

**LEBANESE AMERICAN UNIVERSITY**  
**School of Arts and Science**  
**Department of Computer Science and Mathematics**

**CSC 310: Algorithms and Data Structures**

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**Lab VIII**

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**Important Note:** Input should be read from a file named “graph.in” for all the problems.

**Problem 1**

Given an undirected graph  $G(V, E)$ , where  $V$  is the set of vertices and  $E$  is the set of edges, you are required to print the degree of each vertex.

**Input**

The first line is an integer  $T$  representing the number of test cases.

Each test case is made up of two integers  $n$  and  $m$  representing the number of vertices and edges respectively. Then  $m$  lines follow, each containing two integers  $u$  and  $v$  which are the endpoints of edge  $uv$ .

**Output**

For each test case, output the degree of each vertex in the graph (as in the below sample).

**Sample Input**

```
2
5 5
0 1
0 2
1 3
2 3
3 4
5 5
0 1
0 2
1 2
1 3
2 4
```

**Sample Output**

```
0: 2
1: 2
2: 2
3: 3
4: 1

0: 2
1: 3
2: 3
3: 1
4: 1
```

## **Problem 2**

Given an undirected graph  $G = (V, E)$ , where  $V$  is the set of vertices and  $E$  is the set of edges, you are required to print the vertices of the graph using BFS starting with the vertex of highest index.

### **Input**

The first line is an integer  $T$  representing the number of test cases.

Each test case is made up of two integers  $n$  and  $m$  representing the number of vertices and edges respectively. Then  $m$  lines follow, each containing two integers  $u$  and  $v$  which are the endpoints of edge  $uv$ .

### **Output**

For each test case, list the vertices of the graph via a BFS traversal.

#### **Sample Input**

```
2
5    5
0    1
0    2
1    3
2    3
3    4
5    5
0    1
0    2
1    2
1    3
2    4
```

#### **Sample Output**

```
4 2 0 3 1
4 2 0 1 3
```

## **Problem 3**

Given an undirected graph  $G = (V, E)$ , you are required to print the vertices of  $G$  using DFS starting with the vertex of index zero.

### **Input**

The first line is an integer  $T$  representing the number of test cases.

Each test case is made up of two integers  $n$  and  $m$  representing the number of vertices and edges respectively. Then  $m$  lines follow, each containing two integers  $u$  and  $v$  which are the endpoints of edge  $uv$ .

### **Output**

For each test case, print the vertices according to a DFS traversal.

#### **Sample Input**

```
2
4    3
0    1
1    2
1    3
4    6
0    1
0    2
0    3
1    2
1    3
2    3
```

#### **Sample Output**

```
1 0 2 3
0 1 2 3
```

### **Problem 4**

Given an undirected graph  $G = (V, E)$ , print the connected components in the  $G$ .

### **Input**

The first line is an integer  $T$  representing the number of test cases.

Each test case is made up of two integers  $n$  and  $m$  representing the number of vertices and edges respectively. Then  $m$  lines follow, each containing two integers  $u$  and  $v$  which are the endpoints of edge  $uv$ .

### **Output**

For each test case, print each of the connected components on a separate line as shown in the below sample.

#### **Sample Input**

```
2
```

#### **Sample Output**

```
0: 0 1 2
```

5	4	1: 3 4
0	1	0: 0 1 2
0	2	1: 3 4
1	2	2: 5 6 7 8
3	4	
9	8	
0	1	
0	2	
1	2	
3	4	
5	6	
5	7	
6	8	
7	8	

### **Problem 5**

Given a directed graph  $G(V, E)$ , where  $V$  is the set of vertices and  $E$  is the set of edges, you are required to check if  $G$  is bipartite. A graph is bipartite if the graph can be colored using only 2 colors such that no adjacent vertices have the same color.

### **Input**

The first line is an integer  $T$  representing the number of test cases.

Each test case is made up of two integers  $n$  and  $m$  representing the number of vertices and edges respectively. Then  $m$  lines follow, each containing two integers  $u$  and  $v$  which are the endpoints of edge  $uv$ .

### **Output**

For each test case, output “**bipartite**” if the graph is bipartite and “**not bipartite**” otherwise.

### **Sample Input**

```
2
4 5
0 1
1 2
2 0
2 3
3 1
```

### **Sample Output**

```
bipartite
not bipartite
```

5	5
0	1
0	2
2	4
3	2
4	3

### **Problem 6**

Given an undirected graph  $G (V, E)$ , where  $V$  is the set of vertices and  $E$  is the set of edges, you are required to check if the graph has a cycle.

### **Input**

The first line is an integer  $T$  representing the number of test cases.

Each test case is made up of two integers  $n$  and  $m$  representing the number of vertices and edges respectively. Then  $m$  lines follow, each containing two integers  $u$  and  $v$  which are the endpoints of edge  $uv$ .

### **Output**

For each test case, output “**cycle**” if the graph has a cycle and “**no cycle**” otherwise.

### **Sample Input**

```
2
5 3
0 4
1 2
2 3
7 6
0 1
0 2
0 3
1 4
2 5
3 6
```

### **Sample Output**

```
no cycle
cycle
```

### **Problem 7**

Given an undirected graph  $G(V, E)$ , where  $V$  is the set of vertices and  $E$  is the set of edges, you are required to check if the graph has a cycle of length greater than 4.

### **Input**

The first line is an integer  $T$  representing the number of test cases.

Each test case is made up of two integers  $n$  and  $m$  representing the number of vertices and edges respectively. Then  $m$  lines follow, each containing two integers  $u$  and  $v$  which are the endpoints of edge  $uv$ .

### **Output**

For each test case, output “yes” if the graph has a cycle of length  $> 4$ , and “no” otherwise.

### **Sample Input**

```
2
5    3
0    4
1    2
2    3
5    7
0    1
0    2
0    3
0    4
1    3
3    4
4    2
```

### **Sample Output**

```
no
yes
```