.merge(hs[j], hs[i]);
4982:             rs[j] = rs[i];
4983:             rs[i] = -1;

```



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```

4984:         ls[rs[j]] = j;
4985:         i = j;
4986:     }
4987:
4988:     if(mr && rs[i] + 1 < N) {
4989:         int j = rs[i];
4990:         hs[i] = heap.merge(hs[i], hs[j]);
4991:         rs[i] = rs[j];
4992:         rs[j] = -1;
4993:         ls[rs[i]] = i;
4994:     }
4995:     cs[i] = vs[i] + vs[rs[i]];
4996:
4997:     if(!heap.empty(hs[i])) {
4998:         T top = heap.pop(hs[i]);
4999:         cs[i] = min(cs[i], min(vs[i], vs[rs[i]]) + top);
5000:         if(!heap.empty(hs[i])) cs[i] = min(cs[i], top + heap.top(hs[i]));
5001:         heap.push(hs[i], top);
5002:     }
5003:     que.emplace(cs[i], i);
5004: }
5005: return ret;
5006: }
5007:
5008:
5009: -----
5010: |                                     string                                     |
5011: -----
5012:
5013: #####
5014: ##### manacher.cpp #####
5015: #####
5016:
5017: vector< int > manacher(const string &s) {
5018:     vector< int > radius(s.size());
5019:     int i = 0, j = 0;
5020:     while(i < s.size()) {
5021:         while(i - j >= 0 && i + j < s.size() && s[i - j] == s[i + j]) {
5022:             ++j;
5023:         }
5024:         radius[i] = j;
5025:         int k = 1;
5026:         while(i - k >= 0 && i + k < s.size() && k + radius[i - k] < j) {
5027:             radius[i + k] = radius[i - k];
5028:             ++k;
5029:         }
5030:         i += k;
5031:         j -= k;
5032:     }
5033:     return radius;
5034: }
5035:
5036:
5037: #####
5038: ##### rolling-hash.cpp #####
5039: #####
5040:
5041: template< unsigned mod >
5042: struct RollingHash {
5043:     vector< unsigned > hashed, power;
5044:
5045:     inline unsigned mul(unsigned a, unsigned b) const {
5046:         unsigned long long x = (unsigned long long) a * b;
5047:         unsigned xh = (unsigned) (x >> 32), xl = (unsigned) x, d, m;
5048:         asm("divl %4; \n\t" : "=a" (d), "=d" (m) : "d" (xh), "a" (xl), "r" (mod));
5049:         return m;
5050:     }
5051:
5052:     RollingHash(const string &s, unsigned base = 10007) {
5053:         int sz = (int) s.size();

```

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```
5054:     hashed.assign(sz + 1, 0);
5055:     power.assign(sz + 1, 0);
5056:     power[0] = 1;
5057:     for(int i = 0; i < sz; i++) {
5058:         power[i + 1] = mul(power[i], base);
5059:         hashed[i + 1] = mul(hashed[i], base) + s[i];
5060:         if(hashed[i + 1] >= mod) hashed[i + 1] -= mod;
5061:     }
5062: }
5063:
5064: unsigned get(int l, int r) const {
5065:     unsigned ret = hashed[r] + mod - mul(hashed[l], power[r - l]);
5066:     if(ret >= mod) ret -= mod;
5067:     return ret;
5068: }
5069:
5070: unsigned connect(unsigned h1, int h2, int h2len) const {
5071:     unsigned ret = mul(h1, power[h2len]) + h2;
5072:     if(ret >= mod) ret -= mod;
5073:     return ret;
5074: }
5075:
5076: int LCP(const RollingHash< mod > &b, int l1, int r1, int l2, int r2) {
5077:     int len = min(r1 - l1, r2 - l2);
5078:     int low = -1, high = len + 1;
5079:     while(high - low > 1) {
5080:         int mid = (low + high) / 2;
5081:         if(get(l1, l1 + mid) == b.get(l2, l2 + mid)) low = mid;
5082:         else high = mid;
5083:     }
5084:     return (low);
5085: }
5086: };
5087:
5088: using RH = RollingHash< 1000000007 >;
5089:
5090:
5091: #####
5092: ##### aho-corasick.cpp #####
5093: #####
5094:
5095: template< int char_size, int margin >
5096: struct AhoCorasick : Trie< char_size + 1, margin > {
5097:     using Trie< char_size + 1, margin >::Trie;
5098:
5099:     const int FAIL = char_size;
5100:     vector< int > correct;
5101:
5102:     void build(bool heavy = true) {
5103:         correct.resize(this->size());
5104:         for(int i = 0; i < this->size(); i++) {
5105:             correct[i] = (int) this->nodes[i].accept.size();
5106:         }
5107:         queue< int > que;
5108:         for(int i = 0; i <= char_size; i++) {
5109:             if(~this->nodes[0].nxt[i]) {
5110:                 this->nodes[this->nodes[0].nxt[i]].nxt[FAIL] = 0;
5111:                 que.emplace(this->nodes[0].nxt[i]);
5112:             } else {
5113:                 this->nodes[0].nxt[i] = 0;
5114:             }
5115:         }
5116:         while(!que.empty()) {
5117:             auto &now = this->nodes[que.front()];
5118:             int fail = now.nxt[FAIL];
5119:             correct[que.front()] += correct[fail];
5120:             que.pop();
5121:             for(int i = 0; i < char_size; i++) {
5122:                 if(~now.nxt[i]) {
5123:                     this->nodes[now.nxt[i]].nxt[FAIL] = this->nodes[fail].nxt[i];
```

```

5124:         if(heavy) {
5125:             auto &u = this->nodes[now.nxt[i]].accept;
5126:             auto &v = this->nodes[this->nodes[fail].nxt[i]].accept;
5127:             vector< int > accept;
5128:             set_union(begin(u), end(u), begin(v), end(v), back_inserter(accept));
5129:             u = accept;
5130:         }
5131:         que.emplace(now.nxt[i]);
5132:     } else {
5133:         now.nxt[i] = this->nodes[fail].nxt[i];
5134:     }
5135: }
5136: }
5137: }
5138:
5139: map< int, int > match(const string &str, int now = 0) {
5140:     map< int, int > result;
5141:     for(auto &c : str) {
5142:         now = this->nodes[now].nxt[c - margin];
5143:         for(auto &v : this->nodes[now].accept) result[v] += 1;
5144:     }
5145:     return result;
5146: }
5147:
5148: pair< int64_t, int > move(const char &c, int now = 0) {
5149:     now = this->nodes[now].nxt[c - margin];
5150:     return {correct[now], now};
5151: }
5152:
5153: pair< int64_t, int > move(const string &str, int now = 0) {
5154:     int64_t sum = 0;
5155:     for(auto &c : str) {
5156:         auto nxt = move(c, now);
5157:         sum += nxt.first;
5158:         now = nxt.second;
5159:     }
5160:     return {sum, now};
5161: }
5162: };
5163:
5164:
5165: #####
5166: ##### suffix-array.cpp #####
5167: #####
5168:
5169: struct SuffixArray {
5170:     vector< int > SA;
5171:     const string s;
5172:
5173:     SuffixArray(const string &str) : s(str) {
5174:         SA.resize(s.size());
5175:         iota(begin(SA), end(SA), 0);
5176:         sort(begin(SA), end(SA), [&](int a, int b) {
5177:             return s[a] == s[b] ? a > b : s[a] < s[b];
5178:         });
5179:         vector< int > classes(s.size(), c(s.begin(), s.end(), cnt(s.size())));
5180:         for(int len = 1; len < s.size(); len <= 1) {
5181:             for(int i = 0; i < s.size(); i++) {
5182:                 if(i > 0 && c[SA[i - 1]] == c[SA[i]] && SA[i - 1] + len < s.size() && c[SA
[i - 1] + len / 2] == c[SA[i] + len / 2]) {
5183:                     classes[SA[i]] = classes[SA[i - 1]];
5184:                 } else {
5185:                     classes[SA[i]] = i;
5186:                 }
5187:             }
5188:             iota(begin(cnt), end(cnt), 0);
5189:             copy(begin(SA), end(SA), begin(c));
5190:             for(int i = 0; i < s.size(); i++) {
5191:                 int s1 = c[i] - len;
5192:                 if(s1 >= 0) SA[cnt[classes[s1]]++] = s1;

```

```

5193:     }
5194:     classes.swap(c);
5195: }
5196: }
5197:
5198: int operator[](int k) const {
5199:     return SA[k];
5200: }
5201:
5202: size_t size() const {
5203:     return s.size();
5204: }
5205:
5206: bool lt_substr(const string &t, int si = 0, int ti = 0) {
5207:     int sn = (int) s.size(), tn = (int) t.size();
5208:     while(si < sn && ti < tn) {
5209:         if(s[si] < t[ti]) return true;
5210:         if(s[si] > t[ti]) return false;
5211:         ++si, ++ti;
5212:     }
5213:     return si >= sn && ti < tn;
5214: }
5215:
5216: int lower_bound(const string &t) {
5217:     int low = -1, high = (int) SA.size();
5218:     while(high - low > 1) {
5219:         int mid = (low + high) / 2;
5220:         if(lt_substr(t, SA[mid])) low = mid;
5221:         else high = mid;
5222:     }
5223:     return high;
5224: }
5225:
5226: pair< int, int > lower_upper_bound(string &t) {
5227:     int idx = lower_bound(t);
5228:     int low = idx - 1, high = (int) SA.size();
5229:     t.back()++;
5230:     while(high - low > 1) {
5231:         int mid = (low + high) / 2;
5232:         if(lt_substr(t, SA[mid])) low = mid;
5233:         else high = mid;
5234:     }
5235:     t.back()--;
5236:     return {idx, high};
5237: }
5238:
5239: void output() {
5240:     for(int i = 0; i < size(); i++) {
5241:         cout << i << ": " << s.substr(SA[i]) << endl;
5242:     }
5243: }
5244: };
5245:
5246:
5247: #####
5248: ##### longest-common-prefix-array.cpp #####
5249: #####
5250:
5251: struct LongestCommonPrefixArray {
5252:     const SuffixArray &SA;
5253:     vector< int > LCP, rank;
5254:
5255:     LongestCommonPrefixArray(const SuffixArray &SA) : SA(SA), LCP(SA.size()) {
5256:         rank.resize(SA.size());
5257:         for(int i = 0; i < SA.size(); i++) {
5258:             rank[SA[i]] = i;
5259:         }
5260:         for(int i = 0, h = 0; i < SA.size(); i++) {
5261:             if(rank[i] + 1 < SA.size()) {
5262:                 for(int j = SA[rank[i] + 1]; max(i, j) + h < SA.size() && SA.s[i + h] == S

```

```

A.s[j + h]; ++h);
5263:         LCP[rank[i] + 1] = h;
5264:         if(h > 0) --h;
5265:     }
5266: }
5267: }
5268:
5269: int operator[](int k) const {
5270:     return LCP[k];
5271: }
5272:
5273: size_t size() const {
5274:     return LCP.size();
5275: }
5276:
5277: void output() {
5278:     for(int i = 0; i < size(); i++) {
5279:         cout << i << ": " << LCP[i] << " " << SA.s.substr(SA[i]) << endl;
5280:     }
5281: }
5282: };
5283:
5284:
5285: #####
5286: ##### z_algorithm.cpp #####
5287: #####
5288:
5289: vector< int > z_algorithm(const string &s) {
5290:     vector< int > prefix(s.size());
5291:     for(int i = 1, j = 0; i < s.size(); i++) {
5292:         if(i + prefix[i - j] < j + prefix[j]) {
5293:             prefix[i] = prefix[i - j];
5294:         } else {
5295:             int k = max(0, j + prefix[j] - i);
5296:             while(i + k < s.size() && s[k] == s[i + k]) ++k;
5297:             prefix[i] = k;
5298:             j = i;
5299:         }
5300:     }
5301:     prefix[0] = (int) s.size();
5302:     return prefix;
5303: }
5304:
5305:
5306: -----
5307: | geometry |
5308: -----
5309:
5310: #####
5311: ##### template.cpp #####
5312: #####
5313:
5314: using Real = double;
5315: using Point = complex< Real >;
5316: const Real EPS = 1e-8, PI = acos(-1);
5317:
5318: inline bool eq(Real a, Real b) { return fabs(b - a) < EPS; }
5319:
5320: Point operator*(const Point &p, const Real &d) {
5321:     return Point(real(p) * d, imag(p) * d);
5322: }
5323:
5324: istream &operator>>(istream &is, Point &p) {
5325:     Real a, b;
5326:     is >> a >> b;
5327:     p = Point(a, b);
5328:     return is;
5329: }
5330:
5331: ostream &operator<<(ostream &os, Point &p) {

```

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```
5332:     return os << fixed << setprecision(10) << p.real() << " " << p.imag();
5333: }
5334:
5335: // rotate point p counterclockwise by theta rad
5336: Point rotate(Real theta, const Point &p) {
5337:     return Point(cos(theta) * p.real() - sin(theta) * p.imag(), sin(theta) * p.real(
) + cos(theta) * p.imag());
5338: }
5339:
5340: Real radian_to_degree(Real r) {
5341:     return (r * 180.0 / PI);
5342: }
5343:
5344: Real degree_to_radian(Real d) {
5345:     return (d * PI / 180.0);
5346: }
5347:
5348: // smaller angle of the a-b-c
5349: Real get_angle(const Point &a, const Point &b, const Point &c) {
5350:     const Point v(b - a), w(c - b);
5351:     Real alpha = atan2(v.imag(), v.real()), beta = atan2(w.imag(), w.real());
5352:     if(alpha > beta) swap(alpha, beta);
5353:     Real theta = (beta - alpha);
5354:     return min(theta, 2 * acos(-1) - theta);
5355: }
5356:
5357: namespace std {
5358:     bool operator<(const Point &a, const Point &b) {
5359:         return a.real() != b.real() ? a.real() < b.real() : a.imag() < b.imag();
5360:     }
5361: }
5362:
5363:
5364: struct Line {
5365:     Point a, b;
5366:
5367:     Line() = default;
5368:
5369:     Line(Point a, Point b) : a(a), b(b) {}
5370:
5371:     Line(Real A, Real B, Real C) // Ax + By = C
5372:     {
5373:         if(eq(A, 0)) a = Point(0, C / B), b = Point(1, C / B);
5374:         else if(eq(B, 0)) b = Point(C / A, 0), a = Point(C / A, 1);
5375:         else a = Point(0, C / B), b = Point(C / A, 0);
5376:     }
5377:
5378:     friend ostream &operator<<(ostream &os, Line &p) {
5379:         return os << p.a << " to " << p.b;
5380:     }
5381:
5382:     friend istream &operator>>(istream &is, Line &a) {
5383:         return is >> a.a >> a.b;
5384:     }
5385: };
5386:
5387: struct Segment : Line {
5388:     Segment() = default;
5389:
5390:     Segment(Point a, Point b) : Line(a, b) {}
5391: };
5392:
5393: struct Circle {
5394:     Point p;
5395:     Real r;
5396:
5397:     Circle() = default;
5398:
5399:     Circle(Point p, Real r) : p(p), r(r) {}
5400: };
```

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```
5401:
5402: using Points = vector< Point >;
5403: using Polygon = vector< Point >;
5404: using Segments = vector< Segment >;
5405: using Lines = vector< Line >;
5406: using Circles = vector< Circle >;
5407:
5408: Real cross(const Point &a, const Point &b) {
5409:     return real(a) * imag(b) - imag(a) * real(b);
5410: }
5411:
5412: Real dot(const Point &a, const Point &b) {
5413:     return real(a) * real(b) + imag(a) * imag(b);
5414: }
5415:
5416: // http://judge.u-aizu.ac.jp/onlinejudge/description.jsp?id=CGL_1_C
5417: int ccw(const Point &a, Point b, Point c) {
5418:     b = b - a, c = c - a;
5419:     if(cross(b, c) > EPS) return +1; // "COUNTER_CLOCKWISE"
5420:     if(cross(b, c) < -EPS) return -1; // "CLOCKWISE"
5421:     if(dot(b, c) < 0) return +2; // "ONLINE_BACK" c-a-b
5422:     if(norm(b) < norm(c)) return -2; // "ONLINE_FRONT" a-b-c
5423:     return 0; // "ON_SEGMENT" a-c-b
5424: }
5425:
5426: // http://judge.u-aizu.ac.jp/onlinejudge/description.jsp?id=CGL_2_A
5427: bool parallel(const Line &a, const Line &b) {
5428:     return eq(cross(a.b - a.a, b.b - b.a), 0.0);
5429: }
5430:
5431: // http://judge.u-aizu.ac.jp/onlinejudge/description.jsp?id=CGL_2_A
5432: bool orthogonal(const Line &a, const Line &b) {
5433:     return eq(dot(a.a - a.b, b.a - b.b), 0.0);
5434: }
5435:
5436: // http://judge.u-aizu.ac.jp/onlinejudge/description.jsp?id=CGL_1_A
5437: Point projection(const Line &l, const Point &p) {
5438:     double t = dot(p - l.a, l.a - l.b) / norm(l.a - l.b);
5439:     return l.a + (l.a - l.b) * t;
5440: }
5441:
5442: Point projection(const Segment &l, const Point &p) {
5443:     double t = dot(p - l.a, l.a - l.b) / norm(l.a - l.b);
5444:     return l.a + (l.a - l.b) * t;
5445: }
5446:
5447: // http://judge.u-aizu.ac.jp/onlinejudge/description.jsp?id=CGL_1_B
5448: Point reflection(const Line &l, const Point &p) {
5449:     return p + (projection(l, p) - p) * 2.0;
5450: }
5451:
5452: bool intersect(const Line &l, const Point &p) {
5453:     return abs(ccw(l.a, l.b, p)) != 1;
5454: }
5455:
5456: bool intersect(const Line &l, const Line &m) {
5457:     return abs(cross(l.b - l.a, m.b - m.a)) > EPS || abs(cross(l.b - l.a, m.b - l.a)
) < EPS;
5458: }
5459:
5460: bool intersect(const Segment &s, const Point &p) {
5461:     return ccw(s.a, s.b, p) == 0;
5462: }
5463:
5464: bool intersect(const Line &l, const Segment &s) {
5465:     return cross(l.b - l.a, s.a - l.a) * cross(l.b - l.a, s.b - l.a) < EPS;
5466: }
5467:
5468: Real distance(const Line &l, const Point &p);
5469:
```

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```
5470: bool intersect(const Circle &c, const Line &l) {
5471:     return distance(l, c.p) <= c.r + EPS;
5472: }
5473:
5474: bool intersect(const Circle &c, const Point &p) {
5475:     return abs(abs(p - c.p) - c.r) < EPS;
5476: }
5477:
5478: // http://judge.u-aizu.ac.jp/onlinejudge/description.jsp?id=CGL_2_B
5479: bool intersect(const Segment &s, const Segment &t) {
5480:     return ccw(s.a, s.b, t.a) * ccw(s.a, s.b, t.b) <= 0 && ccw(t.a, t.b, s.a) * ccw(
t.a, t.b, s.b) <= 0;
5481: }
5482:
5483: int intersect(const Circle &c, const Segment &l) {
5484:     if(norm(projection(l, c.p) - c.p) - c.r * c.r > EPS) return 0;
5485:     auto d1 = abs(c.p - l.a), d2 = abs(c.p - l.b);
5486:     if(d1 < c.r + EPS && d2 < c.r + EPS) return 0;
5487:     if(d1 < c.r - EPS && d2 > c.r + EPS || d1 > c.r + EPS && d2 < c.r - EPS) return
1;
5488:     const Point h = projection(l, c.p);
5489:     if(dot(l.a - h, l.b - h) < 0) return 2;
5490:     return 0;
5491: }
5492:
5493: // http://judge.u-aizu.ac.jp/onlinejudge/description.jsp?id=CGL_7_A&lang=jp
5494: int intersect(Circle c1, Circle c2) {
5495:     if(c1.r < c2.r) swap(c1, c2);
5496:     Real d = abs(c1.p - c2.p);
5497:     if(c1.r + c2.r < d) return 4;
5498:     if(eq(c1.r + c2.r, d)) return 3;
5499:     if(c1.r - c2.r < d) return 2;
5500:     if(eq(c1.r - c2.r, d)) return 1;
5501:     return 0;
5502: }
5503:
5504: Real distance(const Point &a, const Point &b) {
5505:     return abs(a - b);
5506: }
5507:
5508: Real distance(const Line &l, const Point &p) {
5509:     return abs(p - projection(l, p));
5510: }
5511:
5512: Real distance(const Line &l, const Line &m) {
5513:     return intersect(l, m) ? 0 : distance(l, m.a);
5514: }
5515:
5516: Real distance(const Segment &s, const Point &p) {
5517:     Point r = projection(s, p);
5518:     if(intersect(s, r)) return abs(r - p);
5519:     return min(abs(s.a - p), abs(s.b - p));
5520: }
5521:
5522: // http://judge.u-aizu.ac.jp/onlinejudge/description.jsp?id=CGL_2_D
5523: Real distance(const Segment &a, const Segment &b) {
5524:     if(intersect(a, b)) return 0;
5525:     return min({distance(a, b.a), distance(a, b.b), distance(b, a.a), distance(b, a.
b)});
5526: }
5527:
5528: Real distance(const Line &l, const Segment &s) {
5529:     if(intersect(l, s)) return 0;
5530:     return min(distance(l, s.a), distance(l, s.b));
5531: }
5532:
5533: Point crosspoint(const Line &l, const Line &m) {
5534:     Real A = cross(l.b - l.a, m.b - m.a);
5535:     Real B = cross(l.b - l.a, l.b - m.a);
5536:     if(eq(abs(A), 0.0) && eq(abs(B), 0.0)) return m.a;
```



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```
5537:     return m.a + (m.b - m.a) * B / A;
5538: }
5539:
5540: // http://judge.u-aizu.ac.jp/onlinejudge/description.jsp?id=CGL_2_C
5541: Point crosspoint(const Segment &l, const Segment &m) {
5542:     return crosspoint(Line(l), Line(m));
5543: }
5544:
5545: // http://judge.u-aizu.ac.jp/onlinejudge/description.jsp?id=CGL_7_D
5546: pair< Point, Point > crosspoint(const Circle &c, const Line l) {
5547:     Point pr = projection(l, c.p);
5548:     Point e = (l.b - l.a) / abs(l.b - l.a);
5549:     if(eq(distance(l, c.p), c.r)) return {pr, pr};
5550:     double base = sqrt(c.r * c.r - norm(pr - c.p));
5551:     return {pr - e * base, pr + e * base};
5552: }
5553:
5554: pair< Point, Point > crosspoint(const Circle &c, const Segment &l) {
5555:     Line aa = Line(l.a, l.b);
5556:     if(intersect(c, l) == 2) return crosspoint(c, aa);
5557:     auto ret = crosspoint(c, aa);
5558:     if(dot(l.a - ret.first, l.b - ret.first) < 0) ret.second = ret.first;
5559:     else ret.first = ret.second;
5560:     return ret;
5561: }
5562:
5563: // http://judge.u-aizu.ac.jp/onlinejudge/description.jsp?id=CGL_7_E
5564: pair< Point, Point > crosspoint(const Circle &c1, const Circle &c2) {
5565:     Real d = abs(c1.p - c2.p);
5566:     Real a = acos((c1.r * c1.r + d * d - c2.r * c2.r) / (2 * c1.r * d));
5567:     Real t = atan2(c2.p.imag() - c1.p.imag(), c2.p.real() - c1.p.real());
5568:     Point p1 = c1.p + Point(cos(t + a) * c1.r, sin(t + a) * c1.r);
5569:     Point p2 = c1.p + Point(cos(t - a) * c1.r, sin(t - a) * c1.r);
5570:     return {p1, p2};
5571: }
5572:
5573: // http://judge.u-aizu.ac.jp/onlinejudge/description.jsp?id=CGL_7_F
5574: // tangent of circle c through point p
5575: pair< Point, Point > tangent(const Circle &c1, const Point &p2) {
5576:     return crosspoint(c1, Circle(p2, sqrt(norm(c1.p - p2) - c1.r * c1.r)));
5577: }
5578:
5579: // http://judge.u-aizu.ac.jp/onlinejudge/description.jsp?id=CGL_7_G
5580: // common tangent of circles c1 and c2
5581: Lines tangent(Circle c1, Circle c2) {
5582:     Lines ret;
5583:     if(c1.r < c2.r) swap(c1, c2);
5584:     Real g = norm(c1.p - c2.p);
5585:     if(eq(g, 0)) return ret;
5586:     Point u = (c2.p - c1.p) / sqrt(g);
5587:     Point v = rotate(PI * 0.5, u);
5588:     for(int s : {-1, 1}) {
5589:         Real h = (c1.r + s * c2.r) / sqrt(g);
5590:         if(eq(1 - h * h, 0)) {
5591:             ret.emplace_back(c1.p + u * c1.r, c1.p + (u + v) * c1.r);
5592:         } else if(1 - h * h > 0) {
5593:             Point uu = u * h, vv = v * sqrt(1 - h * h);
5594:             ret.emplace_back(c1.p + (uu + vv) * c1.r, c2.p - (uu + vv) * c2.r * s);
5595:             ret.emplace_back(c1.p + (uu - vv) * c1.r, c2.p - (uu - vv) * c2.r * s);
5596:         }
5597:     }
5598:     return ret;
5599: }
5600:
5601: // http://judge.u-aizu.ac.jp/onlinejudge/description.jsp?id=CGL_3_B
5602: bool is_convex(const Polygon &p) {
5603:     int n = (int) p.size();
5604:     for(int i = 0; i < n; i++) {
5605:         if(ccw(p[(i + n - 1) % n], p[i], p[(i + 1) % n]) == -1) return false;
5606:     }
}
```

```

5607:     return true;
5608: }
5609:
5610: // http://judge.u-aizu.ac.jp/onlinejudge/description.jsp?id=CGL\_4\_A
5611: Polygon convex_hull(Polygon &p) {
5612:     int n = (int) p.size(), k = 0;
5613:     if(n <= 2) return p;
5614:     sort(p.begin(), p.end());
5615:     vector< Point > ch(2 * n);
5616:     for(int i = 0; i < n; ch[k++] = p[i++]) {
5617:         while(k >= 2 && cross(ch[k - 1] - ch[k - 2], p[i] - ch[k - 1]) < EPS) --k;
5618:     }
5619:     for(int i = n - 2, t = k + 1; i >= 0; ch[k++] = p[i--]) {
5620:         while(k >= t && cross(ch[k - 1] - ch[k - 2], p[i] - ch[k - 1]) < EPS) --k;
5621:     }
5622:     ch.resize(k - 1);
5623:     return ch;
5624: }
5625:
5626: // http://judge.u-aizu.ac.jp/onlinejudge/description.jsp?id=CGL\_3\_C
5627: enum {
5628:     OUT, ON, IN
5629: };
5630:
5631: int contains(const Polygon &Q, const Point &p) {
5632:     bool in = false;
5633:     for(int i = 0; i < Q.size(); i++) {
5634:         Point a = Q[i] - p, b = Q[(i + 1) % Q.size()] - p;
5635:         if(a.imag() > b.imag()) swap(a, b);
5636:         if(a.imag() <= 0 && 0 < b.imag() && cross(a, b) < 0) in = !in;
5637:         if(cross(a, b) == 0 && dot(a, b) <= 0) return ON;
5638:     }
5639:     return in ? IN : OUT;
5640: }
5641:
5642:
5643: // http://judge.u-aizu.ac.jp/onlinejudge/description.jsp?id=1033
5644: // deduplication of line segments
5645: void merge_segments(vector< Segment > &segs) {
5646:
5647:     auto merge_if_able = [](Segment &s1, const Segment &s2) {
5648:         if(abs(cross(s1.b - s1.a, s2.b - s2.a)) > EPS) return false;
5649:         if(ccw(s1.a, s2.a, s1.b) == 1 || ccw(s1.a, s2.a, s1.b) == -1) return false;
5650:         if(ccw(s1.a, s1.b, s2.a) == -2 || ccw(s2.a, s2.b, s1.a) == -2) return false;
5651:         s1 = Segment(min(s1.a, s2.a), max(s1.b, s2.b));
5652:         return true;
5653:     };
5654:
5655:     for(int i = 0; i < segs.size(); i++) {
5656:         if(segs[i].b < segs[i].a) swap(segs[i].a, segs[i].b);
5657:     }
5658:     for(int i = 0; i < segs.size(); i++) {
5659:         for(int j = i + 1; j < segs.size(); j++) {
5660:             if(merge_if_able(segs[i], segs[j])) {
5661:                 segs[j--] = segs.back(), segs.pop_back();
5662:             }
5663:         }
5664:     }
5665: }
5666:
5667: // http://judge.u-aizu.ac.jp/onlinejudge/description.jsp?id=1033
5668: // construct a graph with the vertex of the intersection of any two line segments
5669: vector< vector< int > > segment_arrangement(vector< Segment > &segs, vector< Point
> &ps) {
5670:     vector< vector< int > > g;
5671:     int N = (int) segs.size();
5672:     for(int i = 0; i < N; i++) {
5673:         ps.emplace_back(segs[i].a);
5674:         ps.emplace_back(segs[i].b);
5675:         for(int j = i + 1; j < N; j++) {

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```
5676:     const Point p1 = segs[i].b - segs[i].a;
5677:     const Point p2 = segs[j].b - segs[j].a;
5678:     if(cross(p1, p2) == 0) continue;
5679:     if(intersect(segs[i], segs[j])) {
5680:         ps.emplace_back(crosspoint(segs[i], segs[j]));
5681:     }
5682: }
5683: }
5684: sort(begin(ps), end(ps));
5685: ps.erase(unique(begin(ps), end(ps)), end(ps));
5686:
5687: int M = (int) ps.size();
5688: g.resize(M);
5689: for(int i = 0; i < N; i++) {
5690:     vector< int > vec;
5691:     for(int j = 0; j < M; j++) {
5692:         if(intersect(segs[i], ps[j])) {
5693:             vec.emplace_back(j);
5694:         }
5695:     }
5696:     for(int j = 1; j < vec.size(); j++) {
5697:         g[vec[j] - 1].push_back(vec[j]);
5698:         g[vec[j]].push_back(vec[j] - 1);
5699:     }
5700: }
5701: return (g);
5702: }
5703:
5704: // http://judge.u-aizu.ac.jp/onlinejudge/description.jsp?id=CGL_4_C
5705: // cut with a straight line l and return a convex polygon on the left
5706: Polygon convex_cut(const Polygon &U, Line l) {
5707:     Polygon ret;
5708:     for(int i = 0; i < U.size(); i++) {
5709:         Point now = U[i], nxt = U[(i + 1) % U.size()];
5710:         if(ccw(l.a, l.b, now) != -1) ret.push_back(now);
5711:         if(ccw(l.a, l.b, now) * ccw(l.a, l.b, nxt) < 0) {
5712:             ret.push_back(crosspoint(Line(now, nxt), l));
5713:         }
5714:     }
5715:     return (ret);
5716: }
5717:
5718: // http://judge.u-aizu.ac.jp/onlinejudge/description.jsp?id=CGL_3_A
5719: Real area(const Polygon &p) {
5720:     Real A = 0;
5721:     for(int i = 0; i < p.size(); ++i) {
5722:         A += cross(p[i], p[(i + 1) % p.size()]);
5723:     }
5724:     return A * 0.5;
5725: }
5726:
5727: // http://judge.u-aizu.ac.jp/onlinejudge/description.jsp?id=CGL_7_H
5728: Real area(const Polygon &p, const Circle &c) {
5729:     if(p.size() < 3) return 0.0;
5730:     function< Real(Circle, Point, Point) > cross_area = [&](const Circle &c, const P
oint &a, const Point &b) {
5731:         Point va = c.p - a, vb = c.p - b;
5732:         Real f = cross(va, vb), ret = 0.0;
5733:         if(eq(f, 0.0)) return ret;
5734:         if(max(abs(va), abs(vb)) < c.r + EPS) return f;
5735:         if(distance(Segment(a, b), c.p) > c.r - EPS) return c.r * c.r * arg(vb * conj(
va));
5736:         auto u = crosspoint(c, Segment(a, b));
5737:         vector< Point > tot{a, u.first, u.second, b};
5738:         for(int i = 0; i + 1 < tot.size(); i++) {
5739:             ret += cross_area(c, tot[i], tot[i + 1]);
5740:         }
5741:         return ret;
5742:     };
5743:     Real A = 0;
```

```

5744:     for(int i = 0; i < p.size(); i++) {
5745:         A += cross_area(c, p[i], p[(i + 1) % p.size()]);
5746:     }
5747:     return A;
5748: }
5749:
5750: // http://judge.u-aizu.ac.jp/onlinejudge/description.jsp?id=CGL\_4\_B
5751: Real convex_diameter(const Polygon &p) {
5752:     int N = (int) p.size();
5753:     int is = 0, js = 0;
5754:     for(int i = 1; i < N; i++) {
5755:         if(p[i].imag() > p[is].imag()) is = i;
5756:         if(p[i].imag() < p[js].imag()) js = i;
5757:     }
5758:     Real maxdis = norm(p[is] - p[js]);
5759:
5760:     int maxi, maxj, i, j;
5761:     i = maxi = is;
5762:     j = maxj = js;
5763:     do {
5764:         if(cross(p[(i + 1) % N] - p[i], p[(j + 1) % N] - p[j]) >= 0) {
5765:             j = (j + 1) % N;
5766:         } else {
5767:             i = (i + 1) % N;
5768:         }
5769:         if(norm(p[i] - p[j]) > maxdis) {
5770:             maxdis = norm(p[i] - p[j]);
5771:             maxi = i;
5772:             maxj = j;
5773:         }
5774:     } while(i != is || j != js);
5775:     return sqrt(maxdis);
5776: }
5777:
5778: // http://judge.u-aizu.ac.jp/onlinejudge/description.jsp?id=CGL\_5\_A
5779: Real closest_pair(Points ps) {
5780:     if(ps.size() <= 1) throw (0);
5781:     sort(begin(ps), end(ps));
5782:
5783:     auto compare_y = [&](const Point &a, const Point &b) {
5784:         return imag(a) < imag(b);
5785:     };
5786:     vector< Point > beet(ps.size());
5787:     const Real INF = 1e18;
5788:
5789:     function< Real(int, int) > rec = [&](int left, int right) {
5790:         if(right - left <= 1) return INF;
5791:         int mid = (left + right) >> 1;
5792:         auto x = real(ps[mid]);
5793:         auto ret = min(rec(left, mid), rec(mid, right));
5794:         inplace_merge(begin(ps) + left, begin(ps) + mid, begin(ps) + right, compare_y)
;
5795:         int ptr = 0;
5796:         for(int i = left; i < right; i++) {
5797:             if(abs(real(ps[i]) - x) >= ret) continue;
5798:             for(int j = 0; j < ptr; j++) {
5799:                 auto luz = ps[i] - beet[ptr - j - 1];
5800:                 if(imag(luz) >= ret) break;
5801:                 ret = min(ret, abs(luz));
5802:             }
5803:             beet[ptr++] = ps[i];
5804:         }
5805:         return ret;
5806:     };
5807:     return rec(0, (int) ps.size());
5808: }
5809:
5810:
5811: -----
5812: |                                     structure                                     |

```

```

5813: -----
5814:
5815: #####
5816: ##### convex-hull-trick-add-monotone.cpp #####
5817: #####
5818:
5819: template< typename T, bool isMin >
5820: struct ConvexHullTrickAddMonotone {
5821: #define F first
5822: #define S second
5823:     using P = pair< T, T >;
5824:     deque< P > H;
5825:
5826:     ConvexHullTrickAddMonotone() = default;
5827:
5828:     bool empty() const { return H.empty(); }
5829:
5830:     void clear() { H.clear(); }
5831:
5832:     inline int sgn(T x) { return x == 0 ? 0 : (x < 0 ? -1 : 1); }
5833:
5834:     using D = long double;
5835:
5836:     inline bool check(const P &a, const P &b, const P &c) {
5837:         if(b.S == a.S || c.S == b.S)
5838:             return sgn(b.F - a.F) * sgn(c.S - b.S) >= sgn(c.F - b.F) * sgn(b.S - a.S);
5839:
5840:         //return (b.F-a.F)*(c.S-b.S) >= (b.S-a.S)*(c.F-b.F);
5841:         return
5842:             D(b.F - a.F) * sgn(c.S - b.S) / D(abs(b.S - a.S)) >=
5843:             D(c.F - b.F) * sgn(b.S - a.S) / D(abs(c.S - b.S));
5844:     }
5845:
5846:     void add(T a, T b) {
5847:         if(!isMin) a *= -1, b *= -1;
5848:         P line(a, b);
5849:         if(empty()) {
5850:             H.emplace_front(line);
5851:             return;
5852:         }
5853:         if(H.front().F <= a) {
5854:             if(H.front().F == a) {
5855:                 if(H.front().S <= b) return;
5856:                 H.pop_front();
5857:             }
5858:             while(H.size() >= 2 && check(line, H.front(), H[1])) H.pop_front();
5859:             H.emplace_front(line);
5860:         } else {
5861:             assert(a <= H.back().F);
5862:             if(H.back().F == a) {
5863:                 if(H.back().S <= b) return;
5864:                 H.pop_back();
5865:             }
5866:             while(H.size() >= 2 && check(H[H.size() - 2], H.back(), line)) H.pop_back();
5867:             H.emplace_back(line);
5868:         }
5869:     }
5870:
5871:     inline T get_y(const P &a, const T &x) {
5872:         return a.F * x + a.S;
5873:     }
5874:
5875:     T query(T x) {
5876:         assert(!empty());
5877:         int l = -1, r = H.size() - 1;
5878:         while(l + 1 < r) {
5879:             int m = (l + r) >> 1;
5880:             if(get_y(H[m], x) >= get_y(H[m + 1], x)) l = m;
5881:             else r = m;
5882:         }

```

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```
5883:     if(isMin) return get_y(H[r], x);
5884:     return -get_y(H[r], x);
5885: }
5886:
5887: T query_monotone_inc(T x) {
5888:     assert(!empty());
5889:     while(H.size() >= 2 && get_y(H.front(), x) >= get_y(H[1], x)) H.pop_front();
5890:     if(isMin) return get_y(H.front(), x);
5891:     return -get_y(H.front(), x);
5892: }
5893:
5894: T query_monotone_dec(T x) {
5895:     assert(!empty());
5896:     while(H.size() >= 2 && get_y(H.back(), x) >= get_y(H[H.size() - 2], x)) H.pop_
back();
5897:     if(isMin) return get_y(H.back(), x);
5898:     return -get_y(H.back(), x);
5899: }
5900:
5901: #undef F
5902: #undef S
5903: };
5904:
5905:
5906: #####
5907: ##### skew-heap.cpp #####
5908: #####
5909:
5910: template< typename T, typename E = T >
5911: struct SkewHeap {
5912:     using G = function< T(T, E) >;
5913:     using H = function< E(E, E) >;
5914:
5915:     struct Node {
5916:         T key;
5917:         E lazy;
5918:         Node *l, *r;
5919:     };
5920:
5921:     const bool rev;
5922:     const G g;
5923:     const H h;
5924:
5925:     SkewHeap(bool rev = false) : g([](const T &a, const E &b) { return a + b; }),
5926:                                h([](const E &a, const E &b) { return a + b; }), re
v(rev) {}
5927:
5928:     SkewHeap(const G &g, const H &h, bool rev = false) : g(g), h(h), rev(rev) {}
5929:
5930:     Node *propagate(Node *t) {
5931:         if(t->lazy != 0) {
5932:             if(t->l) t->l->lazy = h(t->l->lazy, t->lazy);
5933:             if(t->r) t->r->lazy = h(t->r->lazy, t->lazy);
5934:             t->key = g(t->key, t->lazy);
5935:             t->lazy = 0;
5936:         }
5937:         return t;
5938:     }
5939:
5940:     Node *merge(Node *x, Node *y) {
5941:         if(!x || !y) return x ? x : y;
5942:         propagate(x), propagate(y);
5943:         if((x->key > y->key) ^ rev) swap(x, y);
5944:         x->r = merge(y, x->r);
5945:         swap(x->l, x->r);
5946:         return x;
5947:     }
5948:
5949:     void push(Node *&root, const T &key) {
5950:         root = merge(root, new Node({key, 0, nullptr, nullptr}));
```

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```
5951:     }
5952:
5953:     T top(Node *root) {
5954:         return propagate(root)->key;
5955:     }
5956:
5957:     T pop(Node *&root) {
5958:         T top = propagate(root)->key;
5959:         auto *temp = root;
5960:         root = merge(root->l, root->r);
5961:         delete temp;
5962:         return top;
5963:     }
5964:
5965:     bool empty(Node *root) const {
5966:         return !root;
5967:     }
5968:
5969:     void add(Node *root, const E &lazy) {
5970:         if(root) {
5971:             root->lazy = h(root->lazy, lazy);
5972:             propagate(root);
5973:         }
5974:     }
5975:
5976:     Node *makeheap() {
5977:         return nullptr;
5978:     }
5979: };
5980:
5981:
5982: #####
5983: ##### segment-tree-2d-2.cpp #####
5984: #####
5985:
5986: template< typename structure_t, typename get_t, typename update_t >
5987: struct SegmentTree2D {
5988:     using merge_f = function< get_t(get_t, get_t) >;
5989:     using get_t = function< get_t(structure_t &, int) >;
5990:     using range_update_f = function< get_t(structure_t &, int, int, update_t) >;
5991:
5992:     int sz;
5993:     vector< structure_t > seg;
5994:     const merge_f &f;
5995:     const get_t &g;
5996:     const range_update_f &h;
5997:
5998:     SegmentTree2D(int n, const merge_f &f, const get_t &g, const range_update_f &h)
: f(f), g(g), h(h) {
5999:         sz = 1;
6000:         while(sz < n) sz <= 1;
6001:         seg.resize(2 * sz - 1);
6002:     }
6003:
6004:     void update(int a, int b, int lower, int upper, update_t x, int k, int l, int r)
{
6005:         if(r <= a || b <= l) {
6006:             return;
6007:         } else if(a <= l && r <= b) {
6008:             g(seg[k], lower, upper, x);
6009:         } else {
6010:             update(a, b, lower, upper, x, 2 * k + 1, l, (l + r) >> 1);
6011:             update(a, b, lower, upper, x, 2 * k + 2, (l + r) >> 1, r);
6012:         }
6013:     }
6014:
6015:     void update(int a, int b, int l, int r, update_t x) {
6016:         update(a, b, l, r, x, 0, 0, sz);
6017:     }
6018:
```

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```
6019: get_t get(int x, int y) {
6020:     x += sz - 1;
6021:     get_t ret = g(seg[x], y);
6022:     while(x > 0) {
6023:         x = (x - 1) >> 1;
6024:         ret = f(ret, g(seg[x], y));
6025:     }
6026: }
6027: };
6028:
6029:
6030: #####
6031: ##### lazy-segment-tree.cpp #####
6032: #####
6033:
6034: template< typename Monoid, typename OperatorMonoid = Monoid >
6035: struct LazySegmentTree {
6036:     using F = function< Monoid(Monoid, Monoid) >;
6037:     using G = function< Monoid(Monoid, OperatorMonoid) >;
6038:     using H = function< OperatorMonoid(OperatorMonoid, OperatorMonoid) >;
6039:
6040:     int sz, height;
6041:     vector< Monoid > data;
6042:     vector< OperatorMonoid > lazy;
6043:     const F f;
6044:     const G g;
6045:     const H h;
6046:     const Monoid M1;
6047:     const OperatorMonoid OM0;
6048:
6049:
6050:     LazySegmentTree(int n, const F f, const G g, const H h,
6051:                     const Monoid &M1, const OperatorMonoid OM0)
6052:         : f(f), g(g), h(h), M1(M1), OM0(OM0) {
6053:         sz = 1;
6054:         height = 0;
6055:         while(sz < n) sz <= 1, height++;
6056:         data.assign(2 * sz, M1);
6057:         lazy.assign(2 * sz, OM0);
6058:     }
6059:
6060:     void set(int k, const Monoid &x) {
6061:         data[k + sz] = x;
6062:     }
6063:
6064:     void build() {
6065:         for(int k = sz - 1; k > 0; k--) {
6066:             data[k] = f(data[2 * k + 0], data[2 * k + 1]);
6067:         }
6068:     }
6069:
6070:     inline void propagate(int k) {
6071:         if(lazy[k] != OM0) {
6072:             lazy[2 * k + 0] = h(lazy[2 * k + 0], lazy[k]);
6073:             lazy[2 * k + 1] = h(lazy[2 * k + 1], lazy[k]);
6074:             data[k] = reflect(k);
6075:             lazy[k] = OM0;
6076:         }
6077:     }
6078:
6079:     inline Monoid reflect(int k) {
6080:         return lazy[k] == OM0 ? data[k] : g(data[k], lazy[k]);
6081:     }
6082:
6083:     inline void recalc(int k) {
6084:         while(k >= 1) data[k] = f(reflect(2 * k + 0), reflect(2 * k + 1));
6085:     }
6086:
6087:     inline void thrust(int k) {
6088:         for(int i = height; i > 0; i--) propagate(k >> i);
```



```

6089:     }
6090:
6091: void update(int a, int b, const OperatorMonoid &x) {
6092:     thrust(a += sz);
6093:     thrust(b += sz - 1);
6094:     for(int l = a, r = b + 1; l < r; l >>= 1, r >>= 1) {
6095:         if(l & 1) lazy[l] = h(lazy[l], x), ++l;
6096:         if(r & 1) --r, lazy[r] = h(lazy[r], x);
6097:     }
6098:     recalc(a);
6099:     recalc(b);
6100: }
6101:
6102: Monoid query(int a, int b) {
6103:     thrust(a += sz);
6104:     thrust(b += sz - 1);
6105:     Monoid L = M1, R = M1;
6106:     for(int l = a, r = b + 1; l < r; l >>= 1, r >>= 1) {
6107:         if(l & 1) L = f(L, reflect(l++));
6108:         if(r & 1) R = f(reflect(--r), R);
6109:     }
6110:     return f(L, R);
6111: }
6112:
6113: Monoid operator[](const int &k) {
6114:     return query(k, k + 1);
6115: }
6116:
6117: template< typename C >
6118: int find_subtree(int a, const C &check, Monoid &M, bool type) {
6119:     while(a < sz) {
6120:         propagate(a);
6121:         Monoid nxt = type ? f(reflect(2 * a + type), M) : f(M, reflect(2 * a + type)
);
6122:         if(check(nxt)) a = 2 * a + type;
6123:         else M = nxt, a = 2 * a + 1 - type;
6124:     }
6125:     return a - sz;
6126: }
6127:
6128: template< typename C >
6129: int find_first(int a, const C &check) {
6130:     Monoid L = M1;
6131:     if(a <= 0) {
6132:         if(check(f(L, reflect(1)))) return find_subtree(1, check, L, false);
6133:         return -1;
6134:     }
6135:     thrust(a + sz);
6136:     int b = sz;
6137:     for(a += sz, b += sz; a < b; a >>= 1, b >>= 1) {
6138:         if(a & 1) {
6139:             Monoid nxt = f(L, reflect(a));
6140:             if(check(nxt)) return find_subtree(a, check, L, false);
6141:             L = nxt;
6142:             ++a;
6143:         }
6144:     }
6145:     return -1;
6146: }
6147:
6148:
6149: template< typename C >
6150: int find_last(int b, const C &check) {
6151:     Monoid R = M1;
6152:     if(b >= sz) {
6153:         if(check(f(reflect(1), R))) return find_subtree(1, check, R, true);
6154:         return -1;
6155:     }
6156:     thrust(b + sz - 1);
6157:     int a = sz;

```

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```
6158:     for(b += sz; a < b; a >>= 1, b >>= 1) {
6159:         if(b & 1) {
6160:             Monoid nxt = f(reflect(--b), R);
6161:             if(check(nxt)) return find_subtree(b, check, R, true);
6162:             R = nxt;
6163:         }
6164:     }
6165:     return -1;
6166: }
6167: };
6168:
6169:
6170: #####
6171: ##### partially-persistent-union-find.cpp #####
6172: #####
6173:
6174: struct PartiallyPersistentUnionFind {
6175:     vector< int > data;
6176:     vector< int > last;
6177:     vector< vector< pair< int, int > > > add;
6178:
6179:     PartiallyPersistentUnionFind() {}
6180:
6181:     PartiallyPersistentUnionFind(int sz) : data(sz, -1), last(sz, 1e9), add(sz) {
6182:         for(auto &vs : add) vs.emplace_back(-1, -1);
6183:     }
6184:
6185:     bool unite(int t, int x, int y) {
6186:         x = find(t, x);
6187:         y = find(t, y);
6188:         if(x == y) return false;
6189:         if(data[x] > data[y]) swap(x, y);
6190:         data[x] += data[y];
6191:         add[x].emplace_back(t, data[x]);
6192:         data[y] = x;
6193:         last[y] = t;
6194:         return true;
6195:     }
6196:
6197:     int find(int t, int x) {
6198:         if(t < last[x]) return x;
6199:         return find(t, data[x]);
6200:     }
6201:
6202:     int size(int t, int x) {
6203:         x = find(t, x);
6204:         return -prev(lower_bound(begin(add[x]), end(add[x]), make_pair(t, 0)))->second
;
6205:     }
6206: };
6207:
6208:
6209: #####
6210: ##### binary-indexed-tree.cpp #####
6211: #####
6212:
6213: template< typename T >
6214: struct BinaryIndexedTree {
6215:     vector< T > data;
6216:
6217:     BinaryIndexedTree(int sz) {
6218:         data.assign(++sz, 0);
6219:     }
6220:
6221:     T sum(int k) {
6222:         T ret = 0;
6223:         for(++k; k > 0; k -= k & -k) ret += data[k];
6224:         return (ret);
6225:     }
6226: }
```

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```
6227: void add(int k, T x) {
6228:     for(++k; k < data.size(); k += k & -k) data[k] += x;
6229: }
6230: };
6231:
6232:
6233: #####
6234: ##### union-find.cpp #####
6235: #####
6236:
6237: struct UnionFind {
6238:     vector< int > data;
6239:
6240:     UnionFind(int sz) {
6241:         data.assign(sz, -1);
6242:     }
6243:
6244:     bool unite(int x, int y) {
6245:         x = find(x), y = find(y);
6246:         if(x == y) return (false);
6247:         if(data[x] > data[y]) swap(x, y);
6248:         data[x] += data[y];
6249:         data[y] = x;
6250:         return (true);
6251:     }
6252:
6253:     int find(int k) {
6254:         if(data[k] < 0) return (k);
6255:         return (data[k] = find(data[k]));
6256:     }
6257:
6258:     int size(int k) {
6259:         return (-data[find(k)]);
6260:     }
6261: };
6262:
6263:
6264: #####
6265: ##### link-cut-tree-subtree.cpp #####
6266: #####
6267:
6268: template< typename SUM, typename KEY >
6269: struct LinkCutTreeSubtree {
6270:
6271:     struct Node {
6272:         Node *l, *r, *p;
6273:
6274:         KEY key;
6275:         SUM sum;
6276:
6277:         bool rev;
6278:         int sz;
6279:
6280:         bool is_root() const {
6281:             return !p || (p->l != this && p->r != this);
6282:         }
6283:
6284:         Node(const KEY &key, const SUM &sum) :
6285:             key(key), sum(sum), rev(false), sz(1),
6286:             l(nullptr), r(nullptr), p(nullptr) {}
6287:     };
6288:
6289:     const SUM ident;
6290:
6291:     LinkCutTreeSubtree(const SUM &ident) : ident(ident) {}
6292:
6293:     Node *make_node(const KEY &key) {
6294:         auto ret = new Node(key, ident);
6295:         update(ret);
6296:         return ret;
```

```

6297:     }
6298:
6299: Node *set_key(Node *t, const KEY &key) {
6300:     expose(t);
6301:     t->key = key;
6302:     update(t);
6303:     return t;
6304: }
6305:
6306: void toggle(Node *t) {
6307:     swap(t->l, t->r);
6308:     t->sum.toggle();
6309:     t->rev ^= true;
6310: }
6311:
6312: void push(Node *t) {
6313:     if(t->rev) {
6314:         if(t->l) toggle(t->l);
6315:         if(t->r) toggle(t->r);
6316:         t->rev = false;
6317:     }
6318: }
6319:
6320:
6321: void update(Node *t) {
6322:     t->sz = 1;
6323:     if(t->l) t->sz += t->l->sz;
6324:     if(t->r) t->sz += t->r->sz;
6325:     t->sum.merge(t->key, t->l ? t->l->sum : ident, t->r ? t->r->sum : ident);
6326: }
6327:
6328: void rotr(Node *t) {
6329:     auto *x = t->p, *y = x->p;
6330:     if((x->l = t->r)) t->r->p = x;
6331:     t->r = x, x->p = t;
6332:     update(x), update(t);
6333:     if((t->p = y)) {
6334:         if(y->l == x) y->l = t;
6335:         if(y->r == x) y->r = t;
6336:         update(y);
6337:     }
6338: }
6339:
6340: void rotl(Node *t) {
6341:     auto *x = t->p, *y = x->p;
6342:     if((x->r = t->l)) t->l->p = x;
6343:     t->l = x, x->p = t;
6344:     update(x), update(t);
6345:     if((t->p = y)) {
6346:         if(y->l == x) y->l = t;
6347:         if(y->r == x) y->r = t;
6348:         update(y);
6349:     }
6350: }
6351:
6352:
6353: void splay(Node *t) {
6354:     push(t);
6355:     while(!t->is_root()) {
6356:         auto *q = t->p;
6357:         if(q->is_root()) {
6358:             push(q), push(t);
6359:             if(q->l == t) rotr(t);
6360:             else rotl(t);
6361:         } else {
6362:             auto *r = q->p;
6363:             push(r), push(q), push(t);
6364:             if(r->l == q) {
6365:                 if(q->l == t) rotr(q), rotr(t);
6366:                 else rotl(t), rotr(t);

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```
6367:         } else {
6368:             if(q->r == t) rotl(q), rotl(t);
6369:             else rotr(t), rotl(t);
6370:         }
6371:     }
6372: }
6373: }
6374:
6375:
6376: Node *expose(Node *t) {
6377:     Node *rp = nullptr;
6378:     for(auto *cur = t; cur; cur = cur->p) {
6379:         splay(cur);
6380:         if(cur->r) cur->sum.add(cur->r->sum);
6381:         cur->r = rp;
6382:         if(cur->r) cur->sum.erase(cur->r->sum);
6383:         update(cur);
6384:         rp = cur;
6385:     }
6386:     splay(t);
6387:     return rp;
6388: }
6389:
6390: void link(Node *child, Node *parent) {
6391:     expose(child);
6392:     expose(parent);
6393:     child->p = parent;
6394:     parent->r = child;
6395:     update(parent);
6396: }
6397:
6398: void cut(Node *child) {
6399:     expose(child);
6400:     auto *parent = child->l;
6401:     child->l = nullptr;
6402:     parent->p = nullptr;
6403:     update(child);
6404: }
6405:
6406: void evert(Node *t) {
6407:     expose(t);
6408:     toggle(t);
6409:     push(t);
6410: }
6411:
6412: Node *lca(Node *u, Node *v) {
6413:     if(get_root(u) != get_root(v)) return nullptr;
6414:     expose(u);
6415:     return expose(v);
6416: }
6417:
6418:
6419: Node *get_kth(Node *x, int k) {
6420:     expose(x);
6421:     while(x) {
6422:         push(x);
6423:         if(x->r && x->r->sz > k) {
6424:             x = x->r;
6425:         } else {
6426:             if(x->r) k -= x->r->sz;
6427:             if(k == 0) return x;
6428:             k -= 1;
6429:             x = x->l;
6430:         }
6431:     }
6432:     return nullptr;
6433: }
6434:
6435: Node *get_root(Node *x) {
6436:     expose(x);
```

```

6437:     while(x->l) {
6438:         push(x);
6439:         x = x->l;
6440:     }
6441:     return x;
6442: }
6443:
6444: SUM &query(Node *t) {
6445:     expose(t);
6446:     return t->sum;
6447: }
6448: };
6449:
6450:
6451: #####
6452: ##### segment-tree-fractional-cascading.cpp #####
6453: #####
6454:
6455: struct SegmentTreeFractionalCascading {
6456:     vector< vector< int > > seg;
6457:     vector< vector< int > > LL, RR;
6458:     int sz;
6459:
6460:     SegmentTreeFractionalCascading(vector< int > &array) {
6461:         sz = 1;
6462:         while(sz < array.size()) sz <= 1;
6463:         seg.resize(2 * sz - 1);
6464:         LL.resize(2 * sz - 1);
6465:         RR.resize(2 * sz - 1);
6466:         for(int k = 0; k < array.size(); k++) {
6467:             seg[k + sz - 1].emplace_back(array[k]);
6468:         }
6469:         for(int k = sz - 2; k >= 0; k--) {
6470:             seg[k].resize(seg[2 * k + 1].size() + seg[2 * k + 2].size());
6471:             LL[k].resize(seg[k].size() + 1);
6472:             RR[k].resize(seg[k].size() + 1);
6473:             merge(begin(seg[2 * k + 1]), end(seg[2 * k + 1]), begin(seg[2 * k + 2]), end
(seg[2 * k + 2]), begin(seg[k]));
6474:             int tail1 = 0, tail2 = 0;
6475:             for(int i = 0; i < seg[k].size(); i++) {
6476:                 while(tail1 < seg[2 * k + 1].size() && seg[2 * k + 1][tail1] < seg[k][i])
++tail1;
6477:                 while(tail2 < seg[2 * k + 2].size() && seg[2 * k + 2][tail2] < seg[k][i])
++tail2;
6478:                 LL[k][i] = tail1, RR[k][i] = tail2;
6479:             }
6480:             LL[k][seg[k].size()] = (int) seg[2 * k + 1].size();
6481:             RR[k][seg[k].size()] = (int) seg[2 * k + 2].size();
6482:         }
6483:     }
6484:
6485:     int query(int a, int b, int lower, int upper, int k, int l, int r) {
6486:         if(a >= r || b <= l) {
6487:             return 0;
6488:         } else if(a <= l && r <= b) {
6489:             return (upper - lower);
6490:         } else {
6491:             return (query(a, b, LL[k][lower], LL[k][upper], 2 * k + 1, l, (l + r) >> 1)
+ query(a, b, RR[k][lower], RR[k][upper], 2 * k + 2, (l + r) >> 1, r));
6492:         }
6493:     }
6494:
6495:     int query(int a, int b, int l, int r) {
6496:         l = lower_bound(begin(seg[0]), end(seg[0]), l) - begin(seg[0]);
6497:         r = lower_bound(begin(seg[0]), end(seg[0]), r) - begin(seg[0]);
6498:         return (query(a, b, l, r, 0, 0, sz));
6499:     }
6500: };
6501:
6502:

```

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```
6503: #####
6504: ##### dual-segment-tree.cpp #####
6505: #####
6506:
6507: template< typename OperatorMonoid >
6508: struct DualSegmentTree {
6509:     using H = function< OperatorMonoid(OperatorMonoid, OperatorMonoid) >;
6510:
6511:     int sz, height;
6512:     vector< OperatorMonoid > lazy;
6513:     const H h;
6514:     const OperatorMonoid OM0;
6515:
6516:
6517:     DualSegmentTree(int n, const H h, const OperatorMonoid OM0)
6518:         : h(h), OM0(OM0) {
6519:         sz = 1;
6520:         height = 0;
6521:         while(sz < n) sz <= 1, height++;
6522:         lazy.assign(2 * sz, OM0);
6523:     }
6524:
6525:     inline void propagate(int k) {
6526:         if(lazy[k] != OM0) {
6527:             lazy[2 * k + 0] = h(lazy[2 * k + 0], lazy[k]);
6528:             lazy[2 * k + 1] = h(lazy[2 * k + 1], lazy[k]);
6529:             lazy[k] = OM0;
6530:         }
6531:     }
6532:
6533:     inline void thrust(int k) {
6534:         for(int i = height; i > 0; i--) propagate(k >> i);
6535:     }
6536:
6537:     void update(int a, int b, const OperatorMonoid &x) {
6538:         thrust(a += sz);
6539:         thrust(b += sz - 1);
6540:         for(int l = a, r = b + 1; l < r; l >>= 1, r >>= 1) {
6541:             if(l & 1) lazy[l] = h(lazy[l], x), ++l;
6542:             if(r & 1) --r, lazy[r] = h(lazy[r], x);
6543:         }
6544:     }
6545:
6546:     OperatorMonoid operator[](int k) {
6547:         thrust(k += sz);
6548:         return lazy[k];
6549:     }
6550: };
6551:
6552:
6553: #####
6554: ##### weighted-union-find.cpp #####
6555: #####
6556:
6557: template< typename T >
6558: struct WeightedUnionFind {
6559:     vector< int > data;
6560:     vector< T > ws;
6561:
6562:     WeightedUnionFind() {}
6563:
6564:     WeightedUnionFind(int sz) : data(sz, -1), ws(sz) {}
6565:
6566:     int find(int k) {
6567:         if(data[k] < 0) return k;
6568:         auto par = find(data[k]);
6569:         ws[k] += ws[data[k]];
6570:         return data[k] = par;
6571:     }
6572: }
```

```

6573: T weight(int t) {
6574:     find(t);
6575:     return ws[t];
6576: }
6577:
6578: bool unite(int x, int y, T w) {
6579:     w += weight(x);
6580:     w -= weight(y);
6581:     x = find(x), y = find(y);
6582:     if(x == y) return false;
6583:     if(data[x] > data[y]) {
6584:         swap(x, y);
6585:         w *= -1;
6586:     }
6587:     data[x] += data[y];
6588:     data[y] = x;
6589:     ws[y] = w;
6590:     return true;
6591: }
6592:
6593: T diff(int x, int y) {
6594:     return weight(y) - weight(x);
6595: }
6596: };
6597:
6598:
6599: #####
6600: ##### sparse-table.cpp #####
6601: #####
6602:
6603: template< typename T >
6604: struct SparseTable {
6605:     vector< vector< T > > st;
6606:     vector< int > lookup;
6607:
6608:     SparseTable(const vector< T > &v) {
6609:         int b = 0;
6610:         while((1 << b) <= v.size()) ++b;
6611:         st.assign(b, vector< T >(1 << b));
6612:         for(int i = 0; i < v.size(); i++) {
6613:             st[0][i] = v[i];
6614:         }
6615:         for(int i = 1; i < b; i++) {
6616:             for(int j = 0; j + (1 << i) <= (1 << b); j++) {
6617:                 st[i][j] = min(st[i - 1][j], st[i - 1][j + (1 << (i - 1))]);
6618:             }
6619:         }
6620:         lookup.resize(v.size() + 1);
6621:         for(int i = 2; i < lookup.size(); i++) {
6622:             lookup[i] = lookup[i >> 1] + 1;
6623:         }
6624:     }
6625:
6626:     inline T rmq(int l, int r) {
6627:         int b = lookup[r - 1];
6628:         return min(st[b][l], st[b][r - (1 << b)]);
6629:     }
6630: };
6631:
6632:
6633: #####
6634: ##### persistent-red-black-tree.cpp #####
6635: #####
6636:
6637: template< class D, class L, D (*f)(D, D), D (*g)(D, L), L (*h)(L, L), L (*p)(L, in
t) >
6638: struct PersistentRedBlackTree : RedBlackTree< D, L, f, g, h, p > {
6639:     using RBT = RedBlackTree< D, L, f, g, h, p >;
6640:     using Node = typename RBT::Node;
6641:

```



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```
6642: PersistentRedBlackTree(int sz, const D &M1, const L &OM0) :
6643:     RBT(sz, M1, OM0) {}
6644:
6645: Node *clone(Node *t) override { return &(*RBT::pool.alloc() = *t); }
6646:
6647: Node *rebuild(Node *r) {
6648:     auto ret = RBT::dump(r);
6649:     RBT::pool.clear();
6650:     return RBT::build(ret);
6651: }
6652: };
6653:
6654:
6655: #####
6656: ##### persistent-array.cpp #####
6657: #####
6658:
6659: template< typename T, int LOG >
6660: struct PersistentArray {
6661:     struct Node {
6662:         T data;
6663:         Node *child[1 << LOG] = {};
6664:
6665:         Node() {}
6666:
6667:         Node(const T &data) : data(data) {}
6668:     };
6669:
6670:     Node *root;
6671:
6672:     PersistentArray() : root(nullptr) {}
6673:
6674:     T get(Node *t, int k) {
6675:         if(k == 0) return t->data;
6676:         return get(t->child[k & ((1 << LOG) - 1)], k >> LOG);
6677:     }
6678:
6679:     T get(const int &k) {
6680:         return get(root, k);
6681:     }
6682:
6683:     pair< Node *, T * > mutable_get(Node *t, int k) {
6684:         t = t ? new Node(*t) : new Node();
6685:         if(k == 0) return {t, &t->data};
6686:         auto p = mutable_get(t->child[k & ((1 << LOG) - 1)], k >> LOG);
6687:         t->child[k & ((1 << LOG) - 1)] = p.first;
6688:         return {t, p.second};
6689:     }
6690:
6691:     T *mutable_get(const int &k) {
6692:         auto ret = mutable_get(root, k);
6693:         root = ret.first;
6694:         return ret.second;
6695:     }
6696:
6697:     Node *build(Node *t, const T &data, int k) {
6698:         if(!t) t = new Node();
6699:         if(k == 0) {
6700:             t->data = data;
6701:             return t;
6702:         }
6703:         auto p = build(t->child[k & ((1 << LOG) - 1)], data, k >> LOG);
6704:         t->child[k & ((1 << LOG) - 1)] = p;
6705:         return t;
6706:     }
6707:
6708:     void build(const vector< T > &v) {
6709:         root = nullptr;
6710:         for(int i = 0; i < v.size(); i++) {
6711:             root = build(root, v[i], i);
```

```

6712:     }
6713: }
6714: };
6715:
6716:
6717:
6718: #####
6719: ##### randomized-binary-search-tree-set.cpp #####
6720: #####
6721:
6722: template< class T >
6723: struct OrderedMultiSet : RandomizedBinarySearchTree< T >
6724: {
6725:     using RBST = RandomizedBinarySearchTree< T >;
6726:     using Node = typename RBST::Node;
6727:
6728:     OrderedMultiSet(int sz) : RBST(sz, [&](T x, T y) { return x; }, T()) {}
6729:
6730:     T kth_element(Node *t, int k)
6731:     {
6732:         if(k < RBST::count(t->l)) return kth_element(t->l, k);
6733:         if(k == RBST::count(t->l)) return t->key;
6734:         return kth_element(t->r, k - RBST::count(t->l) - 1);
6735:     }
6736:
6737:     virtual void insert_key(Node *t, const T &x)
6738:     {
6739:         RBST::insert(t, lower_bound(t, x), x);
6740:     }
6741:
6742:     void erase_key(Node *t, const T &x)
6743:     {
6744:         if(!count(t, x)) return;
6745:         RBST::erase(t, lower_bound(t, x));
6746:     }
6747:
6748:     int count(Node *t, const T &x)
6749:     {
6750:         return upper_bound(t, x) - lower_bound(t, x);
6751:     }
6752:
6753:     int lower_bound(Node *t, const T &x)
6754:     {
6755:         if(!t) return 0;
6756:         if(x <= t->key) return lower_bound(t->l, x);
6757:         return lower_bound(t->r, x) + RBST::count(t->l) + 1;
6758:     }
6759:
6760:     int upper_bound(Node *t, const T &x)
6761:     {
6762:         if(!t) return 0;
6763:         if(x < t->key) return upper_bound(t->l, x);
6764:         return upper_bound(t->r, x) + RBST::count(t->l) + 1;
6765:     }
6766: };
6767: template< class T >
6768: struct OrderedSet : OrderedMultiSet< T >
6769: {
6770:     using SET = OrderedMultiSet< T >;
6771:     using RBST = typename SET::RBST;
6772:     using Node = typename RBST::Node;
6773:
6774:     OrderedSet(int sz) : OrderedMultiSet< T >(sz) {}
6775:
6776:     void insert_key(Node *t, const T &x) override
6777:     {
6778:         if(SET::count(t, x)) return;
6779:         RBST::insert(t, SET::lower_bound(t, x), x);
6780:     }
6781: };

```

```

6782:
6783:
6784: #####
6785: ##### segment-tree-beats.cpp #####
6786: #####
6787:
6788: template< typename Monoid, typename OperatorMonoid = Monoid >
6789: struct SegmentTreeBeats {
6790:     using F = function< Monoid(Monoid, Monoid) >;
6791:     using G = function< Monoid(Monoid, OperatorMonoid) >;
6792:     using H = function< OperatorMonoid(OperatorMonoid, OperatorMonoid) >;
6793:
6794:     int sz, height;
6795:     vector< Monoid > data;
6796:     vector< OperatorMonoid > lazy;
6797:     const F f;
6798:     const G g;
6799:     const H h;
6800:     const Monoid M1;
6801:     const OperatorMonoid OM0;
6802:
6803:
6804:     SegmentTreeBeats(int n, const F f, const G g, const H h,
6805:                     const Monoid &M1, const OperatorMonoid OM0) {
6806:         : f(f), g(g), h(h), M1(M1), OM0(OM0) {
6807:             sz = 1;
6808:             height = 0;
6809:             while(sz < n) sz <= 1, height++;
6810:             data.assign(2 * sz, M1);
6811:             lazy.assign(2 * sz, OM0);
6812:         }
6813:
6814:     void set(int k, const Monoid &x) {
6815:         data[k + sz] = x;
6816:     }
6817:
6818:     void build() {
6819:         for(int k = sz - 1; k > 0; k--) {
6820:             data[k] = f(data[2 * k + 0], data[2 * k + 1]);
6821:         }
6822:     }
6823:
6824:     inline void propagate(int k) {
6825:         if(lazy[k] != OM0) {
6826:             lazy[2 * k + 0] = h(lazy[2 * k + 0], lazy[k]);
6827:             lazy[2 * k + 1] = h(lazy[2 * k + 1], lazy[k]);
6828:             data[k] = reflect(k);
6829:             lazy[k] = OM0;
6830:         }
6831:     }
6832:
6833:     inline Monoid reflect(int k) {
6834:         return lazy[k] == OM0 ? data[k] : g(data[k], lazy[k]);
6835:     }
6836:
6837:     inline void recalc(int k) {
6838:         while(k >= 1) data[k] = f(reflect(2 * k + 0), reflect(2 * k + 1));
6839:     }
6840:
6841:     inline void thrust(int k) {
6842:         for(int i = height; i > 0; i--) propagate(k >> i);
6843:     }
6844:
6845:     void update(int a, int b, const OperatorMonoid &x) {
6846:         thrust(a += sz);
6847:         thrust(b += sz - 1);
6848:         for(int l = a, r = b + 1; l < r; l >= 1, r >= 1) {
6849:             if(l & 1) lazy[l] = h(lazy[l], x), ++l;
6850:             if(r & 1) --r, lazy[r] = h(lazy[r], x);
6851:         }

```

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```
6852:     recalc(a);
6853:     recalc(b);
6854: }
6855:
6856: Monoid query(int a, int b) {
6857:     thrust(a += sz);
6858:     thrust(b += sz - 1);
6859:     Monoid L = M1, R = M1;
6860:     for(int l = a, r = b + 1; l < r; l >= 1, r >= 1) {
6861:         if(l & 1) L = f(L, reflect(l++));
6862:         if(r & 1) R = f(reflect(--r), R);
6863:     }
6864:     return f(L, R);
6865: }
6866:
6867: Monoid operator[](const int &k) {
6868:     return query(k, k + 1);
6869: }
6870:
6871: template< typename Uku, typename Check, typename Func, typename X >
6872: void update_beats_subtree(int k, const X &x, const Uku &uku, const Check &check,
const Func &func) {
6873:     if(k >= sz) {
6874:         auto v = reflect(k);
6875:         if(uku(v, x)) return;
6876:         if(check(v)) lazy[k] = func(v, x);
6877:         return;
6878:     }
6879:     propagate(k);
6880:     if(uku(data[k], x)) return;
6881:     if(check(data[k])) {
6882:         lazy[k] = func(data[k], x);
6883:         return;
6884:     }
6885:     update_beats_subtree(k * 2 + 0, x, uku, check, func);
6886:     update_beats_subtree(k * 2 + 1, x, uku, check, func);
6887:     data[k] = f(reflect(2 * k + 0), reflect(2 * k + 1));
6888: }
6889:
6890: template< typename Uku, typename Check, typename Func, typename X >
6891: void update_beats(int a, int b, const X &x, const Uku &uku, const Check &check,
const Func &func) {
6892:     thrust(a += sz);
6893:     thrust(b += sz - 1);
6894:     for(int l = a, r = b + 1; l < r; l >= 1, r >= 1) {
6895:         if(l & 1) update_beats_subtree(l++, x, uku, check, func);
6896:         if(r & 1) update_beats_subtree(--r, x, uku, check, func);
6897:     }
6898:     recalc(a);
6899:     recalc(b);
6900: }
6901: };
6902:
6903:
6904: #####
6905: ##### trie.cpp #####
6906: #####
6907:
6908: template< int char_size >
6909: struct TrieNode {
6910:     int nxt[char_size];
6911:
6912:     int exist;
6913:     vector< int > accept;
6914:
6915:     TrieNode() : exist(0) {
6916:         memset(nxt, -1, sizeof(nxt));
6917:     }
6918: };
6919:
```

```

6920: template< int char_size, int margin >
6921: struct Trie {
6922:     using Node = TrieNode< char_size >;
6923:
6924:     vector< Node > nodes;
6925:     int root;
6926:
6927:     Trie() : root(0) {
6928:         nodes.push_back(Node());
6929:     }
6930:
6931:     void update_direct(int node, int id) {
6932:         nodes[node].accept.push_back(id);
6933:     }
6934:
6935:     void update_child(int node, int child, int id) {
6936:         ++nodes[node].exist;
6937:     }
6938:
6939:     void add(const string &str, int str_index, int node_index, int id) {
6940:         if(str_index == str.size()) {
6941:             update_direct(node_index, id);
6942:         } else {
6943:             const int c = str[str_index] - margin;
6944:             if(nodes[node_index].nxt[c] == -1) {
6945:                 nodes[node_index].nxt[c] = (int) nodes.size();
6946:                 nodes.push_back(Node());
6947:             }
6948:             add(str, str_index + 1, nodes[node_index].nxt[c], id);
6949:             update_child(node_index, nodes[node_index].nxt[c], id);
6950:         }
6951:     }
6952:
6953:     void add(const string &str, int id) {
6954:         add(str, 0, 0, id);
6955:     }
6956:
6957:     void add(const string &str) {
6958:         add(str, nodes[0].exist);
6959:     }
6960:
6961:     void query(const string &str, const function< void(int) > &f, int str_index, int
node_index) {
6962:         for(auto &idx : nodes[node_index].accept) f(idx);
6963:         if(str_index == str.size()) {
6964:             return;
6965:         } else {
6966:             const int c = str[str_index] - margin;
6967:             if(nodes[node_index].nxt[c] == -1) return;
6968:             query(str, f, str_index + 1, nodes[node_index].nxt[c]);
6969:         }
6970:     }
6971:
6972:     void query(const string &str, const function< void(int) > &f) {
6973:         query(str, f, 0, 0);
6974:     }
6975:
6976:     int count() const {
6977:         return (nodes[0].exist);
6978:     }
6979:
6980:     int size() const {
6981:         return ((int) nodes.size());
6982:     }
6983: };
6984:
6985:
6986: #####
6987: ##### union-find-undo.cpp #####
6988: #####

```

```

6989:
6990: struct UnionFindUndo {
6991:     vector< int > data;
6992:     stack< pair< int, int > > history;
6993:
6994:     UnionFindUndo(int sz) {
6995:         data.assign(sz, -1);
6996:     }
6997:
6998:     bool unite(int x, int y) {
6999:         x = find(x), y = find(y);
7000:         history.emplace(x, data[x]);
7001:         history.emplace(y, data[y]);
7002:         if(x == y) return (false);
7003:         if(data[x] > data[y]) swap(x, y);
7004:         data[x] += data[y];
7005:         data[y] = x;
7006:         return (true);
7007:     }
7008:
7009:     int find(int k) {
7010:         if(data[k] < 0) return (k);
7011:         return (find(data[k]));
7012:     }
7013:
7014:     int size(int k) {
7015:         return (-data[find(k)]);
7016:     }
7017:
7018:     void undo() {
7019:         data[history.top().first] = history.top().second;
7020:         history.pop();
7021:         data[history.top().first] = history.top().second;
7022:         history.pop();
7023:     }
7024:
7025:     void snapshot() {
7026:         while(history.size()) history.pop();
7027:     }
7028:
7029:     void rollback() {
7030:         while(history.size()) undo();
7031:     }
7032: };
7033:
7034:
7035: #####
7036: ##### segment-tree-2d.cpp #####
7037: #####
7038:
7039: template< typename structure_t, typename get_t, typename update_t >
7040: struct SegmentTree2DCompressed {
7041:
7042:     using merge_f = function< get_t(get_t, get_t) >;
7043:     using range_get_f = function< get_t(structure_t &, int, int) >;
7044:     using update_f = function< void(structure_t &, int, update_t) >;
7045:
7046:     int sz;
7047:     vector< structure_t > seg;
7048:     const merge_f f;
7049:     const range_get_f g;
7050:     const update_f h;
7051:     const get_t identity;
7052:     vector< vector< int > > LL, RR;
7053:     vector< vector< int > > beet;
7054:
7055:     SegmentTree2DCompressed(int n, const merge_f &f, const range_get_f &g, const upd
ate_f &h, const get_t &identity)
7056:         : f(f), g(g), h(h), identity(identity) {
7057:         sz = 1;

```

```

7058:     while(sz < n) sz <= 1;
7059:     beet.resize(2 * sz);
7060:     LL.resize(2 * sz);
7061:     RR.resize(2 * sz);
7062: }
7063:
7064: void update(int a, int x, update_t z, int k, int l, int r) {
7065:     if(r <= a || a + 1 <= l) return;
7066:     if(a <= l && r <= a + 1) return h(seg[k], x, z);
7067:     update(a, LL[k][x], z, 2 * k + 0, l, (l + r) >> 1);
7068:     update(a, RR[k][x], z, 2 * k + 1, (l + r) >> 1, r);
7069:     return h(seg[k], x, z);
7070: }
7071:
7072: void update(int x, int y, update_t z) {
7073:     y = lower_bound(begin(beet[1]), end(beet[1]), y) - begin(beet[1]);
7074:     return update(x, y, z, 1, 0, sz);
7075: }
7076:
7077: get_t query(int a, int b, int x, int y, int k, int l, int r) {
7078:     if(a >= r || b <= l) return identity;
7079:     if(a <= l && r <= b) return g(seg[k], x, y);
7080:     return f(query(a, b, LL[k][x], LL[k][y], 2 * k + 0, l, (l + r) >> 1),
7081:             query(a, b, RR[k][x], RR[k][y], 2 * k + 1, (l + r) >> 1, r));
7082: }
7083:
7084: get_t query(int a, int b, int x, int y) {
7085:     x = lower_bound(begin(beet[1]), end(beet[1]), x) - begin(beet[1]);
7086:     y = lower_bound(begin(beet[1]), end(beet[1]), y) - begin(beet[1]);
7087:     return query(a, b, x, y, 1, 0, sz);
7088: }
7089:
7090: void build() {
7091:     for(int k = (int) beet.size() - 1; k >= sz; k--) {
7092:         sort(begin(beet[k]), end(beet[k]));
7093:         beet[k].erase(unique(begin(beet[k]), end(beet[k])), end(beet[k]));
7094:     }
7095:     for(int k = sz - 1; k > 0; k--) {
7096:         beet[k].resize(beet[2 * k + 0].size() + beet[2 * k + 1].size());
7097:         merge(begin(beet[2 * k + 0]), end(beet[2 * k + 0]), begin(beet[2 * k + 1]),
end(beet[2 * k + 1]), begin(beet[k]));
7098:         beet[k].erase(unique(begin(beet[k]), end(beet[k])), end(beet[k]));
7099:         LL[k].resize(beet[k].size() + 1);
7100:         RR[k].resize(beet[k].size() + 1);
7101:         int tail1 = 0, tail2 = 0;
7102:         for(int i = 0; i < beet[k].size(); i++) {
7103:             while(tail1 < beet[2 * k + 0].size() && beet[2 * k + 0][tail1] < beet[k][i
]) ++tail1;
7104:             while(tail2 < beet[2 * k + 1].size() && beet[2 * k + 1][tail2] < beet[k][i
]) ++tail2;
7105:             LL[k][i] = tail1, RR[k][i] = tail2;
7106:         }
7107:         LL[k][beet[k].size()] = (int) beet[2 * k + 0].size();
7108:         RR[k][beet[k].size()] = (int) beet[2 * k + 1].size();
7109:     }
7110:     for(int k = 0; k < beet.size(); k++) {
7111:         seg.emplace_back(structure_t(beet[k].size()));
7112:     }
7113: }
7114:
7115: void preupdate(int x, int y) {
7116:     beet[x + sz].push_back(y);
7117: }
7118: };
7119:
7120:
7121: #####
7122: ##### union-rectangle.cpp #####
7123: #####
7124:

```

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```
7125: template< typename T >
7126: struct UnionRectangle {
7127:     map< T, T > data;
7128:     int64 sum;
7129:
7130:     UnionRectangle() : sum(0) {
7131:         const T INF = numeric_limits< T >::max();
7132:         data[0] = INF;
7133:         data[INF] = 0;
7134:     }
7135:     void add_point(T x, T y) {
7136:         auto p = data.lower_bound(x);
7137:         if(p->second >= y) return;
7138:         const T nxtY = p->second;
7139:         --p;
7140:         while(p->second <= y) {
7141:             auto it = *p;
7142:             p = --data.erase(p);
7143:             sum -= (it.first - p->first) * (it.second - nxtY);
7144:         }
7145:         sum += (x - p->first) * (y - nxtY);
7146:         data[x] = y;
7147:     }
7148:
7149:     int64 get() {
7150:         return sum;
7151:     }
7152: };
7153:
7154:
7155: #####
7156: ##### persistent-segment-tree.cpp #####
7157: #####
7158:
7159: template< typename Monoid >
7160: struct PersistentSegmentTree {
7161:     using F = function< Monoid(Monoid, Monoid) >;
7162:
7163:     struct Node {
7164:         Monoid data;
7165:         Node *l, *r;
7166:
7167:         Node(const Monoid &data) : data(data), l(nullptr), r(nullptr) {}
7168:     };
7169:
7170:
7171:     int sz;
7172:     const F f;
7173:     const Monoid M1;
7174:
7175:     PersistentSegmentTree(const F f, const Monoid &M1) : f(f), M1(M1) {}
7176:
7177:     Node *build(vector< Monoid > &v) {
7178:         sz = (int) v.size();
7179:         return build(0, (int) v.size(), v);
7180:     }
7181:
7182:     Node *merge(Node *l, Node *r) {
7183:         auto t = new Node(f(l->data, r->data));
7184:         t->l = l;
7185:         t->r = r;
7186:         return t;
7187:     }
7188:
7189:     Node *build(int l, int r, vector< Monoid > &v) {
7190:         if(l + 1 >= r) return new Node(v[l]);
7191:         return merge(build(l, (l + r) >> 1, v), build((l + r) >> 1, r, v));
7192:     }
7193:
7194:     Node *update(int a, const Monoid &x, Node *k, int l, int r) {
```



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```
7195:     if(r <= a || a + 1 <= l) {
7196:         return k;
7197:     } else if(a <= l && r <= a + 1) {
7198:         return new Node(x);
7199:     } else {
7200:         return merge(update(a, x, k->l, l, (l + r) >> 1), update(a, x, k->r, (l + r)
>> 1, r));
7201:     }
7202: }
7203:
7204: Node *update(Node *t, int k, const Monoid &x) {
7205:     return update(k, x, t, 0, sz);
7206: }
7207:
7208: Monoid query(int a, int b, Node *k, int l, int r) {
7209:     if(r <= a || b <= l) {
7210:         return M1;
7211:     } else if(a <= l && r <= b) {
7212:         return k->data;
7213:     } else {
7214:         return f(query(a, b, k->l, l, (l + r) >> 1),
7215:                 query(a, b, k->r, (l + r) >> 1, r));
7216:     }
7217: }
7218:
7219: Monoid query(Node *t, int a, int b) {
7220:     return query(a, b, t, 0, sz);
7221: }
7222: };
7223:
7224:
7225: #####
7226: ##### red-black-tree.cpp #####
7227: #####
7228:
7229: template< class T >
7230: struct ArrayPool {
7231:     vector< T > pool;
7232:     vector< T * > stock;
7233:     int ptr;
7234:
7235:     ArrayPool(int sz) : pool(sz), stock(sz) {}
7236:
7237:     inline T *alloc() { return stock[--ptr]; }
7238:
7239:     inline void free(T *t) { stock[ptr++] = t; }
7240:
7241:     void clear() {
7242:         ptr = (int) pool.size();
7243:         for(int i = 0; i < pool.size(); i++) stock[i] = &pool[i];
7244:     }
7245: };
7246:
7247: template< class D, class L, D (*f)(D, D), D (*g)(D, L), L (*h)(L, L), L (*p)(L, in
t) >
7248: struct RedBlackTree {
7249:     enum COLOR {
7250:         BLACK, RED
7251:     };
7252:
7253:     struct Node {
7254:         Node *l, *r;
7255:         COLOR color;
7256:         int level, cnt;
7257:         D key, sum;
7258:         L lazy;
7259:
7260:         Node() {}
7261:
7262:         Node(const D &k, const L &laz) :
```

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```
7263:         key(k), sum(k), l(nullptr), r(nullptr), color(BLACK), level(0), cnt(1), la
zy(laz) {}
7264:
7265:     Node(Node *l, Node *r, const D &k, const L &laz) :
7266:         key(k), color(RED), l(l), r(r), lazy(laz) {}
7267: };
7268:
7269: ArrayPool< Node > pool;
7270:
7271:
7272: const D M1;
7273: const L OM0;
7274:
7275: RedBlackTree(int sz, const D &M1, const L &OM0) :
7276:     pool(sz), M1(M1), OM0(OM0) { pool.clear(); }
7277:
7278:
7279: inline Node *alloc(const D &key) {
7280:     return &(*pool.alloc() = Node(key, OM0));
7281: }
7282:
7283: inline Node *alloc(Node *l, Node *r) {
7284:     auto t = &(*pool.alloc() = Node(l, r, M1, OM0));
7285:     return update(t);
7286: }
7287:
7288: virtual Node *clone(Node *t) { return t; }
7289:
7290: inline int count(const Node *t) { return t ? t->cnt : 0; }
7291:
7292: inline D sum(const Node *t) { return t ? t->sum : M1; }
7293:
7294: Node *update(Node *t) {
7295:     t->cnt = count(t->l) + count(t->r) + (!t->l || !t->r);
7296:     t->level = t->l ? t->l->level + (t->l->color == BLACK) : 0;
7297:     t->sum = f(f(sum(t->l), t->key), sum(t->r));
7298:     return t;
7299: }
7300:
7301: Node *propagate(Node *t) {
7302:     t = clone(t);
7303:     if(t->lazy != OM0) {
7304:         if(!t->l) {
7305:             t->key = g(t->key, p(t->lazy, 1));
7306:         } else {
7307:             if(t->l) {
7308:                 t->l = clone(t->l);
7309:                 t->l->lazy = h(t->l->lazy, t->lazy);
7310:                 t->l->sum = g(t->l->sum, p(t->lazy, count(t->l)));
7311:             }
7312:             if(t->r) {
7313:                 t->r = clone(t->r);
7314:                 t->r->lazy = h(t->r->lazy, t->lazy);
7315:                 t->r->sum = g(t->r->sum, p(t->lazy, count(t->r)));
7316:             }
7317:         }
7318:         t->lazy = OM0;
7319:     }
7320:     return update(t);
7321: }
7322:
7323: Node *rotate(Node *t, bool b) {
7324:     t = propagate(t);
7325:     Node *s;
7326:     if(b) {
7327:         s = propagate(t->l);
7328:         t->l = s->r;
7329:         s->r = t;
7330:     } else {
7331:         s = propagate(t->r);
```

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```

7332:         t->r = s->l;
7333:         s->l = t;
7334:     }
7335:     update(t);
7336:     return update(s);
7337: }
7338:
7339: Node *submerge(Node *l, Node *r) {
7340:     if(l->level < r->level) {
7341:         r = propagate(r);
7342:         Node *c = (r->l = submerge(l, r->l));
7343:         if(r->color == BLACK && c->color == RED && c->l && c->l->color == RED) {
7344:             r->color = RED;
7345:             c->color = BLACK;
7346:             if(r->r->color == BLACK) return rotate(r, true);
7347:             r->r->color = BLACK;
7348:         }
7349:         return update(r);
7350:     }
7351:     if(l->level > r->level) {
7352:         l = propagate(l);
7353:         Node *c = (l->r = submerge(l->r, r));
7354:         if(l->color == BLACK && c->color == RED && c->r && c->r->color == RED) {
7355:             l->color = RED;
7356:             c->color = BLACK;
7357:             if(l->l->color == BLACK) return rotate(l, false);
7358:             l->l->color = BLACK;
7359:         }
7360:         return update(l);
7361:     }
7362:     return alloc(l, r);
7363: }
7364:
7365: Node *merge(Node *l, Node *r) {
7366:     if(!l || !r) return l ? l : r;
7367:     Node *c = submerge(l, r);
7368:     c->color = BLACK;
7369:     return c;
7370: }
7371:
7372: pair< Node *, Node * > split(Node *t, int k) {
7373:     if(!t) return {nullptr, nullptr};
7374:     t = propagate(t);
7375:     if(k == 0) return {nullptr, t};
7376:     if(k >= count(t)) return {t, nullptr};
7377:     Node *l = t->l, *r = t->r;
7378:     pool.free(t);
7379:     if(k < count(l)) {
7380:         auto pp = split(l, k);
7381:         return {pp.first, merge(pp.second, r)};
7382:     }
7383:     if(k > count(l)) {
7384:         auto pp = split(r, k - count(l));
7385:         return {merge(l, pp.first), pp.second};
7386:     }
7387:     return {l, r};
7388: }
7389:
7390: Node *build(int l, int r, const vector< D > &v) {
7391:     if(l + 1 >= r) return alloc(v[l]);
7392:     return merge(build(l, (l + r) >> 1, v), build((l + r) >> 1, r, v));
7393: }
7394:
7395: Node *build(const vector< D > &v) {
7396:     //pool.clear();
7397:     return build(0, (int) v.size(), v);
7398: }
7399:
7400: void dump(Node *r, typename vector< D >::iterator &it, L lazy) {
7401:     if(r->lazy != OM0) lazy = h(lazy, r->lazy);

```

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```
7402:     if(!r->l || !r->r) {
7403:         *it++ = g(r->key, lazy);
7404:         return;
7405:     }
7406:     dump(r->l, it, lazy);
7407:     dump(r->r, it, lazy);
7408: }
7409:
7410: vector< D > dump(Node *r) {
7411:     vector< D > v((size_t) count(r));
7412:     auto it = begin(v);
7413:     dump(r, it, OM0);
7414:     return v;
7415: }
7416:
7417: string to_string(Node *r) {
7418:     auto s = dump(r);
7419:     string ret;
7420:     for(int i = 0; i < s.size(); i++) {
7421:         ret += std::to_string(s[i]);
7422:         ret += ", ";
7423:     }
7424:     return (ret);
7425: }
7426:
7427: void insert(Node *&t, int k, const D &v) {
7428:     auto x = split(t, k);
7429:     t = merge(merge(x.first, alloc(v)), x.second);
7430: }
7431:
7432: D erase(Node *&t, int k) {
7433:     auto x = split(t, k);
7434:     auto y = split(x.second, 1);
7435:     auto v = y.first->key;
7436:     pool.free(y.first);
7437:     t = merge(x.first, y.second);
7438:     return v;
7439: }
7440:
7441: D query(Node *&t, int a, int b) {
7442:     auto x = split(t, a);
7443:     auto y = split(x.second, b - a);
7444:     auto ret = sum(y.first);
7445:     t = merge(x.first, merge(y.first, y.second));
7446:     return ret;
7447: }
7448:
7449: void set_propagate(Node *&t, int a, int b, const L &pp) {
7450:     auto x = split(t, a);
7451:     auto y = split(x.second, b - a);
7452:     y.first->lazy = h(y.first->lazy, pp);
7453:     t = merge(x.first, merge(propagate(y.first), y.second));
7454: }
7455:
7456: void set_element(Node *&t, int k, const D &x) {
7457:     if(!t->l) {
7458:         t->key = t->sum = x;
7459:         return;
7460:     }
7461:     t = propagate(t);
7462:     if(k < count(t->l)) set_element(t->l, k, x);
7463:     else set_element(t->r, k - count(t->l), x);
7464:     t = update(t);
7465: }
7466:
7467: int size(Node *t) {
7468:     return count(t);
7469: }
7470:
7471: bool empty(Node *t) {
```

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```
7472:     return !t;
7473: }
7474:
7475: Node *makeset() {
7476:     return (nullptr);
7477: }
7478: };
7479:
7480:
7481: #####
7482: ##### randomized-binary-search-tree.cpp #####
7483: #####
7484:
7485: template< class Monoid, class OperatorMonoid = Monoid >
7486: struct RandomizedBinarySearchTree {
7487:     using F = function< Monoid(Monoid, Monoid) >;
7488:     using G = function< Monoid(Monoid, OperatorMonoid) >;
7489:     using H = function< OperatorMonoid(OperatorMonoid, OperatorMonoid) >;
7490:     using P = function< OperatorMonoid(OperatorMonoid, int) >;
7491:
7492:     inline int xor128() {
7493:         static int x = 123456789;
7494:         static int y = 362436069;
7495:         static int z = 521288629;
7496:         static int w = 88675123;
7497:         int t;
7498:
7499:         t = x ^ (x << 11);
7500:         x = y;
7501:         y = z;
7502:         z = w;
7503:         return w = (w ^ (w >> 19)) ^ (t ^ (t >> 8));
7504:     }
7505:
7506:     struct Node {
7507:         Node *l, *r;
7508:         int cnt;
7509:         Monoid key, sum;
7510:         OperatorMonoid lazy;
7511:
7512:         Node() = default;
7513:
7514:         Node(const Monoid &k, const OperatorMonoid &p) : cnt(1), key(k), sum(k), lazy(
p), l(nullptr), r(nullptr) {}
7515:     };
7516:
7517:     vector< Node > pool;
7518:     int ptr;
7519:
7520:     const Monoid M1;
7521:     const OperatorMonoid OM0;
7522:     const F f;
7523:     const G g;
7524:     const H h;
7525:     const P p;
7526:
7527:     RandomizedBinarySearchTree(int sz, const F &f, const Monoid &M1) :
7528:         pool(sz), ptr(0), f(f), g(G()), h(H()), p(P()), M1(M1), OM0(OperatorMonoid()
) {}
7529:
7530:     RandomizedBinarySearchTree(int sz, const F &f, const G &g, const H &h, const P &
p,
7531:                                const Monoid &M1, const OperatorMonoid &OM0) :
7532:         pool(sz), ptr(0), f(f), g(g), h(h), p(p), M1(M1), OM0(OM0) {}
7533:
7534:     inline Node *alloc(const Monoid &key) { return &(pool[ptr++] = Node(key, OM0));
}
7535:
7536:     virtual Node *clone(Node *t) { return t; }
7537:
```

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```
7538: inline int count(const Node *t) { return t ? t->cnt : 0; }
7539:
7540: inline Monoid sum(const Node *t) { return t ? t->sum : M1; }
7541:
7542: inline Node *update(Node *t) {
7543:     t->cnt = count(t->l) + count(t->r) + 1;
7544:     t->sum = f(f(sum(t->l), t->key), sum(t->r));
7545:     return t;
7546: }
7547:
7548: Node *propagate(Node *t) {
7549:     t = clone(t);
7550:     if(t->lazy != OM0) {
7551:         t->key = g(t->key, p(t->lazy, 1));
7552:         if(t->l) {
7553:             t->l = clone(t->l);
7554:             t->l->lazy = h(t->l->lazy, t->lazy);
7555:             t->l->sum = g(t->l->sum, p(t->lazy, count(t->l)));
7556:         }
7557:         if(t->r) {
7558:             t->r = clone(t->r);
7559:             t->r->lazy = h(t->r->lazy, t->lazy);
7560:             t->r->sum = g(t->r->sum, p(t->lazy, count(t->r)));
7561:         }
7562:         t->lazy = OM0;
7563:     }
7564:     return update(t);
7565: }
7566:
7567: Node *merge(Node *l, Node *r) {
7568:     if(!l || !r) return l ? l : r;
7569:     if(xor128() % (l->cnt + r->cnt) < l->cnt) {
7570:         l = propagate(l);
7571:         l->r = merge(l->r, r);
7572:         return update(l);
7573:     } else {
7574:         r = propagate(r);
7575:         r->l = merge(l, r->l);
7576:         return update(r);
7577:     }
7578: }
7579:
7580: pair< Node *, Node * > split(Node *t, int k) {
7581:     if(!t) return {t, t};
7582:     t = propagate(t);
7583:     if(k <= count(t->l)) {
7584:         auto s = split(t->l, k);
7585:         t->l = s.second;
7586:         return {s.first, update(t)};
7587:     } else {
7588:         auto s = split(t->r, k - count(t->l) - 1);
7589:         t->r = s.first;
7590:         return {update(t), s.second};
7591:     }
7592: }
7593:
7594: Node *build(int l, int r, const vector< Monoid > &v) {
7595:     if(l + 1 >= r) return alloc(v[l]);
7596:     return merge(build(l, (l + r) >> 1, v), build((l + r) >> 1, r, v));
7597: }
7598:
7599: Node *build(const vector< Monoid > &v) {
7600:     ptr = 0;
7601:     return build(0, (int) v.size(), v);
7602: }
7603:
7604: void dump(Node *r, typename vector< Monoid >::iterator &it) {
7605:     if(!r) return;
7606:     r = propagate(r);
7607:     dump(r->l, it);
```

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```
7608:     *it = r->key;
7609:     dump(r->r, ++it);
7610: }
7611:
7612: vector< Monoid > dump(Node *r) {
7613:     vector< Monoid > v((size_t) count(r));
7614:     auto it = begin(v);
7615:     dump(r, it);
7616:     return v;
7617: }
7618:
7619: string to_string(Node *r) {
7620:     auto s = dump(r);
7621:     string ret;
7622:     for(int i = 0; i < s.size(); i++) ret += ", ";
7623:     return (ret);
7624: }
7625:
7626: void insert(Node *&t, int k, const Monoid &v) {
7627:     auto x = split(t, k);
7628:     t = merge(merge(x.first, alloc(v)), x.second);
7629: }
7630:
7631: void erase(Node *&t, int k) {
7632:     auto x = split(t, k);
7633:     t = merge(x.first, split(x.second, 1).second);
7634: }
7635:
7636: Monoid query(Node *&t, int a, int b) {
7637:     auto x = split(t, a);
7638:     auto y = split(x.second, b - a);
7639:     auto ret = sum(y.first);
7640:     t = merge(x.first, merge(y.first, y.second));
7641:     return ret;
7642: }
7643:
7644: void set_propagate(Node *&t, int a, int b, const OperatorMonoid &p) {
7645:     auto x = split(t, a);
7646:     auto y = split(x.second, b - a);
7647:     y.first->lazy = h(y.first->lazy, p);
7648:     t = merge(x.first, merge(propagate(y.first), y.second));
7649: }
7650:
7651: void set_element(Node *&t, int k, const Monoid &x) {
7652:     t = propagate(t);
7653:     if(k < count(t->l)) set_element(t->l, k, x);
7654:     else if(k == count(t->l)) t->key = t->sum = x;
7655:     else set_element(t->r, k - count(t->l) - 1, x);
7656:     t = update(t);
7657: }
7658:
7659:
7660: int size(Node *t) {
7661:     return count(t);
7662: }
7663:
7664: bool empty(Node *t) {
7665:     return !t;
7666: }
7667:
7668: Node *makeset() {
7669:     return nullptr;
7670: }
7671: };
7672:
7673:
7674: #####
7675: ##### bipartite-graph.cpp #####
7676: #####
7677:
```

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```
7678: struct BipartiteGraph : UnionFind
7679: {
7680:     vector< int > color;
7681:
7682:     BipartiteGraph(int v) : color(v + v, -1), UnionFind(v + v) {}
7683:
7684:     bool bipartite_graph_coloring()
7685:     {
7686:         for(int i = 0; i < color.size() / 2; i++) {
7687:             int a = find(i);
7688:             int b = find(i + (int) color.size() / 2);
7689:             if(a == b) return (false);
7690:             if(color[a] < 0) color[a] = 0, color[b] = 1;
7691:         }
7692:         return (true);
7693:     }
7694:
7695:     bool operator[](int k)
7696:     {
7697:         return (bool(color[find(k)]));
7698:     }
7699: };
7700:
7701:
7702: #####
7703: ##### li-chao-tree.cpp #####
7704: #####
7705:
7706: template< typename T >
7707: struct LiChaoTree {
7708:     struct Line {
7709:         T a, b;
7710:
7711:         Line(T a, T b) : a(a), b(b) {}
7712:
7713:         inline T get(T x) const { return a * x + b; }
7714:
7715:         inline bool over(const Line &b, const T &x) const {
7716:             return get(x) < b.get(x);
7717:         }
7718:     };
7719:
7720:     vector< T > xs;
7721:     vector< Line > seg;
7722:     int sz;
7723:
7724:     LiChaoTree(const vector< T > &x, T INF) : xs(x) {
7725:         sz = 1;
7726:         while(sz < xs.size()) sz <= 1;
7727:         while(xs.size() < sz) xs.push_back(xs.back() + 1);
7728:         seg.assign(2 * sz - 1, Line(0, INF));
7729:     }
7730:
7731:     void update(Line &x, int k, int l, int r) {
7732:         int mid = (l + r) >> 1;
7733:         auto latte = x.over(seg[k], xs[l]), malta = x.over(seg[k], xs[mid]);
7734:         if(malta) swap(seg[k], x);
7735:         if(l + 1 >= r) return;
7736:         else if(latte != malta) update(x, 2 * k + 1, l, mid);
7737:         else update(x, 2 * k + 2, mid, r);
7738:     }
7739:
7740:     void update(T a, T b) { // ax+b
7741:         Line l(a, b);
7742:         update(l, 0, 0, sz);
7743:     }
7744:
7745:     T query(int k) { // xs[k]
7746:         const T x = xs[k];
7747:         k += sz - 1;
```



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```
7748:     T ret = seg[k].get(x);
7749:     while(k > 0) {
7750:         k = (k - 1) >> 1;
7751:         ret = min(ret, seg[k].get(x));
7752:     }
7753:     return ret;
7754: }
7755: };
7756:
7757:
7758: #####
7759: ##### persistent-binary-trie.cpp #####
7760: #####
7761:
7762: template< typename T >
7763: struct BinaryTrieNode {
7764:     using Node = BinaryTrieNode< T >;
7765:
7766:     BinaryTrieNode< T > *nxt[2];
7767:     int max_index;
7768:
7769:     BinaryTrieNode() : max_index(-1) {
7770:         nxt[0] = nxt[1] = nullptr;
7771:     }
7772:
7773:     void update_direct(int id) {
7774:         max_index = max(max_index, id);
7775:     }
7776:
7777:     void update_child(Node *child, int id) {
7778:         max_index = max(max_index, id);
7779:     }
7780:
7781:     Node *add(const T &bit, int bit_index, int id, bool need = true) {
7782:         Node *node = need ? new Node(*this) : this;
7783:         if(bit_index == -1) {
7784:             node->update_direct(id);
7785:         } else {
7786:             const int c = (bit >> bit_index) & 1;
7787:             if(node->nxt[c] == nullptr) node->nxt[c] = new Node(), need = false;
7788:             node->nxt[c] = node->nxt[c]->add(bit, bit_index - 1, id, need);
7789:             node->update_child(node->nxt[c], id);
7790:         }
7791:         return node;
7792:     }
7793:
7794:     inline T min_query(T bit, int bit_index, int bit2, int l) {
7795:         if(bit_index == -1) return bit;
7796:         int c = (bit2 >> bit_index) & 1;
7797:         if(nxt[c] != nullptr && l <= nxt[c]->max_index) {
7798:             return nxt[c]->min_query(bit, bit_index - 1, bit2, l);
7799:         } else {
7800:             return nxt[1 ^ c]->min_query(bit | (1LL << bit_index), bit_index - 1, bit2,
1);
7801:         }
7802:     }
7803: };
7804:
7805: template< typename T, int MAX_LOG >
7806: struct PersistentBinaryTrie {
7807:     using Node = BinaryTrieNode< T >;
7808:     Node *root;
7809:
7810:     PersistentBinaryTrie(Node *root) : root(root) {}
7811:
7812:     PersistentBinaryTrie() : root(new Node()) {}
7813:
7814:     PersistentBinaryTrie add(const T &bit, int id) {
7815:         return PersistentBinaryTrie(root->add(bit, MAX_LOG, id));
7816:     }
}
```

```

7817:
7818:     T min_query(int bit, int l) {
7819:         return root->min_query(0, MAX_LOG, bit, l);
7820:     }
7821: };
7822:
7823:
7824: #####
7825: ##### segment-tree.cpp #####
7826: #####
7827:
7828: template< typename Monoid >
7829: struct SegmentTree {
7830:     using F = function< Monoid(Monoid, Monoid) >;
7831:
7832:     int sz;
7833:     vector< Monoid > seg;
7834:
7835:     const F f;
7836:     const Monoid M1;
7837:
7838:     SegmentTree(int n, const F f, const Monoid &M1) : f(f), M1(M1) {
7839:         sz = 1;
7840:         while(sz < n) sz <= 1;
7841:         seg.assign(2 * sz, M1);
7842:     }
7843:
7844:     void set(int k, const Monoid &x) {
7845:         seg[k + sz] = x;
7846:     }
7847:
7848:     void build() {
7849:         for(int k = sz - 1; k > 0; k--) {
7850:             seg[k] = f(seg[2 * k + 0], seg[2 * k + 1]);
7851:         }
7852:     }
7853:
7854:     void update(int k, const Monoid &x) {
7855:         k += sz;
7856:         seg[k] = x;
7857:         while(k >= 1) {
7858:             seg[k] = f(seg[2 * k + 0], seg[2 * k + 1]);
7859:         }
7860:     }
7861:
7862:     Monoid query(int a, int b) {
7863:         Monoid L = M1, R = M1;
7864:         for(a += sz, b += sz; a < b; a >= 1, b >= 1) {
7865:             if(a & 1) L = f(L, seg[a++]);
7866:             if(b & 1) R = f(seg[--b], R);
7867:         }
7868:         return f(L, R);
7869:     }
7870:
7871:     Monoid operator[](const int &k) const {
7872:         return seg[k + sz];
7873:     }
7874:
7875:     template< typename C >
7876:     int find_subtree(int a, const C &check, Monoid &M, bool type) {
7877:         while(a < sz) {
7878:             Monoid nxt = type ? f(seg[2 * a + type], M) : f(M, seg[2 * a + type]);
7879:             if(check(nxt)) a = 2 * a + type;
7880:             else M = nxt, a = 2 * a + 1 - type;
7881:         }
7882:         return a - sz;
7883:     }
7884:
7885:
7886:     template< typename C >

```

```

7887: int find_first(int a, const C &check) {
7888:     Monoid L = M1;
7889:     if(a <= 0) {
7890:         if(check(f(L, seg[1]))) return find_subtree(1, check, L, false);
7891:         return -1;
7892:     }
7893:     int b = sz;
7894:     for(a += sz, b += sz; a < b; a >= 1, b >= 1) {
7895:         if(a & 1) {
7896:             Monoid nxt = f(L, seg[a]);
7897:             if(check(nxt)) return find_subtree(a, check, L, false);
7898:             L = nxt;
7899:             ++a;
7900:         }
7901:     }
7902:     return -1;
7903: }
7904:
7905: template< typename C >
7906: int find_last(int b, const C &check) {
7907:     Monoid R = M1;
7908:     if(b >= sz) {
7909:         if(check(f(seg[1], R))) return find_subtree(1, check, R, true);
7910:         return -1;
7911:     }
7912:     int a = sz;
7913:     for(b += sz; a < b; a >= 1, b >= 1) {
7914:         if(b & 1) {
7915:             Monoid nxt = f(seg[--b], R);
7916:             if(check(nxt)) return find_subtree(b, check, R, true);
7917:             R = nxt;
7918:         }
7919:     }
7920:     return -1;
7921: }
7922: };
7923:
7924:
7925:
7926: #####
7927: ##### binary-trie.cpp #####
7928: #####
7929:
7930: template< typename T, int MAX_LOG >
7931: struct BinaryTrie {
7932:     BinaryTrie *nxt[2];
7933:     T lazy;
7934:     int exist;
7935:     bool fill;
7936:     vector< int > accept;
7937:
7938:     BinaryTrie() : exist(0), lazy(0), nxt{nullptr, nullptr} {}
7939:
7940:     void add(const T &bit, int bit_index, int id) {
7941:         propagate(bit_index);
7942:         if(bit_index == -1) {
7943:             ++exist;
7944:             accept.push_back(id);
7945:         } else {
7946:             auto &to = nxt[(bit >> bit_index) & 1];
7947:             if(!to) to = new BinaryTrie();
7948:             to->add(bit, bit_index - 1, id);
7949:             ++exist;
7950:         }
7951:     }
7952:
7953:     void add(const T &bit, int id) {
7954:         add(bit, MAX_LOG, id);
7955:     }
7956:

```

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```
7957: void add(const T &bit) {
7958:     add(bit, exist);
7959: }
7960:
7961: void del(const T &bit, int bit_index) {
7962:     propagate(bit_index);
7963:     if(bit_index == -1) {
7964:         exist--;
7965:     } else {
7966:         nxt[(bit >> bit_index) & 1]->del(bit, bit_index - 1);
7967:         exist--;
7968:     }
7969: }
7970:
7971: void del(const T &bit) {
7972:     del(bit, MAX_LOG);
7973: }
7974:
7975:
7976: pair< T, BinaryTrie * > max_element(int bit_index) {
7977:     propagate(bit_index);
7978:     if(bit_index == -1) return {0, this};
7979:     if(nxt[1] && nxt[1]->size()) {
7980:         auto ret = nxt[1]->max_element(bit_index - 1);
7981:         ret.first |= T(1) << bit_index;
7982:         return ret;
7983:     } else {
7984:         return nxt[0]->max_element(bit_index - 1);
7985:     }
7986: }
7987:
7988: pair< T, BinaryTrie * > min_element(int bit_index) {
7989:     propagate(bit_index);
7990:     if(bit_index == -1) return {0, this};
7991:     if(nxt[0] && nxt[0]->size()) {
7992:         return nxt[0]->min_element(bit_index - 1);
7993:     } else {
7994:         auto ret = nxt[1]->min_element(bit_index - 1);
7995:         ret.first |= T(1) << bit_index;
7996:         return ret;
7997:     }
7998: }
7999:
8000: T mex_query(int bit_index) { // distinct-values
8001:     propagate(bit_index);
8002:     if(bit_index == -1 || !nxt[0]) return 0;
8003:     if(nxt[0]->size() == (T(1) << bit_index)) {
8004:         T ret = T(1) << bit_index;
8005:         if(nxt[1]) ret |= nxt[1]->mex_query(bit_index - 1);
8006:         return ret;
8007:     } else {
8008:         return nxt[0]->mex_query(bit_index - 1);
8009:     }
8010: }
8011:
8012: int64_t count_less(const T &bit, int bit_index) {
8013:     propagate(bit_index);
8014:     if(bit_index == -1) return 0;
8015:     int64_t ret = 0;
8016:     if((bit >> bit_index) & 1) {
8017:         if(nxt[0]) ret += nxt[0]->size();
8018:         if(nxt[1]) ret += nxt[1]->count_less(bit, bit_index - 1);
8019:     } else {
8020:         if(nxt[0]) ret += nxt[0]->count_less(bit, bit_index - 1);
8021:     }
8022:     return ret;
8023: }
8024:
8025: pair< T, BinaryTrie * > get_kth(int64_t k, int bit_index) { // 1-indexed
8026:     propagate(bit_index);
```

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```
8027:     if(bit_index == -1) return {0, this};
8028:     if((nxt[0] ? nxt[0]->size() : 0) < k) {
8029:         auto ret = nxt[1]->get_kth(k - (nxt[0] ? nxt[0]->size() : 0), bit_index - 1)
;
8030:         ret.first |= T(1) << bit_index;
8031:         return ret;
8032:     } else {
8033:         return nxt[0]->get_kth(k, bit_index - 1);
8034:     }
8035: }
8036:
8037: pair< T, BinaryTrie * > max_element() {
8038:     assert(exist);
8039:     return max_element(MAX_LOG);
8040: }
8041:
8042: pair< T, BinaryTrie * > min_element() {
8043:     assert(exist);
8044:     return min_element(MAX_LOG);
8045: }
8046:
8047: T mex_query() {
8048:     return mex_query(MAX_LOG);
8049: }
8050:
8051: int size() const {
8052:     return exist;
8053: }
8054:
8055: void xorpush(const T &bit) {
8056:     lazy ^= bit;
8057: }
8058:
8059: int64_t count_less(const T &bit) {
8060:     return count_less(bit, MAX_LOG);
8061: }
8062:
8063: pair< T, BinaryTrie * > get_kth(int64_t k) {
8064:     assert(0 < k && k <= size());
8065:     return get_kth(k, MAX_LOG);
8066: }
8067:
8068: void propagate(int bit_index) {
8069:     if((lazy >> bit_index) & 1) swap(nxt[0], nxt[1]);
8070:     if(nxt[0]) nxt[0]->lazy ^= lazy;
8071:     if(nxt[1]) nxt[1]->lazy ^= lazy;
8072:     lazy = 0;
8073: }
8074: };
8075:
8076:
8077: #####
8078: ##### disjoint-sparse-table.cpp #####
8079: #####
8080:
8081: template< typename Semigroup >
8082: struct DisjointSparseTable {
8083:     using F = function< Semigroup(Semigroup, Semigroup) >;
8084:     const F f;
8085:     vector< vector< Semigroup > > st;
8086:
8087:     DisjointSparseTable(const vector< Semigroup > &v, const F &f) : f(f) {
8088:         int b = 0;
8089:         while((1 << b) <= v.size()) ++b;
8090:         st.resize(b, vector< Semigroup >(v.size(), Semigroup()));
8091:         for(int i = 0; i < v.size(); i++) st[0][i] = v[i];
8092:         for(int i = 1; i < b; i++) {
8093:             int shift = 1 << i;
8094:             for(int j = 0; j < v.size(); j += shift << 1) {
8095:                 int t = min(j + shift, (int) v.size());
```

```

8096:         st[i][t - 1] = v[t - 1];
8097:         for(int k = t - 2; k >= j; k--) st[i][k] = f(v[k], st[i][k + 1]);
8098:         if(v.size() <= t) break;
8099:         st[i][t] = v[t];
8100:         int r = min(t + shift, (int) v.size());
8101:         for(int k = t + 1; k < r; k++) st[i][k] = f(st[i][k - 1], v[k]);
8102:     }
8103: }
8104: }
8105:
8106: Semigroup query(int l, int r) {
8107:     if(l >= --r) return st[0][l];
8108:     int p = 31 - __builtin_clz(l ^ r);
8109:     return f(st[p][l], st[p][r]);
8110: }
8111: };
8112:
8113:
8114: #####
8115: ##### wavelet-matrix.cpp #####
8116: #####
8117:
8118: struct SuccinctIndexableDictionary {
8119:     size_t length;
8120:     size_t blocks;
8121:     vector< unsigned > bit, sum;
8122:
8123:     SuccinctIndexableDictionary() {
8124:     }
8125:
8126:     SuccinctIndexableDictionary(size_t _length) {
8127:         length = _length;
8128:         blocks = (length + 31) >> 5;
8129:         bit.assign(blocks, 0U);
8130:         sum.assign(blocks, 0U);
8131:     }
8132:
8133:     void set(int k) {
8134:         bit[k >> 5] |= 1U << (k & 31);
8135:     }
8136:
8137:     void build() {
8138:         sum[0] = 0U;
8139:         for(int i = 1; i < blocks; i++) {
8140:             sum[i] = sum[i - 1] + __builtin_popcount(bit[i - 1]);
8141:         }
8142:     }
8143:
8144:     bool operator[](int k) const {
8145:         return (bool)((bit[k >> 5] >> (k & 31)) & 1);
8146:     }
8147:
8148:     int rank(int k) {
8149:         return (sum[k >> 5] + __builtin_popcount(bit[k >> 5] & ((1U << (k & 31)) - 1)))
);
8150:     }
8151:
8152:     int rank(bool val, int k) {
8153:         return (val ? rank(k) : k - rank(k));
8154:     }
8155:
8156:     int select(bool val, int k) {
8157:         if(k < 0 || rank(val, length) <= k) return (-1);
8158:         int low = 0, high = length;
8159:         while(high - low > 1) {
8160:             int mid = (low + high) >> 1;
8161:             if(rank(val, mid) >= k + 1) high = mid;
8162:             else low = mid;
8163:         }
8164:         return (high - 1);

```

```

8165:     }
8166:
8167:     int select(bool val, int i, int l) {
8168:         return select(val, i + rank(val, l));
8169:     }
8170: };
8171:
8172: template< class T, int MAXLOG >
8173: struct WaveletMatrix {
8174:     size_t length;
8175:     SuccinctIndexableDictionary matrix[MAXLOG];
8176:     int zs[MAXLOG];
8177:     int buff1[MAXLOG], buff2[MAXLOG];
8178:
8179:     int freq_dfs(int d, int l, int r, T val, T a, T b) {
8180:         if(l == r) return 0;
8181:         if(d == MAXLOG) return (a <= val && val < b) ? r - l : 0;
8182:         T nv = 1ULL << (MAXLOG - d - 1) | val, nnv = ((1ULL << (MAXLOG - d - 1)) - 1)
| nv;
8183:         if(nnv < a || b <= val) return 0;
8184:         if(a <= val && nnv < b) return r - l;
8185:         int lc = matrix[d].rank(l, l), rc = matrix[d].rank(l, r);
8186:         return freq_dfs(d + 1, l - lc, r - rc, val, a, b) +
            freq_dfs(d + 1, lc + zs[d], rc + zs[d], nv, a, b);
8187:     }
8188: }
8189:
8190: WaveletMatrix(vector< T > data) {
8191:     length = data.size();
8192:     vector< T > l(length), r(length);
8193:     for(int depth = 0; depth < MAXLOG; depth++) {
8194:         matrix[depth] = SuccinctIndexableDictionary(length + 1);
8195:         int left = 0, right = 0;
8196:         for(int i = 0; i < length; i++) {
8197:             bool k = (data[i] >> (MAXLOG - depth - 1)) & 1;
8198:             if(k) r[right++] = data[i], matrix[depth].set(i);
8199:             else l[left++] = data[i];
8200:         }
8201:         zs[depth] = left;
8202:         matrix[depth].build();
8203:         swap(l, data);
8204:         for(int i = 0; i < right; i++) data[left + i] = r[i];
8205:     }
8206: }
8207:
8208: T access(int k) {
8209:     int ret = 0;
8210:     bool bit;
8211:     for(int depth = 0; depth < MAXLOG; depth++) {
8212:         bit = matrix[depth][k];
8213:         ret = (ret << 1) | bit;
8214:         k = matrix[depth].rank(bit, k) + zs[depth] * bit;
8215:     }
8216:     return (ret);
8217: }
8218:
8219: int rank(T val, int k) {
8220:     int l = 0, r = k;
8221:     for(int depth = 0; depth < MAXLOG; depth++) {
8222:         buff1[depth] = l, buff2[depth] = r;
8223:         bool bit = (val >> (MAXLOG - depth - 1)) & 1;
8224:         l = matrix[depth].rank(bit, l) + zs[depth] * bit;
8225:         r = matrix[depth].rank(bit, r) + zs[depth] * bit;
8226:     }
8227:     return (r - l);
8228: }
8229:
8230: int select(T val, int kth) {
8231:     rank(val, length);
8232:     for(int depth = MAXLOG - 1; depth >= 0; depth--) {
8233:         bool bit = (val >> (MAXLOG - depth - 1)) & 1;

```

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```
8234:         kth = matrix[depth].select(bit, kth, buffl[depth]);
8235:         if(kth >= buff2[depth] || kth < 0) return (-1);
8236:         kth -= buffl[depth];
8237:     }
8238:     return (kth);
8239: }
8240:
8241: int select(T val, int k, int l) {
8242:     return select(val, k + rank(val, l));
8243: }
8244:
8245: int quantile(int left, int right, int kth) {
8246:     if(right - left <= kth || kth < 0) return (-1);
8247:     T ret = 0;
8248:     for(int depth = 0; depth < MAXLOG; depth++) {
8249:         int l = matrix[depth].rank(1, left);
8250:         int r = matrix[depth].rank(1, right);
8251:         if(r - l > kth) {
8252:             left = l + zs[depth];
8253:             right = r + zs[depth];
8254:             ret |= 1ULL << (MAXLOG - depth - 1);
8255:         } else {
8256:             kth -= r - l;
8257:             left -= l;
8258:             right -= r;
8259:         }
8260:     }
8261:     return ret;
8262: }
8263:
8264: int rangefreq(int left, int right, T lower, T upper) {
8265:     return freq_dfs(0, left, right, 0, lower, upper);
8266: }
8267: };
8268:
8269:
8270:
8271: #####
8272: ##### sqrt-decomposition.cpp #####
8273: #####
8274:
8275: template< typename T, typename E = int >
8276: struct SqrtDecomposition {
8277:
8278:     vector< E > block_add, elem_add;
8279:     vector< int > block_pos;
8280:     vector< T > data, lsum;
8281:     vector< vector< T > > sum;
8282:     int N, B, K;
8283:     E L;
8284:
8285:     SqrtDecomposition(int N, E L = 0) : N(N), L(L) { // find the sum of L or more in
the interval
8286:         B = (int) sqrt(N);
8287:         K = (N + B - 1) / B;
8288:
8289:         block_add.assign(K, 0);
8290:         block_pos.resize(N);
8291:         for(int k = 0; k < K; k++) {
8292:             for(int i = k * B; i < min((k + 1) * B, N); i++) block_pos[i] = k;
8293:         }
8294:         elem_add.assign(N, 0);
8295:         data.assign(N, 0);
8296:         sum.assign(K, vector< T >(B, 0));
8297:         lsum.assign(K, 0);
8298:     }
8299:
8300:
8301: void build(const vector< E > &add, const vector< T > &dat) {
8302:     assert(add.size() == elem_add.size());
```



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```
8303:     assert(dat.size() == data.size());
8304:     elem_add = add;
8305:     data = dat;
8306:     for(int k = 0; k < K; k++) {
8307:         E tap = elem_add[k * B];
8308:         for(int i = k * B; i < min((k + 1) * B, N); i++) tap = min(tap, elem_add[i])
;
8309:         block_add[k] = tap;
8310:         for(int i = k * B; i < min((k + 1) * B, N); i++) {
8311:             elem_add[i] -= block_add[k];
8312:             set(i, dat[i]);
8313:         }
8314:     }
8315: }
8316:
8317: inline void del(int k) {
8318:     sum[block_pos[k]][elem_add[k]] -= data[k];
8319:     if(block_add[block_pos[k]] + elem_add[k] >= L) lsum[block_pos[k]] -= data[k];
8320: }
8321:
8322: inline void set(int k) {
8323:     while(sum[block_pos[k]].size() <= elem_add[k]) sum[block_pos[k]].push_back(0);
8324:     sum[block_pos[k]][elem_add[k]] += data[k];
8325:     if(block_add[block_pos[k]] + elem_add[k] >= L) lsum[block_pos[k]] += data[k];
8326: }
8327:
8328: void set(int k, T x) {
8329:     data[k] = x;
8330:     set(k);
8331: }
8332:
8333: void add(int a, int b) {
8334:     for(int k = 0; k < K; k++) {
8335:         int l = k * B;
8336:         int r = min(l + B, N);
8337:
8338:         if(r <= a || b <= l) {
8339:
8340:         } else if(a <= l && r <= b) {
8341:             block_add[k]++;
8342:             if(0 <= L - block_add[k] && L - block_add[k] < sum[k].size()) {
8343:                 lsum[k] += sum[k][L - block_add[k]];
8344:             }
8345:         } else {
8346:             for(int i = max(a, l); i < min(b, r); i++) {
8347:                 del(i);
8348:                 elem_add[i]++;
8349:                 set(i);
8350:             }
8351:         }
8352:     }
8353: }
8354:
8355: void sub(int a, int b) {
8356:     for(int k = 0; k < K; k++) {
8357:         int l = k * B;
8358:         int r = min(l + B, N);
8359:
8360:         if(r <= a || b <= l) {
8361:
8362:         } else if(a <= l && r <= b) {
8363:             if(0 <= L - block_add[k] && L - block_add[k] < sum[k].size()) {
8364:                 lsum[k] -= sum[k][L - block_add[k]];
8365:             }
8366:             block_add[k]--;
8367:         } else {
8368:             if(0 <= L - block_add[k] && L - block_add[k] < sum[k].size()) {
8369:                 lsum[k] -= sum[k][L - block_add[k]];
8370:             }
8371:         }
8371:     }
```

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```
8372:         block_add[k]--;
8373:         for(int i = l; i < max(a, l); i++) {
8374:             del(i);
8375:             elem_add[i]++;
8376:             set(i);
8377:         }
8378:         for(int i = min(b, r); i < r; i++) {
8379:             del(i);
8380:             elem_add[i]++;
8381:             set(i);
8382:         }
8383:     }
8384: }
8385: }
8386:
8387:
8388: T query(int a, int b, E x) {
8389:     T ret = 0;
8390:     for(int k = 0; k < K; k++) {
8391:         int l = k * B;
8392:         int r = min(l + B, N);
8393:
8394:         if(r <= a || b <= l) {
8395:
8396:         } else if(a <= l && r <= b) {
8397:             if(0 <= x - block_add[k] && x - block_add[k] < sum[k].size()) {
8398:                 ret += sum[k][x - block_add[k]];
8399:             }
8400:         } else {
8401:             for(int i = max(a, l); i < min(b, r); i++) {
8402:                 if(block_add[k] + elem_add[i] == x) ret += data[i];
8403:             }
8404:         }
8405:     }
8406:     return ret;
8407: }
8408:
8409:
8410: T query_low(int a, int b) {
8411:     T ret = 0;
8412:     for(int k = 0; k < K; k++) {
8413:         int l = k * B;
8414:         int r = min(l + B, N);
8415:
8416:         if(r <= a || b <= l) {
8417:
8418:         } else if(a <= l && r <= b) {
8419:             ret += lsum[k];
8420:         } else {
8421:             for(int i = max(a, l); i < min(b, r); i++) {
8422:                 if(block_add[k] + elem_add[i] >= L) ret += data[i];
8423:             }
8424:         }
8425:     }
8426:     return ret;
8427: }
8428: };
8429:
8430:
8431: #####
8432: ##### priority-sum-structure.cpp #####
8433: #####
8434:
8435: template< typename T, typename Compare = less< T >, typename RCompare = greater< T
> >
8436: struct PrioritySumStructure {
8437:
8438:     size_t k;
8439:     T sum;
8440:
```

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```
8441: priority_queue< T, vector< T >, Compare > in, d_in;
8442: priority_queue< T, vector< T >, RCompare > out, d_out;
8443:
8444: PrioritySumStructure(int k) : k(k), sum(0) {}
8445:
8446: void modify() {
8447:     while(in.size() - d_in.size() < k && !out.empty()) {
8448:         auto p = out.top();
8449:         out.pop();
8450:         if(!d_out.empty() && p == d_out.top()) {
8451:             d_out.pop();
8452:         } else {
8453:             sum += p;
8454:             in.emplace(p);
8455:         }
8456:     }
8457:     while(in.size() - d_in.size() > k) {
8458:         auto p = in.top();
8459:         in.pop();
8460:         if(!d_in.empty() && p == d_in.top()) {
8461:             d_in.pop();
8462:         } else {
8463:             sum -= p;
8464:             out.emplace(p);
8465:         }
8466:     }
8467:     while(!d_in.empty() && in.top() == d_in.top()) {
8468:         in.pop();
8469:         d_in.pop();
8470:     }
8471: }
8472:
8473: T query() const {
8474:     return sum;
8475: }
8476:
8477: void insert(T x) {
8478:     in.emplace(x);
8479:     sum += x;
8480:     modify();
8481: }
8482:
8483: void erase(T x) {
8484:     assert(size());
8485:     if(!in.empty() && in.top() == x) {
8486:         sum -= x;
8487:         in.pop();
8488:     } else if(!in.empty() && RCompare()(in.top(), x)) {
8489:         sum -= x;
8490:         d_in.emplace(x);
8491:     } else {
8492:         d_out.emplace(x);
8493:     }
8494:     modify();
8495: }
8496:
8497: void set_k(size_t kk) {
8498:     k = kk;
8499:     modify();
8500: }
8501:
8502: size_t get_k() const {
8503:     return k;
8504: }
8505:
8506: size_t size() const {
8507:     return in.size() + out.size() - d_in.size() - d_out.size();
8508: }
8509: };
8510:
```

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```
8511: template< typename T >
8512: using MaximumSum = PrioritySumStructure< T, greater< T >, less< T > >;
8513:
8514: template< typename T >
8515: using MinimumSum = PrioritySumStructure< T, less< T >, greater< T > >;
8516:
8517:
8518:
8519: #####
8520: ##### link-cut-tree.cpp #####
8521: #####
8522:
8523: template< typename Monoid = int, typename OperatorMonoid = Monoid >
8524: struct LinkCutTree {
8525:     using F = function< Monoid(Monoid, Monoid) >;
8526:     using G = function< Monoid(Monoid, OperatorMonoid, int) >;
8527:     using H = function< OperatorMonoid(OperatorMonoid, OperatorMonoid) >;
8528:     using S = function< Monoid(Monoid) >;
8529:
8530:     struct Node {
8531:         Node *l, *r, *p;
8532:         int idx;
8533:         Monoid key, sum;
8534:         OperatorMonoid lazy;
8535:
8536:         bool rev;
8537:         int sz;
8538:
8539:         bool is_root() {
8540:             return !p || (p->l != this && p->r != this);
8541:         }
8542:
8543:         Node(int idx, const Monoid &key, const OperatorMonoid &om) :
8544:             idx(idx), key(key), sum(key), lazy(om), sz(1),
8545:             l(nullptr), r(nullptr), p(nullptr), rev(false) {}
8546:     };
8547:
8548:     const Monoid M1;
8549:     const OperatorMonoid OM0;
8550:     const F f;
8551:     const G g;
8552:     const H h;
8553:     const S s;
8554:
8555:     LinkCutTree() : LinkCutTree([](Monoid a, Monoid b) { return a + b; }, [](Monoid
a) { return a; }, Monoid()) {}
8556:
8557:     LinkCutTree(const F &f, const S &s, const Monoid &M1) :
8558:         LinkCutTree(f, G(), H(), s, M1, OperatorMonoid()) {}
8559:
8560:     LinkCutTree(const F &f, const G &g, const H &h, const S &s,
8561:                 const Monoid &M1, const OperatorMonoid &OM0) :
8562:         f(f), g(g), h(h), s(s), M1(M1), OM0(OM0) {}
8563:
8564:     Node *make_node(int idx, const Monoid &v = Monoid()) {
8565:         return new Node(idx, v, OM0);
8566:     }
8567:
8568:     void propagate(Node *t, const OperatorMonoid &x) {
8569:         t->lazy = h(t->lazy, x);
8570:         t->key = g(t->key, x, 1);
8571:         t->sum = g(t->sum, x, t->sz);
8572:     }
8573:
8574:     void toggle(Node *t) {
8575:         assert(t);
8576:         swap(t->l, t->r);
8577:         t->sum = s(t->sum);
8578:         t->rev ^= true;
8579:     }
```

```

8580:
8581: void push(Node *t) {
8582:     if(t->lazy != OM0) {
8583:         if(t->l) propagate(t->l, t->lazy);
8584:         if(t->r) propagate(t->r, t->lazy);
8585:         t->lazy = OM0;
8586:     }
8587:     if(t->rev) {
8588:         if(t->l) toggle(t->l);
8589:         if(t->r) toggle(t->r);
8590:         t->rev = false;
8591:     }
8592: }
8593:
8594: void update(Node *t) {
8595:     t->sz = 1;
8596:     t->sum = t->key;
8597:     if(t->l) t->sz += t->l->sz, t->sum = f(t->l->sum, t->sum);
8598:     if(t->r) t->sz += t->r->sz, t->sum = f(t->sum, t->r->sum);
8599: }
8600:
8601: void rotr(Node *t) {
8602:     auto *x = t->p, *y = x->p;
8603:     if((x->l == t->r)) t->r->p = x;
8604:     t->r = x, x->p = t;
8605:     update(x), update(t);
8606:     if((t->p == y)) {
8607:         if(y->l == x) y->l = t;
8608:         if(y->r == x) y->r = t;
8609:         update(y);
8610:     }
8611: }
8612:
8613: void rotl(Node *t) {
8614:     auto *x = t->p, *y = x->p;
8615:     if((x->r == t->l)) t->l->p = x;
8616:     t->l = x, x->p = t;
8617:     update(x), update(t);
8618:     if((t->p == y)) {
8619:         if(y->l == x) y->l = t;
8620:         if(y->r == x) y->r = t;
8621:         update(y);
8622:     }
8623: }
8624:
8625: void splay(Node *t) {
8626:     push(t);
8627:     while(!t->is_root()) {
8628:         auto *q = t->p;
8629:         if(q->is_root()) {
8630:             push(q), push(t);
8631:             if(q->l == t) rotr(t);
8632:             else rotl(t);
8633:         } else {
8634:             auto *r = q->p;
8635:             push(r), push(q), push(t);
8636:             if(r->l == q) {
8637:                 if(q->l == t) rotr(q), rotr(t);
8638:                 else rotl(t), rotr(t);
8639:             } else {
8640:                 if(q->r == t) rotl(q), rotl(t);
8641:                 else rotr(t), rotl(t);
8642:             }
8643:         }
8644:     }
8645: }
8646:
8647: Node *expose(Node *t) {
8648:     Node *rp = nullptr;
8649:     for(Node *cur = t; cur; cur = cur->p) {

```

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```
8650:     splay(cur);
8651:     cur->r = rp;
8652:     update(cur);
8653:     rp = cur;
8654: }
8655: splay(t);
8656: return rp;
8657: }
8658:
8659: void link(Node *child, Node *parent) {
8660:     expose(child);
8661:     expose(parent);
8662:     child->p = parent;
8663:     parent->r = child;
8664:     update(parent);
8665: }
8666:
8667: void cut(Node *child) {
8668:     expose(child);
8669:     auto *parent = child->l;
8670:     child->l = nullptr;
8671:     parent->p = nullptr;
8672:     update(child);
8673: }
8674:
8675: void evert(Node *t) {
8676:     expose(t);
8677:     toggle(t);
8678:     push(t);
8679: }
8680:
8681: Node *lca(Node *u, Node *v) {
8682:     if(get_root(u) != get_root(v)) return nullptr;
8683:     expose(u);
8684:     return expose(v);
8685: }
8686:
8687: vector< int > get_path(Node *x) {
8688:     vector< int > vs;
8689:     function< void(Node *) > dfs = [&](Node *cur) {
8690:         if(!cur) return;
8691:         push(cur);
8692:         dfs(cur->r);
8693:         vs.push_back(cur->idx);
8694:         dfs(cur->l);
8695:     };
8696:     expose(x);
8697:     dfs(x);
8698:     return vs;
8699: }
8700:
8701: void set_propagate(Node *t, const OperatorMonoid &x) {
8702:     expose(t);
8703:     propagate(t, x);
8704:     push(t);
8705: }
8706:
8707: Node *get_kth(Node *x, int k) {
8708:     expose(x);
8709:     while(x) {
8710:         push(x);
8711:         if(x->r && x->r->sz > k) {
8712:             x = x->r;
8713:         } else {
8714:             if(x->r) k -= x->r->sz;
8715:             if(k == 0) return x;
8716:             k -= 1;
8717:             x = x->l;
8718:         }
8719:     }
```

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```
8720:     return nullptr;
8721: }
8722:
8723: Node *get_root(Node *x) {
8724:     expose(x);
8725:     while(x->l) {
8726:         push(x);
8727:         x = x->l;
8728:     }
8729:     return x;
8730: }
8731: };
8732:
8733:
8734:
8735: #####
8736: ##### persistent-union-find.cpp #####
8737: #####
8738:
8739: struct PersistentUnionFind
8740: {
8741:     PersistentArray< int, 3 > data;
8742:
8743:     PersistentUnionFind() {}
8744:
8745:     PersistentUnionFind(int sz)
8746:     {
8747:         data.build(vector< int >(sz, -1));
8748:     }
8749:
8750:     int find(int k)
8751:     {
8752:         int p = data.get(k);
8753:         return p >= 0 ? find(p) : k;
8754:     }
8755:
8756:     int size(int k)
8757:     {
8758:         return (-data.get(find(k)));
8759:     }
8760:
8761:     PersistentUnionFind unite(int x, int y)
8762:     {
8763:         x = find(x);
8764:         y = find(y);
8765:         if(x == y) return *this;
8766:         auto u = data.get(x);
8767:         auto v = data.get(y);
8768:
8769:         if(u < v) {
8770:             auto a = data.mutable_get(x);
8771:             *a += v;
8772:             auto b = data.mutable_get(y);
8773:             *b = x;
8774:         } else {
8775:             auto a = data.mutable_get(y);
8776:             *a += u;
8777:             auto b = data.mutable_get(x);
8778:             *b = y;
8779:         }
8780:         return *this;
8781:     }
8782: };
8783:
8784:
```